

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.
 Find the average velocity of the function over the given interval.

1) $y = x^2 + 2x, [1, 4]$

A) $\frac{21}{4}$

B) 8

C) 7

D) 6

1) _____

2) $y = 4x^3 - 6x^2 - 6, [6, 8]$

A) $\frac{829}{4}$

B) 127

C) 508

D) 829

2) _____

3) $y = \sqrt{2x}, [2, 8]$

A) 7

B) $\frac{1}{3}$

C) $-\frac{3}{10}$

D) 2

3) _____

4) $y = \frac{3}{x-2}, [4, 7]$

A) 2

B) 7

C) $-\frac{3}{10}$

D) $\frac{1}{3}$

4) _____

5) $y = 4x^2, \left[0, \frac{7}{4}\right]$

A) 7

B) $-\frac{3}{10}$

C) $\frac{1}{3}$

D) 2

5) _____

6) $y = -3x^2 - x, [5, 6]$

A) -34

B) $-\frac{1}{6}$

C) $\frac{1}{2}$

D) -2

6) _____

7) $h(t) = \sin(3t), \left[0, \frac{\pi}{6}\right]$

A) $\frac{\pi}{6}$

B) $\frac{3}{\pi}$

C) $\frac{6}{\pi}$

D) $\frac{6}{\pi}$

7) _____

8) $g(t) = 5 + \tan t, \left[-\frac{\pi}{4}, \frac{\pi}{4}\right]$

A) $-\frac{4}{\pi}$

B) $-\frac{16}{11}$

C) 0

D) $\frac{4}{\pi}$

8) _____

Use the table to find the instantaneous velocity of y at the specified value of x .

9) $x = 1$.

x	y	9)
0	0	
0.2	0.02	
0.4	0.08	
0.6	0.18	
0.8	0.32	
1.0	0.5	
1.2	0.72	
1.4	0.98	

A) 2

B) 1.5

C) 1

D) 0.5

10) $x = 1.$

10) _____

x	y
0	0
0.2	0.01
0.4	0.04
0.6	0.09
0.8	0.16
1.0	0.25
1.2	0.36
1.4	0.49

A) 2

B) 0.5

C) 1.5

D) 1

11) $x = 1.$

11) _____

x	y
0	0
0.2	0.12
0.4	0.48
0.6	1.08
0.8	1.92
1.0	3
1.2	4.32
1.4	5.88

A) 6

B) 2

C) 8

D) 4

12) $x = 2.$

12) _____

x	y
0	10
0.5	38
1.0	58
1.5	70
2.0	74
2.5	70
3.0	58
3.5	38
4.0	10

A) 4

B) 8

C) -8

D) 0

13) $x = 1.$

x	y3)
0.900	-0.05263
0.990	-0.00503
0.999	-0.0005
1.000	0.0000
1.001	0.0005
1.010	0.00498
1.100	0.04762

A) 1

B) 0.5

C) -0.5

D) 0

Find the slope of the curve for the given value of x.

14) $y = x^2 + 5x, x = 4$

A) slope is -39

B) slope is 13

C) slope is $\frac{1}{20}$ D) slope is $-\frac{4}{25}$

14) _____

15) $y = x^2 + 11x - 15, x = 1$

A) $\frac{1}{20}$
slope isB) $-\frac{4}{25}$
slope is -

C) slope is 13

D) slope is -39

15) _____

16) $y = x^3 - 9x, x = 1$

A) slope is 1

B) slope is -3

C) slope is -6

D) slope is 3

16) _____

17) $y = x^3 - 2x^2 + 4, x = -1$

A) slope is -1

B) slope is -1

C) slope is 0

D) slope is 1

17) _____

18) $y = -4 - x^3, x = -1$

A) slope is -1

B) slope is 3

C) slope is -3

D) slope is 0

18) _____

Solve the problem.

19) $\lim_{x \rightarrow 0^-} f(x) = L_1, \lim_{x \rightarrow 0^+} f(x) = L_r$

Given $\lim_{x \rightarrow 0^-} f(x) = L_1, \lim_{x \rightarrow 0^+} f(x) = L_r$, and $L_1 \neq L_r$, which of the following statements is true?

19) _____

I. $\lim_{x \rightarrow 0} f(x) = L_1$

II. $\lim_{x \rightarrow 0} f(x) = L_r$

III. $\lim_{x \rightarrow 0} f(x)$ does not exist.

A) I

B) none

C) II

D) III

20) $\lim_{x \rightarrow 0^-} f(x) = L_1, \lim_{x \rightarrow 0^+} f(x) = L_r$

Given $\lim_{x \rightarrow 0^-} f(x) = L_1, \lim_{x \rightarrow 0^+} f(x) = L_r$, and $L_1 = L_r$, which of the following statements is false?

20) _____

I. $\lim_{x \rightarrow 0} f(x) = L_1$

II. $\lim_{x \rightarrow 0} f(x) = L_r$

III. $\lim_{x \rightarrow 0} f(x)$ does not exist.

A) III

B) none

C) II

D) I

21) If $\lim_{x \rightarrow 0} f(x) = L$, which of the following expressions are true?

- I. $\lim_{x \rightarrow 0^-} f(x)$ does not exist.
- II. $\lim_{x \rightarrow 0^+} f(x)$ does not exist.
- III. $\lim_{x \rightarrow 0^-} f(x) = L$
- IV. $\lim_{x \rightarrow 0^+} f(x) = L$

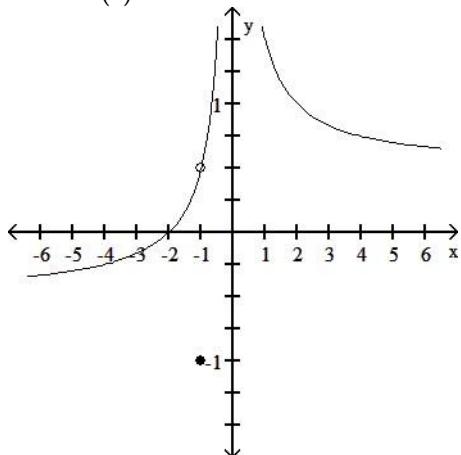
A) II and III only B) III and IV only C) I and II only D) I and IV only

22) What conditions, when present, are sufficient to conclude that a function $f(x)$ has a limit as x approaches some value of a ?

- A) The limit of $f(x)$ as $x \rightarrow a$ from the left exists, the limit of $f(x)$ as $x \rightarrow a$ from the right exists, and these two limits are the same.
- B) The limit of $f(x)$ as $x \rightarrow a$ from the left exists, the limit of $f(x)$ as $x \rightarrow a$ from the right exists, and at least one of these limits is the same as $f(a)$.
- C) $f(a)$ exists, the limit of $f(x)$ as $x \rightarrow a$ from the left exists, and the limit of $f(x)$ as $x \rightarrow a$ from the right exists.
- D) Either the limit of $f(x)$ as $x \rightarrow a$ from the left exists or the limit of $f(x)$ as $x \rightarrow a$ from the right exists

Use the graph to evaluate the limit.

23) $\lim_{x \rightarrow -1} f(x)$



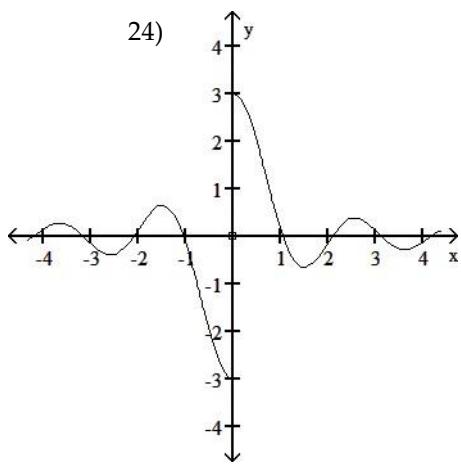
- A) ∞ B) -1 C) $\frac{1}{2}$ D) $\frac{1}{2}$

24) $\lim_{x \rightarrow 0} f(x)$

21) _____

22) _____

23) _____



A) -3

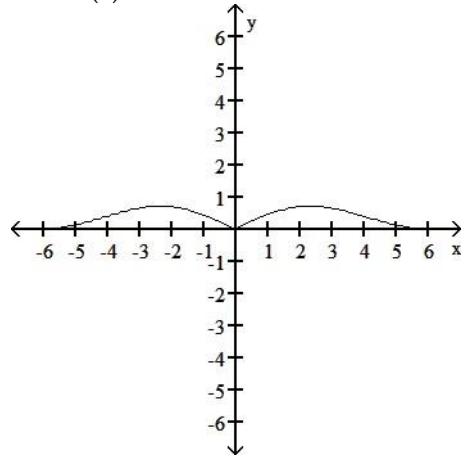
B) does not exist

C) 0

D) 3

25) $\lim_{x \rightarrow 0} f(x)$

25) _____



A) 0

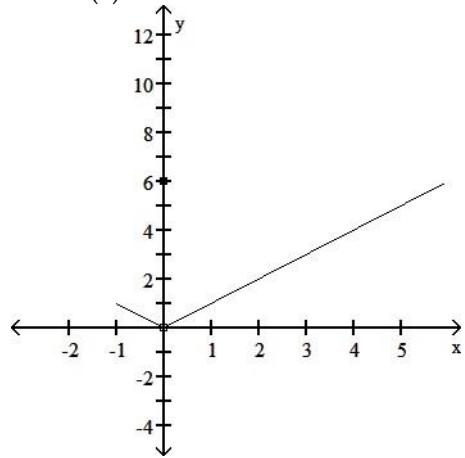
B) -1

C) 1

D) does not exist

26) $\lim_{x \rightarrow 0} f(x)$

26) _____



A) 6

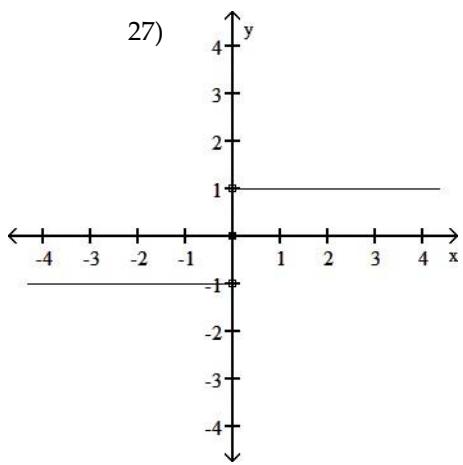
B) does not exist

C) -1

D) 0

27) $\lim_{x \rightarrow 0} f(x)$

27)



A) -1

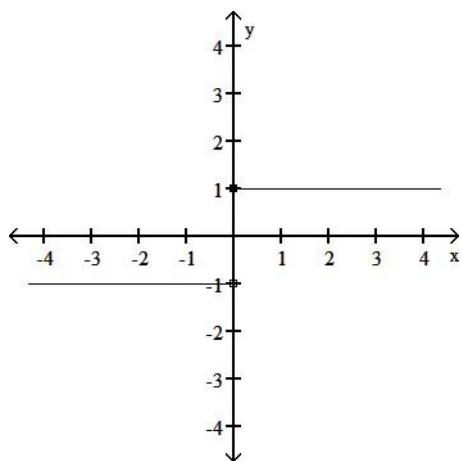
B) ∞

C) does not exist

D) 1

28) $\lim_{x \rightarrow 0} f(x)$

28) _____



A) 1

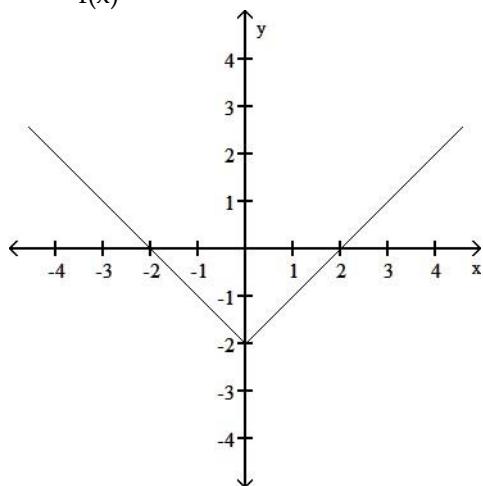
B) does not exist

C) ∞

D) -1

29) $\lim_{x \rightarrow 0} f(x)$

29) _____



A) 2

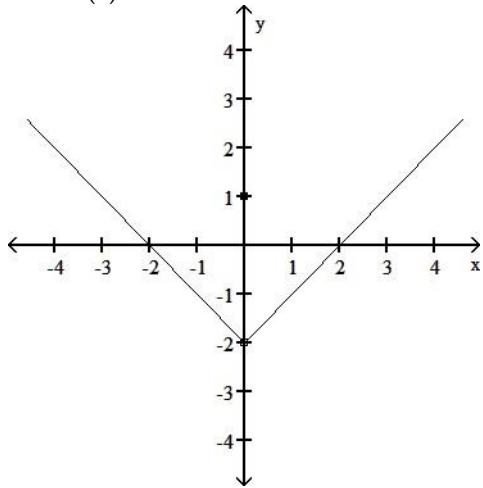
B) -2

C) 0

D) does not exist

30)

30) $\lim_{x \rightarrow 0} f(x)$



A) does not exist

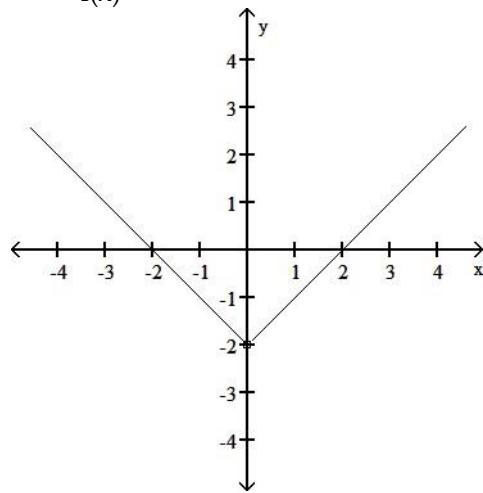
B) -2

C) 0

D) 1

31) _____

31) $\lim_{x \rightarrow 0} f(x)$



A) -1

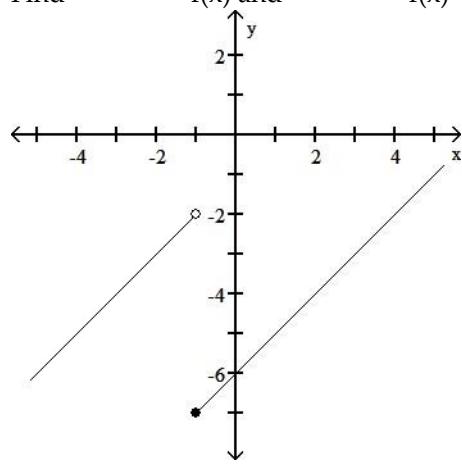
B) 2

C) does not exist

D) -2

32) _____

32) Find $\lim_{x \rightarrow -1^-} f(x)$ and $\lim_{x \rightarrow -1^+} f(x)$



A) -5; -2

B) -7; -5

C) -7; -2

D) -2; -7

Use the table of values of f to estimate the limit.

