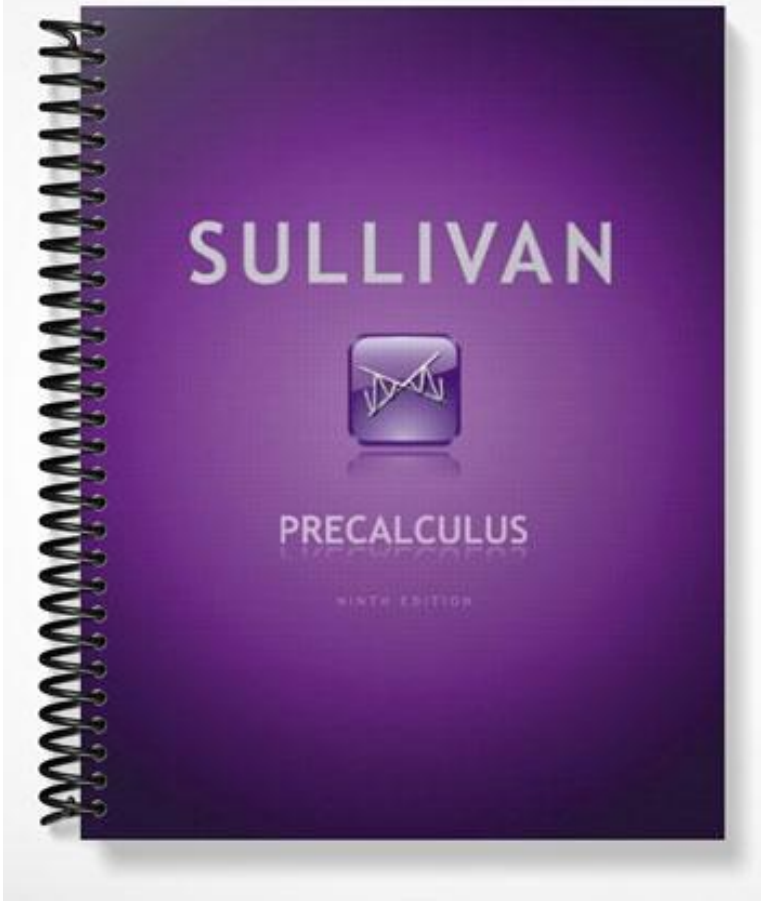
TEST BANK



Ch. 2 Functions and Their Graphs

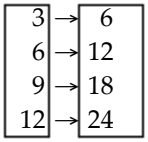
2.1 Functions

1 Determine Whether a Relation Represents a Function

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Determine whether the relation represents a function. If it is a function, state the domain and range.

1)

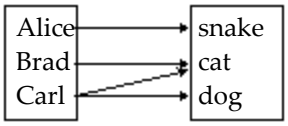


A) function
domain:{6, 12, 18, 24}
range: {3, 6, 9, 12}

B) function
domain: {3, 6, 9, 12}
range: {6, 12, 18, 24}

C) not a function

2)

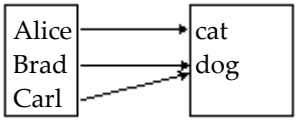


A) function
domain: {snake, cat, dog}
range: {Alice, Brad, Carl}

B) function
domain: {Alice, Brad, Carl}
range: {snake, cat, dog}

C) not a function

3)



A) function
domain: {Alice, Brad, Carl}
range: {cat, dog}

B) function
domain: {cat, dog}
range: {Alice, Brad, Carl}

C) not a function

4) {(−2, 7), (1, 3), (3, −3), (8, −1)}

A) function
domain: {7, 3, −3, −1}
range: {−2, 1, 3, 8}

B) function
domain: {−2, 1, 3, 8}
range: {7, 3, −3, −1}

C) not a function

5) {(41, −2), (5, −1), (5, 0), (6, 1), (14, 3)}

A) function
domain: {41, 6, 5, 14}
range: {−2, −1, 0, 1, 3}

B) function
domain: {−2, −1, 0, 1, 3}
range: {41, 6, 5, 14}

C) not a function

6) {(−2, 9), (−1, 6), (0, 5), (1, 6), (3, 14)}

A) function
domain: {9, 6, 5, 14}
range: {−2, −1, 0, 1, 3}

B) function
domain: {−2, −1, 0, 1, 3}
range: {9, 6, 5, 14}

C) not a function

7) {(6.22, 7.62), (6.222, –7.6), $(\frac{5}{7}, 0)$, (0.71, –6)}

A) function

domain: {6.22, 6.222, $\frac{5}{7}$, 0.71}

range: {7.62, –7.6, 0, –6}

B) function

domain: {7.62, –7.6, 0, –6}

range: {6.22, 6.222, $\frac{5}{7}$, 0.71}

C) not a function

Determine whether the equation defines y as a function of x.

8) $y = x^4$

A) function B) not a function

9) $y = \frac{1}{x}$

A) function B) not a function

10) $y = |x|$

A) function B) not a function

11) $y^2 = 9 - x^2$

A) function B) not a function

12) $y = \pm\sqrt{1 - 6x}$

A) function B) not a function

13) $x = y^2$

A) function B) not a function

14) $y^2 + x = 8$

A) function B) not a function

15) $y = 4x^2 - 7x + 5$

A) function B) not a function

16) $y = \frac{2x - 1}{x - 2}$

A) function B) not a function

17) $x^2 + 5y^2 = 1$

A) function B) not a function

18) $x - 3y = 4$

A) function B) not a function

19) $-5x + x^2 + 36 = y$

A) function B) not a function

2 Find the Value of a Function

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find the value for the function.

1) Find f(1) when $f(x) = x^2 + 2x - 5$.
A) 8 B) 4 C) –2 D) –6

2) Find f(–1) when $f(x) = \frac{x^2 - 8}{x - 3}$.
A) $\frac{7}{4}$ B) $-\frac{9}{2}$ C) $-\frac{9}{4}$ D) $-\frac{1}{4}$

3) Find f(–9) when $f(x) = |x| - 6$.
A) –15 B) 3 C) 15 D) –3

4) Find f(8) when $f(x) = \sqrt{x^2 + 4x}$.
A) $4\sqrt{6}$ B) $2\sqrt{17}$ C) $4\sqrt{5}$ D) $2\sqrt{5}$

5) Find f(–x) when $f(x) = -3x^2 + 4x - 5$.
A) $-3x^2 - 4x - 5$ B) $3x^2 - 4x - 5$ C) $3x^2 - 4x + 5$ D) $-3x^2 - 4x + 5$

6) Find f(–x) when $f(x) = \frac{x}{x^2 + 7}$.
A) $\frac{-x}{x^2 + 7}$ B) $\frac{-x}{x^2 - 7}$ C) $\frac{-x}{-x^2 + 7}$ D) $\frac{x}{-x^2 + 7}$

7) Find –f(x) when $f(x) = 2x^2 + 4x - 1$.
A) $-2x^2 - 4x - 1$ B) $2x^2 - 4x + 1$ C) $-2x^2 - 4x + 1$ D) $2x^2 - 4x - 1$

8) Find –f(x) when $f(x) = |x| - 4$.
A) $|-x| - 4$ B) $|-x| + 4$ C) $-|x| - 4$ D) $-|x| + 4$

9) Find f(x – 1) when $f(x) = 4x^2 - 3x + 3$.
A) $4x^2 + 9x + 4$ B) $4x^2 - 11x + 4$ C) $-11x^2 + 4x + 10$ D) $4x^2 - 11x + 10$

10) Find f(x + 1) when $f(x) = \frac{x^2 - 8}{x - 2}$.
A) $\frac{x^2 + 2x + 9}{x - 1}$ B) $\frac{x^2 - 7}{x - 1}$ C) $\frac{x^2 + 2x - 7}{x - 1}$ D) $\frac{x^2 + 2x - 7}{x + 3}$

11) Find f(–x) when $f(x) = 2x^2 - 2x + 2$.
A) $2x^2 + 2x - 2$ B) $-2x^2 + 2x - 2$ C) $-2x^2 + 2x + 2$ D) $2x^2 + 2x + 2$

12) Find f(2x) when $f(x) = \sqrt{2x^2 - 7x}$.
A) $\sqrt{4x^2 - 14x}$ B) $\sqrt{8x^2 - 14x}$ C) $\sqrt{4x^2 - 28x}$ D) $2\sqrt{2x^2 - 7x}$

13) Find f(x + h) when $f(x) = 2x^2 + 4x + 4$.

A) $2x^2 + 2h^2 + 4x + 4h + 4$ B) $2x^2 + 2h^2 + 8x + 8h + 4$

C) $2x^2 + 2xh + 2h^2 + 4x + 4h + 4$ D) $2x^2 + 4xh + 2h^2 + 4x + 4h + 4$

14) Find f(x + h) when $f(x) = \frac{8x + 5}{5x + 2}$.

A) $\frac{8x + 13h}{5x + 7h}$ B) $\frac{8x + 5h}{5x + 2h}$ C) $\frac{8x + 8h + 5}{5x + 2}$ D) $\frac{8x + 8h + 5}{5x + 5h + 2}$

Solve the problem.

15) If $f(x) = 6x^3 + 9x^2 - x + C$ and f(3) = 1, what is the value of C?

A) C = −239 B) C = 85 C) C = 247 D) C = 25

16) If $f(x) = \frac{x - B}{x - A}$, f(6) = 0, and f(2) is undefined, what are the values of A and B?

A) A = −6, B = −2 B) A = −2, B = −6 C) A = 2, B = 6 D) A = 6, B = 2

17) If $f(x) = \frac{x - 5A}{10x + 1}$ and f(10) = −10, what is the value of A?

A) A = 99 B) A = 204 C) A = −204 D) A = −99

18) If a rock falls from a height of 80 meters on Earth, the height H (in meters) after x seconds is approximately $H(x) = 80 - 4.9x^2$.

What is the height of the rock when x = 2 seconds? Round to the nearest hundredth, if necessary.

A) 99.6 m B) 60.4 m C) 60.8 m D) 70.2 m

19) If a rock falls from a height of 90 meters on Earth, the height H (in meters) after x seconds is approximately $H(x) = 90 - 4.9x^2$.

When does the rock strike the ground? Round to the nearest hundredth, if necessary.

A) 3.75 sec B) 1.94 sec C) 18.37 sec D) 4.29 sec

20) It has been determined that the number of fish f(t) that can be caught in t minutes in a certain pond using a certain bait is $f(t) = 0.28t + 1$, for $t > 10$. Find the approximate number of fish that can be caught if you fish for 25 minutes.

A) About 17 fish B) About 8 fish C) About 27 fish D) About 29 fish

21) The function $P(d) = 1 + \frac{d}{33}$ gives the pressure, in atmospheres (atm), at a depth d feet in the sea. Find the pressure at 36 feet.

A) $\frac{37}{33}$ atm B) $\frac{1}{11}$ atm C) $\frac{23}{11}$ atm D) $\frac{12}{11}$ atm

22) The function F described by $F(C) = \frac{9}{5}C + 32$ gives the Fahrenheit temperature corresponding to the Celsius temperature C. Find the Fahrenheit temperature equivalent to −25°C.

A) −13°F B) −103°F C) −58°F D) −148°F

3 Find the Domain of a Function Defined by an Equation

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find the domain of the function.

1) $f(x) = 7x - 4$

A) $\{x \mid x > 0\}$ B) $\{x \mid x \geq 4\}$ C) $\{x \mid x \neq 0\}$ D) all real numbers

2) $f(x) = x^2 + 4$

A) $\{x \mid x > -4\}$ B) $\{x \mid x \neq -4\}$ C) $\{x \mid x \geq -4\}$ D) all real numbers

3) $f(x) = \dfrac{x^2}{x^2 + 4}$

A) $\{x \mid x > -4\}$ B) all real numbers C) $\{x \mid x \neq -4\}$ D) $\{x \mid x \neq 0\}$

4) $g(x) = \dfrac{3x}{x^2 - 25}$

A) $\{x \mid x > 25\}$ B) $\{x \mid x \neq -5, 5\}$ C) all real numbers D) $\{x \mid x \neq 0\}$

5) $h(x) = \dfrac{x - 1}{x^3 - 81x}$

A) all real numbers B) $\{x \mid x \neq -9, 0, 9\}$ C) $\{x \mid x \neq 0\}$ D) $\{x \mid x \neq 1\}$

6) $f(x) = \sqrt{13 - x}$

A) $\{x \mid x \leq 13\}$ B) $\{x \mid x \neq 13\}$ C) $\{x \mid x \neq \sqrt{13}\}$ D) $\{x \mid x \leq \sqrt{13}\}$

7) $\dfrac{x}{\sqrt{x - 6}}$

A) $\{x \mid x > 6\}$ B) all real numbers C) $\{x \mid x \neq 6\}$ D) $\{x \mid x \geq 6\}$

4 Form the Sum, Difference, Product, and Quotient of Two Functions

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

For the given functions f and g, find the requested function and state its domain.

1) $f(x) = 9 - 9x$; $g(x) = -7x + 9$

Find $f + g$.

A) $(f + g)(x) = -16x + 18$; all real numbers B) $(f + g)(x) = 2x$; all real numbers

C) $(f + g)(x) = -2x + 18$; $\{x \mid x \neq -9\}$ D) $(f + g)(x) = -7x + 9$; $\{x \mid x \neq \dfrac{9}{7}\}$

2) $f(x) = 8x - 8$; $g(x) = 6x - 3$

Find $f - g$.

A) $(f - g)(x) = 14x - 11$; $\{x \mid x \neq 1\}$ B) $(f - g)(x) = -2x + 5$; all real numbers

C) $(f - g)(x) = 2x - 5$; all real numbers D) $(f - g)(x) = 2x - 11$; $\{x \mid x \neq \dfrac{11}{2}\}$

3) $f(x) = 7x - 4;\ g(x) = 9x - 9$

Find $f \cdot g$.

A) $(f \cdot g)(x) = 63x^2 - 99x + 36;$ all real numbers

B) $(f \cdot g)(x) = 16x^2 - 99x - 13;$ all real numbers

C) $(f \cdot g)(x) = 63x^2 + 36;\ \{x \mid x \neq 36\}$

D) $(f \cdot g)(x) = 63x^2 - 45x + 36;\ \{x \mid x \neq 36\}$

4) $f(x) = 5x + 4;\ g(x) = 4x - 1$

Find $\frac{f}{g}$.

A) $\left(\frac{f}{g}\right)(x) = \frac{4x - 1}{5x + 4};\ \left\{x \mid x \neq \frac{1}{4}\right\}$

B) $\left(\frac{f}{g}\right)(x) = \frac{4x - 1}{5x + 4};\ \left\{x \mid x \neq -\frac{4}{5}\right\}$

C) $\left(\frac{f}{g}\right)(x) = \frac{5x + 4}{4x - 1};\ \left\{x \mid x \neq -\frac{4}{5}\right\}$

D) $\left(\frac{f}{g}\right)(x) = \frac{5x + 4}{4x - 1};\ \left\{x \mid x \neq \frac{1}{4}\right\}$

5) $f(x) = 16 - x^2;\ g(x) = 4 - x$

Find $f + g$.

A) $(f + g)(x) = 4 + x;\ \{x \mid x \neq -4\}$

B) $(f + g)(x) = x^3 - 4x^2 - 16x + 64;$ all real numbers

C) $(f + g)(x) = -x^2 + x + 12;$ all real numbers

D) $(f + g)(x) = -x^2 - x + 20;$ all real numbers

6) $f(x) = x + 7;\ g(x) = 7x^2$

Find $f - g$.

A) $(f - g)(x) = -7x^2 + x + 7;$ all real numbers

B) $(f - g)(x) = -7x^2 + x + 7;\ \{x \mid x \neq -7\}$

C) $(f - g)(x) = 7x^2 - x - 7;$ all real numbers

D) $(f - g)(x) = 7x^2 + x + 7;$ all real numbers

7) $f(x) = 3x^3 + 2;\ g(x) = 5x^2 + 2$

Find $f \cdot g$.

A) $(f \cdot g)(x) = 15x^6 + 6x^3 + 10x^2 + 4;$ all real numbers

B) $(f \cdot g)(x) = 15x^5 + 6x^3 + 10x^2 + 4;$ all real numbers

C) $(f \cdot g)(x) = 3x^3 + 5x^2 + 4;$ all real numbers

D) $(f \cdot g)(x) = 15x^5 + 6x^3 + 10x^2 + 4;\ \{x \mid x \neq 0\}$

8) $f(x) = \sqrt{x};\ g(x) = 4x - 9$

Find $\frac{f}{g}$.

A) $\left(\frac{f}{g}\right)(x) = \frac{\sqrt{x}}{4x - 9};\ \{x \mid x \neq 0\}$

B) $\left(\frac{f}{g}\right)(x) = \frac{\sqrt{x}}{4x - 9};\ \left\{x \mid x \geq 0,\ x \neq \frac{9}{4}\right\}$

C) $\left(\frac{f}{g}\right)(x) = \frac{4x - 9}{\sqrt{x}};\ \{x \mid x \geq 0\}$

D) $\left(\frac{f}{g}\right)(x) = \frac{\sqrt{x}}{4x - 9};\ \left\{x \mid x \neq \frac{9}{4}\right\}$

9) $f(x) = \sqrt{9 - x};\ g(x) = \sqrt{x - 4}$

Find $f \cdot g$.

A) $(f \cdot g)(x) = \sqrt{(9 - x)(x - 4)};\ \{x \mid 4 \leq x \leq 9\}$

B) $(f \cdot g)(x) = \sqrt{(9 - x)(x - 4)};\ \{x \mid x \geq 0\}$

C) $(f \cdot g)(x) = \sqrt{-x^2 - 36};\ \{x \mid x \neq 36\}$

D) $(f \cdot g)(x) = \sqrt{(9 - x)(x - 4)};\ \{x \mid x \neq 4,\ x \neq 9\}$

10) $f(x) = \frac{5x + 6}{6x - 1}$; $g(x) = \frac{8x}{6x - 1}$

Find f + g.

A) $(f + g)(x) = \frac{-3x - 6}{6x - 1}$; $\left\{x \mid x \neq \frac{1}{6}\right\}$

B) $(f + g)(x) = \frac{13x + 6}{6x - 1}$; $\left\{x \mid x \neq \frac{1}{6}\right\}$

C) $(f + g)(x) = \frac{13x + 6}{6x - 1}$; $\{x \mid x \neq 0\}$

D) $(f + g)(x) = \frac{13x + 6}{6x - 1}$; $\left\{x \mid x \neq \frac{1}{6}, x \neq -\frac{6}{13}\right\}$

11) $f(x) = \sqrt{x + 11}$; $g(x) = \frac{4}{x}$

Find f • g.

A) $(f \cdot g)(x) = \sqrt{\frac{4x + 44}{x}}$; $\{x \mid x \geq -11, x \neq 0\}$

B) $(f \cdot g)(x) = \frac{\sqrt{4x + 44}}{x}$; $\{x \mid x \geq -11, x \neq 0\}$

C) $(f \cdot g)(x) = \sqrt{\frac{15}{x}}$; $\{x \mid x \neq 0\}$

D) $(f \cdot g)(x) = \frac{4\sqrt{x + 11}}{x}$; $\{x \mid x \geq -11, x \neq 0\}$

Solve the problem.

12) Given $f(x) = \frac{1}{x}$ and $(\frac{f}{g})(x) = \frac{x - 6}{x^2 + 5x}$, find the function g.

A) $g(x) = \frac{x + 6}{x - 5}$ B) $g(x) = \frac{x - 6}{x + 5}$ C) $g(x) = \frac{x + 5}{x - 6}$ D) $g(x) = \frac{x - 5}{x + 6}$

13) Find (f + g)(1) when f(x) = x + 5 and g(x) = x + 2.

A) 5 B) –1 C) 9 D) –5

14) Find (f – g)(–1) when $f(x) = 4x^2 + 5$ and g(x) = x + 4.

A) 4 B) –8 C) 6 D) 14

15) Find (fg)(4) when f(x) = x – 3 and $g(x) = -5x^2 + 12x - 4$.

A) –588 B) –36 C) –252 D) 60

16) Find $\left(\frac{f}{g}\right)(-2)$ when f(x) = 2x – 5 and $g(x) = 3x^2 + 14x + 4$.

A) – 3 B) 0 C) $\frac{3}{4}$ D) $-\frac{1}{4}$

Find and simplify the difference quotient of f, $\frac{f(x + h) - f(x)}{h}$, h≠ 0, for the function.

17) f(x) = 8x – 1

A) $8 + \frac{-2}{h}$ B) $8 + \frac{16(x - 1)}{h}$ C) 0 D) 8

18) $f(x) = 3x^2$

A) 3(2x+h) B) $\frac{3(2x^2 + 2xh + h^2)}{h}$ C) 3 D) $\frac{6}{h} + x + 3h$

19) f(x) = 5

A) $1 + \frac{10}{h}$ B) 5 C) 0 D) 1

20) $f(x) = \frac{1}{9x}$

A) $\frac{-1}{x(x + h)}$ B) $\frac{1}{9x}$ C) $\frac{-1}{9x\,(x + h)}$ D) 0

21) $f(x) = x^2 + 5x + 6$

A) $2x + h + 5$ B) $2x + h + 6$

C) 1 D) $\frac{2x^2 + 2x + 2xh + h^2 + h + 12}{h}$

Solve the problem.

22) Express the gross salary G of a person who earns \$10 per hour as a function of the number x of hours worked.

A) $G(x) = 10 + x$ B) $G(x) = 10x^2$ C) $G(x) = 10x$ D) $G(x) = \frac{10}{x}$

23) Jacey, a commissioned salesperson, earns \$370 base pay plus \$30 per item sold. Express Jacey's gross salary G as a function of the number x of items sold.

A) $G(x) = 30(x + 370)$ B) $G(x) = 30x + 370$ C) $G(x) = 370x + 30$ D) $G(x) = 370(x + 30)$

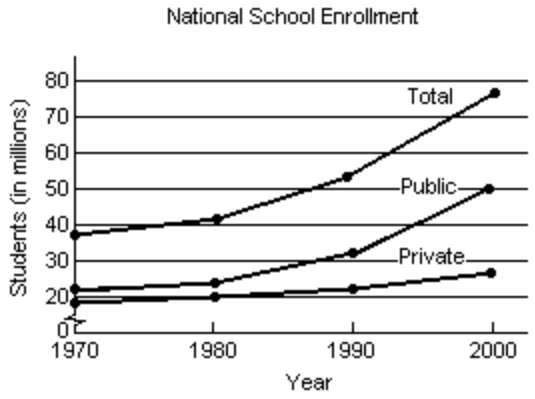
24) Suppose that P(x) represents the percentage of income spent on food in year x and I(x) represents income in year x. Determine a function F that represents total food expenditures in year x.

A) $F(x) = \left(\frac{I}{P}\right)(x)$ B) $F(x) = (P \cdot I)(x)$ C) $F(x) = (I - P)(x)$ D) $F(x) = (P + I)(x)$

25) A retail store buys 55 VCRs from a distributor at a cost of \$150 each plus an overhead charge of \$25 per order. The retail markup is 40% on the total price paid. Find the profit on the sale of one VCR.

A) \$6018.18 B) \$59.82 C) \$60.00 D) \$60.18

26) The following graph shows the private, public and total national school enrollment for students for select years from 1970 through 2000.



i) How is the graph for total school enrollment, T, determined from the graph of the private enrollment, r, and the public enrollment, u?
ii) During which 10–year period did the total number of students enrolled increase the least?
iii) During which 10–year period did the total number of students enrolled increase the most?

A) i) T is the sum of r and u.
ii) 1970 – 1980
iii) 1980–1990

B) i) T is the sum of r and u.
ii) 1990–2000
iii) 1970–1980

C) i) T is the difference of r and u.
ii) 1970 – 1980
iii) 1990–2000

D) i) T is the sum of r and u.
ii) 1970 – 1980
iii) 1990–2000

27) A firm is considering a new product. The accounting department estimates that the total cost, C(x), of producing x units will be

$C(x) = 70x + 6410.$

The sales department estimates that the revenue, R(x), from selling x units will be

$R(x) = 80x,$

but that no more than 898 units can be sold at that price. Find and interpret (R – C)(898).

A) $141,110 profit, income exceeds cost
It is worth it to develop product.

B) $1539 profit, income exceeds cost
It is worth it to develop product.

C) $2570 profit, income exceeds cost
It is worth it to develop product.

D) –$2570 loss, cost exceeds income
It is not worth it to develop product.

28) The function $f(t) = -0.14t^2 + 0.5t + 30.6$ models the U.S. population in millions, ages 65 and older, where t represents years after 1990. The function $g(t) = 0.56t^2 + 12.36t + 105.7$ models the total yearly cost of Medicare in billions of dollars, where t represents years after 1990. What does the function $\frac{g}{f}$ represent? Find $\left(\frac{g}{f}\right)(15)$.

A) Cost per person in thousands of dollars. $0.02 thousand
B) Cost per person in thousands of dollars. $63.20 thousand
C) Cost per person in thousands of dollars. $7.98 thousand
D) Cost per person in thousands of dollars. $0.17 thousand

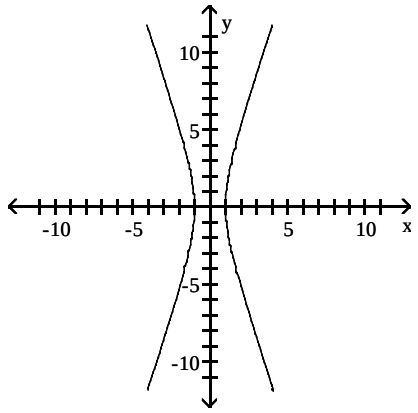
2.2 The Graph of a Function

1 Identify the Graph of a Function

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Determine whether the graph is that of a function. If it is, use the graph to find its domain and range, the intercepts, if any, and any symmetry with respect to the x–axis, the y–axis, or the origin.

