## Survey of Mathematics With Applications With Applications Angel Abbott Runde

## A Survey of Mathematics with Applications, 8e

Chapter 2 – Sets Form 1

In Exercises 1-9, determine whether each is true or false. If the statement is false, explain why.

- 1.  $7 \in \{1, 3, 5, 7\}$ .
- 2.  $\{1,2,3\}$  is equivalent to  $\{1,2,3,4\}$ .
- 3.  $\{b, a, t\}$  has eight subsets.
- 4.  $\{dog\} \not\subset \{cat, dog, mouse\}$ .
- 5.  $\{ \} = \emptyset$ .
- 6.  $\{\text{rose, tulip, lily}\} = \{\text{rose, lily, daisy}\}$
- 7.  $\{5\} \subseteq \{x | x \in \mathbb{N} \text{ and } x \leq 5\}.$
- 8. The set of even natural numbers greater than 100 is an infinite set.
- 9. For any set  $A, A \cap A' = \emptyset$ .

In Exercises 10-11, use set  $A = \{2, 4, 6, 8, 10, 12, 14\}$ .

- 10. Write set *A* using set builder notation.
- 11. Express set *A* with a written description.

*In Exercises 12-15, use the following information:* 

$$U = \{1, 2, 3, 4, 5, 6, 7, 8\}$$

$$A = \{2, 4, 6, 8\}$$

$$B = \{1, 3, 5, 7\}$$

$$C = \{1, 2, 3, 4\}$$

Determine the following.

- 12.  $A \cap C$
- 13.  $A \cup B'$
- 14.  $B \cup (A \cap C')$
- 15.  $n(B \cap C)$
- 16. Using the sets provided for Exercises 12-15, draw a Venn diagram illustrating the relationship among the sets.
- 17. Use a Venn diagram to determine whether  $(B \cup C')' = B' \cap C$  for all sets B and C. Show your work.
- 18. The Ice Cream Shoppe surveyed its customers about their preferences of three ice cream flavors. The results of the survey showed:
  - 170 people liked vanilla.
  - 135 people liked chocolate.
  - 103 people liked strawberry.
  - 100 people liked vanilla and chocolate.
  - 74 people liked vanilla and strawberry.
  - 52 people liked chocolate and strawberry.
  - 35 people liked all three flavors.
  - 7 people did not like any of the three flavors.

Draw a Venn diagram to represent this situation and then determine how many people...

- a) Completed the survey.
- b) Liked only strawberry.
- c) Liked vanilla and chocolate, but not strawberry.
- d) Liked vanilla or chocolate, but not strawberry.
- e) Liked exactly two flavors.
- f) Liked only one flavor.
- 19. Show that the following set is infinite by setting up a one-to-one correspondence between the set and a proper subset of itself: {5,10,15,20,...}
- 20. Show that the following set has cardinal number  $\aleph_0$  by setting up a one-to-one correspondence between the set of counting numbers and the given set:  $\{10, 20, 30, 40, ...\}$