33) Let $f(x) = x^2 + 8x - 2$, find $\lim_{x \rightarrow 2} f(x)$.

33) _____

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)						

A)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	16.692	17.592	17.689	17.710	17.808	18.789

; limit = 17.70

B)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	5.043	5.364	5.396	5.404	5.436	5.763

; limit = ∞

C)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	16.810	17.880	17.988	18.012	18.120	19.210

; limit = 18.0

D)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	5.043	5.364	5.396	5.404	5.436	5.763

; limit = 5.40

34) Let $f(x) = \frac{x-4}{\sqrt{x-2}}$, find $\lim_{x \rightarrow 4} f(x)$.

34) _____

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)						

A)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	1.19245	1.19925	1.19993	1.20007	1.20075	1.20745

; limit = ∞

B)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	5.07736	5.09775	5.09978	5.10022	5.10225	5.12236

; limit = 5.10

C)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	3.97484	3.99750	3.99975	4.00025	4.00250	4.02485

; limit = 4.0

D)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	1.19245	1.19925	1.19993	1.20007	1.20075	1.20745

; limit = 1.20

35) Let $f(x) = x^2 - 5$, find $\lim_{x \rightarrow 0} f(x)$.

35) _____

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)						

A)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-4.9900	-4.9999	-5.0000	-5.0000	-4.9999	-4.9900

; limit = -5.0

B)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-2.9910	-2.9999	-3.0000	-3.0000	-2.9999	-2.9910

; limit = -3.0

C)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-1.4970	-1.4999	-1.5000	-1.5000	-1.4999	-1.4970

; limit = -15.0

D)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-1.4970	-1.4999	-1.5000	-1.5000	-1.4999	-1.4970

; limit = ∞

36) $\lim_{x \rightarrow 4} f(x)$
Let $f(x) = \frac{x-4}{x^2 - 5x + 4}$, find $\lim_{x \rightarrow 4} f(x)$.

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)						

A)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	0.2448	0.2344	0.2334	0.2332	0.2322	0.2226

; limit = 0.2333

B)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	0.3448	0.3344	0.3334	0.3332	0.3322	0.3226

; limit = 0.3333

C)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	0.4448	0.4344	0.4334	0.4332	0.4322	0.4226

; limit = 0.4333

D)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	-0.3448	-0.3344	-0.3334	-0.3332	-0.3322	-0.3226

; limit = -0.3333

37) $\lim_{x \rightarrow 3} f(x)$
Let $f(x) = \frac{x^2 + 2x - 15}{x^2 - 2x - 3}$, find $\lim_{x \rightarrow 3} f(x)$.

x	2.9	2.99	2.999	3.001	3.01	3.1
f(x)						

A)

x	2.9	2.99	2.999	3.001	3.01	3.1
f(x)	2.1256	2.1025	2.1003	2.0998	2.0975	2.0756

; limit = 2.1

B)

x	2.9	2.99	2.999	3.001	3.01	3.1
f(x)	2.0256	2.0025	2.0003	1.9998	1.9975	1.9756

; limit = 2

C)

x	2.9	2.99	2.999	3.001	3.01	3.1
f(x)	1.9256	1.9025	1.9003	1.8998	1.8975	1.8756

; limit = 1.9

D)

x	2.9	2.99	2.999	3.001	3.01	3.1
f(x)	-0.9048	-0.9900	-0.9990	-1.0010	-1.0101	-1.1053

; limit = -1

38) $\lim_{x \rightarrow 0} f(x)$
Let $f(x) = \frac{\sin(5x)}{x}$, find $\lim_{x \rightarrow 0} f(x)$.

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	4.99791693	4.99791693	4.99791693	4.99791693	4.99791693	4.99791693

38)

- A) limit = 4.5
C) limit = 0

- B) limit does not exist
D) limit = 5

39) $\lim_{\theta \rightarrow 0} \frac{\cos(5\theta)}{\theta}$
Let $f(\theta) = \frac{\cos(5\theta)}{\theta}$, find $\lim_{\theta \rightarrow 0} f(\theta)$.

39) _____

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
$f(\theta)$	-8.7758256					8.7758256

- A) limit does not exist
B) limit = 8.7758256
C) limit = 5
D) limit = 0

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.
Provide an appropriate response.

40) $1 - \frac{x^2}{6} < \frac{x \sin(x)}{2 - 2 \cos(x)} < 1$ hold for all values of x
It can be shown that the inequalities $1 - \frac{x^2}{6} < \frac{x \sin(x)}{2 - 2 \cos(x)} < 1$ hold for all values of x
close to zero. What, if anything, does this tell you about $\frac{x \sin(x)}{2 - 2 \cos(x)}$? Explain.

40) _____

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

- 41) Write the formal notation for the principle "the limit of a quotient is the quotient of the limits" 41) _____
and include a statement of any restrictions on the principle.

A) $\lim_{x \rightarrow a} \frac{g(x)}{f(x)} = \frac{\lim_{x \rightarrow a} g(x)}{\lim_{x \rightarrow a} f(x)}$

B) $\lim_{x \rightarrow a} \frac{g(x)}{f(x)} = \frac{\lim_{x \rightarrow a} g(x)}{\lim_{x \rightarrow a} f(x)}$, provided that $f(a) \neq 0$.

C) If $\lim_{x \rightarrow a} g(x) = M$ and $\lim_{x \rightarrow a} f(x) = L$, then $\lim_{x \rightarrow a} \frac{g(x)}{f(x)} = \frac{\lim_{x \rightarrow a} g(x)}{\lim_{x \rightarrow a} f(x)} = \frac{M}{L}$, provided that $L \neq 0$.

D) If $\lim_{x \rightarrow a} g(x) = M$ and $\lim_{x \rightarrow a} f(x) = L$, then $\lim_{x \rightarrow a} \frac{g(x)}{f(x)} = \frac{\lim_{x \rightarrow a} g(x)}{\lim_{x \rightarrow a} f(x)} = \frac{M}{L}$, provided that $f(a) \neq 0$.

- 42) Provide a short sentence that summarizes the general limit principle given by the formal

$\lim_{x \rightarrow a} [f(x) \pm g(x)] = \lim_{x \rightarrow a} f(x) \pm \lim_{x \rightarrow a} g(x) = L \pm M$, given that $\lim_{x \rightarrow a} f(x) = L$
notation $\lim_{x \rightarrow a} g(x) = M$. and

42) _____

- A) The limit of a sum or a difference is the sum or the difference of the limits.
B) The limit of a sum or a difference is the sum or the difference of the functions.
C) The sum or the difference of two functions is the sum of two limits.
D) The sum or the difference of two functions is continuous.

- 43) The statement "the limit of a constant times a function is the constant times the limit" follows 43) _____
from a combination of two fundamental limit principles. What are they?

- A) The limit of a constant is the constant, and the limit of a product is the product of the limits.
 B) The limit of a function is a constant times a limit, and the limit of a constant is the constant.
 C) The limit of a product is the product of the limits, and the limit of a quotient is the quotient of the limits.
 D) The limit of a product is the product of the limits, and a constant is continuous.

Find the limit.

44) $\lim_{x \rightarrow 18} \sqrt[3]{2}$

A) $3\sqrt[3]{2}$

B) $\sqrt[3]{2}$

C) 2

D) 18

44) _____

45) $\lim_{x \rightarrow -9} (6x^2 - 10)$

A) -44

B) -64

C) 44

D) 64

45) _____

46) $\lim_{x \rightarrow 18} (19x^2 - 3x)$

A) 73

B) -73

C) 35

D) -35

46) _____

Give an appropriate answer.

47) $\lim_{x \rightarrow -3} f(x) = 1$ and $\lim_{x \rightarrow -3} g(x) = -10$. Find $\lim_{x \rightarrow -3} [f(x) \cdot g(x)]$.

A) -3

B) -9

C) 11

D) 1

47) _____

48) $\lim_{x \rightarrow 7} f(x) = 4$ and $\lim_{x \rightarrow 7} g(x) = 5$. Find $\lim_{x \rightarrow 7} [f(x) \cdot g(x)]$.

A) 7

B) 9

C) 5

D) 20

48) _____

49) $\lim_{x \rightarrow -8} f(x) = -7$ and $\lim_{x \rightarrow -8} g(x) = -4$. Find $\lim_{x \rightarrow -8} \frac{f(x)}{g(x)}$.

A) $\frac{4}{7}$

B) $\frac{7}{4}$

C) -3

D) -8

49) _____

50) $\lim_{x \rightarrow -4} f(x) = 121$. Find $\lim_{x \rightarrow -4} \sqrt{f(x)}$.

A) -4

B) 121

C) 3.3166

D) 11

50) _____

51) $\lim_{x \rightarrow 6} f(x) = 2$ and $\lim_{x \rightarrow 6} g(x) = 5$. Find $\lim_{x \rightarrow 6} [f(x) + g(x)]^2$.

A) 49

B) -3

C) 7

D) 29

51) _____

52) $\lim_{x \rightarrow 7} f(x) = 32$. Find $\lim_{x \rightarrow 7} \sqrt[5]{f(x)}$.

A) 7

B) 5

C) 32

D) 2

52) _____

53) $\lim_{x \rightarrow -7} f(x) = 2$ and $\lim_{x \rightarrow -7} g(x) = 3$. Find $\lim_{x \rightarrow -7} \left[\frac{8f(x) - 5g(x)}{4 + g(x)} \right]$.

A) $\frac{31}{7}$

B) $\frac{1}{7}$

C) -7

D) -1

53) _____

Find the limit.

- 54) $\lim_{x \rightarrow 2} (x^3 + 5x^2 - 7x + 1)$ 54) _____
- A) 0 B) 15 C) 29 D) does not exist
- 55) $\lim_{x \rightarrow 2} (2x^5 - 3x^4 - 4x^3 + x^2 - 5)$ 55) _____
- A) 47 B) -49 C) -17 D) 79
- 56) $\lim_{x \rightarrow -1} \frac{x}{3x + 2}$ 56) _____
- A) 1 B) 0 C) $\frac{1}{5}$ D) does not exist
- 57) $\lim_{x \rightarrow 0} \frac{x^3 - 6x + 8}{x - 2}$ 57) _____
- A) Does not exist B) 4 C) 0 D) -4
- 58) $\lim_{x \rightarrow 1} \frac{3x^2 + 7x - 2}{3x^2 - 4x - 2}$ 58) _____
- A) $\frac{7}{4}$ B) 0 C) $\frac{8}{3}$ D) Does not exist
- 59) $\lim_{x \rightarrow -2} (x + 3)^2(x - 1)^3$ 59) _____
- A) -1 B) -25 C) -675 D) -27
- 60) $\lim_{x \rightarrow 5} \sqrt[3]{x^2 + 2x + 1}$ 60) _____
- A) ± 6 B) 6 C) 36 D) does not exist
- 61) $\lim_{x \rightarrow -1} \sqrt[4]{6x + 54}$ 61) _____
- A) $4\sqrt[4]{3}$ B) $-4\sqrt[4]{3}$ C) -48 D) 48
- 62) $\lim_{h \rightarrow 0} \frac{2}{\sqrt{3h + 4} + 2}$ 62) _____
- A) 2 B) 1 C) Does not exist D) 1/2
- 63) $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{x}$ 63) _____
- A) Does not exist B) 0 C) 1/2 D) 1/4
- Determine the limit by sketching an appropriate graph.**
- 64) $\lim_{x \rightarrow 6^-} f(x)$, where $f(x) = \begin{cases} -2x - 6 & \text{for } x < 6 \\ 4x - 5 & \text{for } x \geq 6 \end{cases}$ 64) _____
- A) -5 B) 19 C) -18 D) -4
- 65) $\lim_{x \rightarrow 6^+} f(x)$, where $f(x) = \begin{cases} -4x - 3 & \text{for } x < 6 \\ 5x - 2 & \text{for } x \geq 6 \end{cases}$ 65) _____
- A) 28 B) -27 C) -1 D) -2

66) $\lim_{x \rightarrow 4^+} f(x)$, where $f(x) = \begin{cases} x^2 + 4 & \text{for } x \neq 4 \\ 0 & \text{for } x = 4 \end{cases}$ 66) _____

A) 0 B) 12 C) 20 D) 16

67) $\lim_{x \rightarrow 5^-} f(x)$, where $f(x) = \begin{cases} \sqrt{16 - x^2} & 0 \leq x < 4 \\ 4 & 4 \leq x < 5 \\ 5 & x = 5 \end{cases}$ 67) _____

A) Does not exist B) 5 C) 4 D) 0

68) $\lim_{x \rightarrow -7^+} f(x)$, where $f(x) = \begin{cases} x & -7 \leq x < 0, \text{ or } 0 < x \leq 3 \\ 1 & x = 0 \\ 0 & x < -7 \text{ or } x > 3 \end{cases}$ 68) _____

A) -0 B) Does not exist C) 7 D) -7

Find the limit, if it exists.

69) $\lim_{x \rightarrow 0} \frac{x^3 + 12x^2 - 5x}{5x}$ 69) _____

A) -1 B) Does not exist C) 5 D) 0

70) $\lim_{x \rightarrow 1} \frac{x^4 - 1}{x - 1}$ 70) _____

A) 2 B) 4 C) 0 D) Does not exist

71) $\lim_{x \rightarrow 10} \frac{x^2 - 100}{x - 10}$ 71) _____

A) 10 B) 1 C) Does not exist D) 20

72) $\lim_{x \rightarrow -9} \frac{x^2 + 17x + 72}{x + 9}$ 72) _____

A) Does not exist B) -1 C) 306 D) 17

73) $\lim_{x \rightarrow 5} \frac{x^2 + 3x - 40}{x - 5}$ 73) _____

A) 0 B) Does not exist C) 13 D) 3

74) $\lim_{x \rightarrow 2} \frac{x^2 + 2x - 8}{x^2 - 4}$ 74) _____

A) $\frac{1}{2}$ B) Does not exist C) 0 D) $\frac{3}{2}$

75) $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x^2 - 7x + 12}$ 75) _____

A) -6 B) Does not exist C) 0 D) -3

76) $\lim_{x \rightarrow 2} \frac{x^2 - 5x + 6}{x^2 + 3x - 10}$ 76) _____

A) $\frac{1}{7}$ B) $\frac{1}{7}$ C) $\frac{5}{7}$ D) Does not exist

77) $\lim_{h \rightarrow 0} \frac{(x+h)^3 - x^3}{h}$

77) _____

A) Does not exist

B) $3x^2$

C) $3x^2 + 3xh + h^2$

D) 0

78) $\lim_{x \rightarrow 9} \frac{|9-x|}{9-x}$

78) _____

A) Does not exist

B) 1

C) 0

D) -1

Provide an appropriate response.

79)

$$\left(\frac{1}{x}\right)$$

79) _____

It can be shown that the inequalities $-x \leq x \cos\left(\frac{1}{x}\right) \leq x$ hold for all values of $x \geq 0$.

Find $\lim_{x \rightarrow 0} x \cos\left(\frac{1}{x}\right)$ if it exists.