1)



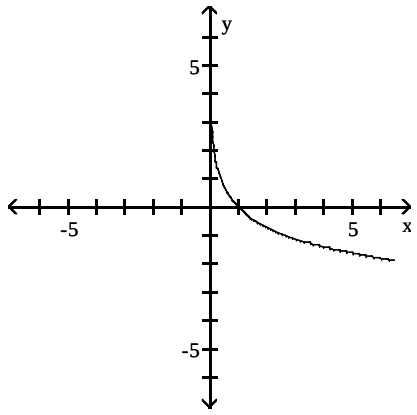
A) function
domain: all real numbers
range: {y | y ≤ –1 or y ≥ 1}
intercepts: (–1, 0), (1, 0)
symmetry: y–axis

B) function
domain: {x | x ≤ –1 or x ≥ 1}
range: all real numbers
intercepts: (–1, 0), (1, 0)
symmetry: x–axis, y–axis, origin

C) function
domain: {x | –1 ≤ x ≤ 1}
range: all real numbers
intercepts: (–1, 0), (1, 0)
symmetry: x–axis, y–axis

D) not a function

2)



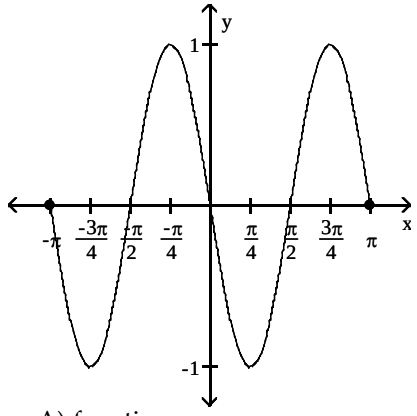
A) function
domain: $\{x \mid x > 0\}$
range: all real numbers
intercept: (1, 0)
symmetry: none

B) function
domain: $\{x \mid x > 0\}$
range: all real numbers
intercept: (0, 1)
symmetry: origin

C) function
domain: all real numbers
range: $\{y \mid y > 0\}$
intercept: (1, 0)
symmetry: none

D) not a function

3)



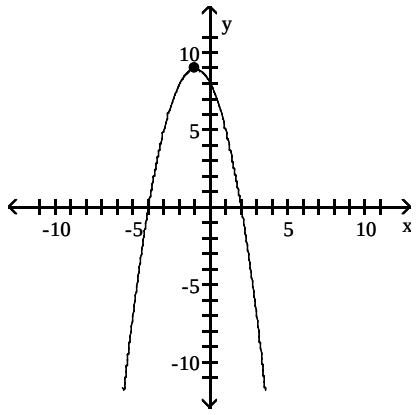
A) function
domain: $\{x \mid -\pi \le x \le \pi\}$
range: $\{y \mid -1 \le y \le 1\}$
intercepts: $(-\pi, 0), (-\frac{\pi}{2}, 0), (0, 0), (\frac{\pi}{2}, 0), (\pi, 0)$
symmetry: origin

B) function
domain: all real numbers
range: $\{y \mid -1 \le y \le 1\}$
intercepts: $(-\pi, 0), (-\frac{\pi}{2}, 0), (0, 0), (\frac{\pi}{2}, 0), (\pi, 0)$
symmetry: origin

C) function
domain: $\{x \mid -1 \le x \le 1\}$
range: $\{y \mid -\pi \le y \le \pi\}$
intercepts: $(-\pi, 0), (-\frac{\pi}{2}, 0), (0, 0), (\frac{\pi}{2}, 0), (\pi, 0)$
symmetry: none

D) not a function

4)



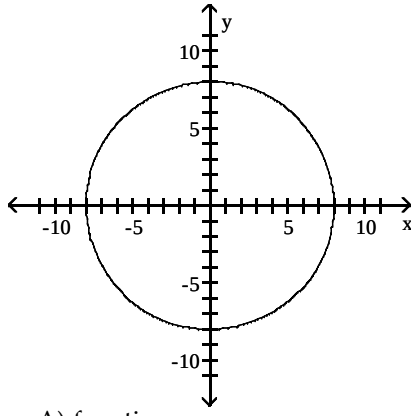
A) function
domain: {x | x ≤ 9}
range: all real numbers
intercepts: (–4, 0), (0, 8), (2, 0)
symmetry: y–axis

B) function
domain: all real numbers
range: {y | y ≤ 9}
intercepts: (0, –4), (8, 0), (0, 2)
symmetry: none

C) function
domain: all real numbers
range: {y | y ≤ 9}
intercepts: (–4, 0), (0, 8), (2, 0)
symmetry: none

D) not a function

5)



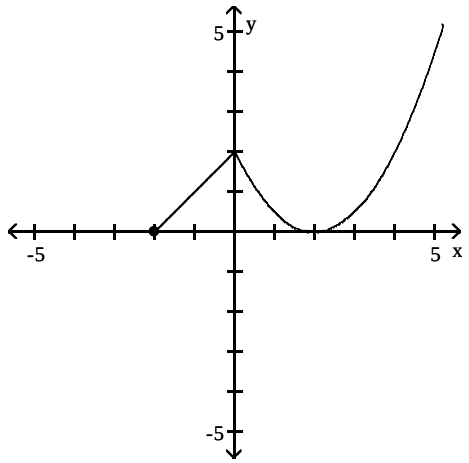
A) function
domain: {x | –8 ≤ x ≤ 8}
range: {y | –8 ≤ y ≤ 8}
intercepts: (–8, 0), (0, –8), (0, 8), (8, 0)
symmetry: x–axis, y–axis, origin

B) function
domain: {x | –8 ≤ x ≤ 8}
range: {y | –8 ≤ y ≤ 8}
intercepts: (–8, 0), (0, –8), (0, 8), (8, 0)
symmetry: x–axis, y–axis

C) function
domain: {x | –8 ≤ x ≤ 8}
range: {y | –8 ≤ y ≤ 8}
intercepts: (–8, 0), (0, –8), (0, 0), (0, 8), (8, 0)
symmetry: origin

D) not a function

6)



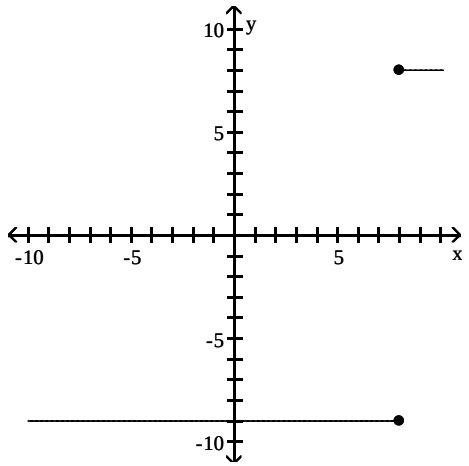
A) function
domain: {x | x ≥ 0}
range: {y | y ≥ –2}
intercepts: (–2, 0), (0, 2), (2, 0)
symmetry: y–axis

B) function
domain: all real numbers
range: all real numbers
intercepts: (–2, 0), (0, 2), (2, 0)
symmetry: none

C) function
domain: {x | x ≥ –2}
range: {y | y ≥ 0}
intercepts: (–2, 0), (0, 2), (2, 0)
symmetry: none

D) not a function

7)



A) function
domain: {x | x = 8 or x = –9}
range: all real numbers
intercept: (–9, 0)
symmetry: x–axis

B) function
domain: all real numbers
range: {y | y = 8 or y = –9}
intercept: (0, –9)
symmetry: none

C) function
domain: all real numbers
range: all real numbers
intercept: (0, –9)
symmetry: none

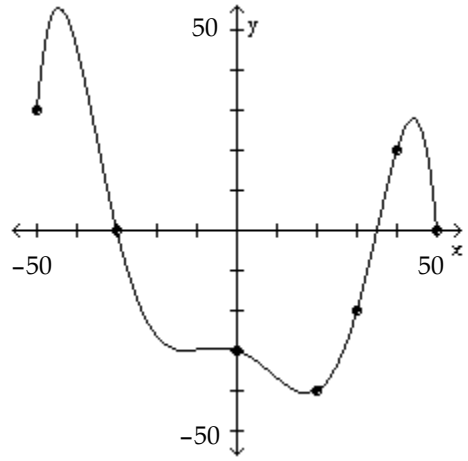
D) not a function

2 Obtain Information from or about the Graph of a Function

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

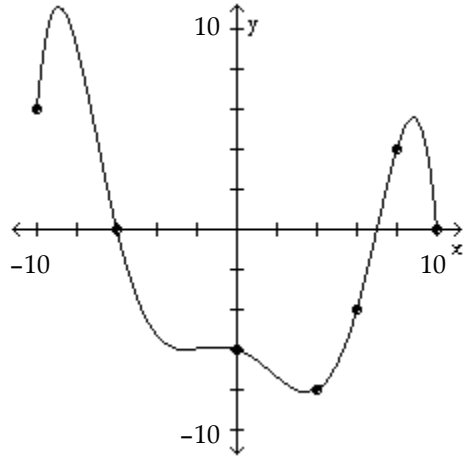
The graph of a function f is given. Use the graph to answer the question.

1) Use the graph of f given below to find f(50).



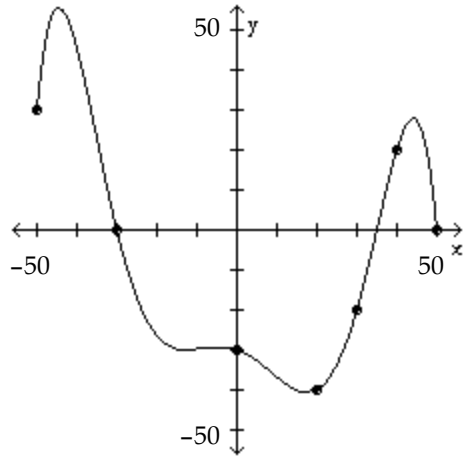
A) 100 B) 60 C) 50 D) 0

2) Is f(8) positive or negative?



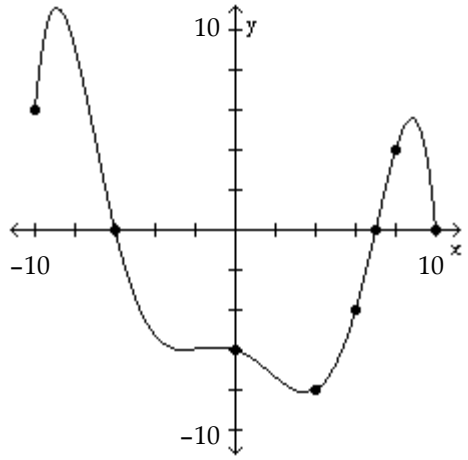
A) positive B) negative

3) Is f(30) positive or negative?



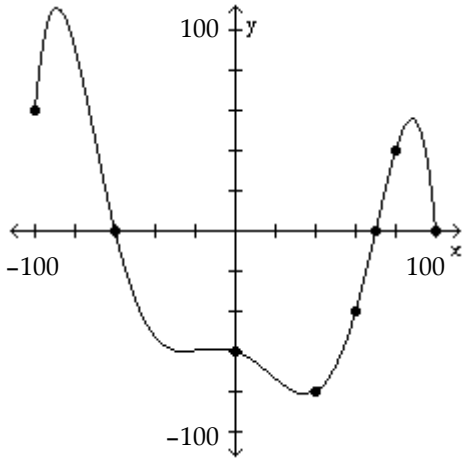
A) positive B) negative

4) For what numbers x is f(x) = 0?



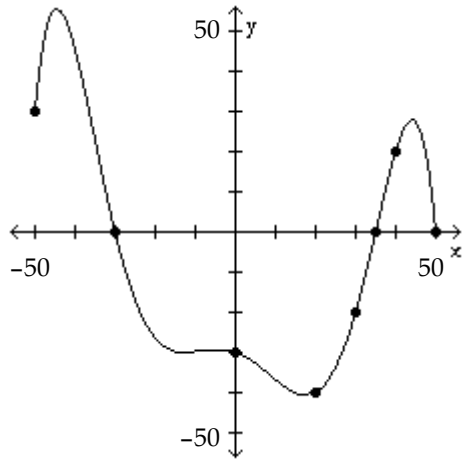
A) –6 B) (–10, –6), (7, 10) C) –6, 7, 10 D) (–6, 7)

5) For what numbers x is f(x) > 0?



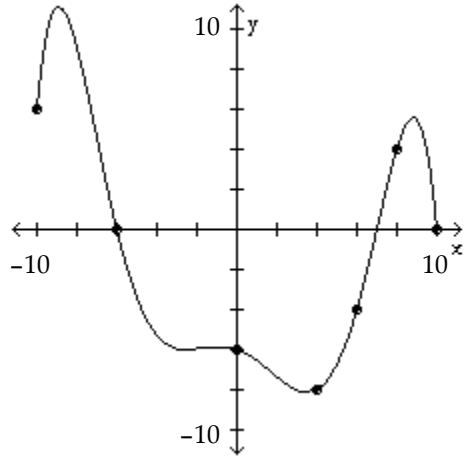
A) (–∞ –60) B) [–100, –60), (70, 100)
C) (–60, ∞) D) (–60, 70)

6) For what numbers x is f(x) < 0?



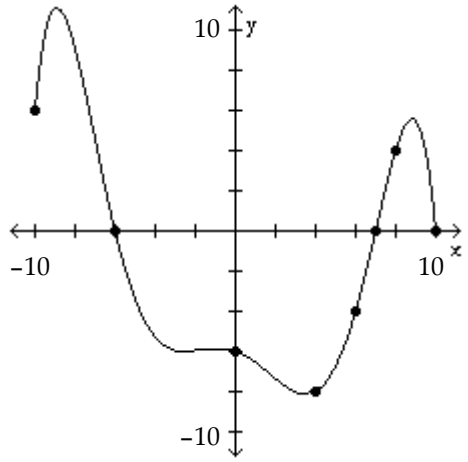
A) (–∞, –30) B) (–30, ∞) C) [–50, –30), (35, 50) D) (–30, 35)

7) What is the domain of f?



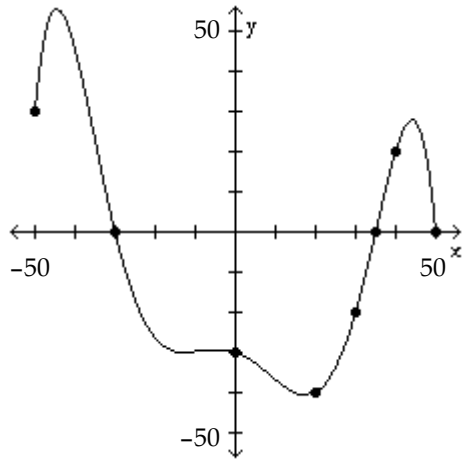
A) all real numbers B) {x | –10 ≤ x ≤ 10} C) {x | x ≥ 0} D) {x | –8 ≤ x ≤ 11}

8) What are the x–intercepts?



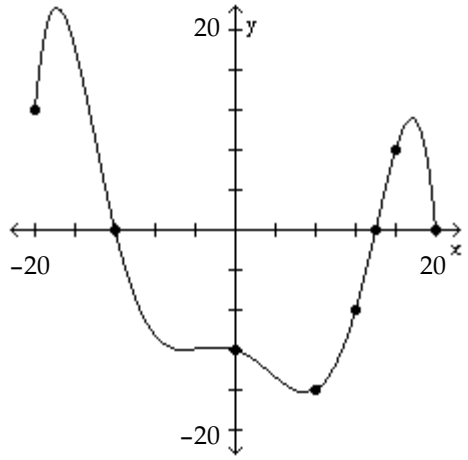
A) –6, 7, 10 B) –6, 7 C) –6 D) –10, –6, 7, 10

9) What is the y–intercept?



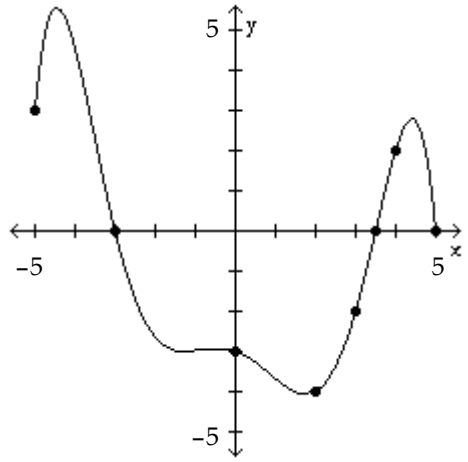
A) 35 B) –40 C) 50 D) –30

10) How often does the line y = –20 intersect the graph?



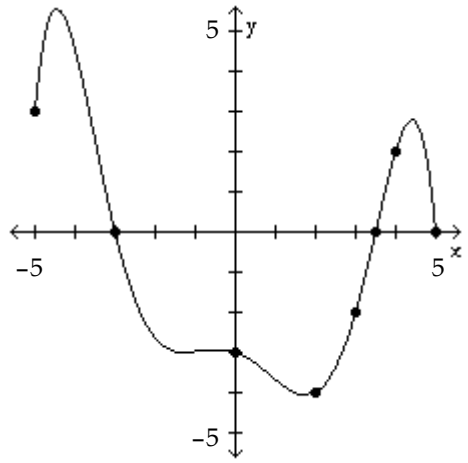
A) once B) twice C) three times D) does not intersect

11) How often does the line y = 1 intersect the graph?



A) once B) twice C) three times D) does not intersect

12) For which of the following values of x does f(x) = –4?



A) –4 B) 0 C) 2 D) 3

Answer the question about the given function.

13) Given the function $f(x) = 5x^2 + 10x + 8$, is the point (–1, 3) on the graph of f?

A) Yes B) No

14) Given the function $f(x) = 4x^2 + 8x - 6$, is the point (–2, 2) on the graph of f?

A) Yes B) No

15) Given the function $f(x) = 3x^2 + 6x + 3$, if x = –1, what is f(x)? What point is on the graph of f?

A) 0; (–1, 0) B) 0; (0, –1) C) 12; (12, –1) D) 12; (–1, 12)

16) Given the function $f(x) = 2x^2 - 4x - 8$, what is the domain of f?

A) all real numbers B) $\{x \mid x \geq 1\}$ C) $\{x \mid x \leq 1\}$ D) $\{x \mid x \geq -1\}$

17) Given the function $f(x) = x^2 + 2x - 48$, list the x–intercepts, if any, of the graph of f.

A) (–8, 0), (6, 0) B) (8, 0), (6, 0) C) (–8, 0), (1, 0) D) (8, 0), (–6, 0)

18) Given the function $f(x) = 5x^2 - 10x + 1$, list the y–intercept, if there is one, of the graph of f.

A) 1 B) 11 C) 16 D) –4

19) Given the function $f(x) = \frac{x^2 - 3}{x - 1}$, is the point $(-2, -\frac{1}{3})$ on the graph of f?

A) Yes B) No

20) Given the function $f(x) = \frac{x^2 - 5}{x - 3}$, is the point $(-1, -\frac{3}{2})$ on the graph of f?

A) Yes B) No

21) Given the function $f(x) = \frac{x^2 - 9}{x + 3}$, if x = –1, what is f(x)? What point is on the graph of f?

A) 5; (–1, 5) B) 5; (5, –1) C) – 4; (–1, – 4) D) – 4; (– 4, –1)

22) Given the function $f(x) = \frac{x^2 + 2}{x + 5}$, what is the domain of f?

A) $\{x \mid x \neq 2\}$ B) $\{x \mid x \neq -\frac{2}{5}\}$ C) $\{x \mid x \neq -5\}$ D) $\{x \mid x \neq 5\}$

23) Given the function $f(x) = \frac{x^2 + 5}{x + 9}$, list the x–intercepts, if any, of the graph of f.

A) $(-\sqrt{5}, 0)$ B) $(-9, 0)$ C) $(5, 0), (-5, 0)$ D) none

24) Given the function $f(x) = \frac{x^2 + 9}{x - 2}$, list the y–intercept, if there is one, of the graph of f.

A) $(-\frac{9}{2}, 0)$ B) $(0, -9)$ C) $(0, 2)$ D) $(0, -\frac{9}{2})$

Solve the problem.

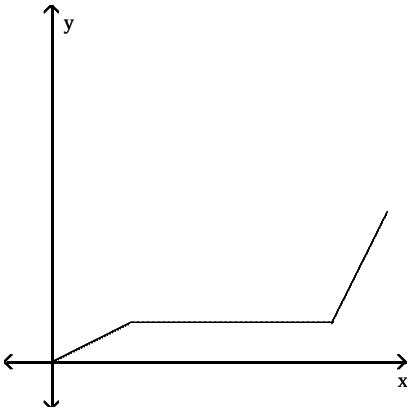
25) If an object weighs m pounds at sea level, then its weight W (in pounds) at a height of h miles above sea level is given approximately by $W(h) = m\left(\frac{4000}{4000 + h}\right)^2$. How much will a man who weighs 165 pounds at sea level weigh on the top of a mountain which is 14,494 feet above sea level? Round to the nearest hundredth of a pound, if necessary.

A) 165 pounds B) 164.77 pounds C) 165.23 pounds D) 7.72 pounds

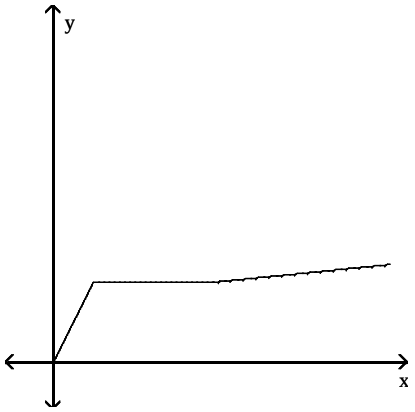
Match the function with the graph that best describes the situation.

26) The amount of rainfall as a function of time, if the rain fell more and more softly.

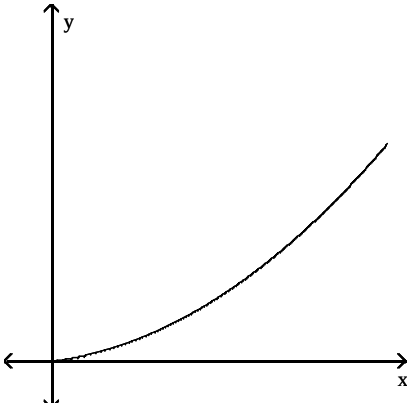
A)



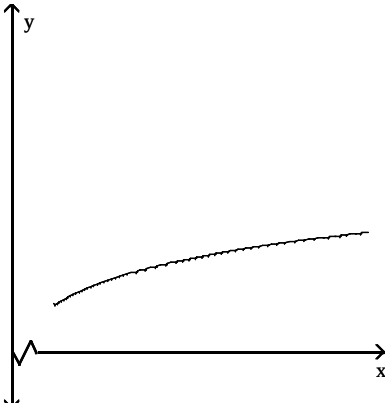
B)



C)

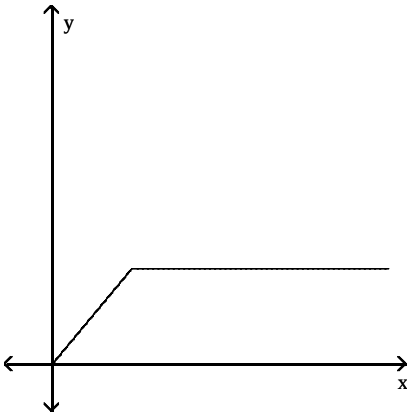


D)

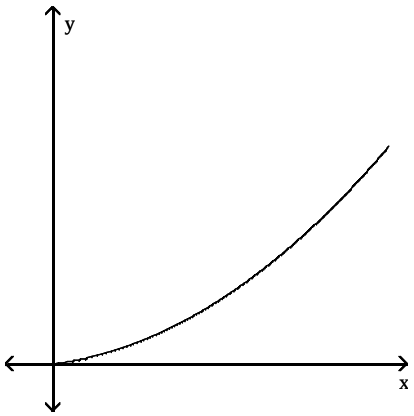


27) The height of an animal as a function of time.

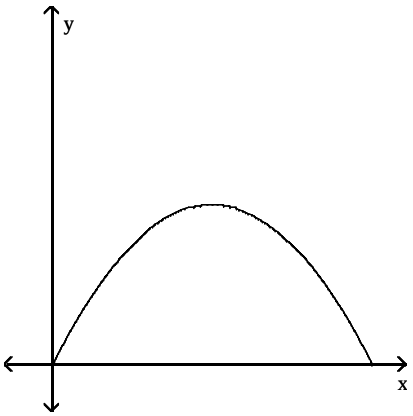
A)



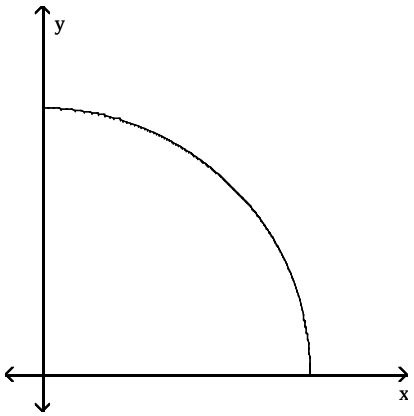
B)



C)



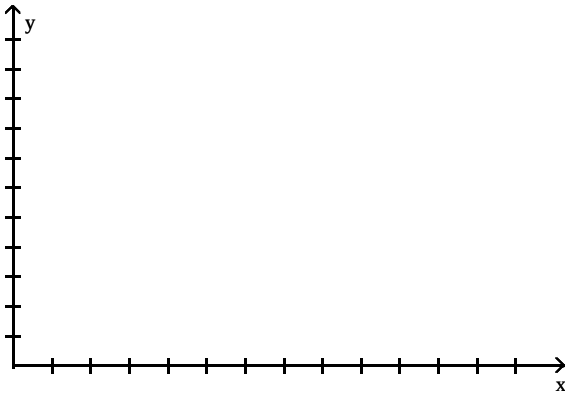
D)



SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

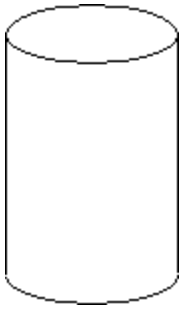
Solve the problem.

28) Michael decides to walk to the mall to do some errands. He leaves home, walks 3 blocks in 9 minutes at a constant speed, and realizes that he forgot his wallet at home. So Michael runs back in 7 minutes. At home, it takes him 3 minutes to find his wallet and close the door. Michael walks 4 blocks in 11 minutes and then decides to jog to the mall. It takes him 5 minutes to get to the mall which is 2 blocks away. Draw a graph of Michael's distance from home (in blocks) as a function of time.



MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

29) A steel can in the shape of a right circular cylinder must be designed to hold 400 cubic centimeters of juice (see figure). It can be shown that the total surface area of the can (including the ends) is given by $S(r) = 2\pi r^2 + \frac{800}{r}$, where r is the radius of the can in centimeters. Using the TABLE feature of a graphing utility, find the radius that minimizes the surface area (and thus the cost) of the can. Round to the nearest tenth of a centimeter.



A) 3.2 cm B) 4 cm C) 5.2 cm D) 0 cm

30) The concentration C (arbitrary units) of a certain drug in a patient's bloodstream can be modeled using $C(t) = \frac{t}{(0.587t + 1.703)^2}$, where t is the number of hours since a 500 milligram oral dose was administered. Using the TABLE feature of a graphing utility, find the time at which the concentration of the drug is greatest. Round to the nearest tenth of an hour.