A) 1

B) 0

C) does not exist

D) 0.0007

80) $\lim_{x \rightarrow 0} \frac{x^2}{2} - \frac{\sin x}{x}$

80) _____

The inequality $1 - \frac{x^2}{2} < \frac{\sin x}{x} < 1$ holds when x is measured in radians and $|x| < 1$.

Find $\lim_{x \rightarrow 0} \frac{\sin x}{x}$ if it exists.

A) 1

B) 0

C) does not exist

D) 0.0007

81) If $x^3 \leq f(x) \leq x$ for x in $[-1, 1]$, find $\lim_{x \rightarrow 0} f(x)$ if it exists.

81) _____

A) -1

B) 0

C) 1

D) does not exist

Compute the values of $f(x)$ and use them to determine the indicated limit.

82) If $f(x) = x^2 + 8x - 2$, find $\lim_{x \rightarrow 2} f(x)$.

82) _____

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)						

A)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	5.043	5.364	5.396	5.404	5.436	5.763

; limit = ∞

B)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	16.692	17.592	17.689	17.710	17.808	18.789

; limit = 17.70

C)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	16.810	17.880	17.988	18.012	18.120	19.210

; limit = 18.0

D)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	5.043	5.364	5.396	5.404	5.436	5.763

; limit = 5.40

83) If $f(x) = \frac{x^4 - 1}{x - 1}$, find $\lim_{x \rightarrow 1} f(x)$.

83)

x	0.9
f(x)	

A)

x	0.9	0.99	0.999	1.001	1.01	1.1
f(x)	1.032	1.182	1.198	1.201	1.218	1.392

; limit = 1.210

B)

x	0.9	0.99	0.999	1.001	1.01	1.1
f(x)	1.032	1.182	1.198	1.201	1.218	1.392

; limit = ∞

C)

x	0.9	0.99	0.999	1.001	1.01	1.1
f(x)	4.595	5.046	5.095	5.105	5.154	5.677

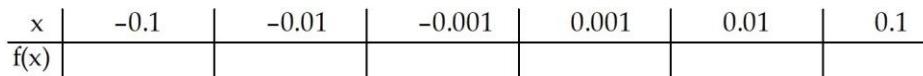
; limit = 5.10

D)

x	0.9	0.99	0.999	1.001	1.01	1.1
f(x)	3.439	3.940	3.994	4.006	4.060	4.641

; limit = 4.0

84) If $f(x) = \frac{x^3 - 6x + 8}{x - 2}$, find $\lim_{x \rightarrow 0} f(x)$.



84) _____

A)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-1.22843	-1.20298	-1.20030	-1.19970	-1.19699	-1.16858

; limit = ∞

B)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-1.22843	-1.20298	-1.20030	-1.19970	-1.19699	-1.16858

; limit = -1.20

C)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-2.18529	-2.10895	-2.10090	-2.99910	-2.09096	-2.00574

; limit = -2.10

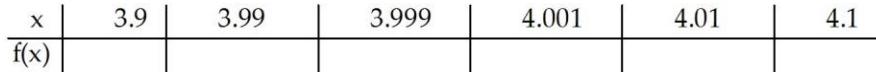
D)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-4.09476	-4.00995	-4.00100	-3.99900	-3.98995	-3.89526

; limit = -4.0

85) If $f(x) = \frac{x - 4}{\sqrt{x - 2}}$, find $\lim_{x \rightarrow 4} f(x)$.

85) _____



A)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	1.19245	1.19925	1.19993	1.20007	1.20075	1.20745

; limit = ∞

B)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	3.97484	3.99750	3.99975	4.00025	4.00250	4.02485

; limit = 4.0

C)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	5.07736	5.09775	5.09978	5.10022	5.10225	5.12236

; limit = 5.10

D)

x	3.9	3.99	limit	3.999	4.001	4.01	4.1
f(x)	1.19245	1.19925	1.19993	1.20007	1.20075	1.20745	

86) If $f(x) = x^2 - 5$, find $\lim_{x \rightarrow 0} f(x)$.

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)						

A)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-4.9900	-4.9999	-5.0000	-5.0000	-4.9999	-4.9900

; limit = -5.0

B)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-1.4970	-1.4999	-1.5000	-1.5000	-1.4999	-1.4970

; limit = -15.0

C)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-1.4970	-1.4999	-1.5000	-1.5000	-1.4999	-1.4970

; limit = ∞

D)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-2.9910	-2.9999	-3.0000	-3.0000	-2.9999	-2.9910

; limit = -3.0

87) If $f(x) = \frac{\sqrt{x+1}}{x+1}$, find $\lim_{x \rightarrow 1} f(x)$.

x	0.9	0.99	0.999	1.001	1.01	1.1
f(x)						

A)

x	0.9	0.99	0.999	1.001	1.01	1.1
f(x)	0.72548	0.70888	0.70728	0.70693	0.70535	0.69007

; limit = 0.7071

B)

x	0.9	0.99	0.999	1.001	1.01	1.1
f(x)	0.21764	0.21266	0.21219	0.21208	0.21160	0.20702

; limit = ∞

C)

x	0.9	0.99	0.999	1.001	1.01	1.1
f(x)	0.21764	0.21266	0.21219	0.21208	0.21160	0.20702

; limit = 0.21213

D)

x	0.9	0.99	0.999	1.001	1.01	1.1
f(x)	2.15293	2.13799	2.13656	2.13624	2.13481	2.12106

; limit = 2.13640

88) If $f(x) = \sqrt{x} - 2$, find $\lim_{x \rightarrow 4} f(x)$.

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)						

A)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	3.9000	2.9000	1.9000	2.0000	3.0000	4.0000

; limit = ∞

B)

x	3.9	3.99	limit 3.999	4.001	4.01	4.1
f(x)	3.9000	2.9000	1.9000	2.0000	3.0000	4.0000

C)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	1.47736	1.49775	1.49977	1.50022	1.50225	1.52236

; limit = 1.50

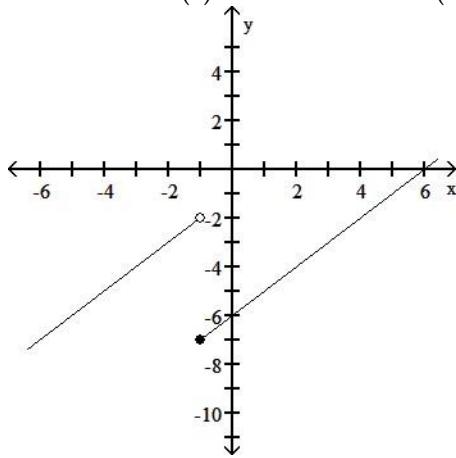
D)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	-0.02516	-0.00250	-0.00025	0.00025	0.00250	0.02485

; limit = 0

For the function f whose graph is given, determine the limit.

89) $\lim_{x \rightarrow -1^-} f(x)$ and $\lim_{x \rightarrow -1^+} f(x)$.



A) -5; -2

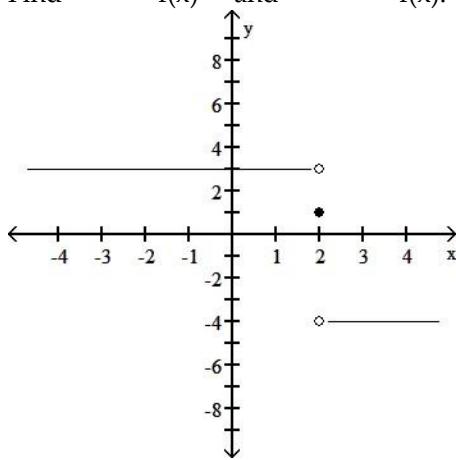
B) -7; -5

C) -2; -7

D) -7; -2

89) _____

90) $\lim_{x \rightarrow 2^-} f(x)$ and $\lim_{x \rightarrow 2^+} f(x)$.



A) does not exist; does not exist

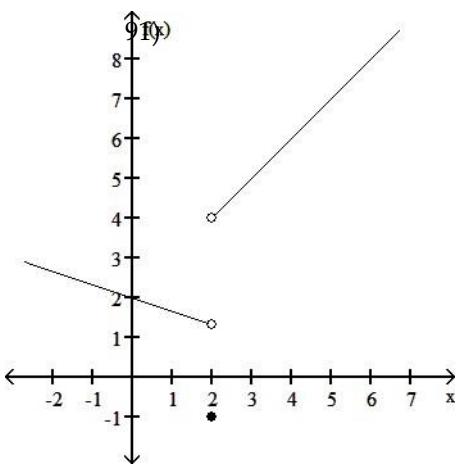
B) 1; 1

C) -4; 3

D) 3; -4

90) _____

91) $\lim_{x \rightarrow 2^+} f(x)$.



A) 5

B) 1.3

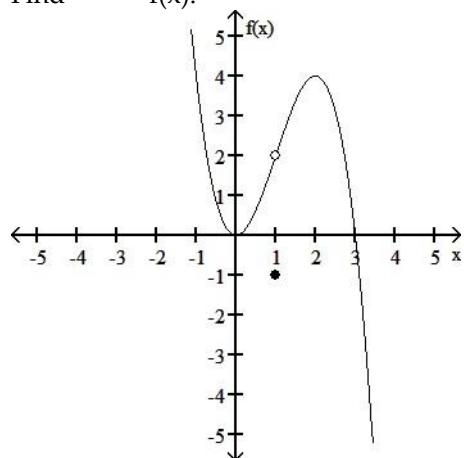
C) -1

D) 4

—
—

92) Find $\lim_{x \rightarrow 1^-} f(x)$.

92) _____



A) 2

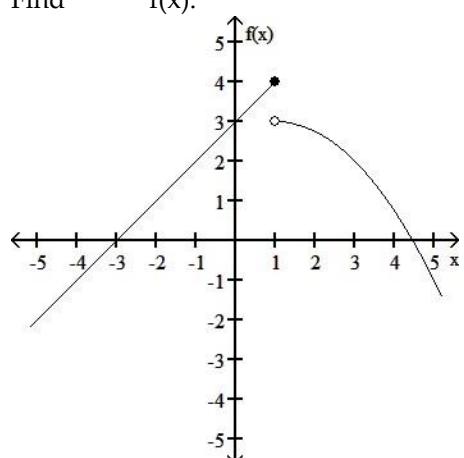
B) $\frac{1}{2}$

C) -1

D) does not exist

93) Find $\lim_{x \rightarrow 1^+} f(x)$.

93) _____



A) $3\frac{1}{2}$

B) does not exist

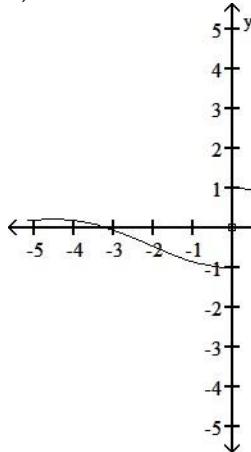
C) 3

D) 4

94)

Fin

94) $\lim_{x \rightarrow 0} f(x)$



A) 1

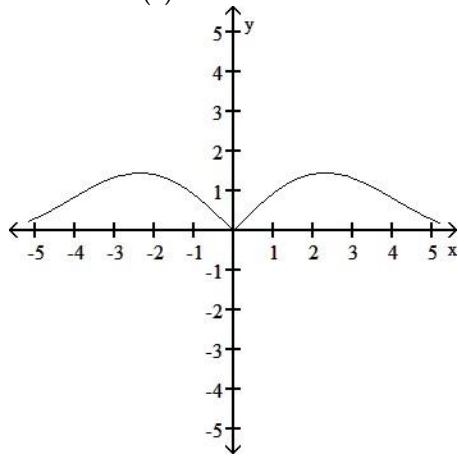
B) does not exist

C) -1

D) 0

—
—

95) Find $\lim_{x \rightarrow 0} f(x)$.



A) 2

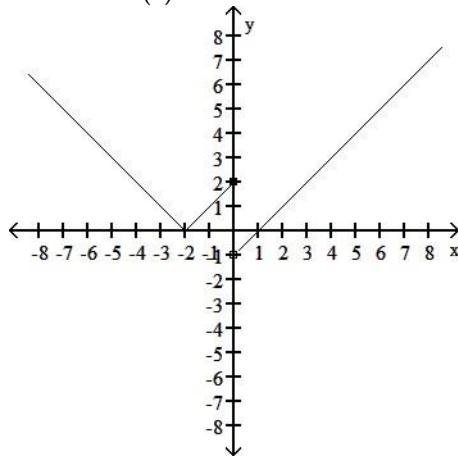
B) 0

C) does not exist

D) -2

95) _____

96) Find $\lim_{x \rightarrow 0} f(x)$.



A) 0

B) does not exist

C) 2

D) -2

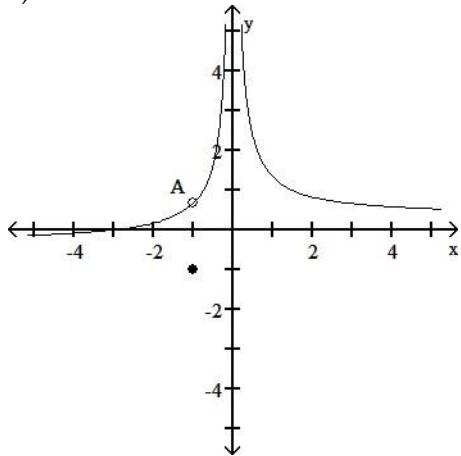
96) _____

97)

Fin d

97) $\lim_{x \rightarrow -1} f(x)$

x).



A) -1

B) $\frac{2}{3}$

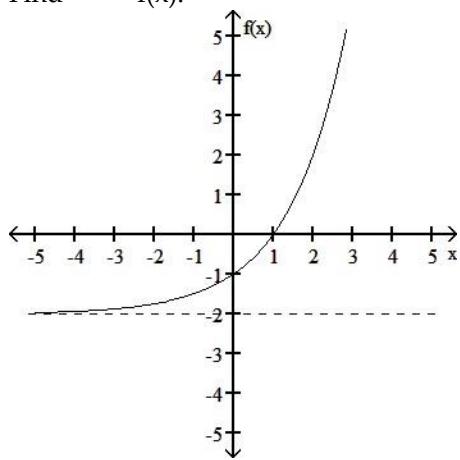
C) does not exist

D) $\frac{2}{3}$

—
—

98) $\lim_{x \rightarrow \infty} f(x)$
Find $f(x)$.

98) _____



A) -2

B) ∞

C) 0

D) does not exist

Find the limit.