A) 3.7 hours B) 2.9 hours C) 4.4 hours D) 5.2 hours

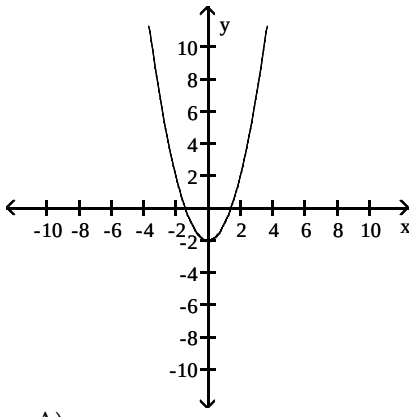
2.3 Properties of Functions

1 Determine Even and Odd Functions from a Graph

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

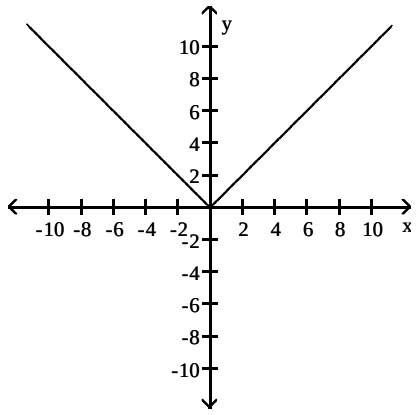
The graph of a function is given. Decide whether it is even, odd, or neither.

1)



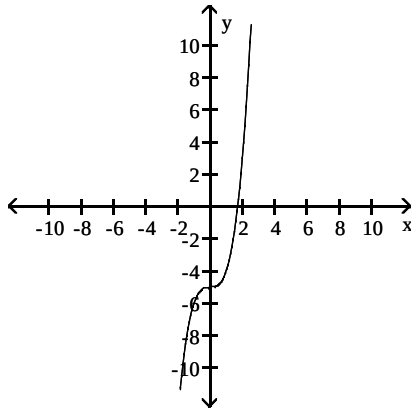
A) even B) odd C) neither

2)



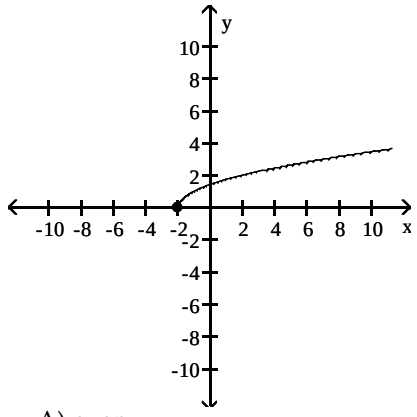
A) even B) odd C) neither

3)



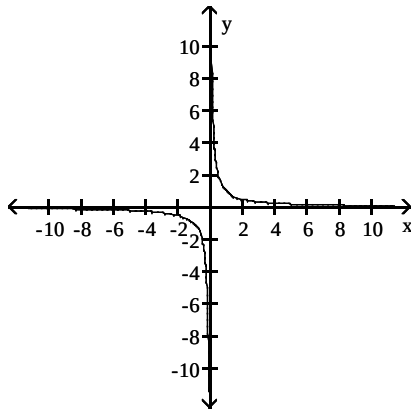
A) even B) odd C) neither

4)



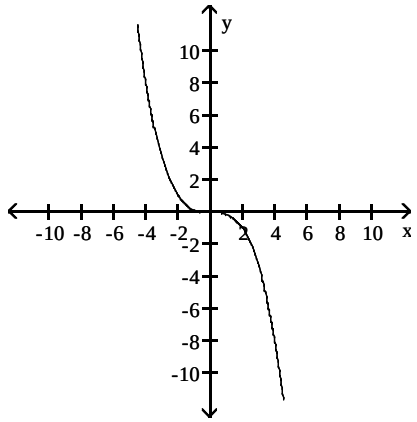
A) even B) odd C) neither

5)



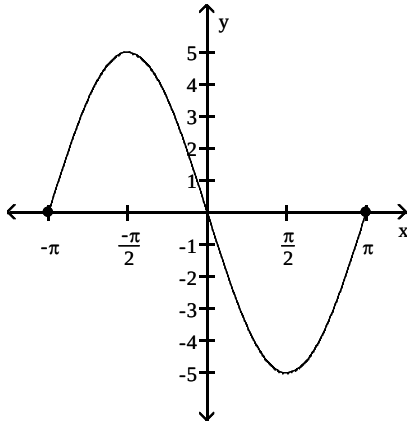
A) even B) odd C) neither

6)



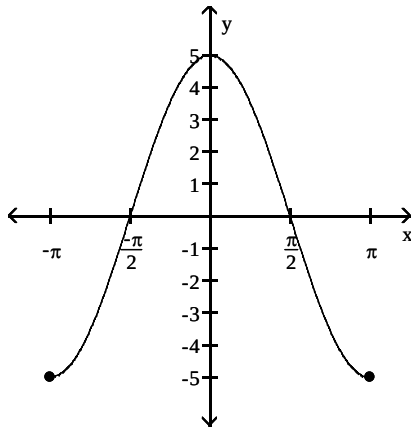
A) even B) odd C) neither

7)



A) even B) odd C) neither

8)



A) even B) odd C) neither

2 Identify Even and Odd Functions from the Equation

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Determine algebraically whether the function is even, odd, or neither.

1) $f(x) = 2x^3$
A) even B) odd C) neither

2) $f(x) = -3x^4 - x^2$
A) even B) odd C) neither

3) $f(x) = -7x^2 - 5$
A) even B) odd C) neither

4) $f(x) = 5x^3 - 2$
A) even B) odd C) neither

5) $f(x) = \sqrt[3]{x}$
A) even B) odd C) neither

6) $f(x) = \sqrt{x}$
A) even B) odd C) neither

7) $\sqrt[3]{2x^2 + 3}$
A) even B) odd C) neither

8) $f(x) = \frac{1}{x^2}$
A) even B) odd C) neither

9) $f(x) = \frac{x}{x^2 + 4}$
A) even B) odd C) neither

10) $f(x) = \dfrac{-x^3}{6x^2 + 4}$

A) even B) odd C) neither

11) $f(x) = \dfrac{-4x}{|x|}$

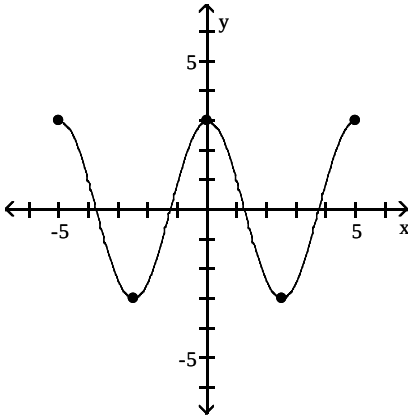
A) even B) odd C) neither

3 Use a Graph to Determine Where a Function Is Increasing, Decreasing, or Constant

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

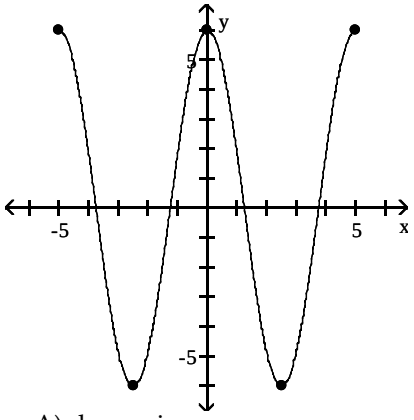
The graph of a function is given. Determine whether the function is increasing, decreasing, or constant on the given interval.

1) $(-5, -\frac{5}{2})$



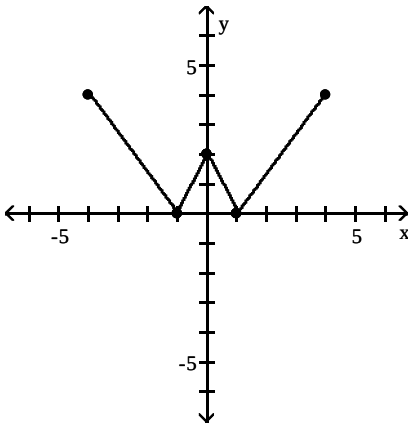
A) increasing B) constant C) decreasing

2) $(-\frac{5}{2}, 0)$



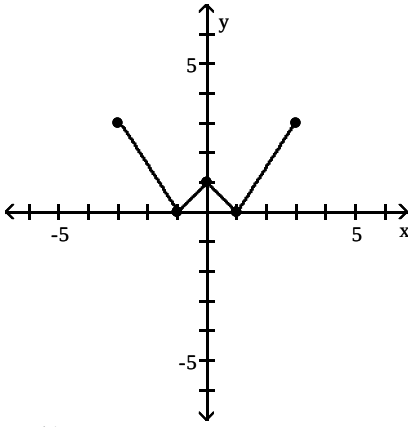
A) decreasing B) increasing C) constant

3) (0, 1)



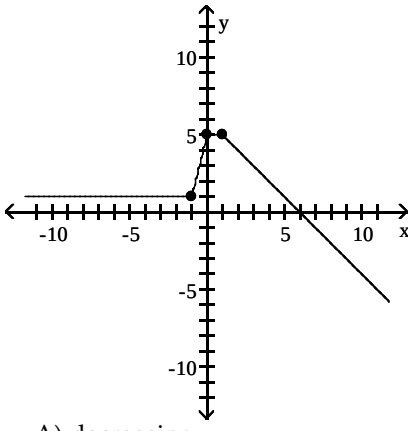
A) constant B) increasing C) decreasing

4) (1, 3)



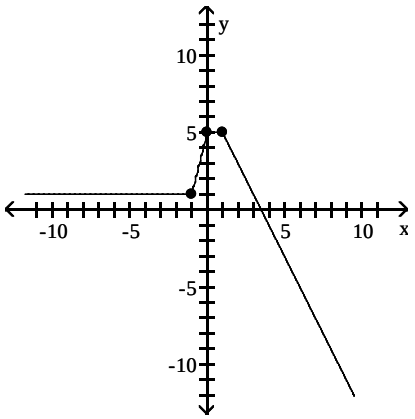
A) increasing B) constant C) decreasing

5) (0, 1)



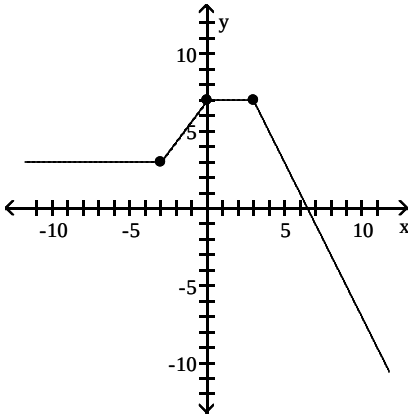
A) decreasing B) increasing C) constant

6) (–1, 0)



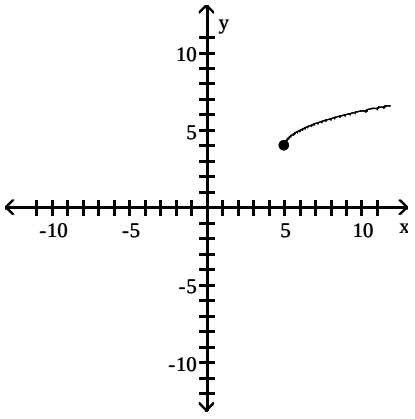
A) decreasing B) increasing C) constant

7) (3, ∞)



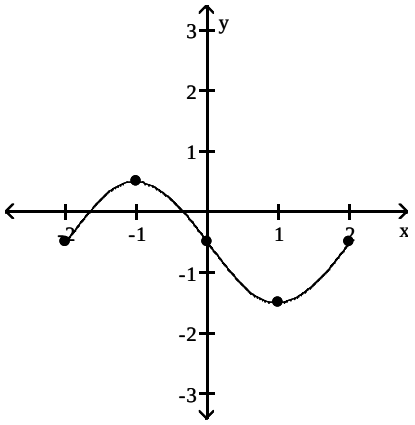
A) decreasing B) constant C) increasing

8) (5, ∞)



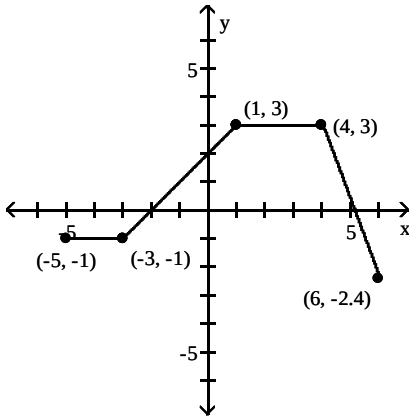
A) increasing B) constant C) decreasing

9) (1, 2)



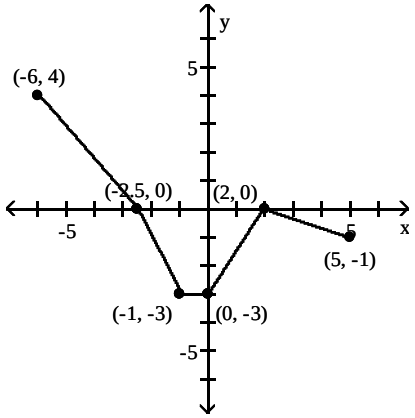
A) decreasing B) increasing C) constant

10) (–3, 1)



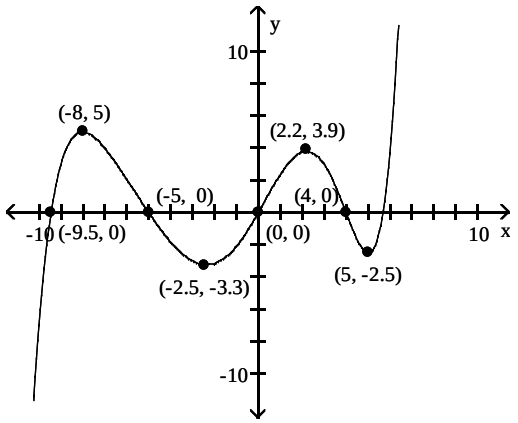
A) increasing B) decreasing C) constant

11) (0, 2)



A) constant B) increasing C) decreasing

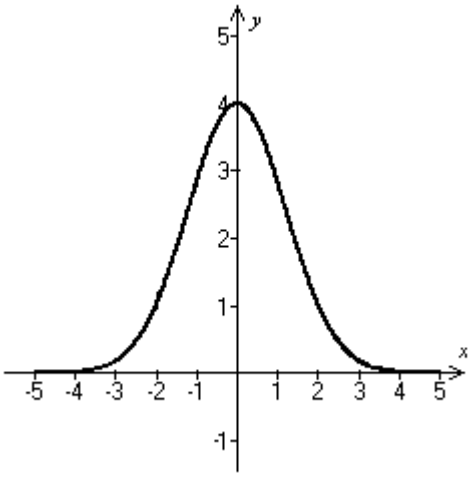
12) (–2.5, 2.2)



A) increasing B) constant C) decreasing

Use the graph to find the intervals on which it is increasing, decreasing, or constant.

13)



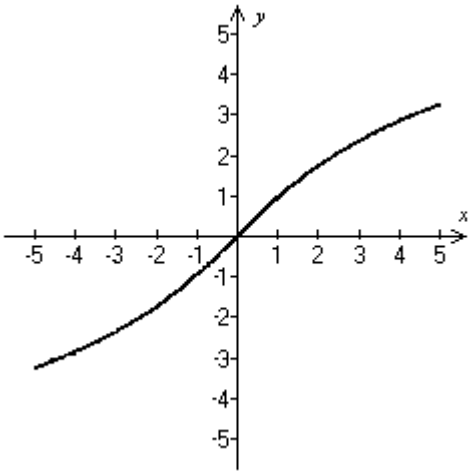
A) Decreasing on (–∞, ∞)

B) Increasing on (–∞, 0); decreasing on (0, ∞)

C) Decreasing on (–∞, 0); increasing on (0, ∞)

D) Increasing on (–∞, ∞)

14)



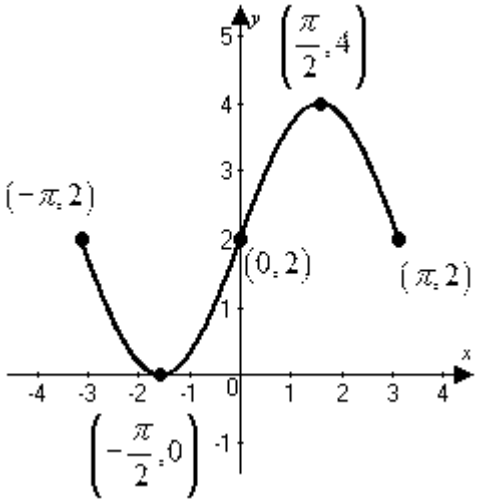
A) Decreasing on $(-\infty, \infty)$

B) Decreasing on $(-\infty, 0)$; increasing on $(0, \infty)$

C) Increasing on $(-\infty, \infty)$

D) Increasing on $(-\infty, 0)$; decreasing on $(0, \infty)$

15)



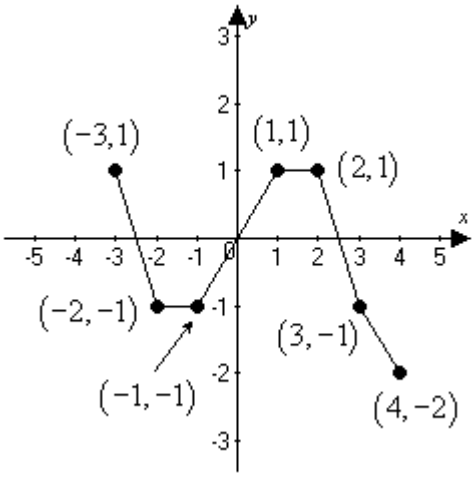
A) Increasing on $\left(-\pi, -\frac{\pi}{2}\right)$ and $\left(\frac{\pi}{2}, \pi\right)$; decreasing on $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

B) Decreasing on $\left(-\pi, -\frac{\pi}{2}\right)$ and $\left(\frac{\pi}{2}, \pi\right)$; increasing on $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

C) Increasing on $(-\infty, \infty)$

D) Decreasing on $(-\pi, 0)$; increasing on $(0, \pi)$

16)



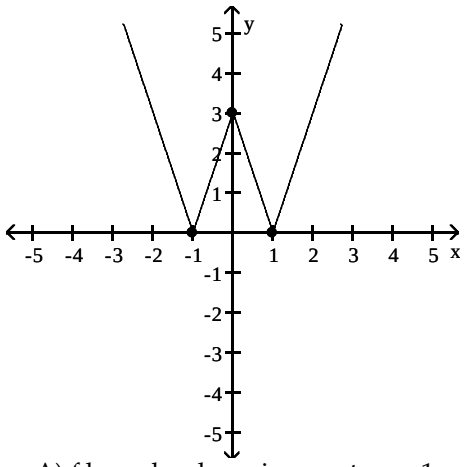
A) Decreasing on (–3, –1) and (1, 4); increasing on (–2, 1)
B) Increasing on (–3, –2) and (2, 4); decreasing on (–1, 1); constant on (–2, –1) and (1, 2)
C) Decreasing on (–3, –2) and (2, 4); increasing on (–1, 1)
D) Decreasing on (–3, –2) and (2, 4); increasing on (–1, 1); constant on (–2, –1) and (1, 2)

4 Use a Graph to Locate Local Maxima and Local Minima

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

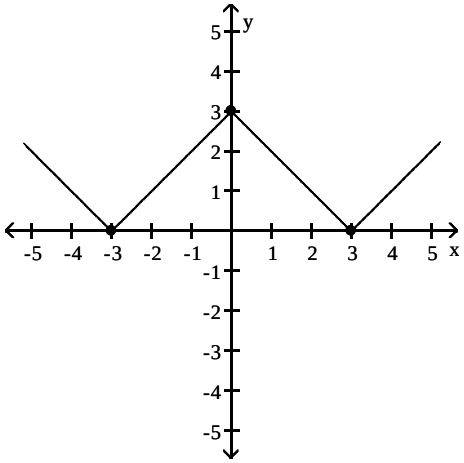
The graph of a function f is given. Use the graph to answer the question.

1) Find the numbers, if any, at which f has a local maximum. What are the local maxima?



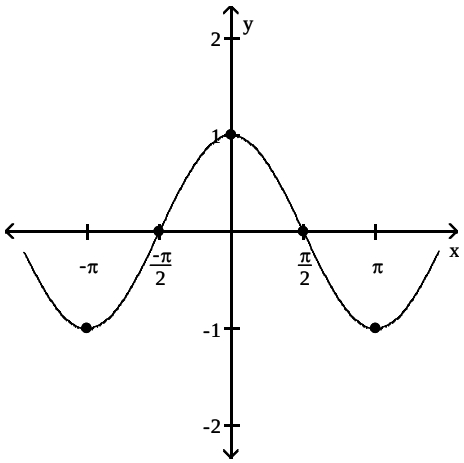
A) f has a local maximum at x = –1 and 1; the local maximum is 0
B) f has a local maximum at x = 1; the local maximum is 3
C) f has a local maximum at x = 0; the local maximum is 3
D) f has no local maximum

2) Find the numbers, if any, at which f has a local minimum. What are the local minima?



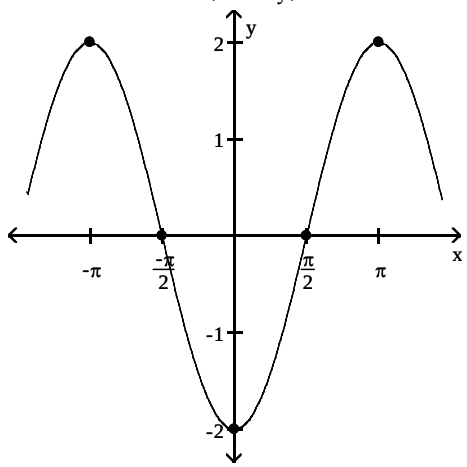
A) f has a local minimum at x = –3; the local minimum is 0
B) f has a local minimum at x = 0; the local minimum is 3
C) f has a local minimum at x = –3 and 3; the local minimum is 0
D) f has no local minimum

3) Find the numbers, if any, at which f has a local maximum. What are the local maxima?



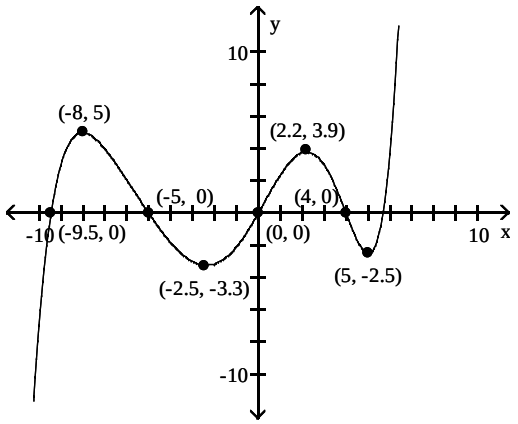
A) f has a local maximum at x = –π and π; the local maximum is –1
B) f has a local maximum at –π; the local maximum is 1
C) f has a local maximum at x = 0; the local maximum is 1
D) f has no local maximum

4) Find the numbers, if any, at which f has a local minimum. What are the local minima?



A) f has a local minimum at $x = -\pi$ and π; the local minimum is 2
B) f has no local minimum
C) f has a local minimum at $x = 0$; the local minimum is −2
D) f has a local minimum at $x = -\pi$; the local minimum is −2

5)

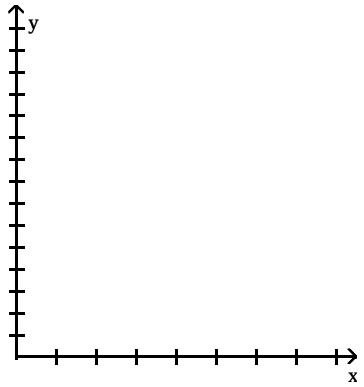


Find the numbers, if any, at which f has a local minimum. What are the local maxima?

A) f has a local minimum at $x = -2.5$ and 5; the local minimum at −2.5 is −3.3; the local minimum at 5 is −2.5
B) f has a local maximum at $x = -2.5$ and 5; the local maximum at −2.5 is −3.3; the local maximum at 5 is −2.5
C) f has a local minimum at $x = -3.3$ and −2.5; the local minimum at −3.3 is −2.5; the local minimum at −2.5 is 5
D) f has a local maximum at $x = -3.3$ and −2.5; the local maximum at −3.3 is −2.5; the local maximum at −2.5 is 5

Solve the problem.

6) The height s of a ball (in feet) thrown with an initial velocity of 70 feet per second from an initial height of 8 feet is given as a function of time t (in seconds) by $s(t) = -16t^2 + 70t + 8$. What is the maximum height? Round to the nearest hundredth, if necessary.



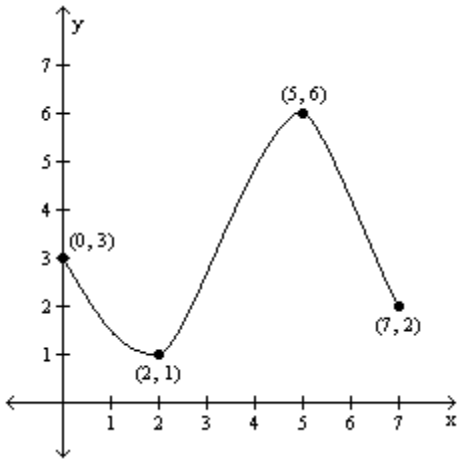
A) 84.56 ft B) –54.19 ft C) 95.5 ft D) 77.06 ft

5 Use a Graph to Locate the Absolute Maximum and the Absolute Minimum

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

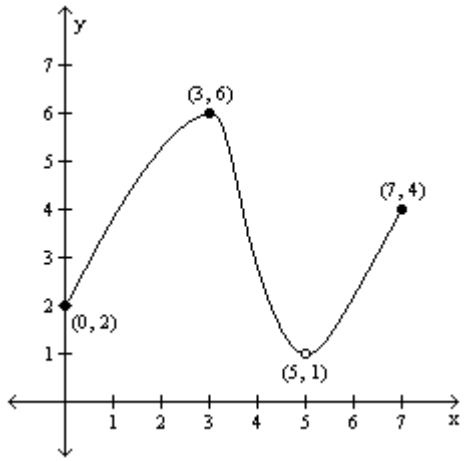
For the graph of the function y = f(x), find the absolute maximum and the absolute minimum, if it exists.