99) $\lim_{x \rightarrow -2} \frac{1}{x+2}$

99) _____

A) Does not exist

B) $-\infty$

C) 1/2

D) ∞

100) $\lim_{x \rightarrow -3^-} \frac{1}{x+3}$

100) _____

A) ∞

B) 0

C) $-\infty$

D) -1

101) $\lim_{x \rightarrow 7^+} \frac{1}{(x-7)^2}$

101) _____

A) ∞

B) -1

C) 0

D) $-\infty$

102) $\lim_{x \rightarrow -4^-} \frac{5}{x^2 - 16}$

102) _____

- A) 0 B) $-\infty$ C) -1 D) ∞

103) $\lim_{x \rightarrow 3^+} \frac{2}{x^2 - 9}$

- A) $-\infty$ B) ∞ C) 1 D) 0

103) _____

104) $\lim_{x \rightarrow (\pi/2)^+} \tan x$

- A) ∞ B) 1 C) $-\infty$ D) 0

104) _____

105) $\lim_{x \rightarrow (-\pi/2)^-} \sec x$

- A) $-\infty$ B) 1 C) ∞ D) 0

105) _____

106) $\lim_{x \rightarrow 0^+} (1 + \csc x)$

- A) ∞ B) 1 C) 0 D) Does not exist

106) _____

107) $\lim_{x \rightarrow 0} (1 - \cot x)$

- A) $-\infty$ B) 0 C) ∞ D) Does not exist

107) _____

108) $\lim_{x \rightarrow 1^-} \frac{x^2 - 4x + 3}{x^3 - x}$

- A) -1 B) 0 C) $-\infty$ D) ∞

108) _____

109) $\lim_{x \rightarrow 4^+} \frac{x^2 - 6x + 8}{x^3 - 4x}$

- A) Does not exist B) $-\infty$ C) 0 D) ∞

109) _____

Find all vertical asymptotes of the given function.

110) $g(x) = \frac{9x}{x - 1}$

- A) $x = -1$ B) $x = 1$ C) none D) $x = 9$

110) _____

111) $g(x) = \frac{x + 9}{x^2 - 4}$

- A) $x = -4, x = -9$ B) $x = -2, x = 2$
C) $x = 0, x = -4$ D) $x = -2, x = 2, x = -9$

111) _____

112) $f(x) = \frac{x + 6}{x^2 + 25}$

- A) none B) $x = -5, x = 5$
C) $x = -5, x = -6$ D) $x = -5, x = 5, x = -6$

112) _____

113) $g(x) = \frac{x + 11}{x^2 - 36x}$

- A) $x = 0, x = 36$ B) $x = 36, x = -11$

113) _____

C) $x = -6, x = 6$

D) $x = 0, x = -6, x = 6$

114) $f(x) = \frac{x(x-1)}{x^3 + 4x}$

- A) $x = -2, x = 2$
C) $x = 0$

114) _____

- B) $x = 0, x = -2, x = 2$
D) $x = 0, x = -4$

115) $R(x) = \frac{-3x^2}{x^2 + 4x - 21}$

- A) $x = 7, x = -3$
C) $x = -7, x = 3, x = -3$

115) _____

- B) $x = -7, x = 3$
D) $x = -21$

116) $R(x) = \frac{x-1}{x^3 + 4x^2 - 45x}$

- A) $x = -5, x = 0, x = 9$
C) $x = -5, x = -30, x = 9$

116) _____

- B) $x = -9, x = 0, x = 5$
D) $x = -9, x = 5$

117) $f(x) = \frac{-2x(x+2)}{4x^2 - 5x - 9}$

A) $x = \frac{9}{4}, x = -1$

B) $x = -\frac{4}{9}, x = 1$

C) $x = -\frac{9}{4}, x = 1$

D) $x = \frac{4}{9}, x = -1$

117) _____

118) $f(x) = \frac{x-7}{49x - x^3}$

- A) $x = 0, x = -7, x = 7$
C) $x = 0, x = -7$

- B) $x = 0, x = -7$
D) $x = -7, x = 7$

118) _____

119) $f(x) = \frac{-x^2 + 16}{x^2 + 5x + 4}$

A) $x = -1, x = 4$

B) $x = 1, x = -4$

C) $x = -1, x = -4$

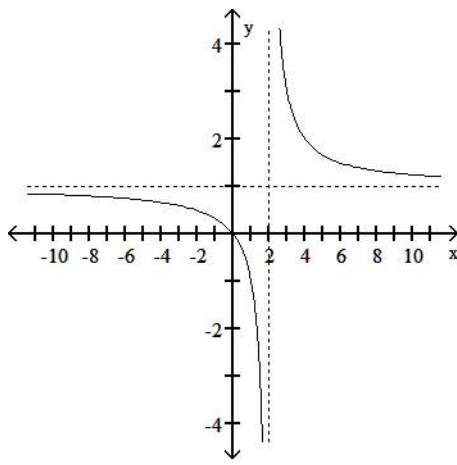
D) $x = -1$

119) _____

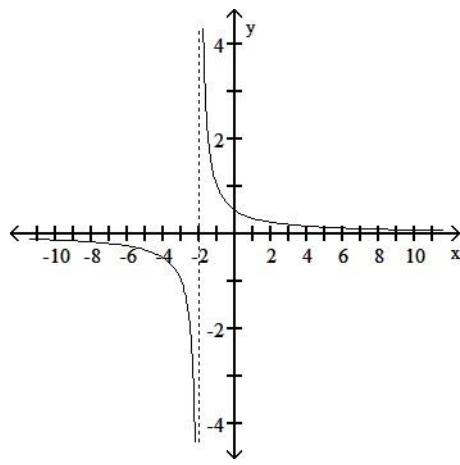
Choose the graph that represents the given function without using a graphing utility.

120) $f(x) = \frac{x}{x+2}$

A)

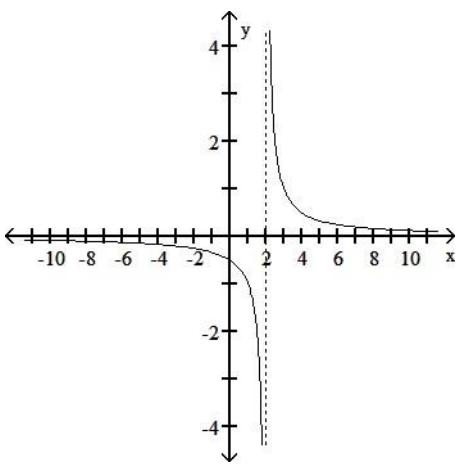


B)

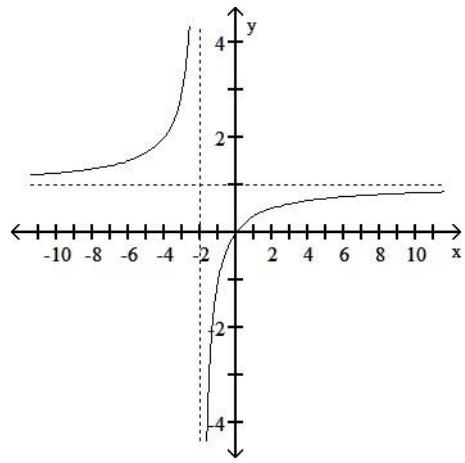


120) _____

C)

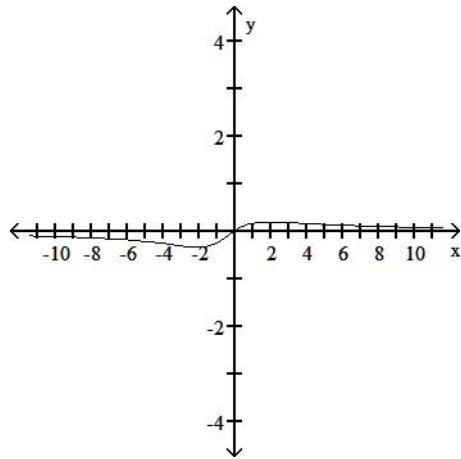


D)

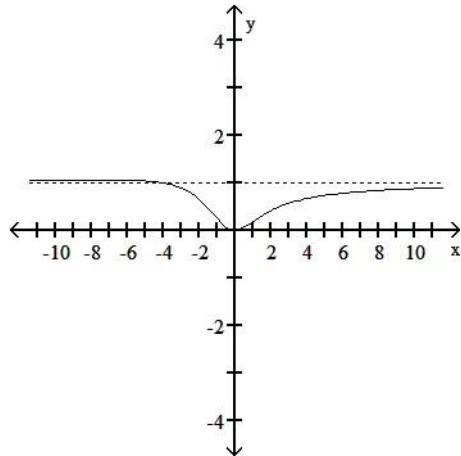


121) $f(x) = \frac{x}{x^2 + x + 4}$

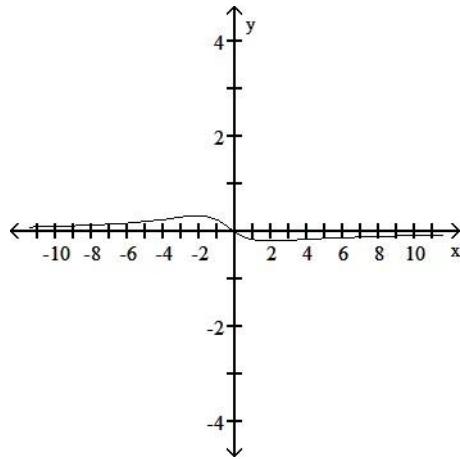
A)



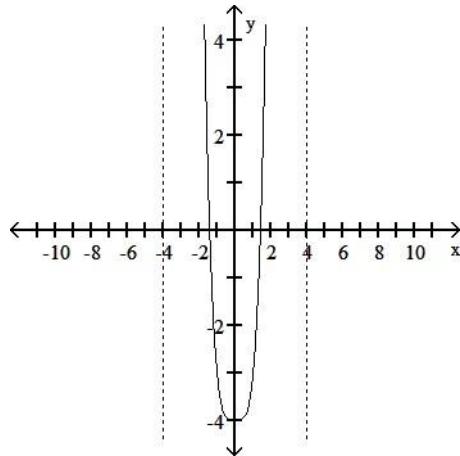
C)



B)



D)

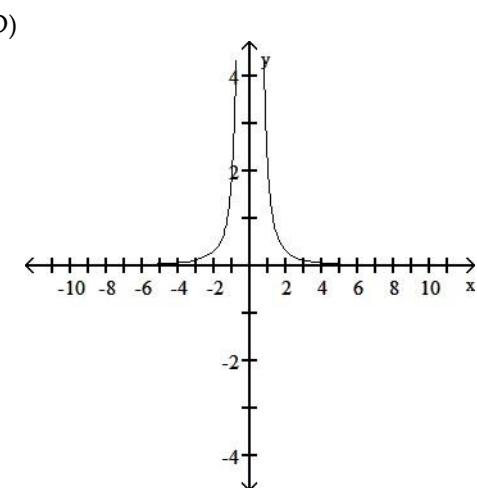
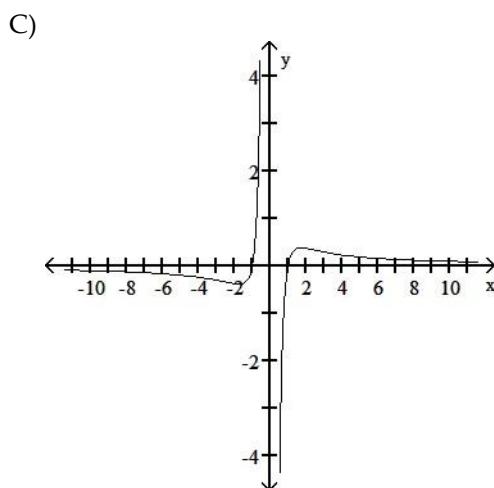
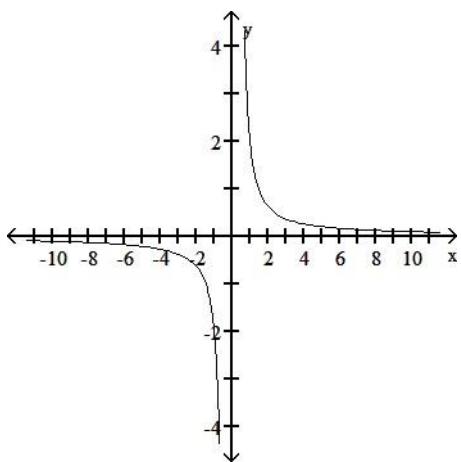
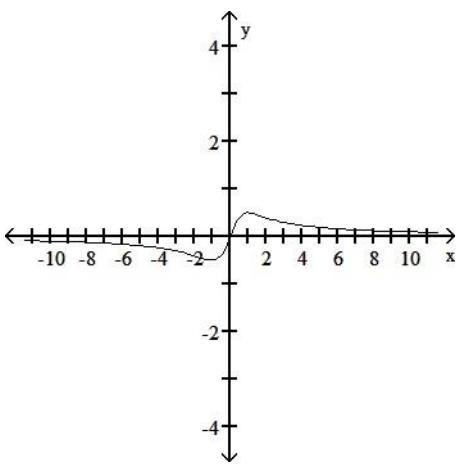


121) _____

122) $f(x) = \frac{x^2 + 1}{x^3}$

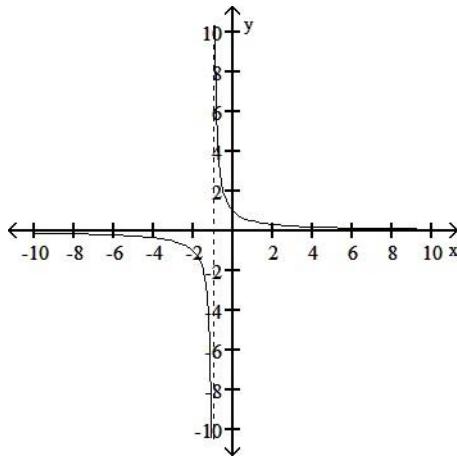
A)

122) _____



123) $f(x) = \frac{1}{x+1}$

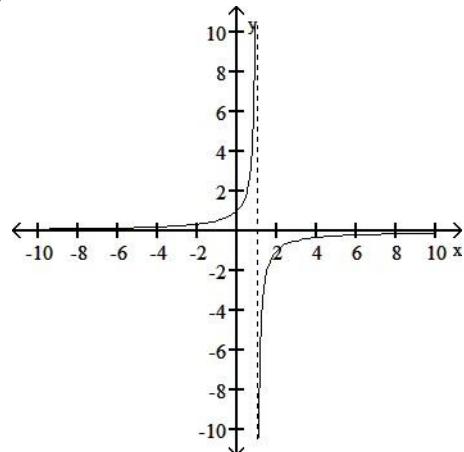
A)

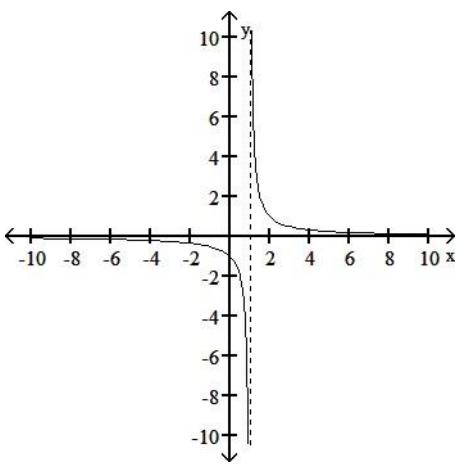


C)

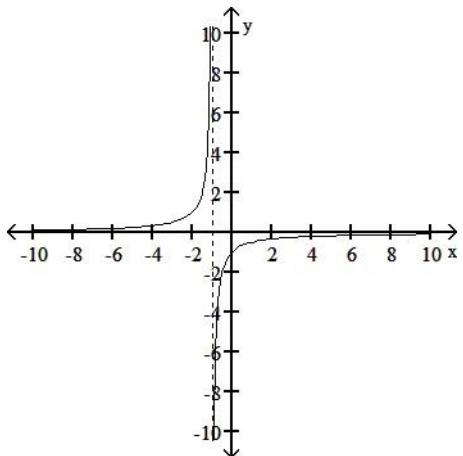
123) _____

B)



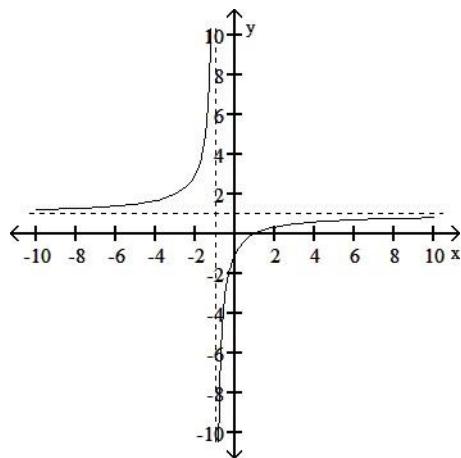


D)

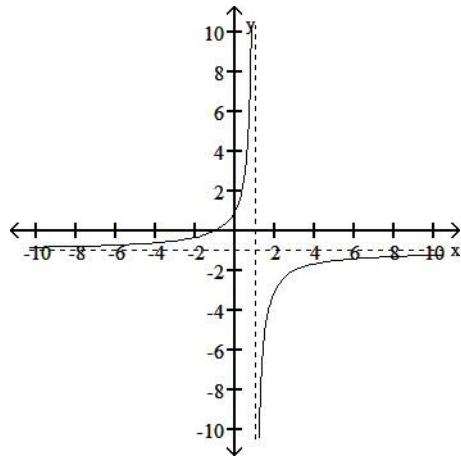


124) $f(x) = \frac{x-1}{x+1}$

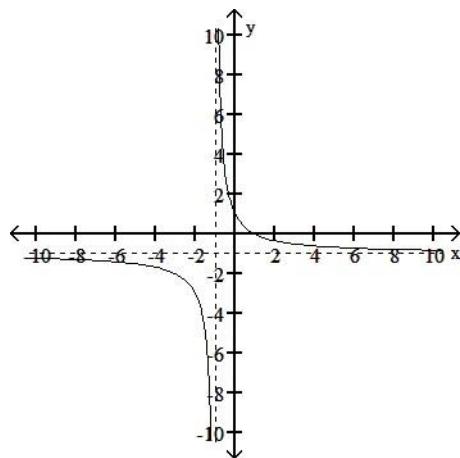
A)



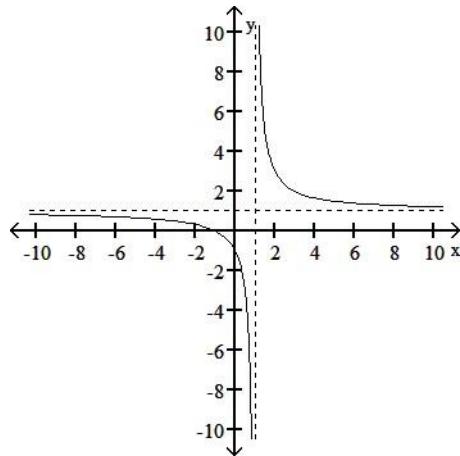
C)



B)



D)

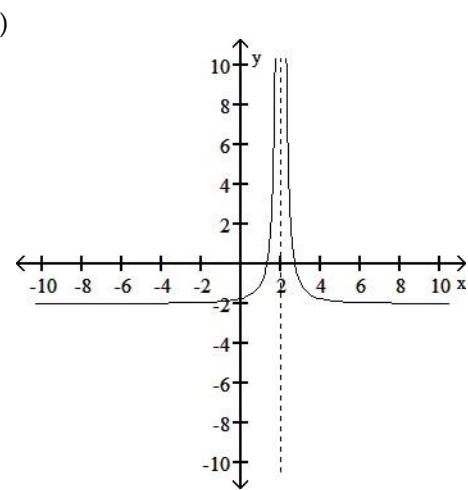
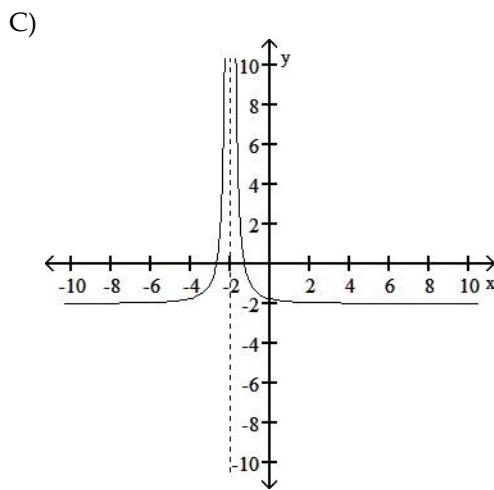
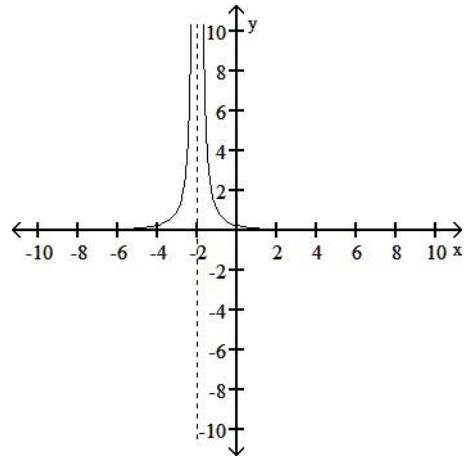
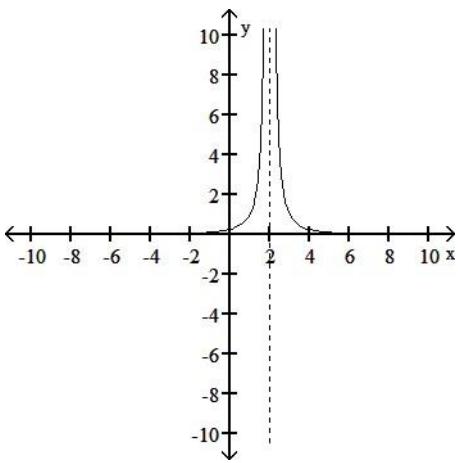


124) _____

125) $f(x) = \frac{1}{(x+2)^2}$

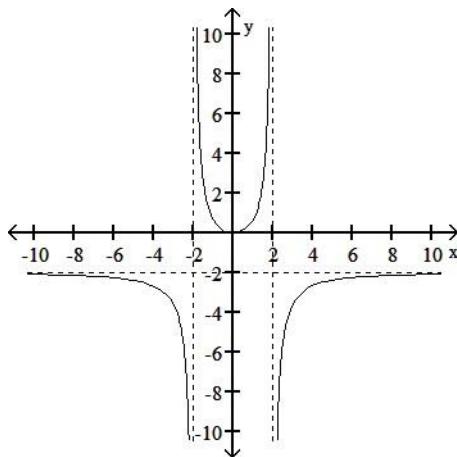
A)

125) _____



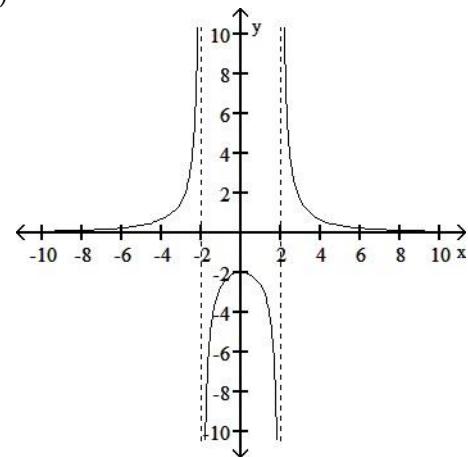
126) $f(x) = \frac{2x^2}{4 - x^2}$

A)

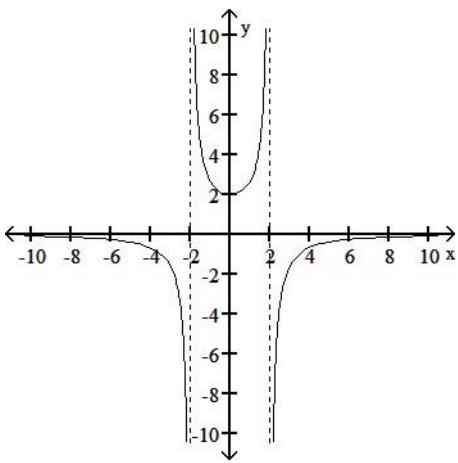


C)

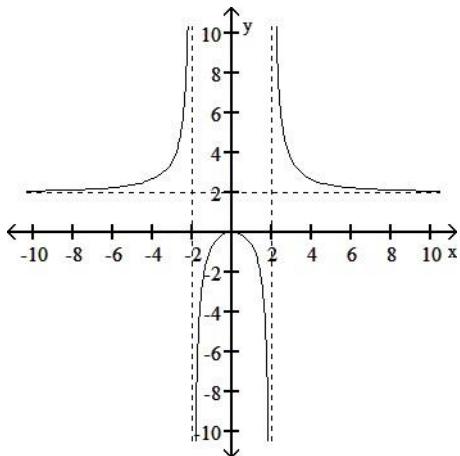
B)



126) _____



D)

**Find the limit.**

127) $\lim_{x \rightarrow \infty} \frac{7}{x}$

A) -8

B) 6

C) 1

127) _____

128) $\lim_{x \rightarrow -\infty} \frac{5}{5 - (9/x^2)}$

A) $\frac{5}{4}$

B) 1

C) $-\infty$

D) 5

128) _____

129) $\lim_{x \rightarrow -\infty} \frac{-5 + (5/x)}{7 - (1/x^2)}$

A) ∞ B) $\frac{5}{7}$ C) $-\infty$ D) $\frac{5}{7}$

129) _____

130) $\lim_{x \rightarrow \infty} \frac{x^2 - 7x + 9}{x^3 - 6x^2 + 14}$

A) 1

B) $\frac{9}{14}$

C) 0

D) ∞

130) _____

131) $\lim_{x \rightarrow -\infty} \frac{-4x^2 - 3x + 6}{-18x^2 - 4x + 9}$

A) 1

B) ∞ C) $\frac{2}{9}$ D) $\frac{2}{3}$

131) _____

132) $\lim_{x \rightarrow \infty} \frac{2x + 1}{15x - 7}$

A) 0

B) $\frac{1}{7}$ C) $\frac{2}{15}$ D) ∞

132) _____

133) $\lim_{x \rightarrow \infty} \frac{9x^3 - 5x^2 + 3x}{-x^3 - 2x + 6}$

A) 9

B) -9

C) ∞

D)

133) _____

$\frac{3}{2}$

134) $\lim_{x \rightarrow -\infty} \frac{2x^3 + 4x^2}{x - 6x^2}$

A) $-\infty$

B) 2

C) ∞

D) $\frac{2}{3}$

134) _____

135) $\lim_{x \rightarrow -\infty} \frac{\cos 4x}{x}$

A) 4

B) 1

C) 0

D) $-\infty$

135) _____

Divide numerator and denominator by the highest power of x in the denominator to find the limit.

136) $\lim_{x \rightarrow \infty} \sqrt{\frac{25x^2}{6 + 16x^2}}$

A) $\frac{5}{4}$

B) does not exist

C) $\frac{25}{6}$

D) $\frac{25}{16}$

136) _____

137) $\lim_{x \rightarrow \infty} \sqrt{\frac{36x^2 + x - 3}{(x - 13)(x + 1)}}$

A) 0

B) 36

C) 6

D) ∞

137) _____

138) $\lim_{x \rightarrow \infty} \frac{5\sqrt{x} + x^{-1}}{4x + 3}$

A) ∞

B) $\frac{1}{4}$

C) $\frac{5}{4}$

D) 0

138) _____

139) $\lim_{x \rightarrow \infty} \frac{-5x^{-1} - 4x^{-3}}{-3x^{-2} + x^{-5}}$

A) $-\infty$

B) ∞

C) $\frac{5}{3}$

D) 0

139) _____

140) $\lim_{x \rightarrow -\infty} \frac{\sqrt[3]{x + 3x + 5}}{6x + x^{2/3} + 7}$

A) 0

B) $\frac{1}{2}$

C) $-\infty$

D) 2

140) _____

141) $\lim_{t \rightarrow \infty} \frac{\sqrt{81t^2 - 729}}{t - 9}$

A) does not exist

B) 729

C) 81

D) 9

141) _____

142) $\lim_{t \rightarrow \infty} \frac{\sqrt{81t^2 - 729}}{t - 9}$

A) 9

B) does not exist

C) 81

D) 729

142) _____

143) $\lim_{x \rightarrow \infty} \frac{5x + 6}{\sqrt{6x^2 + 1}}$

143) _____

A) 0

B) ∞ C) $\frac{5}{6}$ D) $\frac{5}{\sqrt{6}}$ **Find all horizontal asymptotes of the given function, if any.**

144)
$$h(x) = \frac{8x - 4}{x - 2}$$

- A) $y = 8$
C) $y = 0$

144) _____

- B) $y = 2$
D) no horizontal asymptotes

145)
$$h(x) = 8 - \frac{5}{x}$$

- A) $y = 5$
C) $x = 0$

145) _____

- B) $y = 8$
D) no horizontal asymptotes

146)
$$g(x) = \frac{x^2 + 2x - 8}{x - 8}$$

- A) $y = 8$
C) $y = 0$

146) _____

- B) $y = 1$
D) no horizontal asymptotes

147)
$$h(x) = \frac{9x^2 - 2x - 2}{4x^2 - 6x + 7}$$

- A) $y = \frac{1}{3}$
y =
C) $y = 0$

- B) $y = \frac{9}{4}$
y =
D) no horizontal asymptotes

147) _____

148)
$$h(x) = \frac{3x^4 - 3x^2 - 4}{5x^5 - 7x + 9}$$

- A) $y = \frac{3}{5}$
y =
C) $y = 0$

- B) $y = \frac{3}{7}$
y =
D) no horizontal asymptotes

148) _____

149)
$$h(x) = \frac{9x^3 - 8x}{3x^3 - 5x + 2}$$

- A) $y = 0$
C) $y = 3$

- B) $y = \frac{8}{5}$
y =
D) no horizontal asymptotes

149) _____

150)
$$h(x) = \frac{3x^3 - 9x - 3}{9x^2 + 3}$$

- A) $y = 3$
C) $y = 0$

- B) $y = \frac{1}{3}$
y =
D) no horizontal asymptotes

150) _____

151)
$$f(x) = \frac{8x + 1}{x^2 - 4}$$

- A) $y = 8$
C) $y = -2, y = 2$

- B) no horizontal asymptotes
D) $y = 0$

151) _____

152) $R(x) = \frac{-3x^2 + 1}{x^2 + 4x - 12}$

- A) $y = -6, y = 2$
B) $y = 0$
C) $y = -3$

- D) no horizontal asymptotes

152) _____

153) $f(x) = \frac{x^2 - 2}{4x - x^4}$

- A) $y = -2, y = 2$
B) $y = -1$
C) no horizontal asymptotes

- D) $y = 0$

153) _____

154) $f(x) = \frac{4x^4 + x^2 - 2}{x - x^3}$

- A) $y = -4$
B) $y = 0$
C) $y = -1, y = 1$

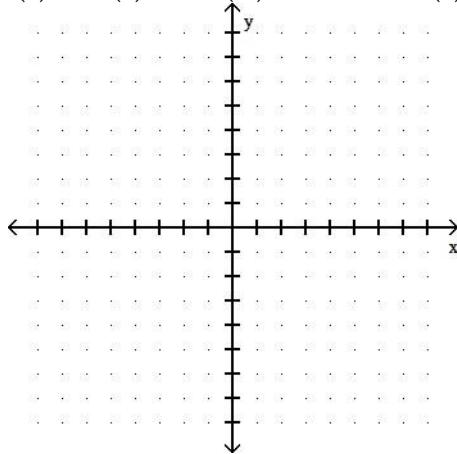
- D) no horizontal asymptotes

154) _____

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

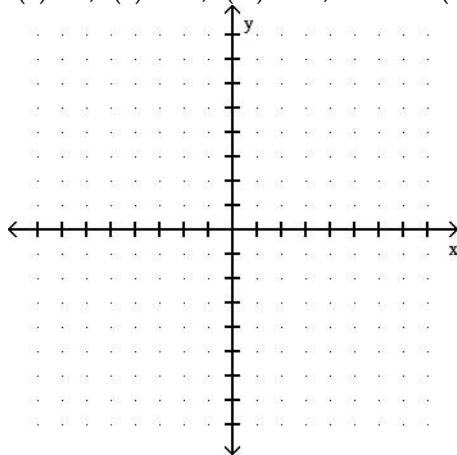
Sketch the graph of a function $y = f(x)$ that satisfies the given conditions.