1)



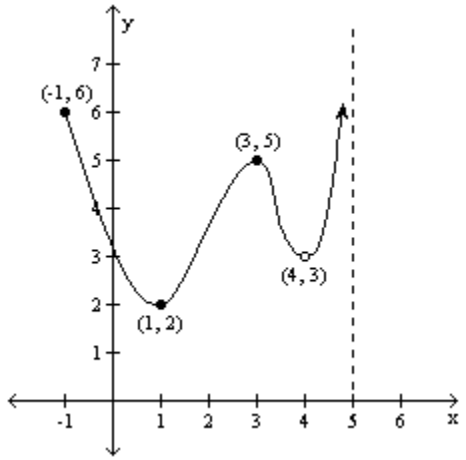
A) Absolute maximum: f(5) = 6; Absolute minimum: f(2) = 1
B) Absolute maximum: f(6) = 5; Absolute minimum: f(1) = 2
C) Absolute maximum: f(2) = 7; Absolute minimum: f(3) = 0
D) Absolute maximum: f(7) = 2; Absolute minimum: f(0) = 3

2)



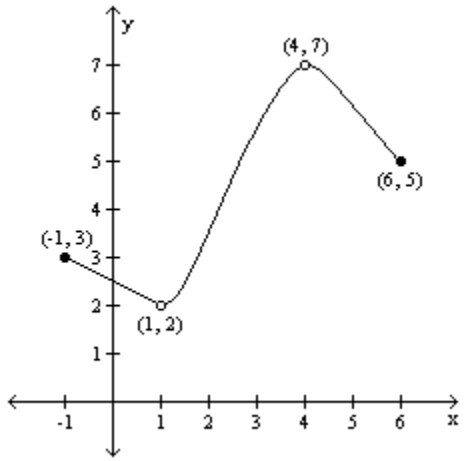
A) Absolute maximum: f(3) = 6; Absolute minimum: f(5) = 1
B) Absolute maximum: f(3) = 6; Absolute minimum: none
C) Absolute maximum: f(7) = 4; Absolute minimum: f(0) = 2
D) Absolute maximum: f(3) = 6; Absolute minimum: f(0) = 2

3)



A) Absolute maximum: none; Absolute minimum: f(1) = 2
B) Absolute maximum: f(3) = 5; Absolute minimum: f(1) = 2
C) Absolute maximum: f(−1) = 6; Absolute minimum: f(1) = 2
D) Absolute maximum: none; Absolute minimum: none

4)



A) Absolute maximum: none; Absolute minimum: f(1) = 2
B) Absolute maximum: f(4) = 7; Absolute minimum: f(1) = 2
C) Absolute maximum: none; Absolute minimum: none
D) Absolute maximum: f(4) = 7; Absolute minimum: none

6 Use Graphing Utility to Approximate Local Maxima/Minima and to Determine Where Function Is Incrs/Decrs

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Use a graphing utility to graph the function over the indicated interval and approximate any local maxima and local minima. Determine where the function is increasing and where it is decreasing. If necessary, round answers to two decimal places.

1) $f(x) = x^3 - 3x + 1, (-2, 2)$

A) local maximum at (–1, 3)
local minimum at (1, –1)
increasing on (–2, –1) and (1, 2)
decreasing on (–1, 1)

B) local maximum at (1, –1)
local minimum at (–1, 3)
increasing on (–2, –1) and (1, 2)
decreasing on (–1, 1)

C) local maximum at (–1, 3)
local minimum at (1, –1)
increasing on (–1, 1)
decreasing on (–2, –1) and (1, 2)

D) local maximum at (1, –1)
local minimum at (–1, 3)
increasing on (–2, –1)
decreasing on (–1, 1)

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

2) $f(x) = x^3 - 4x^2 + 6;\ (-1, 4)$

3) $f(x) = x^5 - x^2;\ (-2, 2)$

4) $f(x) = -0.3x^3 + 0.2x^2 + 4x - 5;\ (-4, 5)$

5) $f(x) = 0.15x^4 + 0.3x^3 - 0.8x^2 + 5;\ (-4, 2)$

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Use a graphing utility to graph the function over the indicated interval and approximate any local maxima and local minima. If necessary, round answers to two decimal places.

6) $f(x) = x^2 + 2x - 3;\ (-5, 5)$

A) local maximum at (1, –4)
B) local maximum at (–1, 4)
C) local minimum at (–1, –4)
D) local minimum at (1, 4)

7) $f(x) = 2 + 8x - x^2$; $(-5, 5)$

A) local minimum at (4, 50)
C) local maximum at (−4, 50)
B) local minimum at (−4, 18)
D) local maximum at (4, 18)

8) $f(x) = x^3 - 3x^2 + 1$; $(-5, 5)$

A) local minimum at (0, 1)
local maximum at (2, −3)
C) local minimum at (2, −3)
B) local maximum at (0, 1)
local minimum at (2, −3)
D) none

9) $f(x) = x^3 - 12x + 2$; $(-5, 5)$

A) local maximum at (−2, 18)
local minimum at (0, 0)
local minimum at (2, −14)
C) local minimum at (0, 0)
B) local maximum at (−2, 18)
local minimum at (2, −14)
D) none

10) $f(x) = x^4 - 5x^3 + 3x^2 + 9x - 3$; $(-5, 5)$

A) local minimum at (−0.57, −6.12)
local maximum at (1.32, 5.64)
local minimum at (3, −3)
C) local minimum at (−1, −6)
local maximum at (1, 6)
local minimum at (3, −3)
B) local minimum at (−0.61, −5.64)
local maximum at (1.41, 6.12)
local minimum at (3, −3)
D) local minimum at (−3, −3)
local maximum at (−1.32, 5.64)
local minimum at (0.57, −6.12)

Solve.

11) John owns a hotdog stand. He has found that his profit is represented by the equation $P(x) = -x^2 + 52x + 74$, with P being profits and x the number of hotdogs sold. How many hotdogs must he sell to earn the most profit?

A) 27 hotdogs B) 26 hotdogs C) 48 hotdogs D) 24 hotdogs

12) Bob owns a watch repair shop. He has found that the cost of operating his shop is given by $c(x) = 4x^2 - 384x + 87$, where c is cost and x is the number of watches repaired. How many watches must he repair to have the lowest cost?

A) 43 watches B) 87 watches C) 48 watches D) 40 watches

13) John owns a hotdog stand. His profit is represented by the equation $P(x) = -x^2 + 14x + 58$, with P being profits and x the number of hotdogs sold. What is the most he can earn?

A) $49 B) $93 C) $107 D) $135

14) A rock falls from a tower that is 102.9 m high. As it is falling, its height is given by the formula $h(t) = 102.9 - 4.9t^2$. How many seconds will it take for the rock to hit the ground (h=0)? Round to the nearest tenth.

A) 21.2 sec B) 2200 sec C) 4.6 sec D) 10.1 sec

15) A projectile is thrown upward so that its distance above the ground after t seconds is $h(t) = -16t^2 + 546t$. After how many seconds does it reach its maximum height? Round to the nearest second.

A) 42 sec B) 31.5 sec C) 10 sec D) 17 sec

16) A rock falls from a tower that is 352 ft high. As it is falling, its height is given by the formula $h(t) = 352 - 16t^2$. How many seconds will it take for the rock to hit the ground ($h = 0$)? Round to the nearest tenth.

A) 4.7 sec B) 18.8 sec C) 22.1 sec D) 7744 sec

7 Find the Average Rate of Change of a Function

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

For the function, find the average rate of change of f from 1 to x:

$\frac{f(x) - f(1)}{x - 1}$, $x \neq 1$

1) $f(x) = 5x$

A) $\frac{5}{x - 1}$ B) 5 C) 0 D) 4

2) $f(x) = x^2 - 2x$

A) $\frac{x^2 - 2x - 1}{x - 1}$ B) 1 C) $x - 1$ D) $x + 1$

3) $f(x) = \frac{6}{x + 5}$

A) $\frac{6}{x(x + 5)}$ B) $\frac{1}{x + 5}$ C) $\frac{6}{(x - 1)(x + 5)}$ D) $-\frac{1}{x + 5}$

4) $f(x) = \sqrt{x + 8}$

A) $\frac{\sqrt{x + 8} + 3}{x + 1}$ B) $\frac{\sqrt{x + 8} + 3}{x - 1}$ C) $\frac{\sqrt{x + 8} - 3}{x + 1}$ D) $\frac{\sqrt{x + 8} - 3}{x - 1}$

Find the average rate of change for the function between the given values.

5) $f(x) = -3x + 9$; from 1 to 3

A) -3 B) -9 C) 3 D) 9

6) $f(x) = x^2 + 7x$; from 1 to 5

A) $\frac{52}{5}$ B) 12 C) 13 D) 15

7) $f(x) = 2x^3 + 4x^2 + 6$; from -9 to -5

A) -36 B) $\frac{144}{5}$ C) 246 D) $-\frac{984}{5}$

8) $f(x) = \sqrt{2x}$; from 2 to 8

A) 7 B) 2 C) $-\frac{3}{10}$ D) $\frac{1}{3}$

9) $f(x) = \frac{3}{x - 2}$; from 4 to 7

A) 7 B) $-\frac{3}{10}$ C) $\frac{1}{3}$ D) 2

10) $f(x) = 4x^2$; from 0 to $\frac{7}{4}$

A) $-\frac{3}{10}$ B) 2 C) $\frac{1}{3}$ D) 7

11) $f(x) = -3x^2 - x$; from 5 to 6

A) –2 B) $-\frac{1}{6}$ C) –34 D) $\frac{1}{2}$

12) $f(x) = x^3 + x^2 - 8x - 7$; from 0 to 2

A) –2 B) $-\frac{1}{6}$ C) –28 D) $\frac{1}{2}$

13) $f(x) = \sqrt{2x - 1}$; from 1 to 5

A) $-\frac{1}{6}$ B) –2 C) $\frac{1}{2}$ D) –28

14) $f(x) = \frac{3}{x + 2}$; from 1 to 4

A) $\frac{1}{2}$ B) $-\frac{1}{6}$ C) –2 D) –28

Find an equation of the secant line containing (1, f(1)) and (2, f(2)).

15) $f(x) = x^3 - x$

A) $y = -6x - 6$ B) $y = -6x + 6$ C) $y = 6x + 6$ D) $y = 6x - 6$

16) $f(x) = \frac{2}{x + 1}$

A) $y = \frac{2}{3}x + \frac{1}{3}$ B) $y = -\frac{1}{3}x + \frac{4}{3}$ C) $y = \frac{1}{3}x + \frac{2}{3}$ D) $y = \frac{1}{3}x + 2$

17) $f(x) = \sqrt{x + 3}$

A) $y = (-\sqrt{5} - 2)x - \sqrt{5} + 4$ B) $y = (-\sqrt{5} + 2)x + \sqrt{5} - 4$

C) $y = (\sqrt{5} - 2)x - \sqrt{5} + 4$ D) $y = (\sqrt{5} - 2)x + \sqrt{5} - 4$

Solve the problem.

18) From April through December 2000, the stock price of QRS Company had a roller coaster ride. The chart below indicates the price of the stock at the beginning of each month during that period. Find the monthly average rate of change in price between June and September.

Month	Price
April (x = 1)	116
May	108
June	87
July	100
August	94
September	111
October	92
November	84
December	65

A) –$12.00 per month B) $12.00 per month C) $8.00 per month D) –$8.00 per month

19) Along with incomes, people's charitable contributions have steadily increased over the past few years. The table below shows the average deduction for charitable contributions reported on individual income tax returns for the period 1993 to 1998. Find the average rate of change between 1995 and 1997.

Year	Charitable Contributions
1993	$1980
1994	$2350
1995	$2490
1996	$2760
1997	$3060
1998	$3120

A) $355 per year B) $315 per year C) $285 per year D) $570 per year

20) A deep sea diving bell is being lowered at a constant rate. After 10 minutes, the bell is at a depth of 500 ft. After 55 minutes the bell is at a depth of 1600 ft. What is the average rate of lowering per minute? Round to the nearest hundredth is needed.

A) 20.0 ft per minute B) 24.4 ft per minute C) 29.1 ft per minute D) 0.04 ft per minute

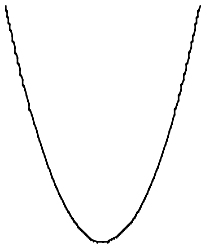
2.4 Library of Functions; Piecewise-defined Functions

1 Graph the Functions Listed in the Library of Functions

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Match the graph to the function listed whose graph most resembles the one given.

1)

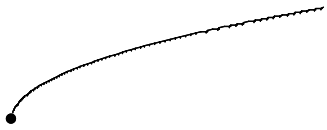


A) absolute value function B) reciprocal function
C) cube function D) square function

2)

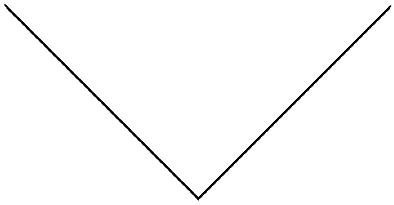
A) reciprocal function B) absolute value function
C) linear function D) constant function

3)



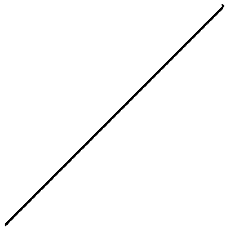
A) square root function B) cube root function
C) square function D) cube function

4)



A) square function
B) absolute value function
C) reciprocal function
D) linear function

5)

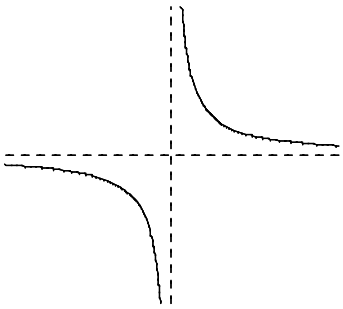


A) constant function
B) absolute value function
C) reciprocal function
D) linear function

6)

A) square root function
B) square function
C) cube function
D) cube root function

7)



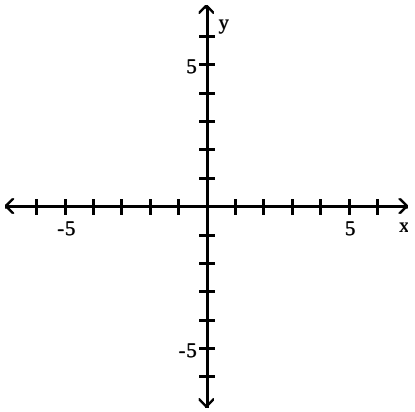
A) absolute value function
B) square function
C) reciprocal function
D) square root function

8)

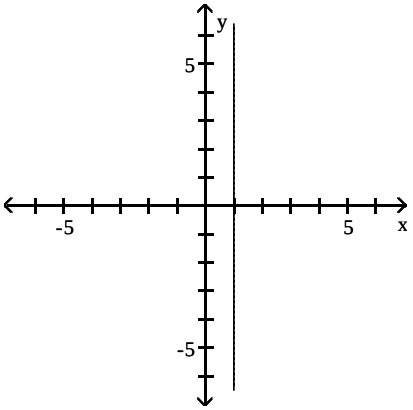
A) square function
B) square root function
C) cube root function
D) cube function

Graph the function.

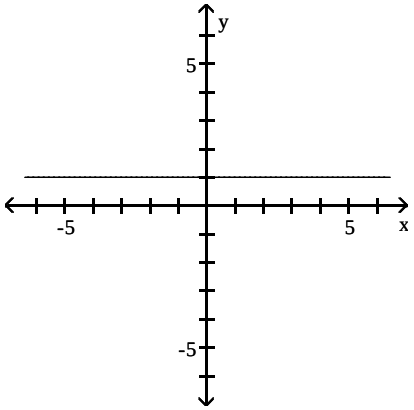
9) f(x) = x



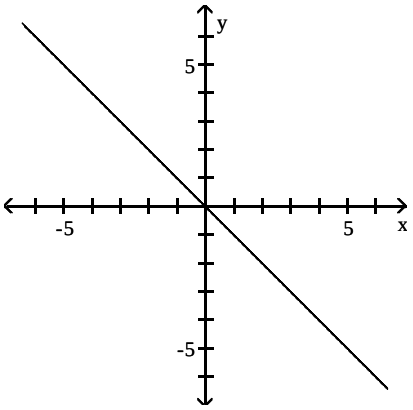
A)



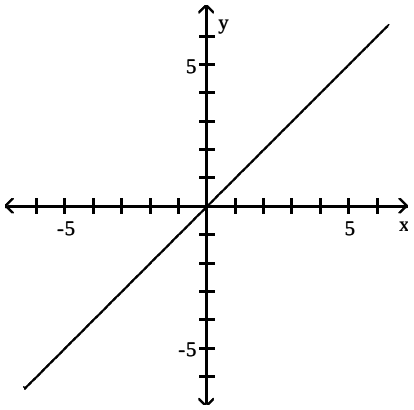
B)



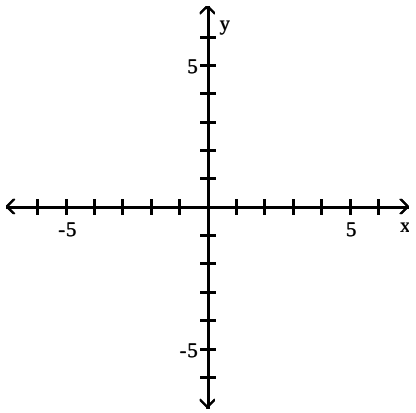
C)



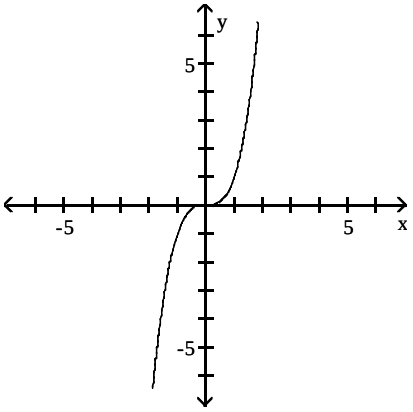
D)



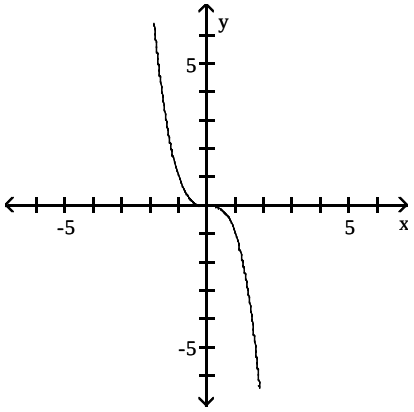
10) $f(x) = x^2$



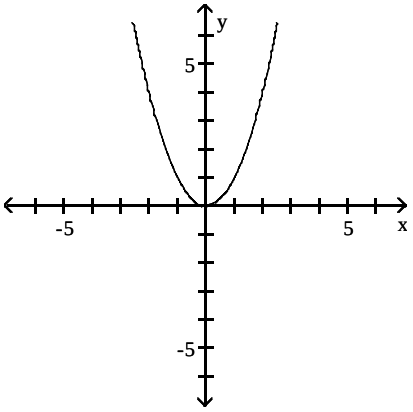
A)



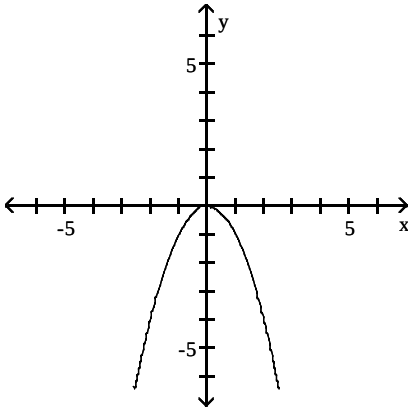
B)



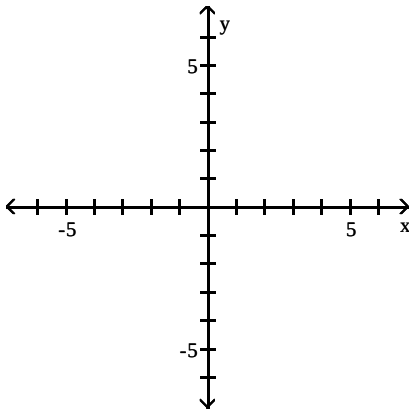
C)



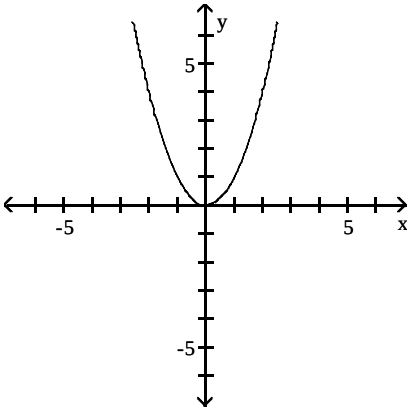
D)



11) $f(x) = x^3$



A)



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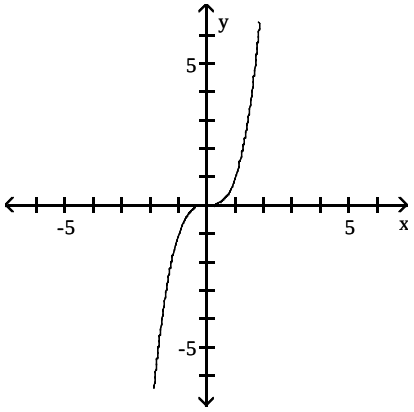
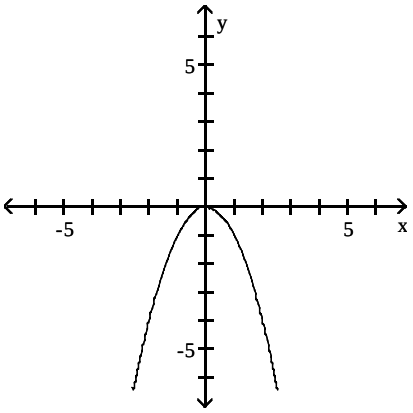
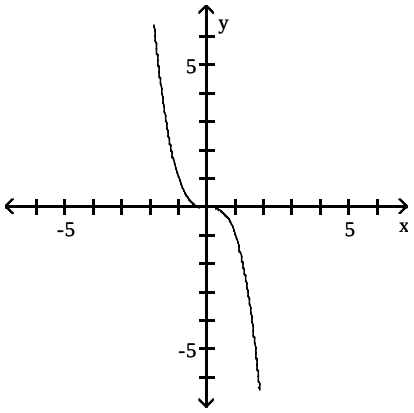


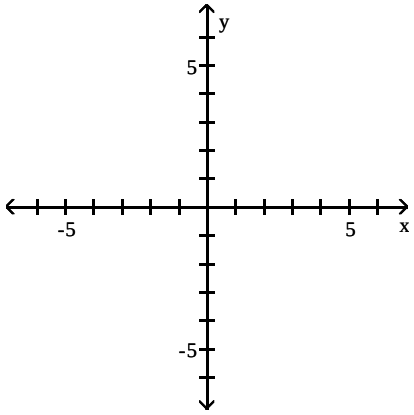
C)



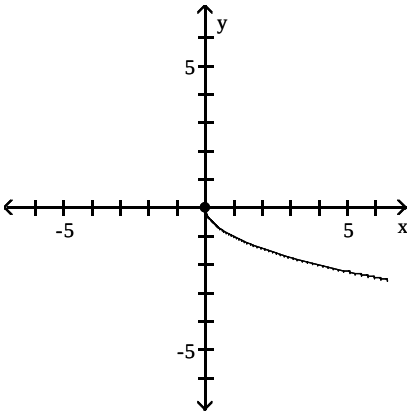
D)



12) $f(x) = \sqrt{x}$



A)



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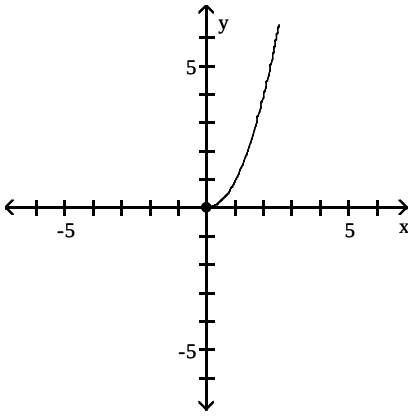

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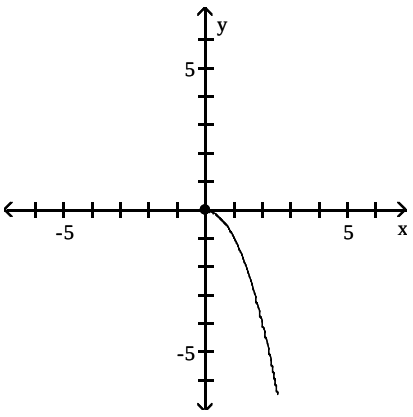
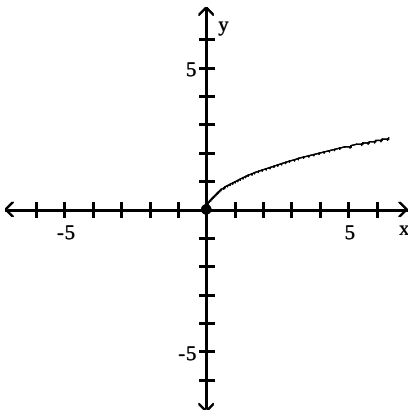
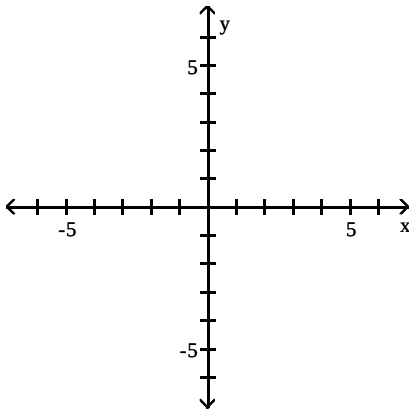


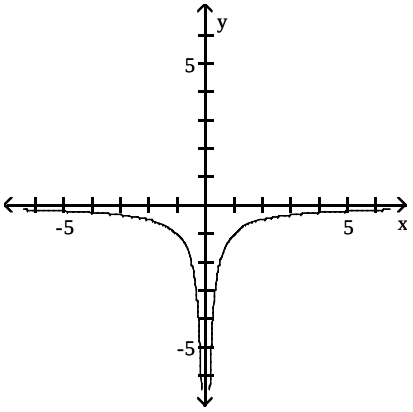
D)