155) $f(0) = 0, f(1) = 6, f(-1) = -6, \lim_{x \rightarrow -\infty} f(x) = -5, \lim_{x \rightarrow \infty} f(x) = 5.$



155) _____

156) $f(0) = 0, f(1) = 4, f(-1) = -4, \lim_{x \rightarrow \pm\infty} f(x) = -4.$



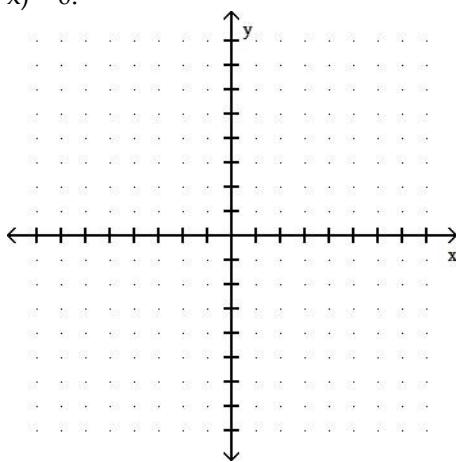
156) _____

157)

$f(0) = 4, f(1) = -4,$

$$f(-1) = -4, \quad 157)$$

$$\lim_{x \rightarrow \pm\infty} f(x) = 0.$$

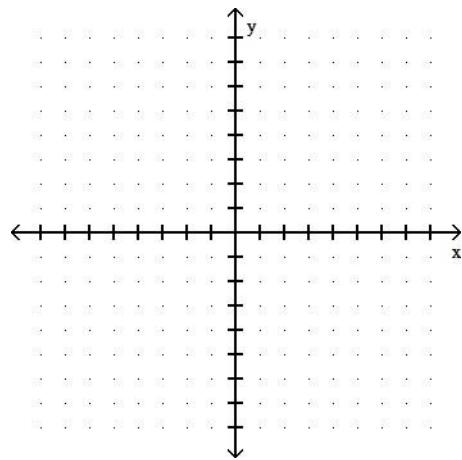


158)

$$f(0) = 0, \quad \lim_{x \rightarrow \pm\infty} f(x) = 0, \quad \lim_{x \rightarrow 3^-} f(x) = -\infty, \quad \lim_{x \rightarrow -3^+} f(x) = -\infty, \quad \lim_{x \rightarrow 3^+} f(x) = \infty,$$

$$\lim_{x \rightarrow -3^-} f(x) = \infty.$$

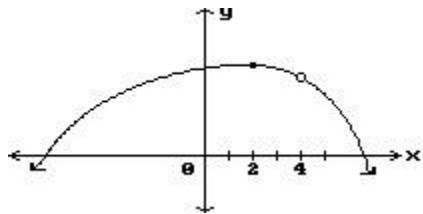
158) _____



MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find all points where the function is discontinuous.

159)



159) _____

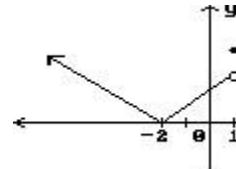
A) None

B) $x = 4$

C) $x = 4, x = 2$

D) $x = 2$

160)



160)

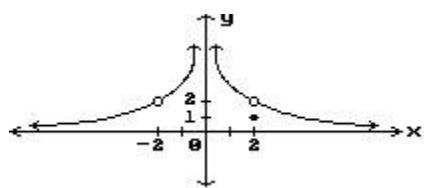
A) $x = -2$

B) $x = -2, x = 1$

C) $x = 1$

D) None

161)

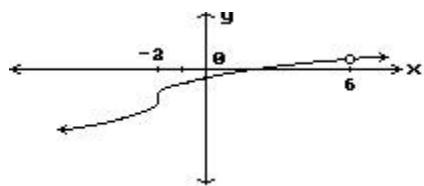


- A) $x = -2, x = 0, x = 2$
 C) $x = 2$

- B) $x = 0, x = 2$
 D) $x = -2, x = 0$

161) _____

162)

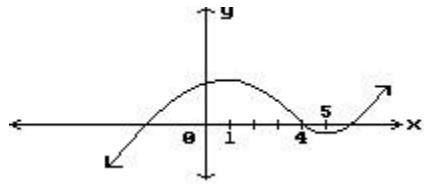


- A) $x = -2, x = 6$
 B) None

- C) $x = 6$
 D) $x = -2$

162) _____

163)

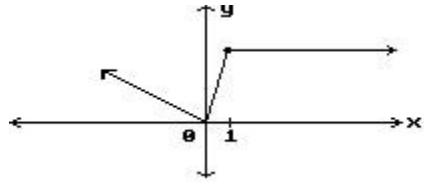


- A) None
 C) $x = 1, x = 4, x = 5$

- B) $x = 4$
 D) $x = 1, x = 5$

163) _____

164)

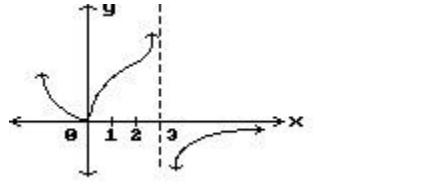


- A) None
 B) $x = 0$

- C) $x = 0, x = 1$
 D) $x = 1$

164) _____

165)

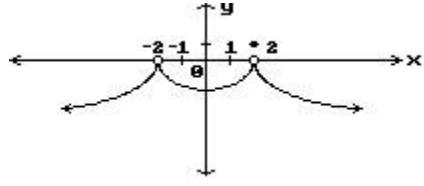


- A) $x = 3$
 B) $x = 0$

- C) $x = 0, x = 3$
 D) None

165) _____

166)

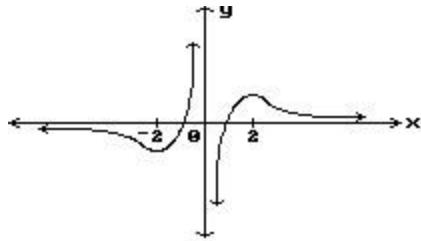


- A) $x = -2, x = 2$
 B) $x = -2$

- C) None
 D) $x = 2$

166) _____

167)



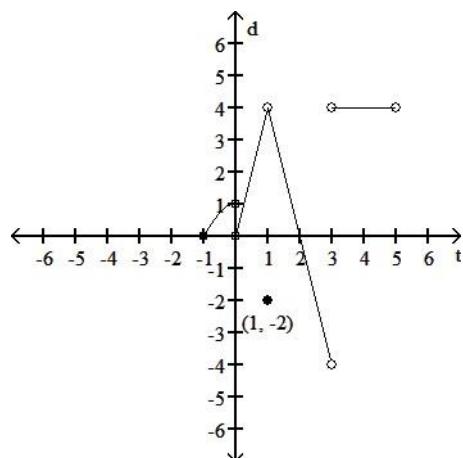
- A) None
B) $x = -2, x = 0, x = 2$
C) $x = -2, x = 2$
D) $x = 0$

167) _____

Provide an appropriate response.168) Is f continuous at $f(1)$?

$$f(x) = \begin{cases} -x^2 + 1, & -1 \leq x < 0 \\ 4x, & 0 < x < 1 \\ -2, & x = 1 \\ -4x + 8 & 1 < x < 3 \\ 4, & 3 < x < 5 \end{cases}$$

- A) No



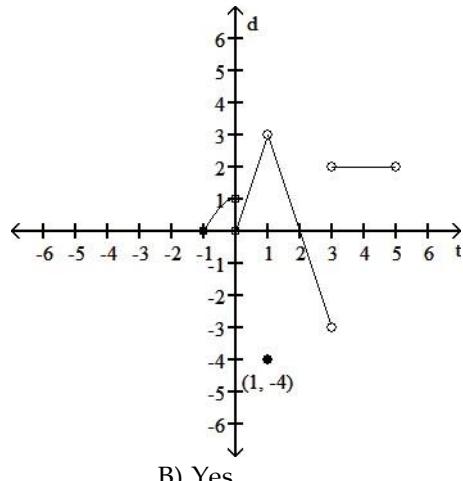
- B) Yes

168) _____

169) Is f continuous at $f(3)$?

$$f(x) = \begin{cases} -x^2 + 1, & -1 \leq x < 0 \\ 3x, & 0 < x < 1 \\ -4, & x = 1 \\ -3x + 6 & 1 < x < 3 \\ 2, & 3 < x < 5 \end{cases}$$

- A) No



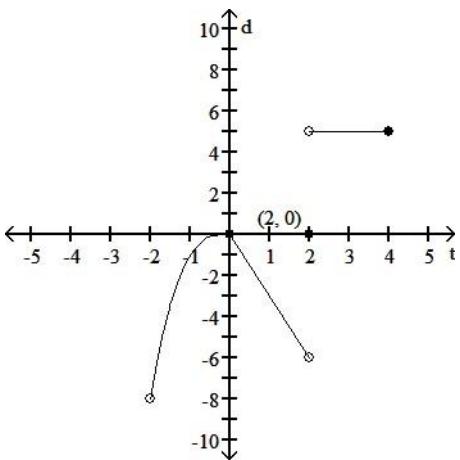
- B) Yes

169) _____

170) Is f continuous at $x = 0$?

170)

$$f(x) = \begin{cases} x^3, & -2 < x \leq 0 \\ -3x, & 0 \leq x < 2 \\ 5, & 2 < x \leq 4 \\ 0, & x = 2 \end{cases}$$

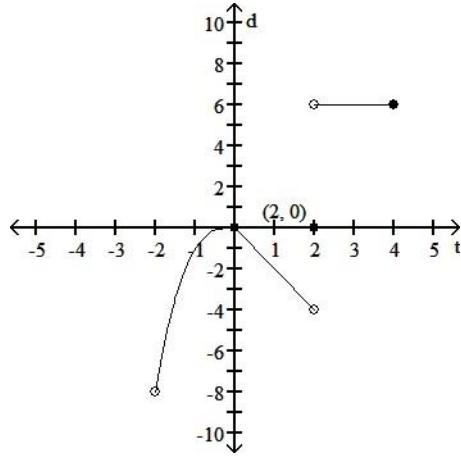


A) Yes

B) No

171) Is f continuous at $x = 4$?

$$f(x) = \begin{cases} x^3, & -2 < x \leq 0 \\ -2x, & 0 \leq x < 2 \\ 6, & 2 < x \leq 4 \\ 0, & x = 2 \end{cases}$$



A) Yes

B) No

Find the intervals on which the function is continuous.

172) $y = \frac{3}{x+8} - 5x$

- A) continuous everywhere
- C) discontinuous only when $x = -8$

172) _____

- B) discontinuous only when $x = -13$
- D) discontinuous only when $x = 8$

173)

$y =$

$$\frac{4}{(x+3)^2+6} \quad \text{_____}$$

- A) discontinuous only when $x = -24$
C) discontinuous only when $x = -3$

- B) continuous everywhere
D) discontinuous only when $x = 15$

174) $y = \frac{x+3}{x^2 - 13x + 40}$

- A) discontinuous only when $x = 5$
C) discontinuous only when $x = 5$ or $x = 8$

174) _____

- B) discontinuous only when $x = -5$ or $x = 8$
D) discontinuous only when $x = -8$ or $x = 5$

175) $y = \frac{3}{x^2 - 25}$

- A) discontinuous only when $x = -5$
B) discontinuous only when $x = -25$ or $x = 25$
C) discontinuous only when $x = 25$
D) discontinuous only when $x = -5$ or $x = 5$

175) _____

176) $y = \frac{4}{|x|+2} - \frac{x^2}{3}$

- A) discontinuous only when $x = -3$ or $x = -2$
C) discontinuous only when $x = -2$

176) _____

- B) discontinuous only when $x = -5$
D) continuous everywhere

177) $y = \frac{\sin(2\theta)}{2\theta}$

- A) discontinuous only when $\theta = 0$
C) discontinuous only when $\theta = \pi$

177) _____

- B) $\frac{\pi}{2}$
discontinuous only when $\theta = \frac{\pi}{2}$
D) continuous everywhere

178) $y = \frac{3 \cos \theta}{\theta + 6}$

- A) continuous everywhere
C) discontinuous only when $\theta = 6$

178) _____

- B) discontinuous only when $\theta = -6$
D) $\frac{\pi}{2}$
discontinuous only when $\theta = \frac{\pi}{2}$

179) $y = \sqrt{9x+1}$

- A) continuous on the interval $\left[-\frac{1}{9}, \infty\right)$
C) continuous on the interval $\left[-\frac{1}{9}, \infty\right]$

179) _____

- B) continuous on the interval $\left[-\infty, -\frac{1}{9}\right]$
D) continuous on the interval $\left[\frac{1}{9}, \infty\right)$

180) $y = \sqrt[4]{5x-2}$

- A) continuous on the interval $\left[\frac{2}{5}, \infty\right)$
C) continuous on the interval $\left(\frac{2}{5}, \infty\right)$

180) _____

- B) continuous on the interval $\left[-\infty, \frac{2}{5}\right]$
D) continuous on the interval $\left[-\frac{2}{5}, \infty\right)$

181) $y = \sqrt{x^2 - 6}$

181) _____

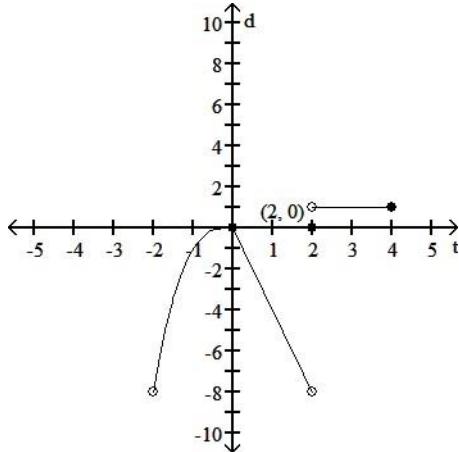
- A) continuous on the interval $[\sqrt{6}, \infty)$
 B) continuous everywhere
 C) continuous on the intervals $(-\infty, -\sqrt{6}]$ and $[\sqrt{6}, \infty)$
 D) continuous on the interval $[-\sqrt{6}, \sqrt{6}]$

Provide an appropriate response.

182) Is f continuous on $(-2, 4]$?

182) _____

$$f(x) = \begin{cases} x^3, & -2 < x \leq 0 \\ -4x, & 0 \leq x < 2 \\ 1, & 2 < x \leq 4 \\ 0, & x = 2 \end{cases}$$



A) No

B) Yes

Find the limit, if it exists.

183) $\lim_{x \rightarrow 0} \sqrt{x} - 2$

183) _____

A) Does not exist

B) 0

C) -2

D) 2

184) $\lim_{x \rightarrow 7} \sqrt{x^2 + 2x + 1}$

184) _____

A) 64

B) Does not exist

C) ± 8

D) 8

185) $\lim_{x \rightarrow 4} \sqrt{x - 9}$

185) _____

A) 2.23606798

B) 0

C) -2.236068

D) Does not exist

186) $\lim_{x \rightarrow 14} \sqrt{x^2 - 9}$

186) _____

A) $\sqrt{187}$

B) 93.5

C) $\pm \sqrt{187}$

D) Does not exist

187) $\lim_{x \rightarrow -7^-} \sqrt{x^2 - 49}$

187) _____

A) $7\sqrt{3}$

B) 3.5

C) 0

D) Does not exist

188) $\lim_{x \rightarrow 7^+} \frac{-7\sqrt{(x - 7)^3}}{x - 7}$

188) _____

A) -7

B) 0

C) $-7\sqrt{7}$

D) Does not exist

189) $\lim_{t \rightarrow 1^+} \frac{\sqrt{(t + 81)(t - 1)^2}}{19t - 19}$

189) _____

A) 0

B) $\frac{\sqrt{82}}{19}$

C) $\frac{1}{19}$

D) Does not exist

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**Provide an appropriate response.**

- 190) Use the Intermediate Value Theorem to prove that $6x^3 + 5x^2 + 4x + 7 = 0$ has a solution between -2 and -1. 190) _____

- 191) Use the Intermediate Value Theorem to prove that $2x^4 + 10x^3 - 6x - 6 = 0$ has a solution between -5 and -4. 191) _____

- 192) Use the Intermediate Value Theorem to prove that $x^{(x-2)^2} = 2$ has a solution between 1 and 3. 192) _____

- 193) Use the Intermediate Value Theorem to prove that $5 \sin x = x$ has a solution between $\frac{\pi}{2}$ and π . 193) _____

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question. Find numbers a and b , or k , so that f is continuous at every point.

- 194) $f(x) = \begin{cases} -7, & x < -4 \\ ax + b, & -4 \leq x \leq 3 \\ 21, & x > 3 \end{cases}$ 194) _____

- A) $a = -4, b = 9$ B) $a = -7, b = 21$ C) $a = 4, b = 33$ D) Impossible

- 195) $f(x) = \begin{cases} x^2, & x < -5 \\ ax + b, & -5 \leq x \leq -2 \\ x + 6, & x > -2 \end{cases}$ 195) _____

- A) $a = 7, b = -10$ B) $a = -7, b = -10$ C) $a = -7, b = 10$ D) Impossible

- 196) $f(x) = \begin{cases} 3x + 8, & \text{if } x < -1 \\ kx + 4, & \text{if } x \geq -1 \end{cases}$ 196) _____

- A) $k = -1$ B) $k = 7$ C) $k = 4$ D) $k = -4$

- 197) $f(x) = \begin{cases} x^2, & \text{if } x \leq 4 \\ x + k, & \text{if } x > 4 \end{cases}$ 197) _____

- A) $k = 12$ B) $k = 20$ C) $k = -4$ D) Impossible

- 198) $f(x) = \begin{cases} x^2, & \text{if } x \leq 2 \\ kx, & \text{if } x > 2 \end{cases}$ 198) _____

- A) $k = 2$ B) $k = \frac{1}{2}$ C) $k = -4$ D) Impossible

Solve the problem.

199)

$$\lim_{x \rightarrow x_0} f(x) = L$$

199) _____

Select the correct statement for the definition of the limit: $\lim_{x \rightarrow x_0} f(x) = L$
means that _____

- A) if given any number $\varepsilon > 0$, there exists a number $\delta > 0$, such that for all x ,
 $0 < |x - x_0| < \varepsilon$ implies $|f(x) - L| > \delta$.
- B) if given any number $\varepsilon > 0$, there exists a number $\delta > 0$, such that for all x ,
 $0 < |x - x_0| < \delta$ implies $|f(x) - L| < \varepsilon$.
- C) if given a number $\varepsilon > 0$, there exists a number $\delta > 0$, such that for all x ,
 $0 < |x - x_0| < \delta$ implies $|f(x) - L| > \varepsilon$.
- D) if given any number $\varepsilon > 0$, there exists a number $\delta > 0$, such that for all x ,
 $0 < |x - x_0| < \varepsilon$ implies $|f(x) - L| < \delta$.

200) Identify the incorrect statements about limits.

200) _____

- I. The number L is the limit of $f(x)$ as x approaches x_0 if $f(x)$ gets closer to L as x approaches x_0 .
- II. The number L is the limit of $f(x)$ as x approaches x_0 if, for any $\varepsilon > 0$, there corresponds a $\delta > 0$ such that $|f(x) - L| < \varepsilon$ whenever $0 < |x - x_0| < \delta$.
- III. The number L is the limit of $f(x)$ as x approaches x_0 if, given any $\varepsilon > 0$, there exists a value of x for which $|f(x) - L| < \varepsilon$.

A) I and II

B) I and III

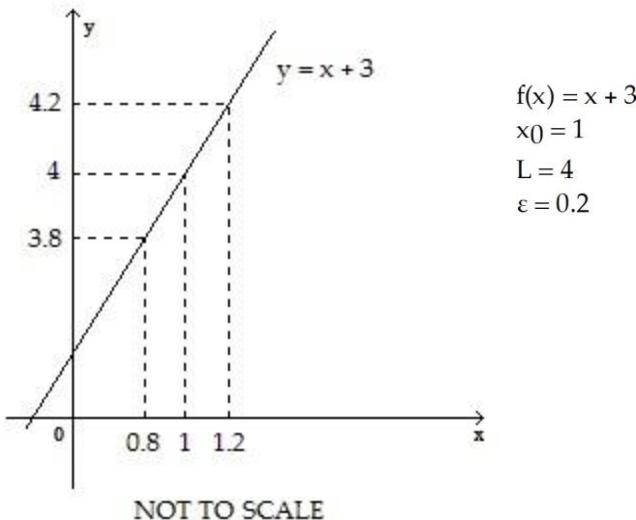
C) II and III

D) I, II, and III

Use the graph to find a $\delta > 0$ such that for all x , $0 < |x - x_0| < \delta \Rightarrow |f(x) - L| < \varepsilon$.

201)

201) _____



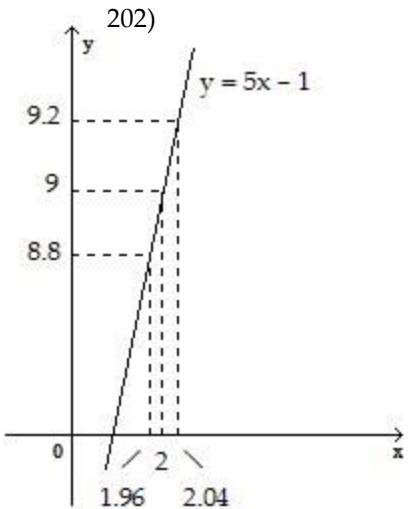
A) 0.4

B) 0.2

C) 0.1

D) 3

202)



NOT TO SCALE

$$f(x) = 5x - 1$$

$$x_0 = 2$$

$$L = 9$$

$$\varepsilon = 0.2$$

A) 0.04

B) 0.4

C) 0.08

D) 7

203)

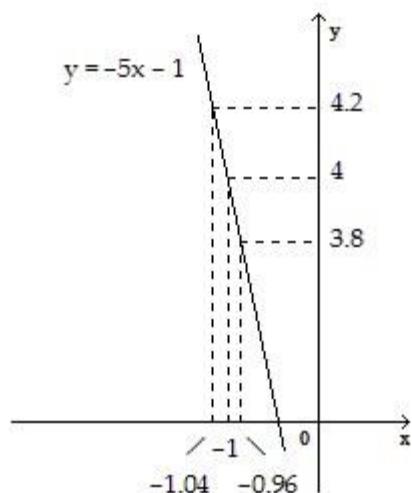
203) _____

$$f(x) = -5x - 1$$

$$x_0 = -1$$

$$L = 4$$

$$\varepsilon = 0.2$$



NOT TO SCALE

A) 0.04

B) 0.4

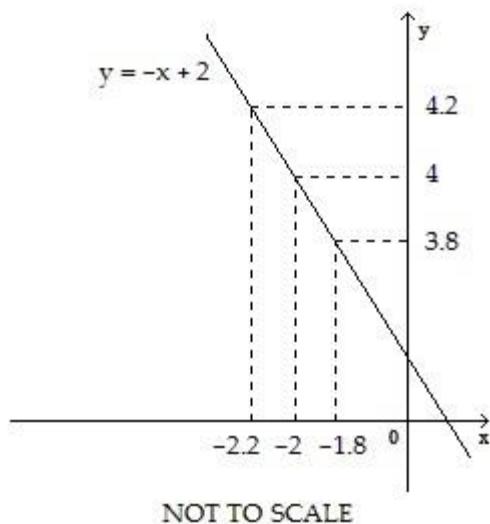
C) 7

D) -0.04

204)

204) _____

$$\begin{aligned}y &= -x + 2 \\f(x) &= -x + 2 \\x_0 &= -2 \\L &= 4 \\\varepsilon &= 0.2\end{aligned}$$



A) 0.2

B) -0.2

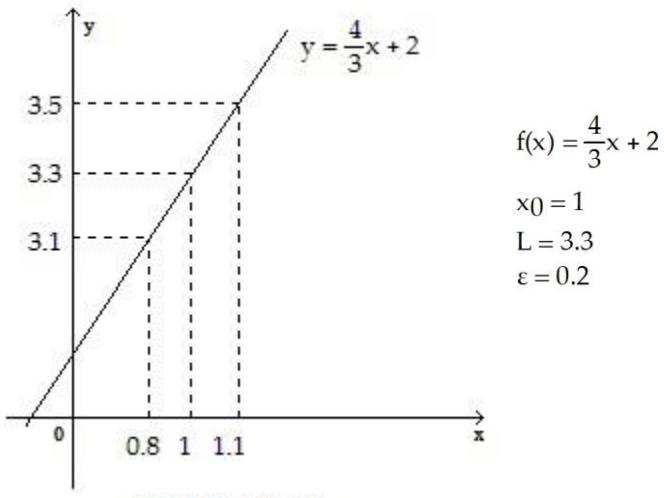
C) 0.4

D) 6

205)

205) _____

$$\begin{aligned}y &= \frac{4}{3}x + 2 \\f(x) &= \frac{4}{3}x + 2 \\x_0 &= 1 \\L &= 3.3 \\\varepsilon &= 0.2\end{aligned}$$



A) -0.3

B) 0.3

C) 0.1

D) 2.3

206)

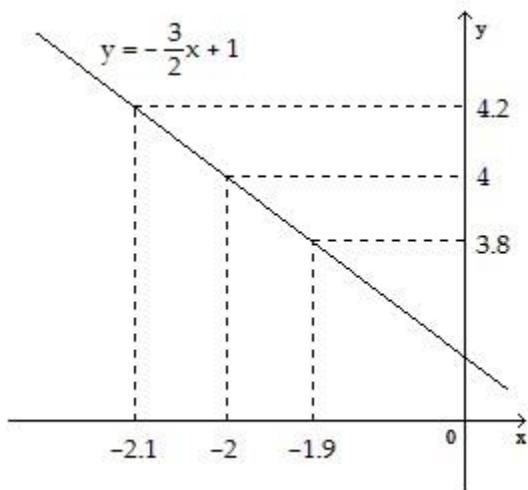
206)

$$f(x) = -\frac{3}{2}x + 1$$

$$x_0 = -2$$

$$L = 4$$

$$\epsilon = 0.2$$



NOT TO SCALE

A) -0.2

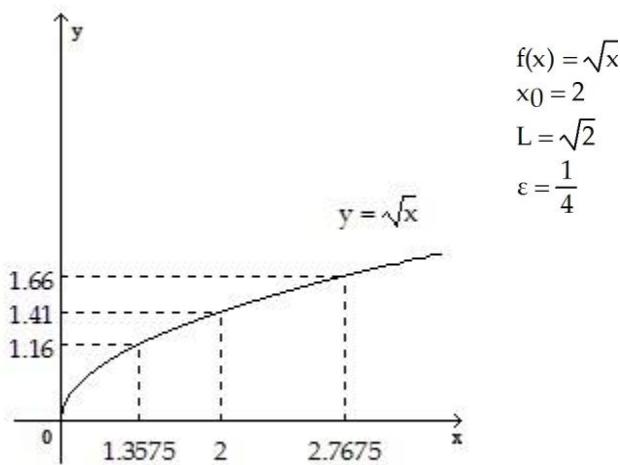
B) 0.1

C) 0.2

D) 6

207)