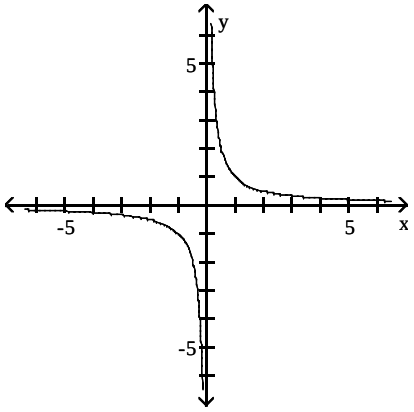
13) $f(x) = \frac{1}{x}$



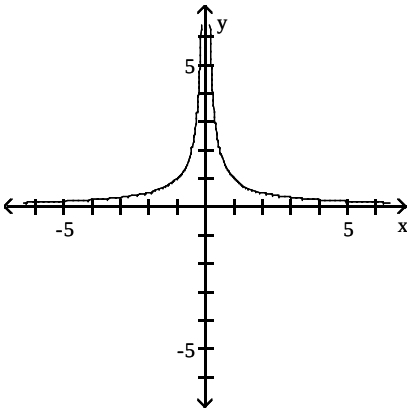
A)



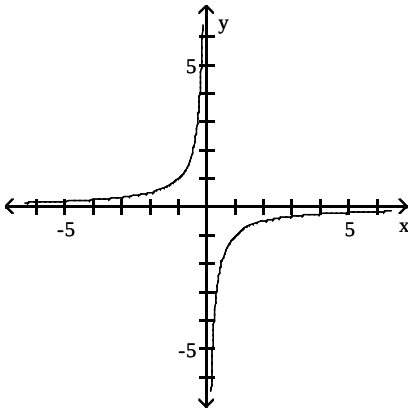
B)



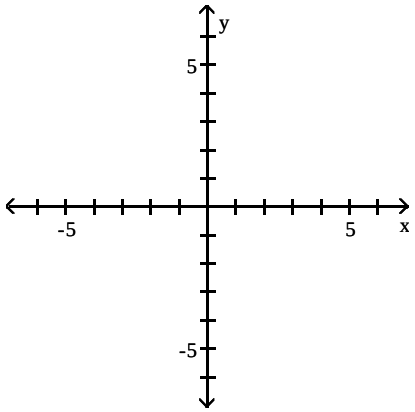
C)



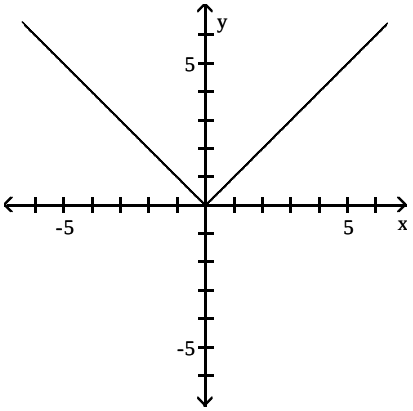
D)



14) $f(x) = |x|$



A)



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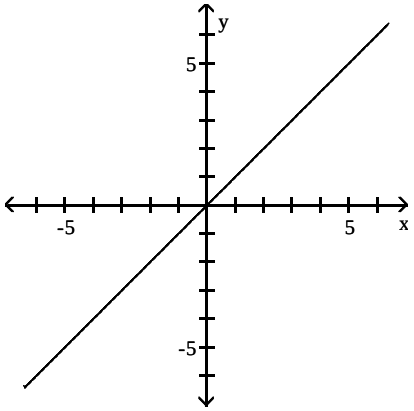
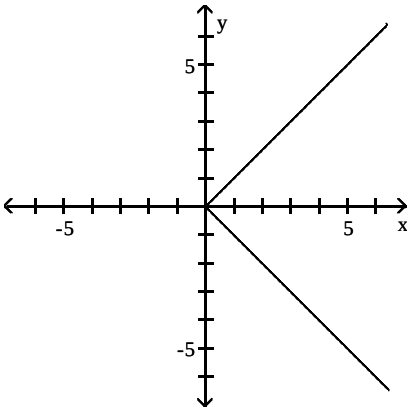
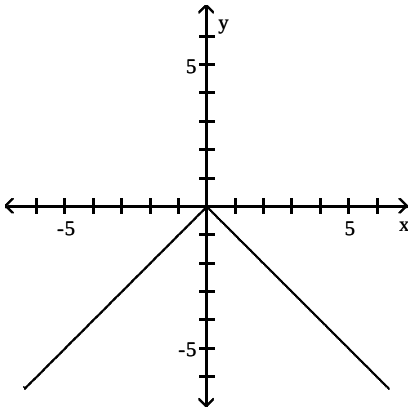


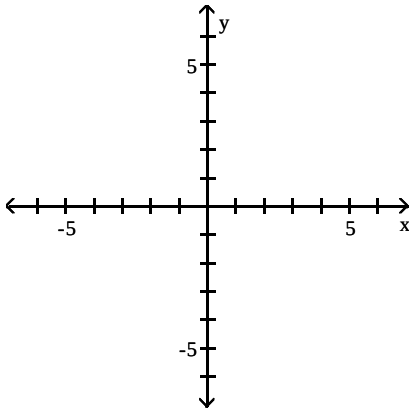
C)



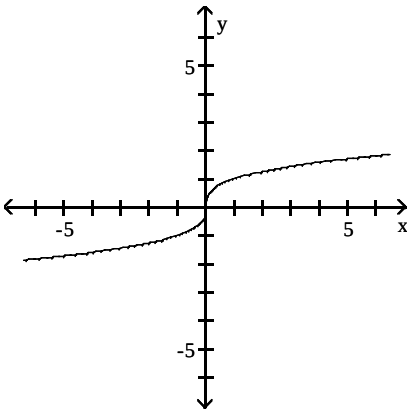
D)



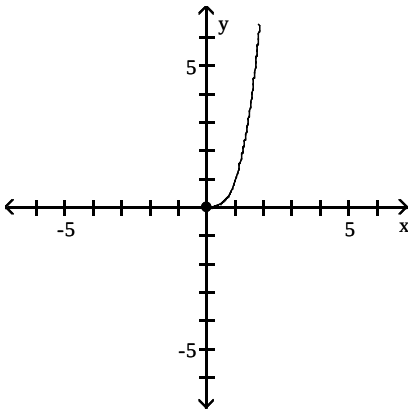
15) $f(x) = \sqrt[3]{x}$



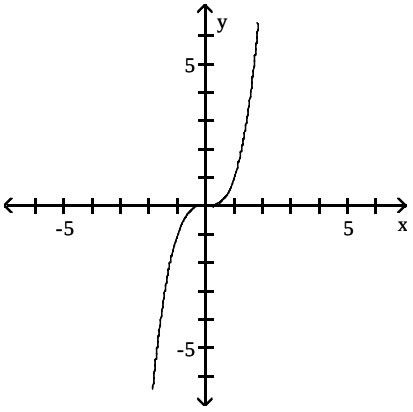
A)



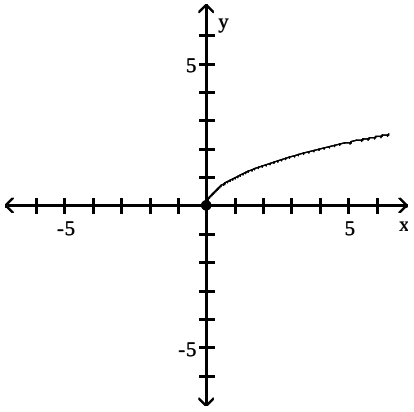
B)



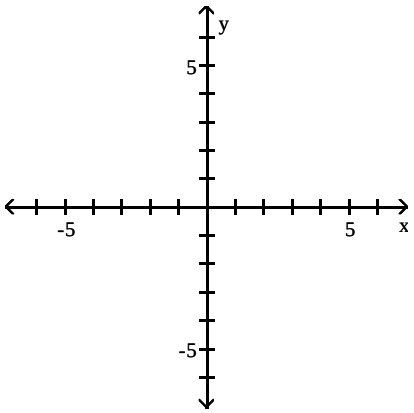
C)



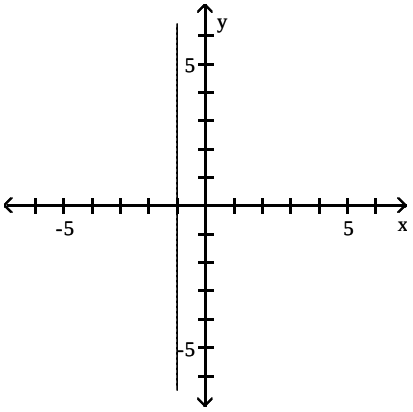
D)



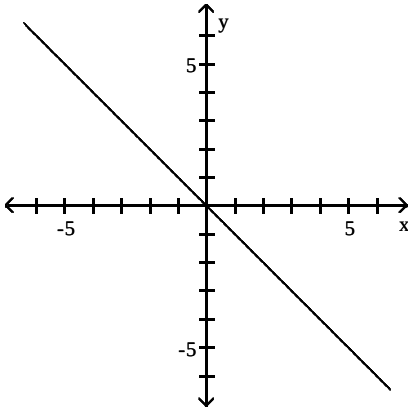
16) f(x) = –1



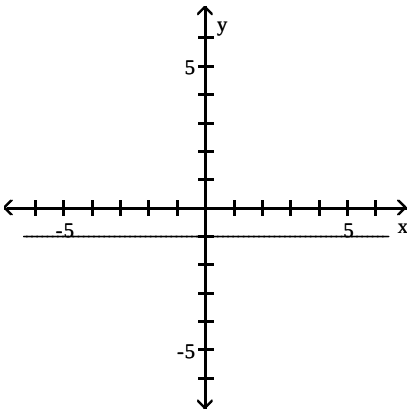
A)



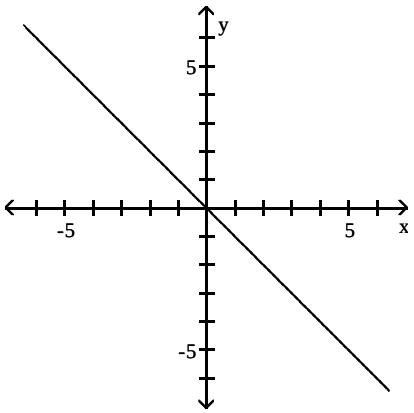
B)



C)



D)



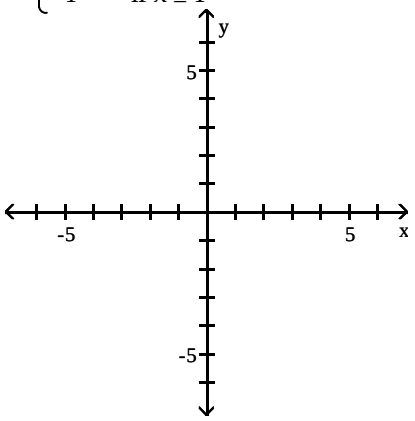
2 Graph Piecewise-defined Functions

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

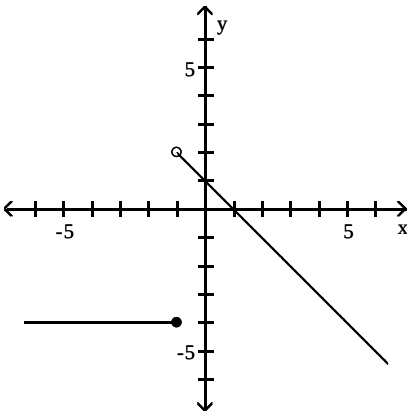
Graph the function.

1)

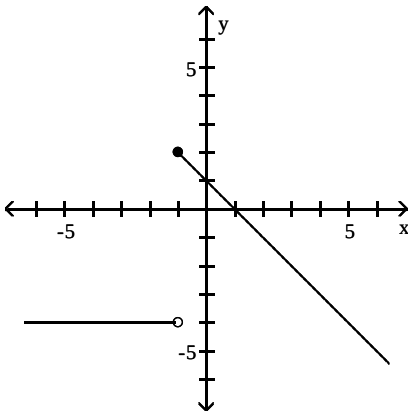
$$f(x) = \begin{cases} x + 1 & \text{if } x < 1 \\ -4 & \text{if } x \geq 1 \end{cases}$$



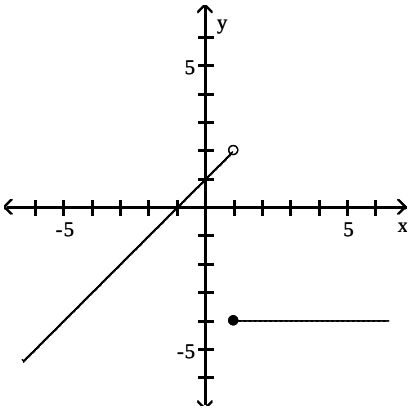
A)



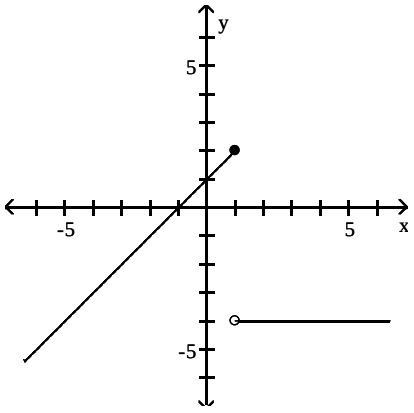
B)



C)

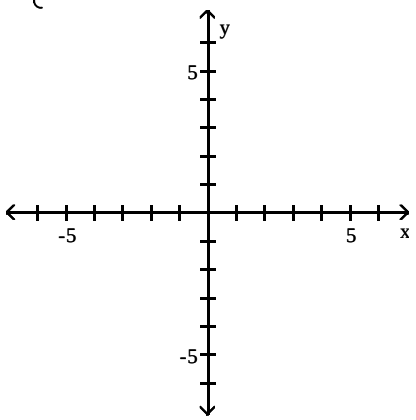


D)

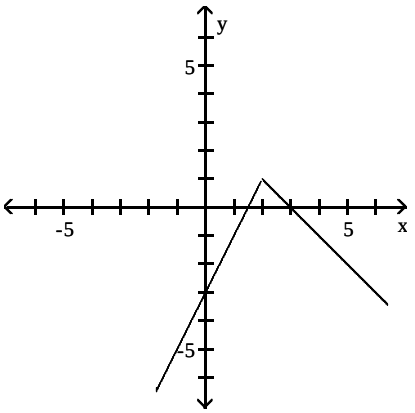


2)

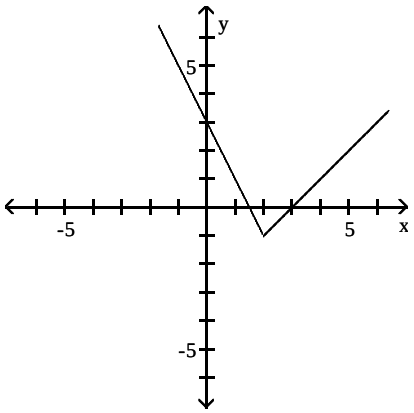
$$f(x) = \begin{cases} -x + 3 & \text{if } x < 2 \\ 2x - 3 & \text{if } x \geq 2 \end{cases}$$



A)



B)



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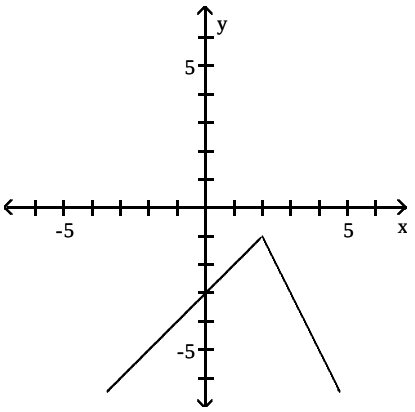

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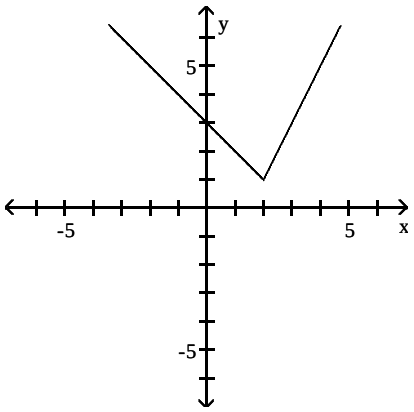
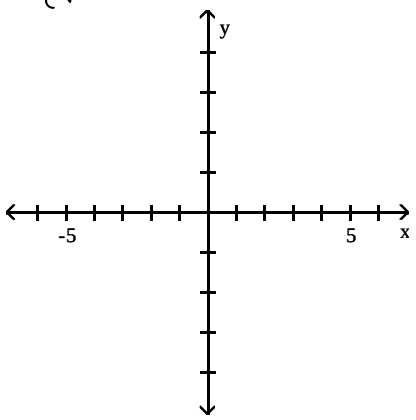
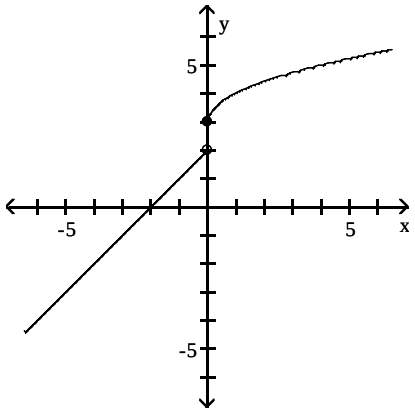


3)

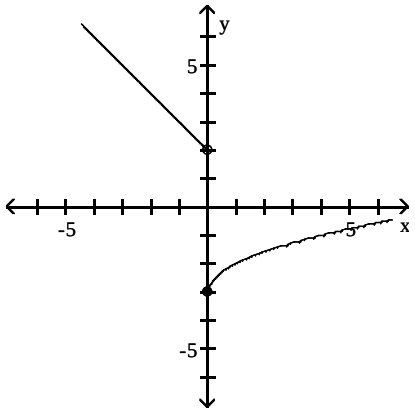
$$f(x) = \begin{cases} -x + 2 & x < 0 \\ \sqrt{x} + 3 & x \geq 0 \end{cases}$$



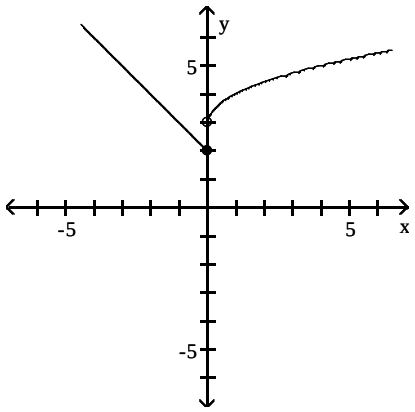
A)



B)



C)



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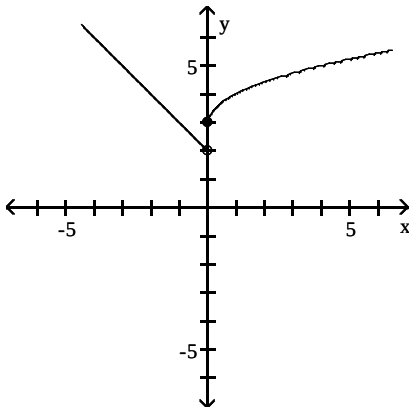
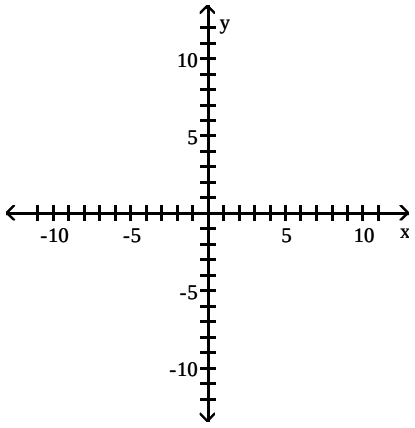
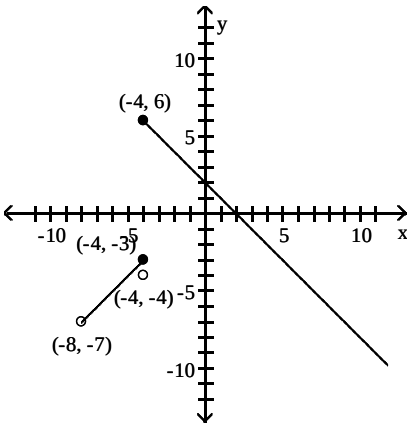


4)

$$f(x) = \begin{cases} x + 1 & \text{if } -8 \le x < -4 \\ -4 & \text{if } x = -4 \\ -x + 2 & \text{if } x > -4 \end{cases}$$



A)



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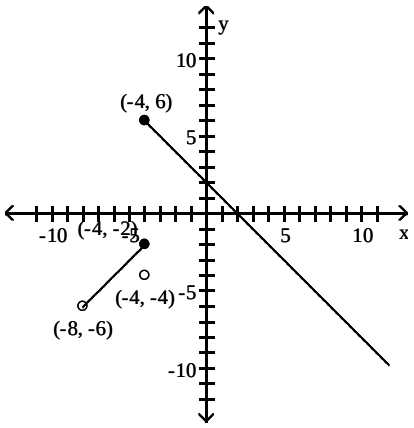

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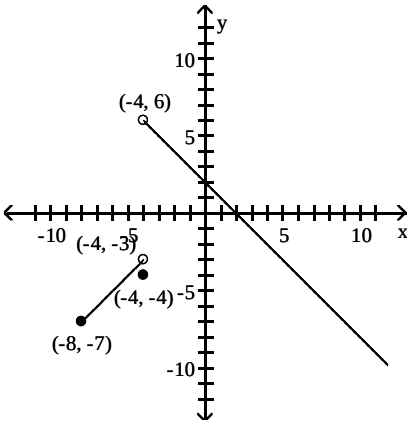
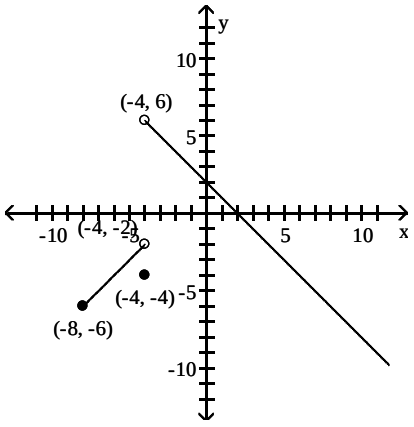
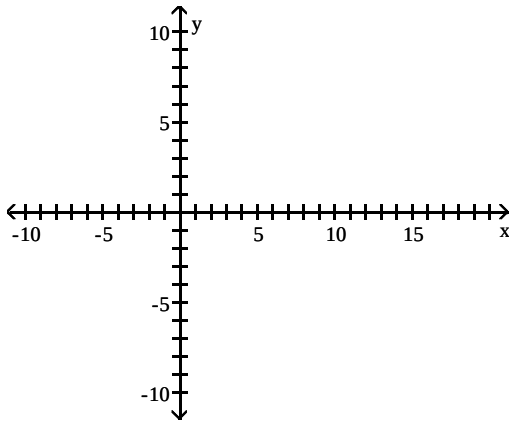


D)

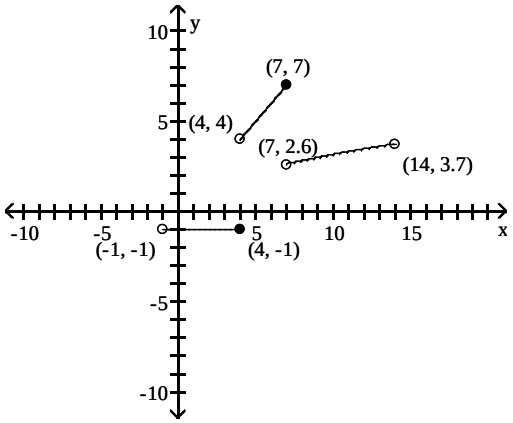


5)

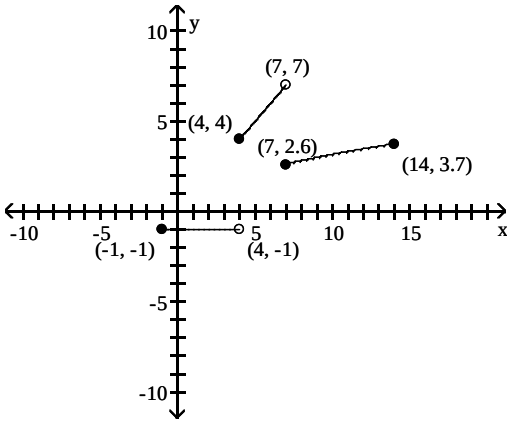
$$f(x) = \begin{cases} 1 & \text{if } -1 \le x < 4 \\ |x| & \text{if } 4 \le x < 7 \\ \sqrt{x} & \text{if } 7 \le x \le 14 \end{cases}$$



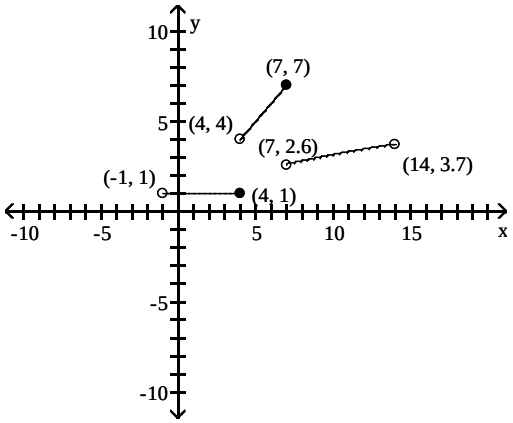
A)



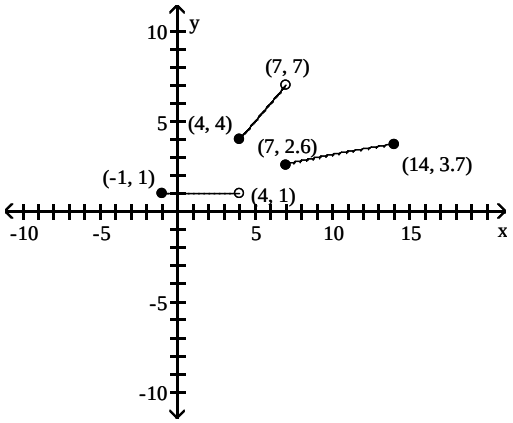
B)



C)



D)



Find the domain of the function.