207) _____



NOT TO SCALE

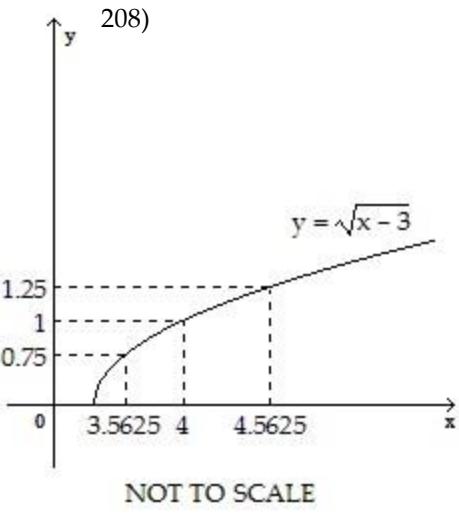
A) -0.59

B) 0.7675

C) 1.41

D) 0.6425

208)



$$f(x) = \sqrt{x - 3}$$

$$x_0 = 4$$

$$L = 1$$

$$\varepsilon = \frac{1}{4}$$

A) 3

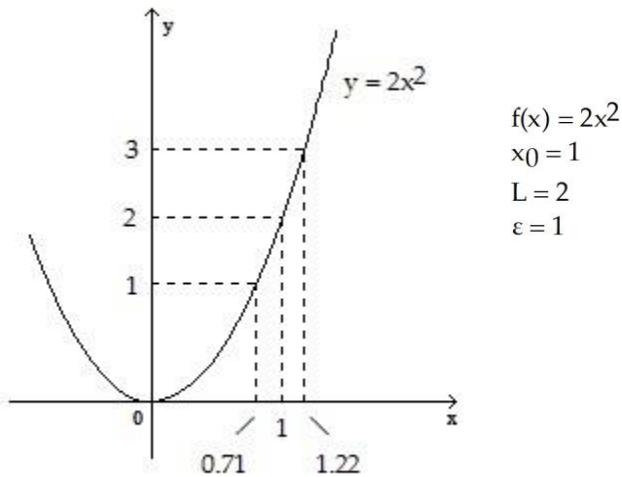
B) 0.4375

C) 1

D) 0.5625

209)

209) _____



NOT TO SCALE

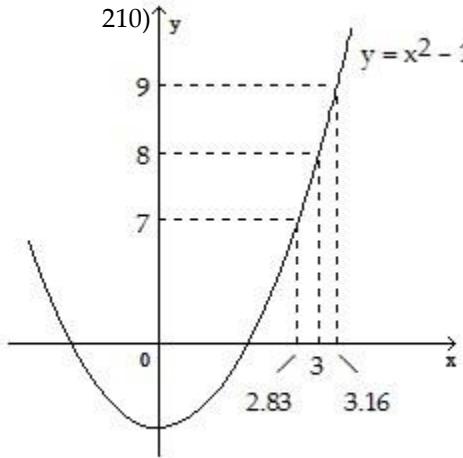
A) 0.22

B) 0.29

C) 1

D) 0.51

210)



NOT TO SCALE

$$f(x) = x^2 - 1$$

$$x_0 = 3$$

$$L = 8$$

$$\varepsilon = 1$$

A) 5

B) 0.33

C) 0.16

D) 0.17

A function $f(x)$, a point x_0 , the limit of $f(x)$ as x approaches x_0 , and a positive number ε is given. Find a number $\delta > 0$ such that for all x , $0 < |x - x_0| < \delta \Rightarrow |f(x) - L| < \varepsilon$.

211) $f(x) = 6x + 7$, $L = 19$, $x_0 = 2$, and $\varepsilon = 0.01$
 A) 0.001667 B) 0.003333

211) _____
 C) 0.008333 D) 0.005

212) $f(x) = 6x - 9$, $L = -3$, $x_0 = 1$, and $\varepsilon = 0.01$
 A) 0.01 B) 0.003333

212) _____
 C) 0.000833 D) 0.001667

213) $f(x) = -7x + 10$, $L = -11$, $x_0 = 3$, and $\varepsilon = 0.01$
 A) 0.001429 B) -0.003333

213) _____
 C) 0.002857 D) 0.005714

214) $f(x) = -2x - 6$, $L = -12$, $x_0 = 3$, and $\varepsilon = 0.01$
 A) 0.005 B) -0.003333

214) _____
 C) 0.01 D) 0.0025

215) $f(x) = 3x^2$, $L = 48$, $x_0 = 4$, and $\varepsilon = 0.1$
 A) 0.00416 B) 4.00416

215) _____
 C) 3.99583 D) 0.00417

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

Prove the limit statement

216)

$$\lim_{x \rightarrow 1} \frac{216}{(5x - 4)} =$$

—
—
—

$$217) \lim_{x \rightarrow 7} \frac{x^2 - 49}{x - 7} = 14$$

217) _____

$$218) \lim_{x \rightarrow 6} \frac{2x^2 - 7x - 30}{x - 6} = 17$$

218) _____

$$219) \lim_{x \rightarrow 3} \frac{1}{x} = \frac{1}{3}$$

219) _____

- 1) C
 2) C
 3) B
 4) C
 5) A
 6) A
 7) C
 8) D
 9) C
 10) B
 11) A
 12) D
 13) B
 14) B
 15) C
 16) C
 17) A
 18) C
 19) D
 20) A
 21) B
 22) A
 23) D
 24) B
 25) A
 26) D
 27) C
 28) B
 29) B
 30) B
 31) D
 32) D
 33) C
 34) C
 35) A
 36) B
 37) B
 38) D
 39) A

40)

$$\lim_{x \rightarrow 0} 1 - \frac{x^2}{6}$$

$$\lim_{x \rightarrow 0} 1 = 1$$

Answers may vary. One possibility: According to the squeeze theorem, the function

$$\frac{x \sin(x)}{2 - 2 \cos(x)}$$

$$1 - \frac{x^2}{6}$$

, which is squeezed between and 1, must also approach 1 as x approaches 0. Thus,

$$\lim_{x \rightarrow 0} \frac{x \sin(x)}{2 - 2 \cos(x)} = 1.$$

- 41) C
 42) A
 43) A
 44) B
 45) B

- 46) D
- 47) C
- 48) D
- 49) B
- 50) D
- 51) A
- 52) D
- 53) B
- 54) B
- 55) C
- 56) A
- 57) D
- 58) C
- 59) D
- 60) B
- 61) A
- 62) D
- 63) C
- 64) C
- 65) A
- 66) C
- 67) C
- 68) D
- 69) A
- 70) B
- 71) D
- 72) B
- 73) C
- 74) D
- 75) A
- 76) A
- 77) B
- 78) A
- 79) B
- 80) A
- 81) B
- 82) C
- 83) D
- 84) D
- 85) B
- 86) A
- 87) A
- 88) D
- 89) C
- 90) D
- 91) D
- 92) A
- 93) C
- 94) B
- 95) B
- 96) B
- 97) D

- 98) B
- 99) A
- 100) C
- 101) A
- 102) D
- 103) B
- 104) C
- 105) C
- 106) A
- 107) D
- 108) A
- 109) C
- 110) B
- 111) B
- 112) A
- 113) A
- 114) C
- 115) B
- 116) B
- 117) A
- 118) B
- 119) D
- 120) D
- 121) A
- 122) B
- 123) A
- 124) A
- 125) B
- 126) A
- 127) D
- 128) B
- 129) D
- 130) C
- 131) C
- 132) C
- 133) B
- 134) C
- 135) C
- 136) A
- 137) C
- 138) D
- 139) B
- 140) B
- 141) D
- 142) A
- 143) D
- 144) A
- 145) B
- 146) D
- 147) B
- 148) C
- 149) C

150) D

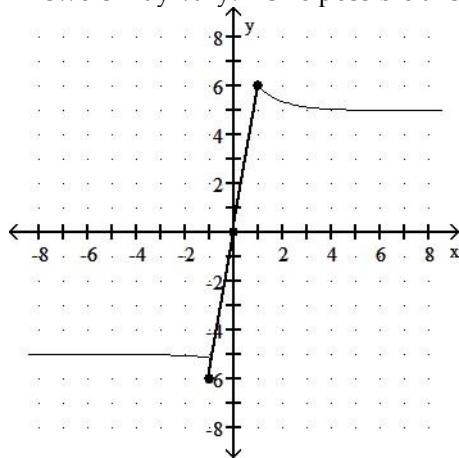
151) D

152) C

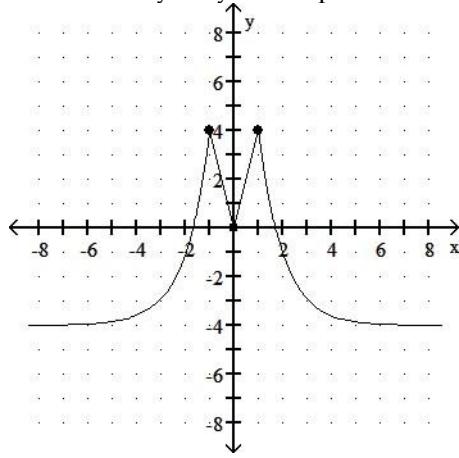
153) D

154) D

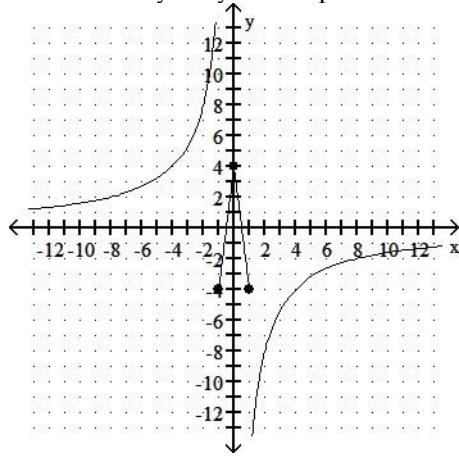
155) Answers may vary. One possible answer:



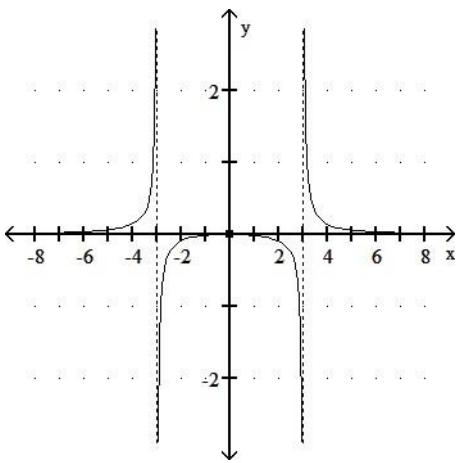
156) Answers may vary. One possible answer:



157) Answers may vary. One possible answer:



158) Answers may vary. One possible answer:



- 159) B
 160) C
 161) A
 162) C
 163) A
 164) A
 165) A
 166) A
 167) D
 168) A
 169) A
 170) A
 171) A
 172) C
 173) B
 174) C
 175) D
 176) D
 177) A
 178) B
 179) C
 180) A
 181) C
 182) A
 183) C
 184) D
 185) D
 186) A
 187) C
 188) B
 189) B
- 190) Let $f(x) = 6x^3 + 5x^2 + 4x + 7$ and let $y_0 = 0$. $f(-2) = -29$ and $f(-1) = -2$. Since f is continuous on $[-2, -1]$ and since $y_0 = 0$ is between $f(-2)$ and $f(-1)$, by the Intermediate Value Theorem, there exists a c in the interval $(-2, -1)$ with the property that $f(c) = 0$. Such a c is a solution to the equation $6x^3 + 5x^2 + 4x + 7 = 0$.
- 191) Let $f(x) = 2x^4 + 10x^3 - 6x - 6$ and let $y_0 = 0$. $f(-5) = -24$ and $f(-4) = -110$. Since f is continuous on $[-5, -4]$ and since $y_0 = 0$ is between $f(-5)$ and $f(-4)$, by the Intermediate Value Theorem, there exists a c in the interval $(-5, -4)$ with the property that $f(c) = 0$. Such a c is a solution to the equation $2x^4 + 10x^3 - 6x - 6 = 0$.
- 192) Let $f(x) = x(x - 2)^2$ and let $y_0 = 2$. $f(1) = 1$ and $f(3) = 3$. Since f is continuous on $[1, 3]$ and since $y_0 = 2$ is

betw $f(1)$ and $f(3)$, by the Intermediate Value Theorem, there exists a c in the interval $(1, 3)$ with the property that $f(c) = 2$. Such a c is a solution to the equation $x(x - 2)^2 = 2$.

193) Let $f(x) = \frac{\sin x}{x}$ and let $y_0 = \frac{1}{5}$. $f\left(\frac{\pi}{2}\right) \approx 0.6366$ and $f(\pi) = 0$. Since f is continuous on $\left[\frac{\pi}{2}, \pi\right]$ and since $y_0 = \frac{1}{5}$ is between $f\left(\frac{\pi}{2}\right)$ and $f(\pi)$, by the Intermediate Value Theorem, there exists a c in the interval $\left[\frac{\pi}{2}, \pi\right]$, with the property that $f(c) = \frac{1}{5}$. Such a c is a solution to the equation $5 \sin x = x$.

194) A

195) B

196) A

197) A

198) A

199) B

200) B

201) B

202) A

203) A

204) A

205) C

206) B

207) D

208) B

209) A

210) C

211) A

212) D

213) A

214) A

215) A

216)

Let $\varepsilon > 0$ be given. Choose $\delta = \varepsilon/5$. Then $0 < |x - 1| < \delta$ implies that

$$\begin{aligned} |(5x - 4) - 1| &= |5x - 5| \\ &= |5(x - 1)| \\ &= 5|x - 1| < 5\delta = \varepsilon \end{aligned}$$

Thus, $0 < |x - 1| < \delta$ implies that $|(5x - 4) - 1| < \varepsilon$

217) Let $\varepsilon > 0$ be given. Choose $\delta = \varepsilon$. Then $0 < |x - 7| < \delta$ implies that

$$\begin{aligned} \left| \frac{x^2 - 49}{x - 7} - 14 \right| &= \left| \frac{(x - 7)(x + 7)}{x - 7} - 14 \right| \\ &= |(x + 7) - 14| \quad \text{for } x \neq 7 \\ &= |x - 7| < \delta = \varepsilon \end{aligned}$$

Thus, $0 < |x - 7| < \delta$ implies that $\left| \frac{x^2 - 49}{x - 7} - 14 \right| < \varepsilon$

218) Let $\varepsilon > 0$ be given. Choose $\delta = \varepsilon/2$. Then $0 < |x - 6| < \delta$ implies that

$$\begin{aligned} \left| \frac{2x^2 - 7x - 30}{x - 6} - 17 \right| &= \left| \frac{(x - 6)(2x + 5)}{x - 6} - 17 \right| \\ &= |(2x + 5) - 17| \quad \text{for } x \neq 6 \\ &= |2x - 12| \\ &= |2(x - 6)| \\ &= 2|x - 6| < 2\delta = \varepsilon \end{aligned}$$

Thus

$$0 < |x - 6| < \delta \text{ implies that } \left| \frac{2x^2 - 7x - 30}{x - 6} - 17 \right| < \varepsilon$$

219) Let $\varepsilon > 0$ be given. Choose $\delta = \min\{3/2, 9\varepsilon/2\}$. Then $0 < |x - 3| < \delta$ implies that

$$\begin{aligned} \left| \frac{1}{x} - \frac{1}{3} \right| &= \left| \frac{3 - x}{3x} \right| \\ &= \frac{1}{|x|} \cdot \frac{1}{3} \cdot |x - 3| \\ &< \frac{1}{3/2} \cdot \frac{1}{3} \cdot \frac{9\varepsilon}{2} = \varepsilon \end{aligned}$$

Thus, $0 < |x - 3| < \delta$ implies that $\left| \frac{1}{x} - \frac{1}{3} \right| < \varepsilon$