6)

$$f(x) = \begin{cases} 4x & \text{if } x \ne 0 \\ 3 & \text{if } x = 0 \end{cases}$$

A) all real numbers B) $\{0\}$ C) $\{x \mid x \le 0\}$ D) $\{x \mid x \ne 0\}$

7)

$$f(x) = \begin{cases} 1 & \text{if } -4 \le x < -2 \\ |x| & \text{if } -2 \le x < 4 \\ \sqrt{x} & \text{if } 4 \le x \le 32 \end{cases}$$

A) $\{x \mid 4 \le x \le 32\}$
B) $\{x \mid -4 \le x \le 32\}$
C) $\{x \mid x \ge -4\}$
D) $\{x \mid -4 \le x < 4 \text{ or } 4 < x \le 32\}$

Locate any intercepts of the function.

8)

$$f(x) = \begin{cases} -3x + 9 & \text{if } x < 1 \\ 9x - 3 & \text{if } x \ge 1 \end{cases}$$

A) (0, 9), (3, 0), $(\frac{1}{3}, 0)$
B) (0, –3)
C) (0, 9)
D) (0, –3), (3, 0), $(\frac{1}{3}, 0)$

9)

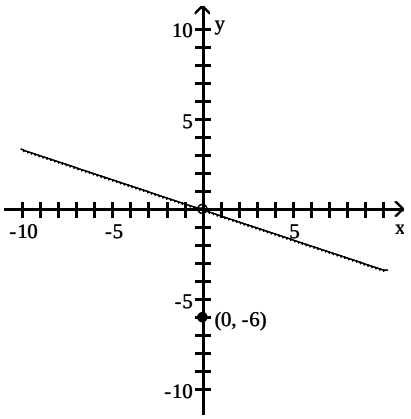
$$f(x) = \begin{cases} 1 & \text{if } -4 \le x < -8 \\ |x| & \text{if } -8 \le x < 4 \\ \sqrt[3]{x} & \text{if } 4 \le x \le 33 \end{cases}$$

A) (0, 0)
B) (0, 0), (1, 0)
C) (0, 0), (0, 1)
D) none

Based on the graph, find the range of y = f(x).

10)

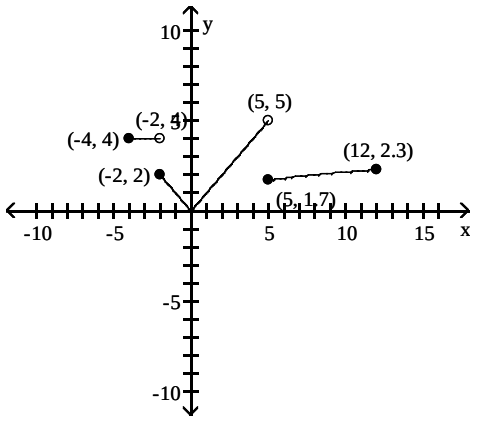
$$f(x) = \begin{cases} -\frac{1}{3}x & \text{if } x \ne 0 \\ -6 & \text{if } x = 0 \end{cases}$$



A) $(-\infty, \infty)$
B) $(-\infty, 0)$ or $(0, \infty)$
C) (–10, 10)
D) $(-\infty, 0)$ or $\{0\}$ or $(0, \infty)$

11)

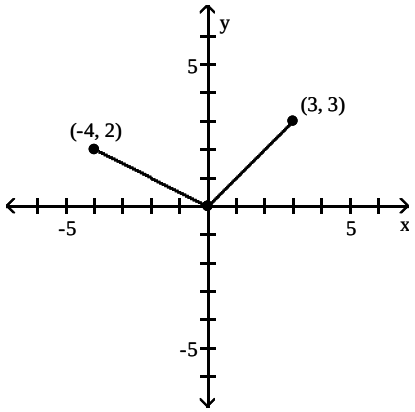
$$f(x) = \begin{cases} 4 & \text{if } -4 \le x < -2 \\ |x| & \text{if } -2 \le x < 5 \\ \sqrt[3]{x} & \text{if } 5 \le x \le 12 \end{cases}$$



A) $[0, \infty)$ B) $[0, 5]$ C) $[0, 5)$ D) $[0, \sqrt[3]{12}]$

The graph of a piecewise–defined function is given. Write a definition for the function.

12)



A)

$$f(x) = \begin{cases} -\frac{1}{2}x & \text{if } -4 < x < 0 \\ x & \text{if } 0 < x < 3 \end{cases}$$

B)

$$f(x) = \begin{cases} -2x & \text{if } -4 \le x \le 0 \\ x & \text{if } 0 < x \le 3 \end{cases}$$

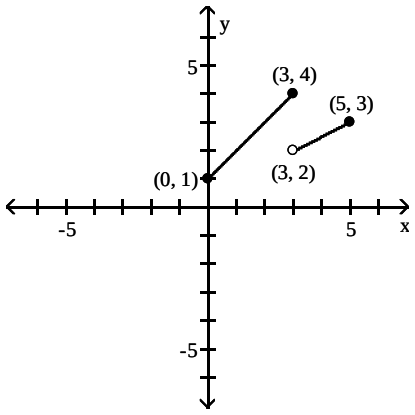
C)

$$f(x) = \begin{cases} -\frac{1}{2}x & \text{if } -4 \le x \le 0 \\ x & \text{if } 0 < x \le 3 \end{cases}$$

D)

$$f(x) = \begin{cases} \frac{1}{2}x & \text{if } -4 < x < 0 \\ x & \text{if } 0 < x < 3 \end{cases}$$

13)



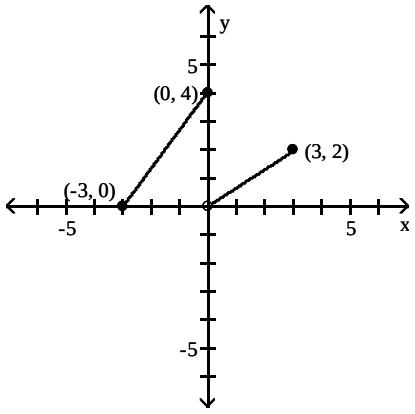
A)
$$f(x) = \begin{cases} x + 1 & \text{if } 0 \le x \le 3 \\ \frac{1}{2}x & \text{if } 3 < x \le 5 \end{cases}$$

B)
$$f(x) = \begin{cases} x + 1 & \text{if } 0 \le x \le 3 \\ \frac{1}{2}x + 2 & \text{if } 3 < x \le 5 \end{cases}$$

C)
$$f(x) = \begin{cases} x + 1 & \text{if } 0 \le x \le 3 \\ \frac{1}{2}x - \frac{1}{2} & \text{if } 3 < x \le 5 \end{cases}$$

D)
$$f(x) = \begin{cases} x + 1 & \text{if } 0 \le x \le 3 \\ \frac{1}{2}x + \frac{1}{2} & \text{if } 3 < x \le 5 \end{cases}$$

14)



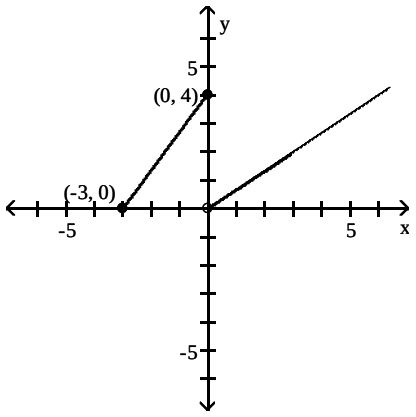
A)
$$f(x) = \begin{cases} \frac{4}{3}x - 4 & \text{if } -3 \le x \le 0 \\ \frac{2}{3}x & \text{if } 0 \le x \le 3 \end{cases}$$

B)
$$f(x) = \begin{cases} \frac{3}{4}x + 4 & \text{if } -3 \le x \le 0 \\ \frac{3}{2}x & \text{if } 0 < x \le 3 \end{cases}$$

C)
$$f(x) = \begin{cases} \frac{4}{3}x + 4 & \text{if } -3 \le x \le 0 \\ \frac{2}{3}x & \text{if } 0 < x \le 3 \end{cases}$$

D)
$$f(x) = \begin{cases} \frac{4}{3}x + 4 & \text{if } -3 \le x \le 0 \\ \frac{2}{3}x + 2 & \text{if } 0 < x \le 3 \end{cases}$$

15)



A)
$$f(x) = \begin{cases} \frac{3}{4}x + 4 & \text{if } -3 \le x \le 0 \\ \frac{3}{2}x & \text{if } x > 0 \end{cases}$$

B)
$$f(x) = \begin{cases} \frac{4}{3}x + 4 & \text{if } -3 \le x \le 0 \\ \frac{2}{3}x & \text{if } 0 < x \le 3 \end{cases}$$

C)
$$f(x) = \begin{cases} \frac{3}{4}x + 4 & \text{if } -3 \le x \le 0 \\ \frac{3}{2}x & \text{if } x \ge 0 \end{cases}$$

D)
$$f(x) = \begin{cases} \frac{4}{3}x + 4 & \text{if } -3 \le x \le 0 \\ \frac{2}{3}x & \text{if } x > 0 \end{cases}$$

Solve the problem.

16) If f(x) = int(2x), find f(1.6).

A) 3 B) 4 C) 1 D) 2

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

17) A gas company has the following rate schedule for natural gas usage in single–family residences:

Monthly service charge	\$8.80
Per therm service charge	
1st 25 therms	\$0.6686/therm
Over 25 therms	\$0.85870/therm

What is the charge for using 25 therms in one month?
What is the charge for using 45 therms in one month?
Construct a function that gives the monthly charge C for x therms of gas.

18) An electric company has the following rate schedule for electricity usage in single–family residences:

Monthly service charge	\$4.93
Per kilowatt service charge	
1st 300 kilowatts	\$0.11589/kW
Over 300 kilowatts	\$0.13321/kW

What is the charge for using 300 kilowatts in one month?
What is the charge for using 375 kilowatts in one month?
Construct a function that gives the monthly charge C for x kilowatts of electricity.

19) One Internet service provider has the following rate schedule for high–speed Internet service:

Monthly service charge	\$18.00
1st 50 hours of use	free
Next 50 hours of use	\$0.25/hour
Over 100 hours of use	\$1.00/hour

What is the charge for 50 hours of high–speed Internet use in one month?
What is the charge for 75 hours of high–speed Internet use in one month?
What is the charge for 135 hours of high–speed Internet use in one month?

20) The wind chill factor represents the equivalent air temperature at a standard wind speed that would produce the same heat loss as the given temperature and wind speed. One formula for computing the equivalent temperature is

$$W(t) = \begin{cases} t & \text{if } 0 \le v < 1.79 \\ 33 - \dfrac{(10.45 + 10\sqrt{v} - v)(33 - t)}{22.04} & \text{if } 1.79 \le v < 20 \\ 33 - 1.5958(33 - t) & \text{if } v \ge 20 \end{cases}$$

where v represents the wind speed (in meters per second) and t represents the air temperature (°C). Compute the wind chill for an air temperature of 15°C and a wind speed of 12 meters per second. (Round the answer to one decimal place.)

21) A cellular phone plan had the following schedule of charges:

Basic service, including 100 minutes of calls	\$20.00 per month
2nd 100 minutes of calls	\$0.075 per minute
Additional minutes of calls	\$0.10 per minute

What is the charge for 200 minutes of calls in one month?
What is the charge for 250 minutes of calls in one month?
Construct a function that relates the monthly charge C for x minutes of calls.

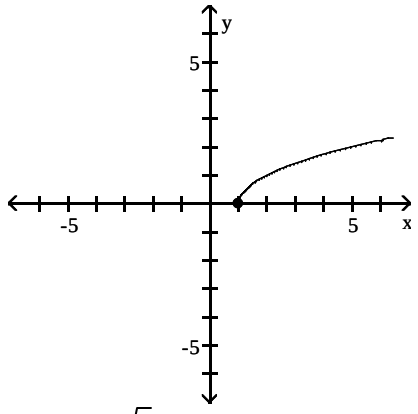
2.5 Graphing Techniques: Transformations

1 Graph Functions Using Vertical and Horizontal Shifts

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

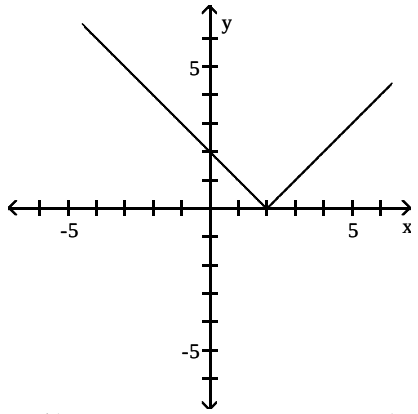
Match the correct function to the graph.

1)



A) $y = \sqrt{x}$ B) $y = \sqrt{x - 1}$ C) $y = \sqrt{x + 1}$ D) $y = x - 1$

2)



A) $y = x - 2$ B) $y = |2 - x|$ C) $y = |x + 2|$ D) $y = |1 - x|$

Write the equation of a sine function that has the given characteristics.

3) The graph of $y = x^2$, shifted 6 units upward

A) $y = x^2 - 6$ B) $y = \frac{x^2}{6}$ C) $y = 6x^2$ D) $y = x^2 + 6$

4) The graph of $y = |x|$, shifted 6 units to the right

A) $y = |x| - 6$ B) $y = |x| + 6$ C) $y = |x - 6|$ D) $y = |x + 6|$

5) The graph of $y = |x|$, shifted 9 units upward

A) $y = |x + 9|$ B) $y = |x| + 9$ C) $y = |x - 9|$ D) $y = |x| - 9$

6) The graph of $y = \sqrt{x}$, shifted 7 units to the right

A) $y = \sqrt{x - 7}$ B) $y = \sqrt{x} - 7$ C) $y = \sqrt{x + 7}$ D) $y = \sqrt{x} + 7$

7) The graph of $y = \sqrt{x}$, shifted 9 units to the left

A) $y = \sqrt{x + 9}$ B) $y = \sqrt{x} + 9$ C) $y = \sqrt{x - 9}$ D) $y = \sqrt{x} - 9$

8) The graph of $y = \sqrt{x}$, shifted 9 units upward

A) $y = \sqrt{x - 9}$ B) $y = \sqrt{x + 9}$ C) $y = \sqrt{x} + 9$ D) $y = \sqrt{x} - 9$

9) The graph of $y = \sqrt{x}$, shifted 2 units downward

A) $y = \sqrt{x - 2}$ B) $y = \sqrt{x} - 2$ C) $y = \sqrt{x} + 2$ D) $y = \sqrt{x + 2}$

Suppose the point (2, 4) is on the graph of y = f(x). Find a point on the graph of the given function.

10) y = f(x + 2)

A) (2, 6) B) (2, 2) C) (0, 4) D) (4, 4)

11) f(x) + 2

A) (2, –2) B) (0, 4) C) (4, 4) D) (2, 6)

Solve the problem.

12) Suppose that the x–intercepts of the graph of y = f(x) are 5 and 8. What are the x–intercepts of y = f(x + 9)?

A) 5 and 17 B) –4 and –1 C) 14 and 17 D) 45 and 72

13) Suppose that the x–intercepts of the graph of y = f(x) are 6 and 3. What are the x–intercepts of y = f(x – 7)?

A) 6 and –4 B) 13 and 10 C) –1 and –4 D) 42 and 21

14) Suppose that the function y = f(x) is increasing on the interval (7, 9). Over what interval is the graph of y = f(x + 5) increasing?

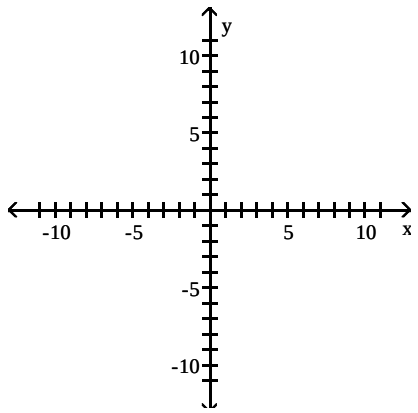
A) (35, 45) B) (7, 9) C) (2, 4) D) (12, 14)

15) Suppose that the function y = f(x) is increasing on the interval (2, 6). Over what interval is the graph of y = f(x – 8) increasing?

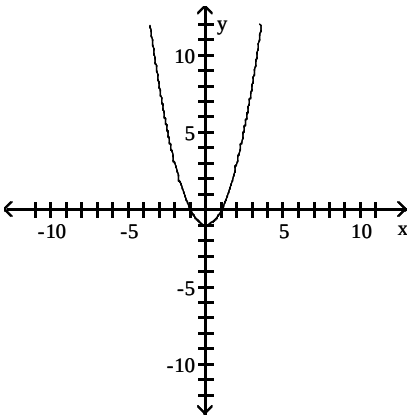
A) (10, 14) B) (16 , 48) C) (2, 6) D) (–6, –2)

Graph the function by starting with the graph of the basic function and then using the techniques of shifting, compressing, stretching, and/or reflecting.

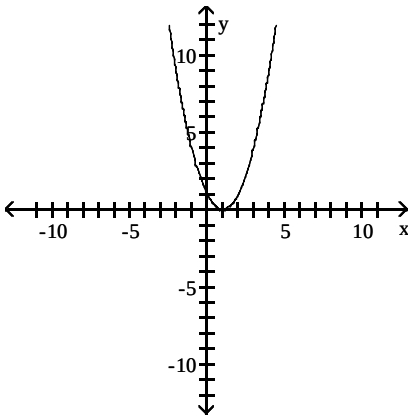
16) $f(x) = x^2 + 1$



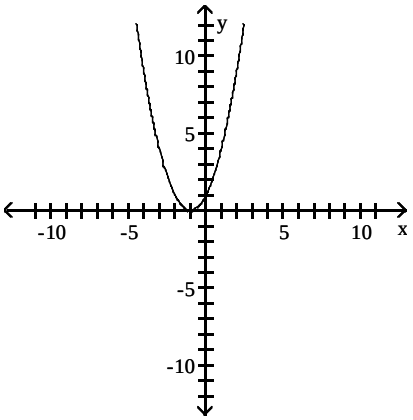
A)


y
10
5
-10
-5
5
10
x
-10
-5

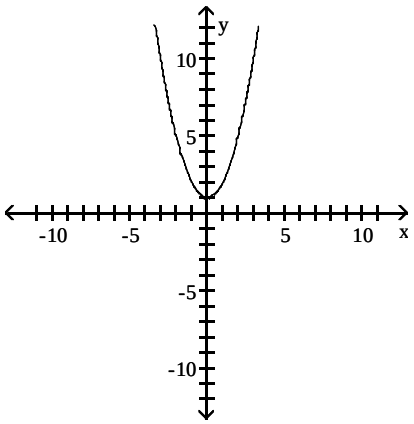
B)


y
10
5
-10
-5
5
10
x
-10
-5

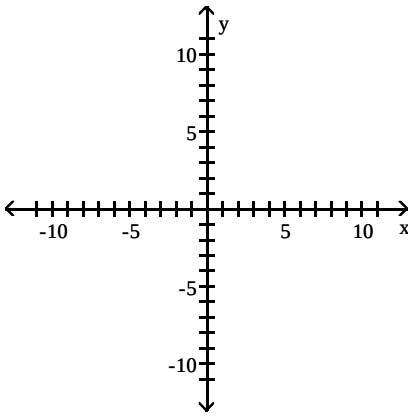
C)


y
10
5
-10
-5
5
10
x
-10
-5

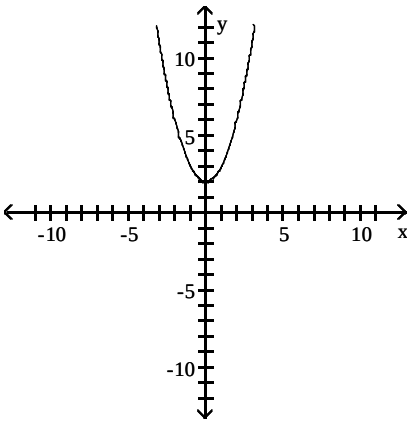
D)


y
10
5
-10
-5
5
10
x
-10
-5

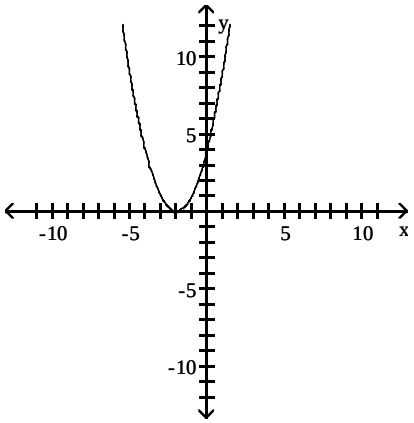
17) $f(x) = (x + 2)^2$



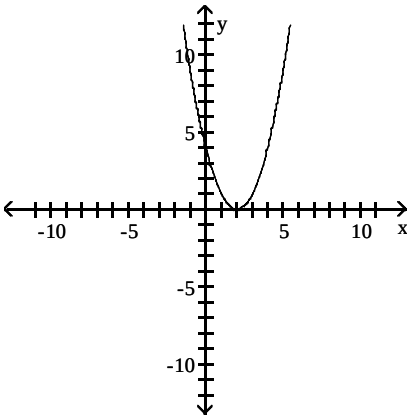
A)



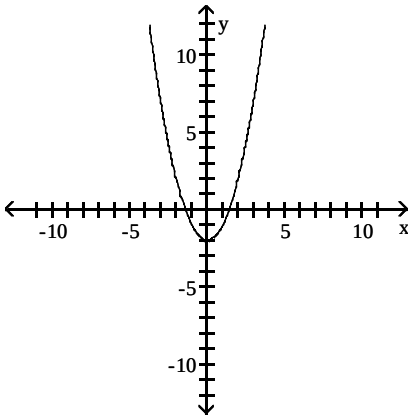
B)



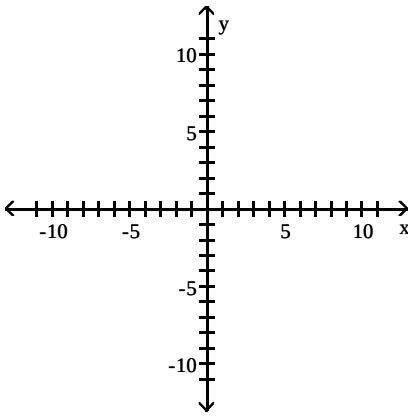
C)



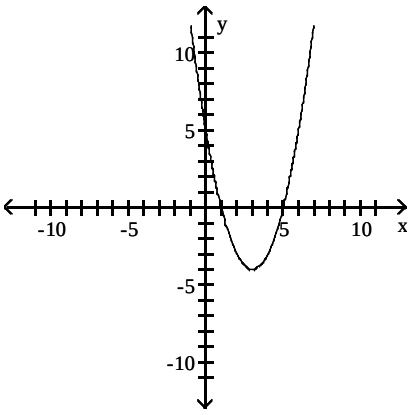
D)



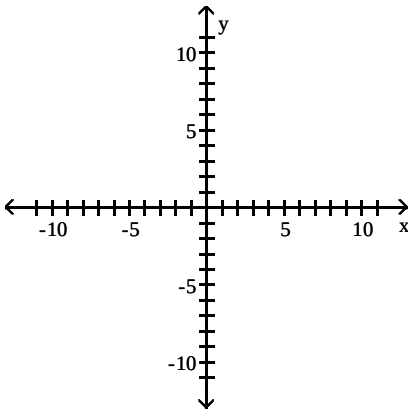
18) $f(x) = (x - 3)^2 - 4$



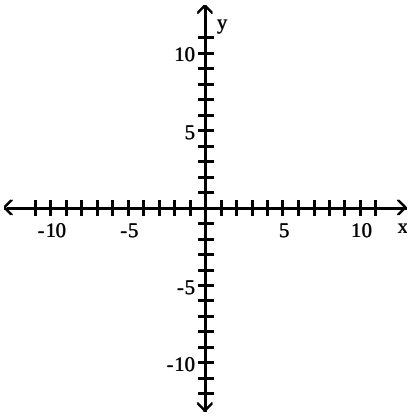
A)



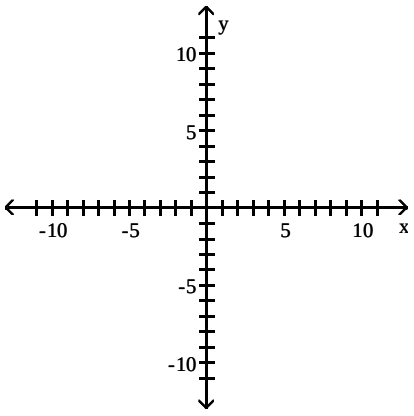
B)



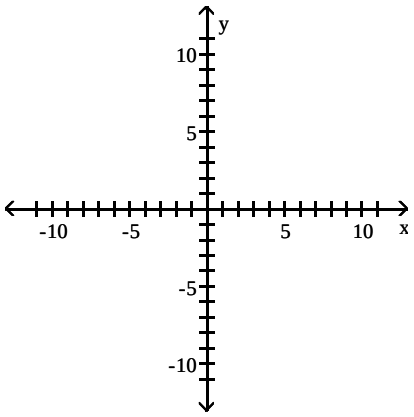
C)



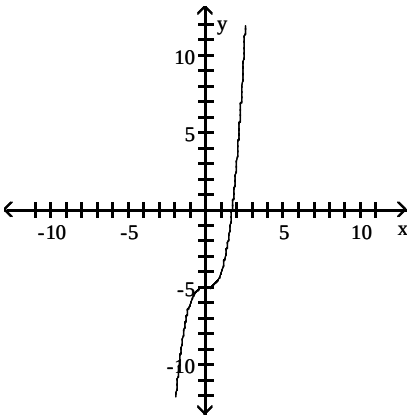
D)



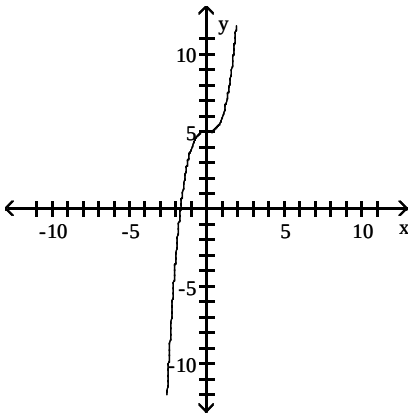
19) $f(x) = x^3 - 5$



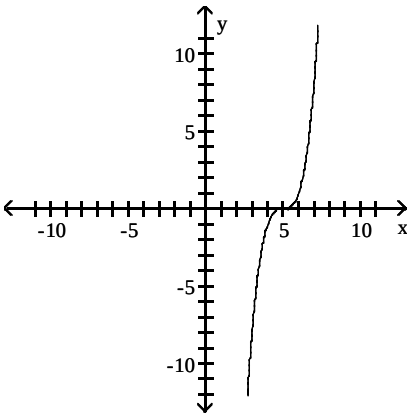
A)



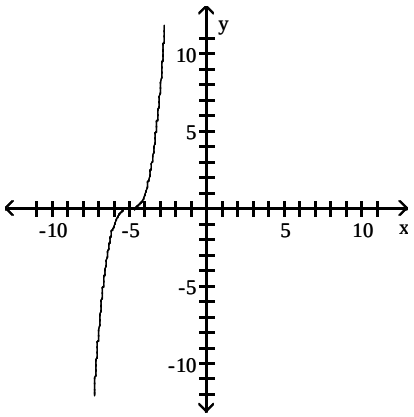
B)



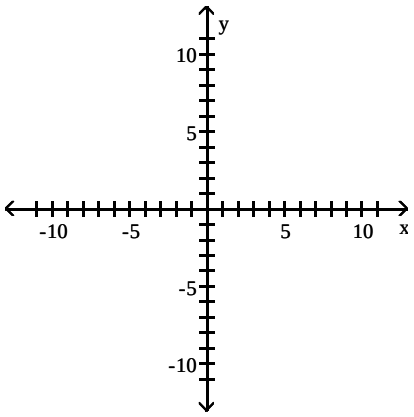
C)



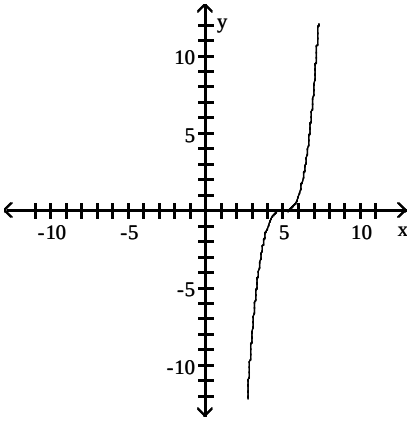
D)



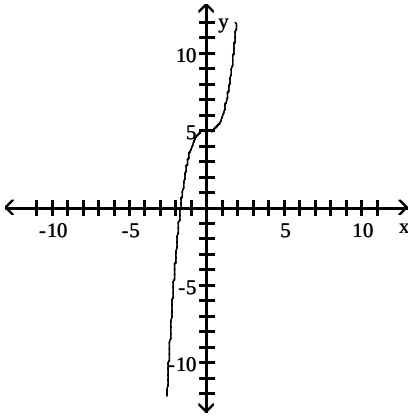
20) $f(x) = (x - 5)^3$



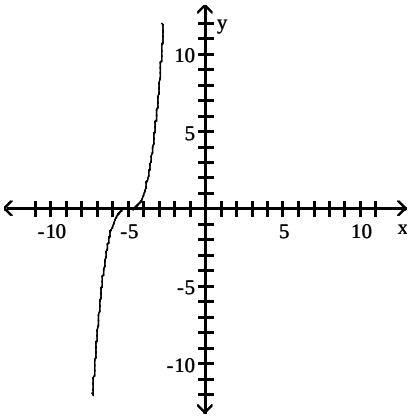
A)



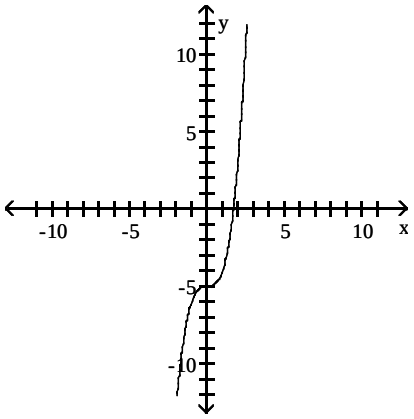
B)



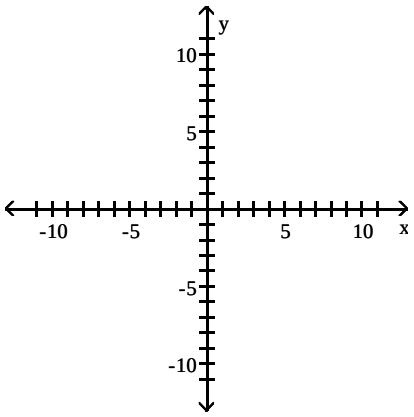
C)



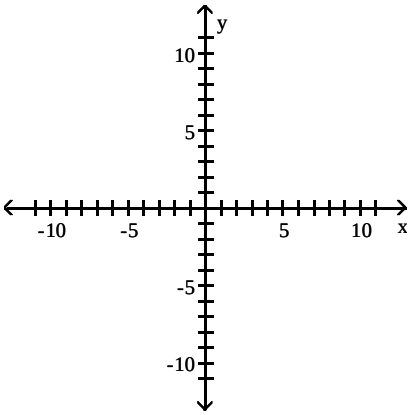
D)



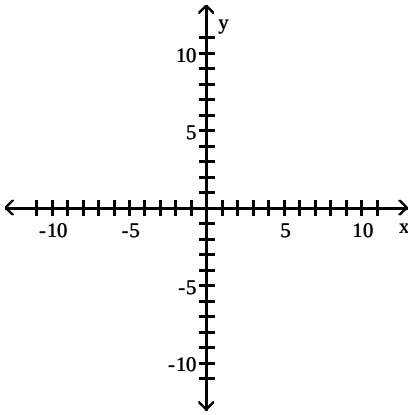
21) $f(x) = (x + 6)^3 + 7$



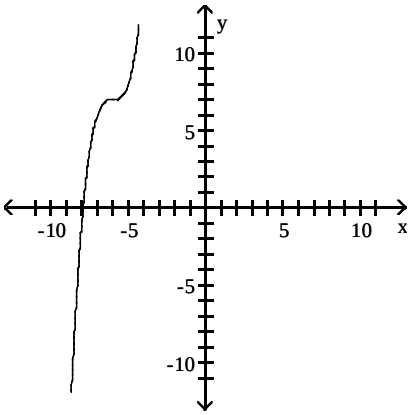
A)



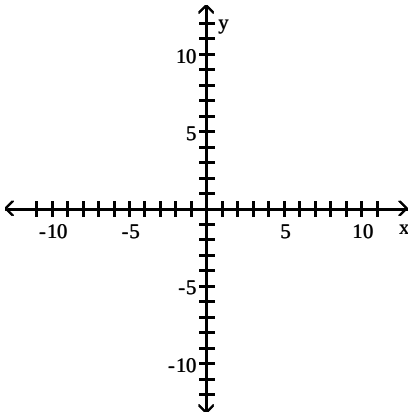
B)



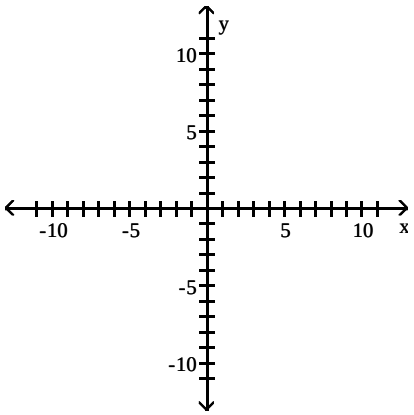
C)



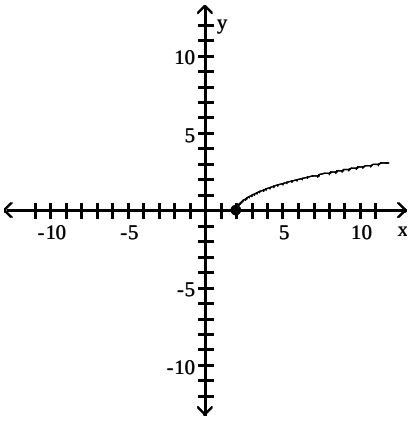
D)



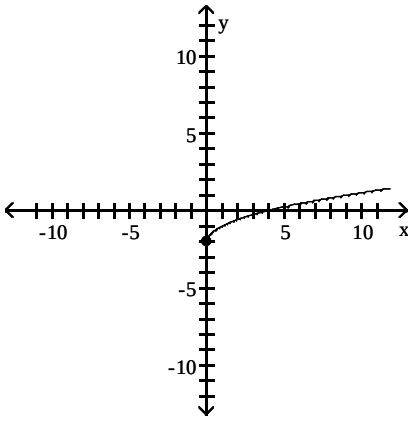
22) $f(x) = \sqrt{x} + 2$



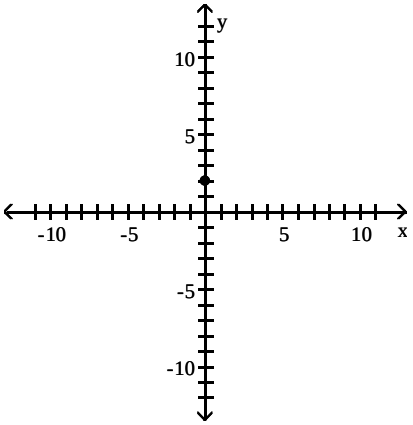
A)



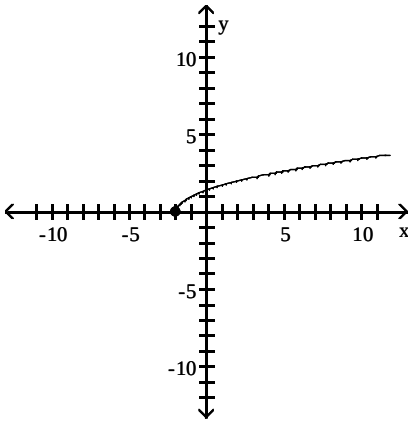
B)



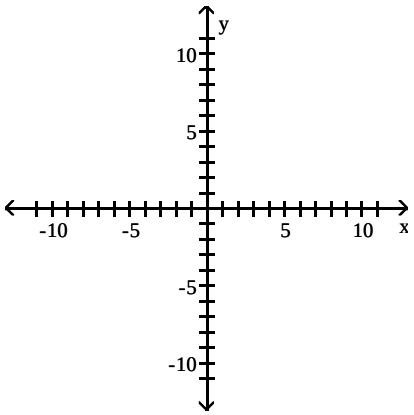
C)



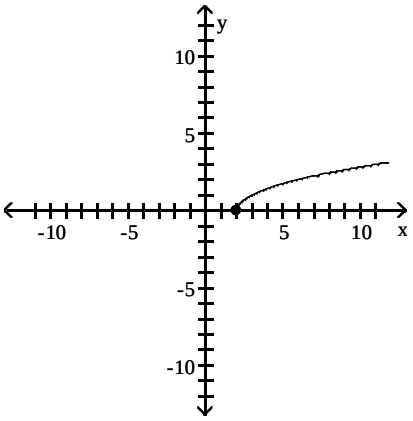
D)



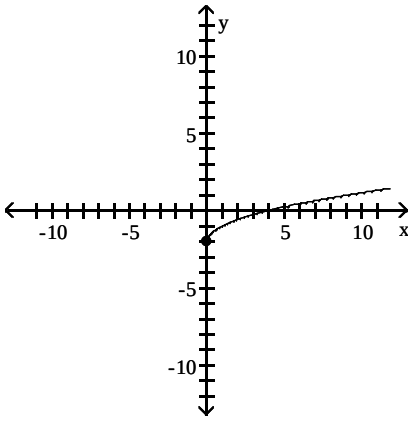
23) $f(x) = \sqrt{x + 2}$



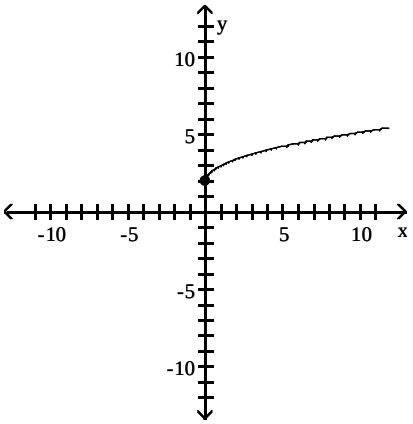
A)



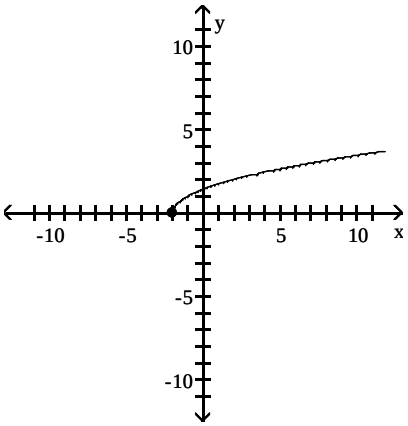
B)



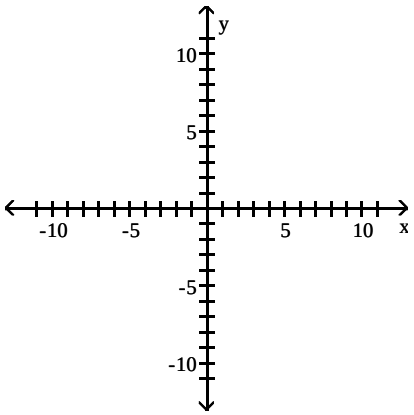
C)



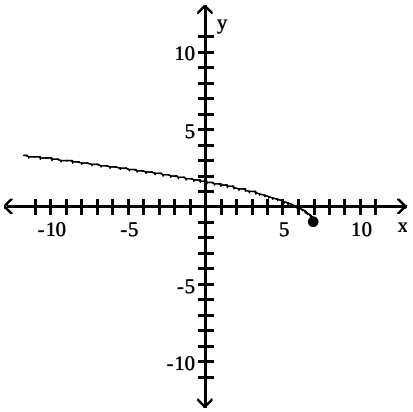
D)



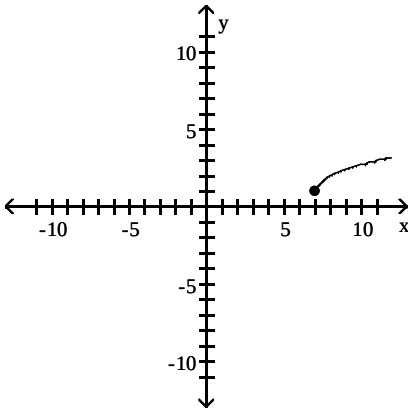
24) $f(x) = \sqrt{x + 7} - 1$



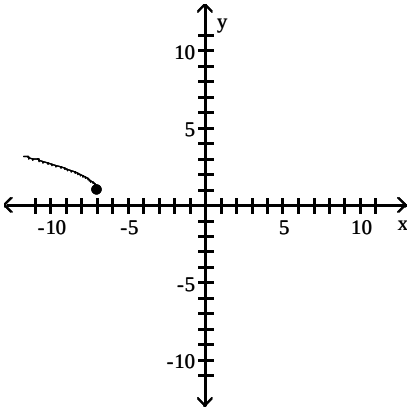
A)



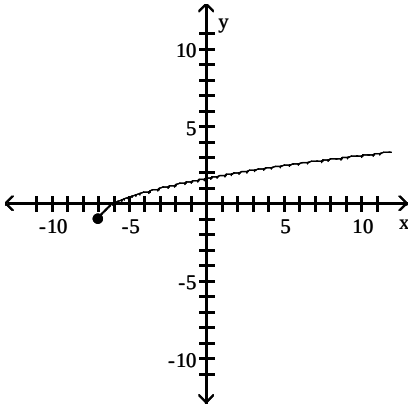
B)



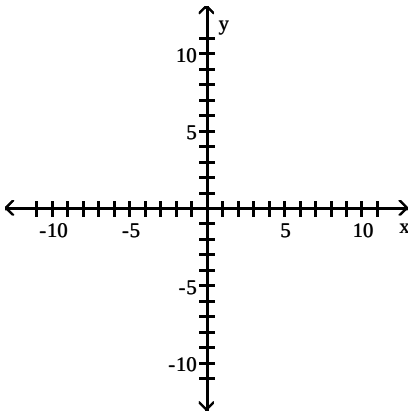
C)



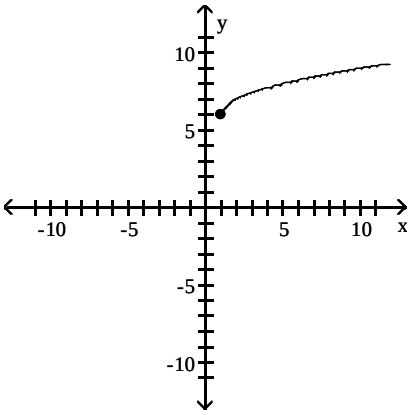
D)



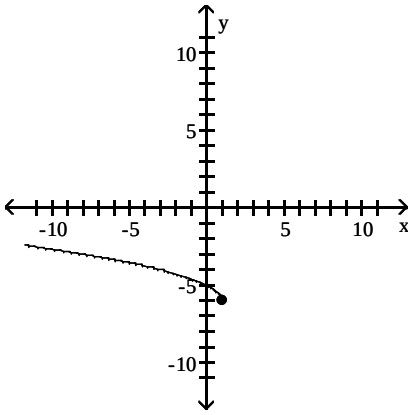
25) $f(x) = \sqrt{x - 1} + 6$



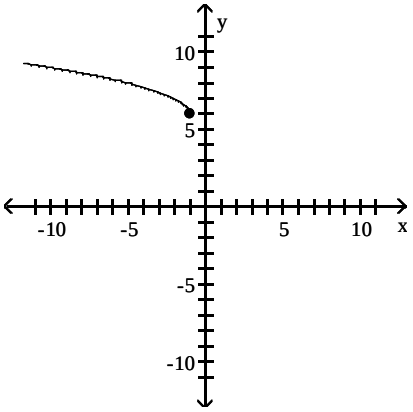
A)



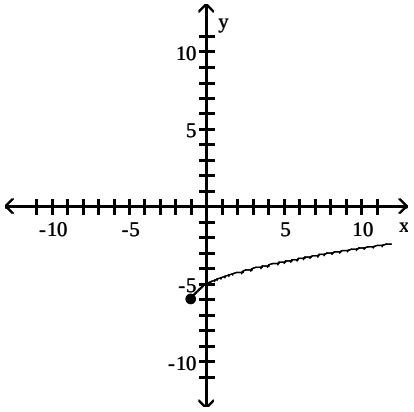
B)



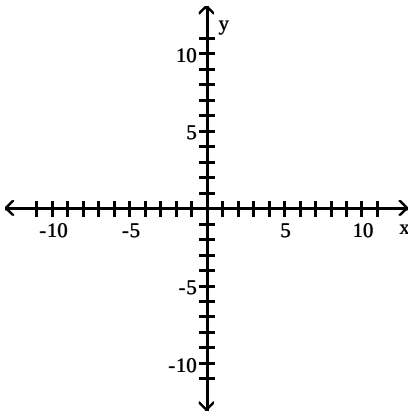
C)



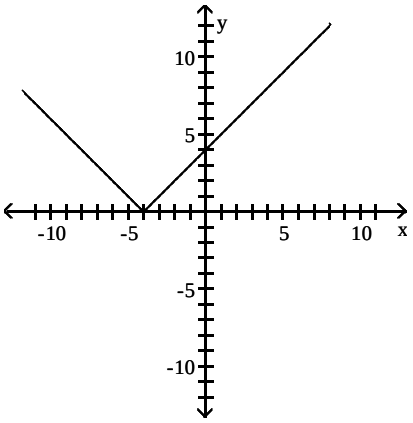
D)



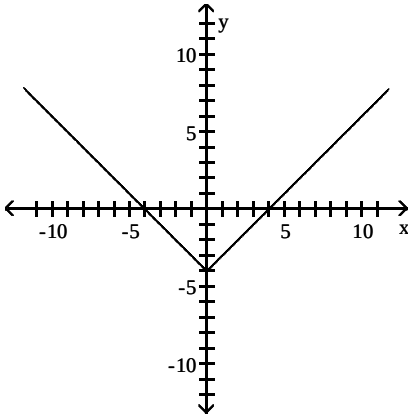
26) f(x) = |x| + 4


y
10
5
-10
-5
5
10
x
-5
-10

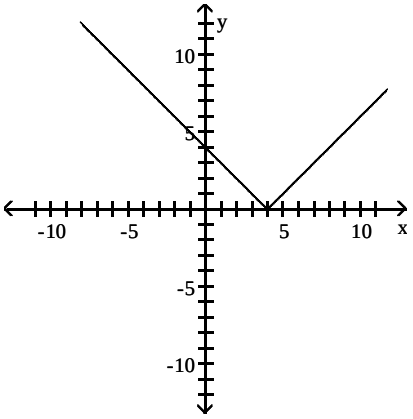
A)


y
10
5
-10
-5
5
10
x
-5
-10

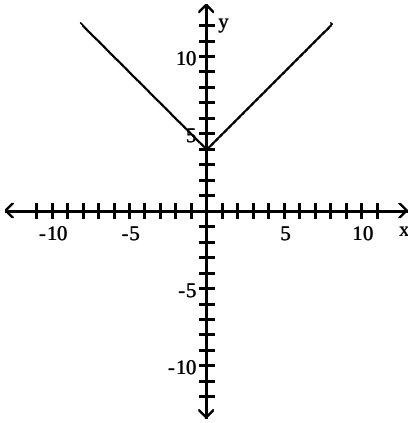
B)


y
10
5
-10
-5
5
10
x
-5
-10

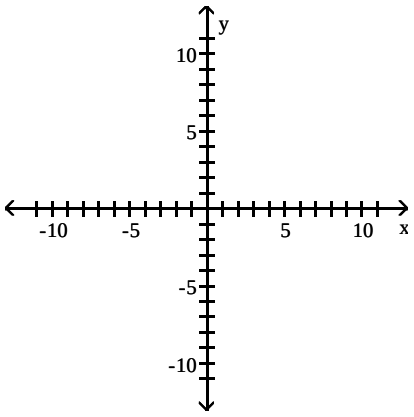
C)


y
10
5
-10
-5
5
10
x
-5
-10

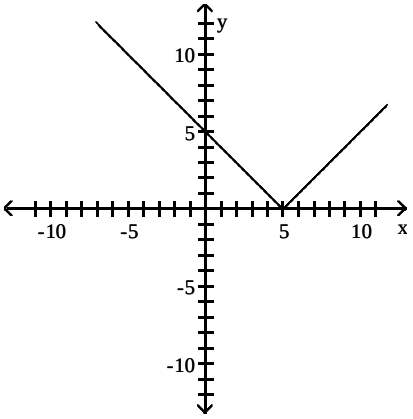
D)


y
10
5
-10
-5
5
10
x
-5
-10

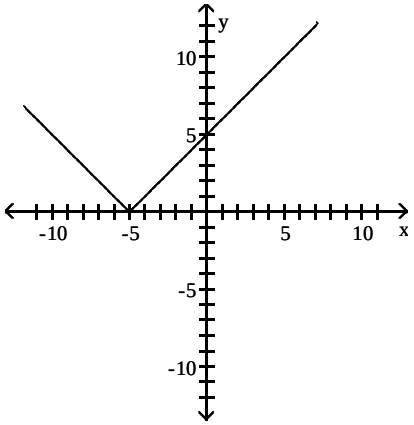
27) $f(x) = |x + 5|$


y
10
5
-10
-5
5
10
x
-5
-10

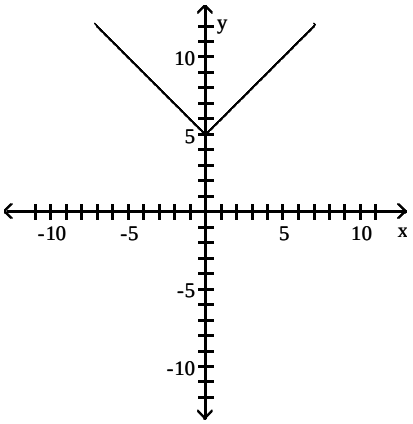
A)


y
10
5
-10
-5
5
10
x
-5
-10

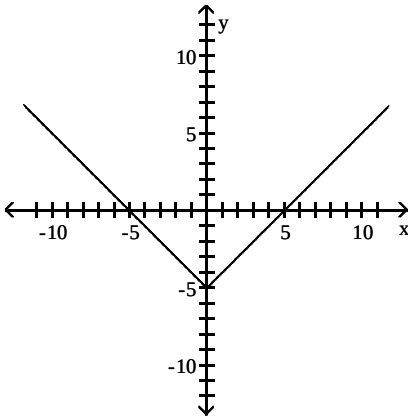
B)


y
10
5
-10
-5
5
10
x
-5
-10

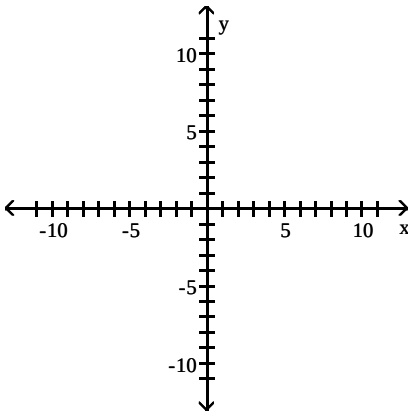
C)


y
10
5
-10
-5
5
10
x
-5
-10

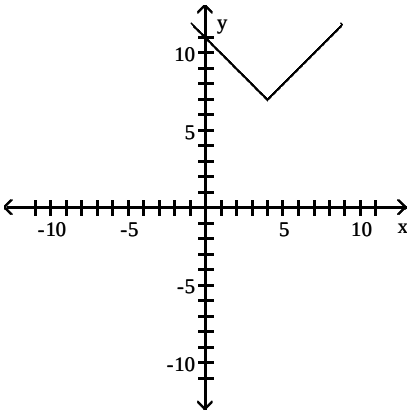
D)


y
10
5
-10
-5
5
10
x
-5
-10

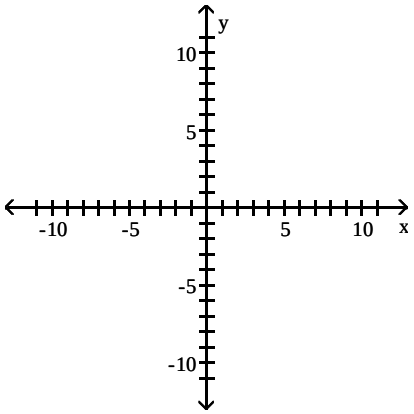
28) $f(x) = |x - 4| + 7$



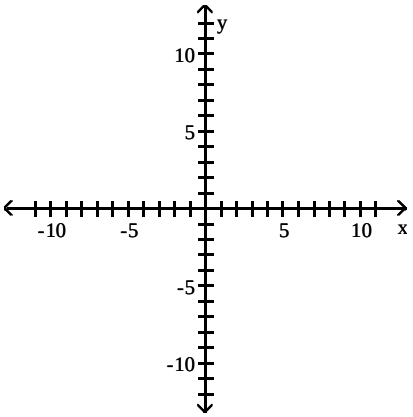
A)



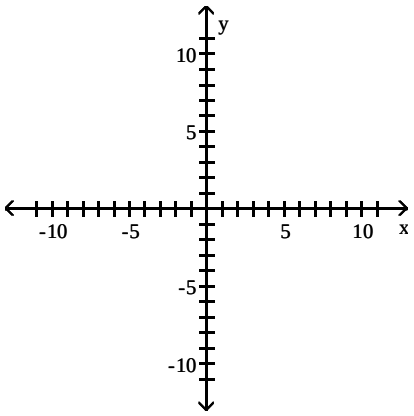
B)



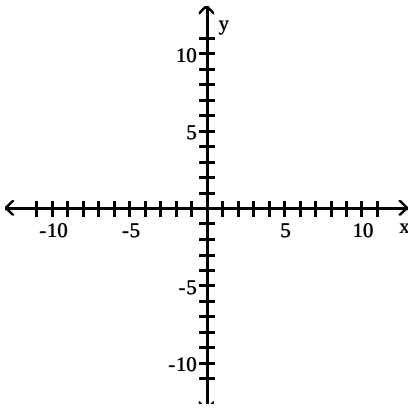
C)



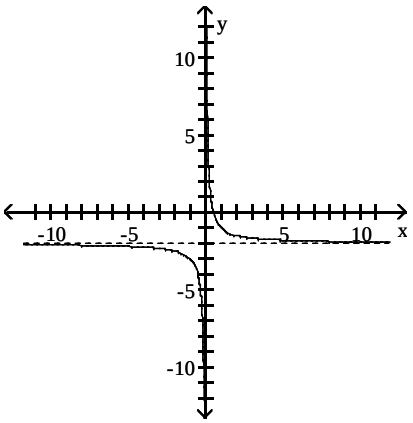
D)



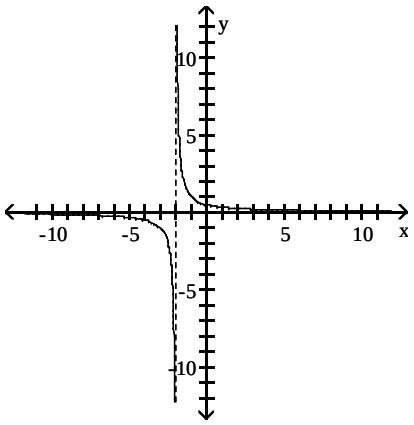
29) $f(x) = \frac{1}{x} + 2$



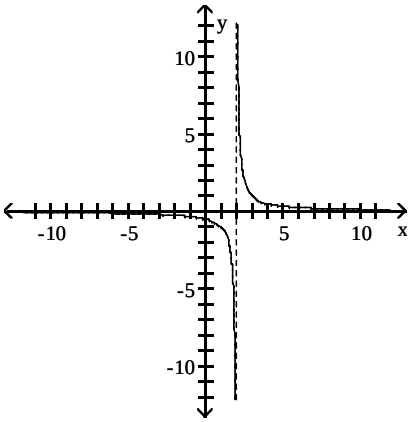
A)



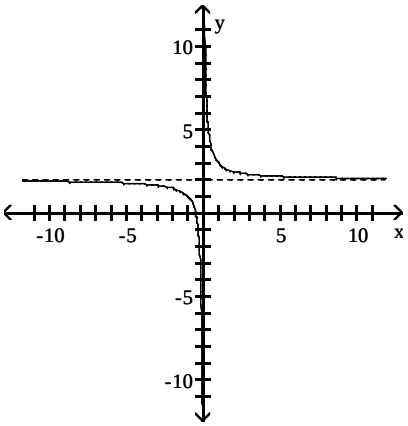
B)



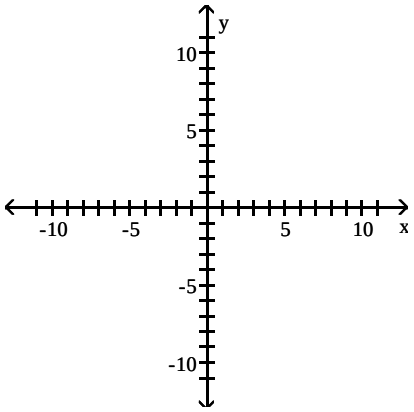
C)



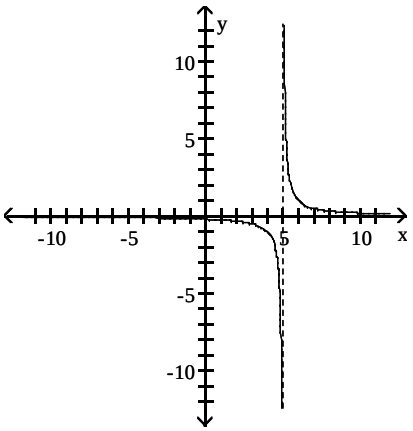
D)



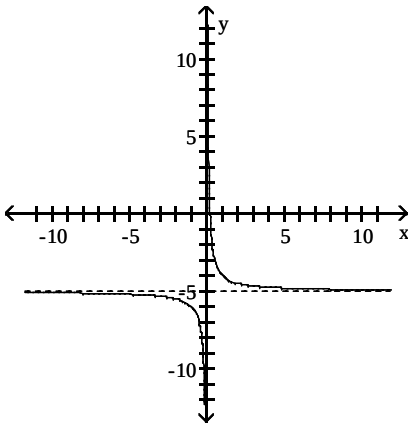
30) $f(x) = \frac{1}{x - 5}$



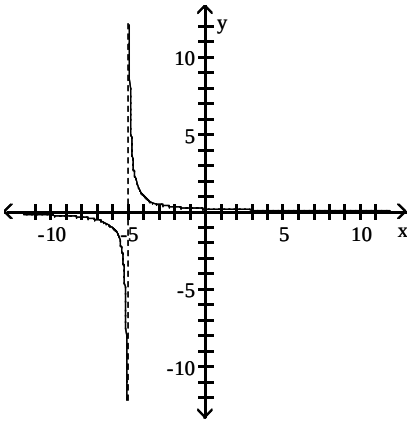
A)


y
10
5
-10
-5
5
10
x
-5
-10

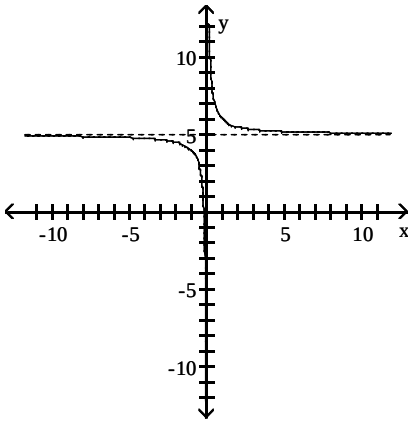
B)


y
10
5
-10
-5
5
10
x
-5
-10

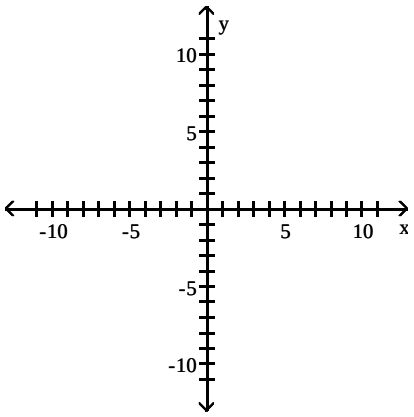
C)


y
10
5
-10
-5
5
10
x
-5
-10

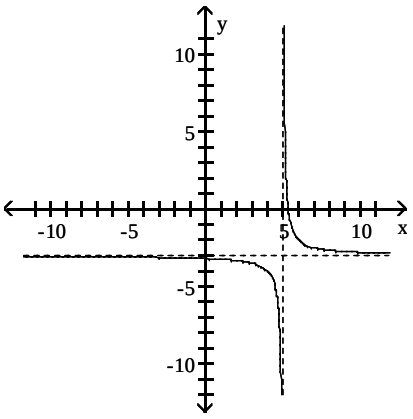
D)


y
10
-5
-10
-5
5
10
x
-5
-10

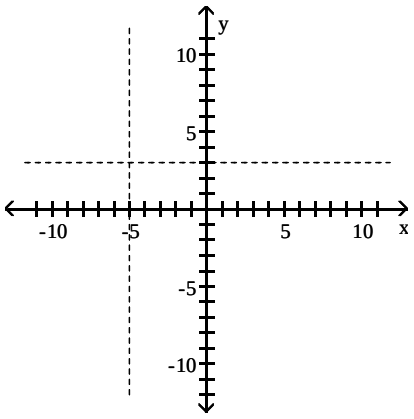
31) $f(x) = \frac{1}{x - 5} - 3$



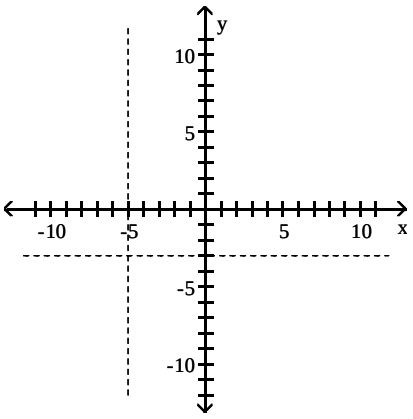
A)



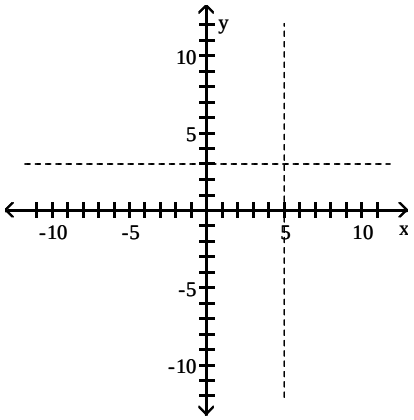
B)



C)

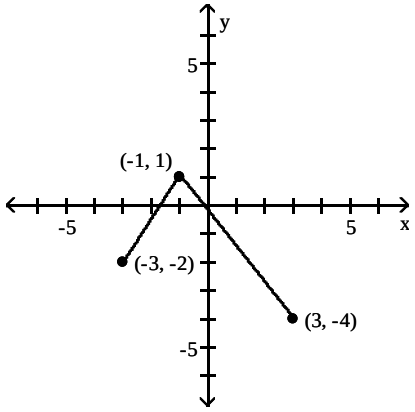


D)

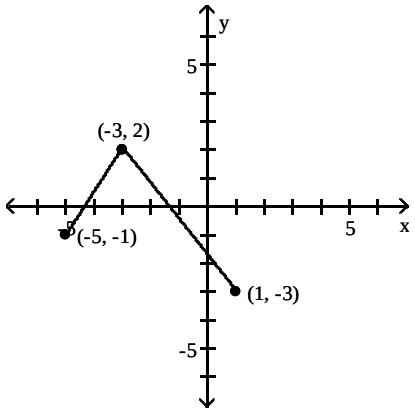


Using transformations, sketch the graph of the requested function.

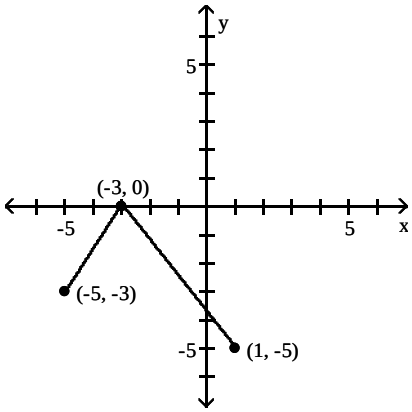
32) The graph of a function f is illustrated. Use the graph of f as the first step toward graphing the function F(x), where $F(x) = f(x + 2) - 1$.



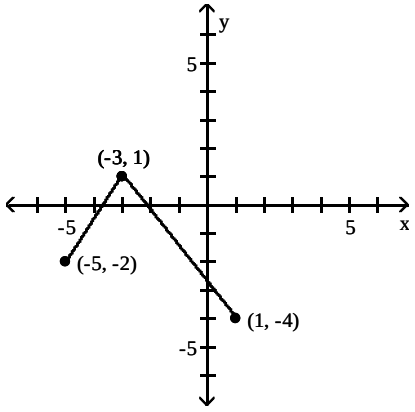
A)



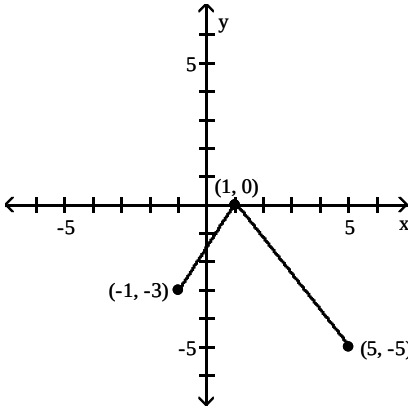
B)



C)

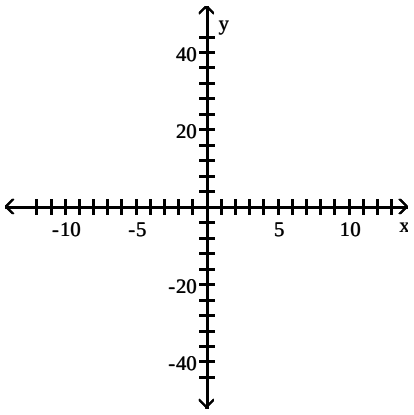


D)

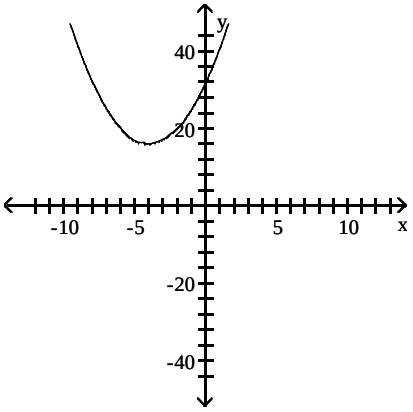


Complete the square and then use the shifting technique to graph the function.

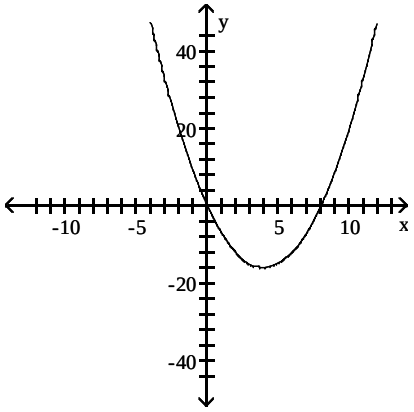
33) $f(x) = x^2 + 8x$



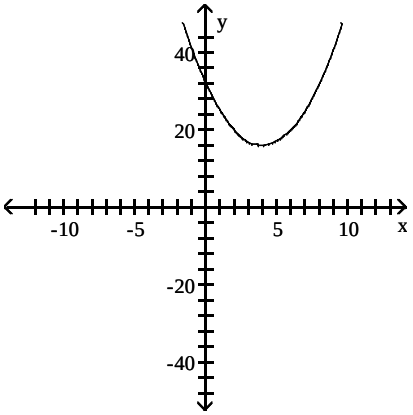
A)



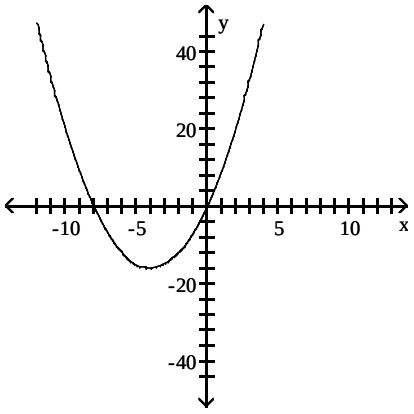
B)



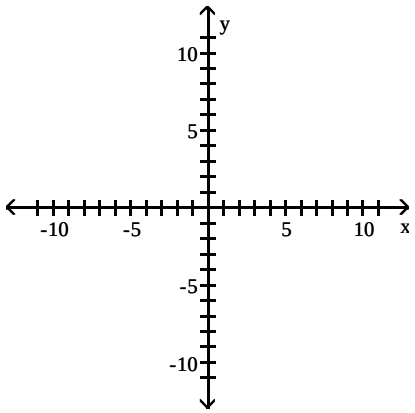
C)



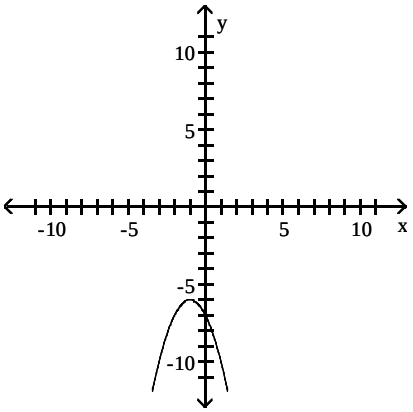
D)



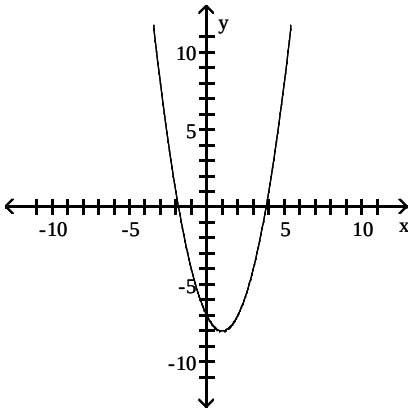
34) $f(x) = x^2 - 2x - 7$



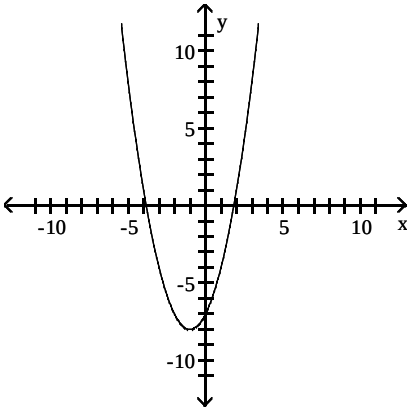
A)



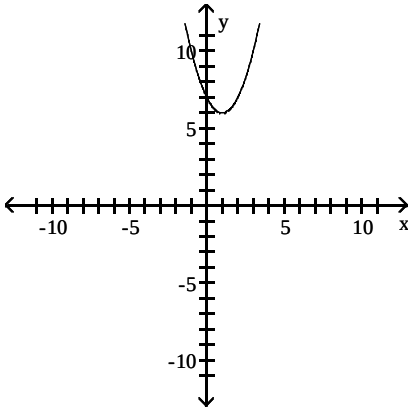
B)



C)



D)



Solve the problem.

35) The following numerical representation for f computes the average number of hours of television watched per day based on year of birth x.

x	1975	1980	1983	1988	1990	1992	1995
f(x)	2	2.5	3	3.5	4	3.5	4

Give a numerical representation for a function g that computes the average number of hours of television watched per day for the year x, where x = 0 corresponds to the birth year 1975. Write an equation that shows the relationship between f(x) and g(x).

A)

x	75	80	83	88	90	92	95
g(x)	2	2.5	3	3.5	4	3.5	4

f(x) = g(x – 1900)

B)

x	0	5	8	13	15	17	20
g(x)	2	2.5	3	3.5	4	3.5	4

f(x) = g(x – 1975)

C)

x	0	5	8	13	15	17	20
g(x)	2	2.5	3	3.5	4	3.5	4

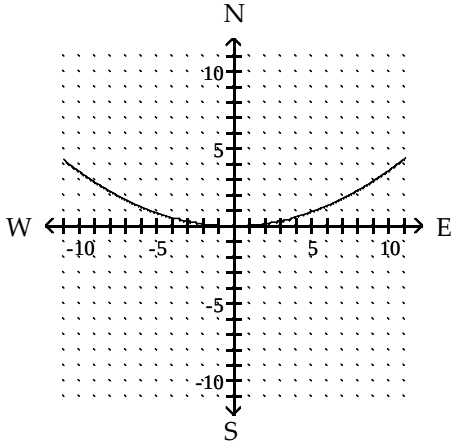
f(x) = g(x) – 1975

D)

x	0	5	8	13	15	17	20
g(x)	2	2.5	3	3.5	4	3.5	4

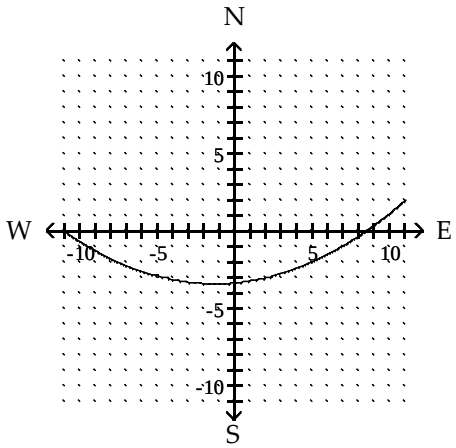
f(x) = g(x + 1975)

36) Suppose a cold front is passing through the United States at noon with a shape described by the function $y = \frac{1}{28}x^2$, where each unit represents 100 miles. St. Louis, Missouri is located at (0, 0), and the positive y–axis points north.

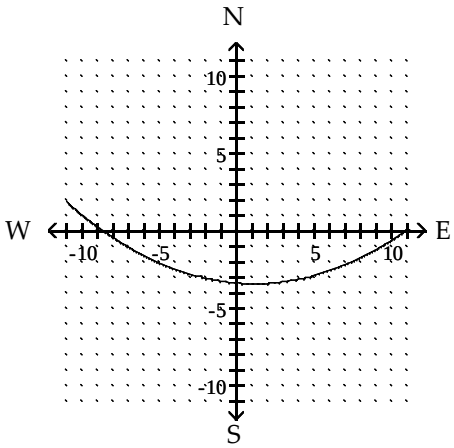


Suppose the front moves south 340 miles and west 120 miles and maintains its shape. Give the equation for the new front and plot the new position of the front.

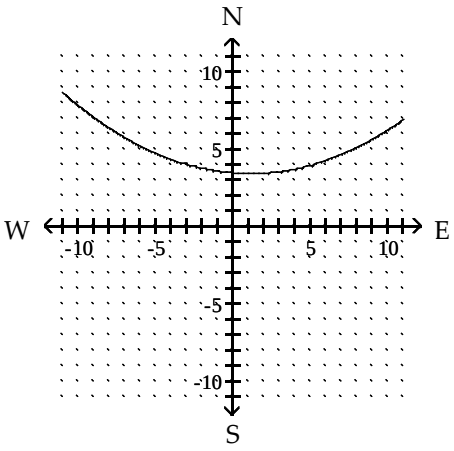
A) $y = \frac{1}{28}(x + 1.2)^2 - 3.4$



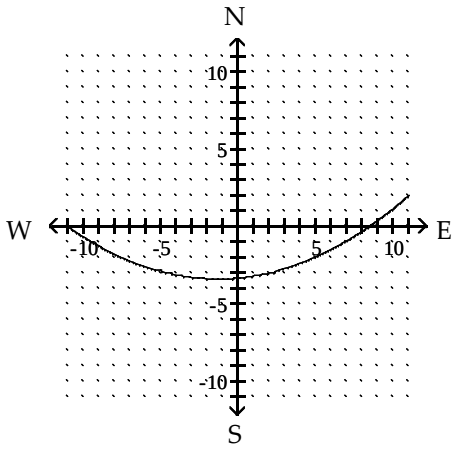
B) $y = \frac{1}{28}(x - 1.2)^2 - 3.4$



C) $y = \frac{1}{28}(x - 1.2)^2 + 3.4$



D) $y = -\frac{1}{28}(x + 1.2)^2 - 3.4$



2 Graph Functions Using Compressions and Stretches

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Write the equation that results in the desired transformation.

1) The graph of $y = x^2$, vertically stretched by a factor of 6

A) $y = -6x^2$ B) $y = (x - 6)^2$ C) $y = 6(x - 6)x^2$ D) $y = 6x^2$

2) The graph of $y = x^3$, vertically compressed by a factor of 0.7

A) $y = (x - 0.7)^3$ B) $y = 0.7x^3$ C) $y = (x + 0.7)^3$ D) $y = 0.7\sqrt[3]{x}$

Suppose the point (2, 4) is on the graph of y = f(x). Find a point on the graph of the given function.

3) $y = 4f(x)$

A) (8, 4) B) (5, 3) C) (3, 8) D) (2, 16)

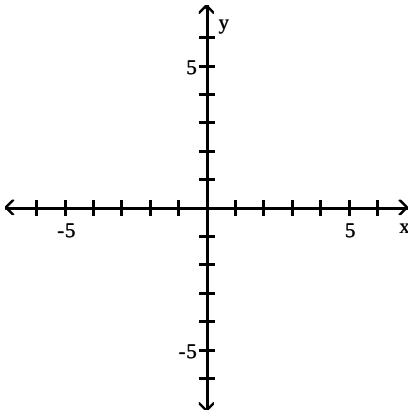
Solve the problem.

4) Suppose that the x-intercepts of the graph of $y = f(x)$ are 7 and 4. What are the x-intercepts of $y = 6f(x)$?

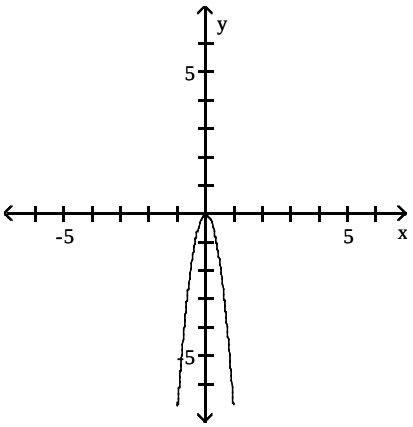
A) 7 and 4 B) 13 and 10 C) 1 and -2 D) 28 and 24

Graph the function by starting with the graph of the basic function and then using the techniques of shifting, compressing, stretching, and/or reflecting.

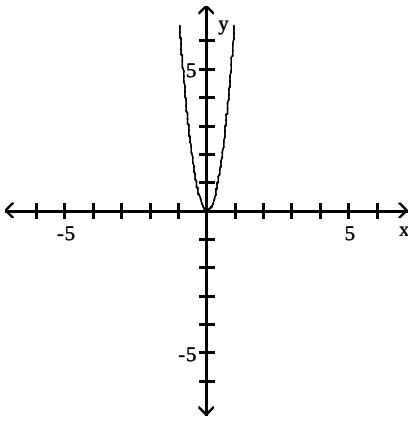
5) $f(x) = 7x^2$



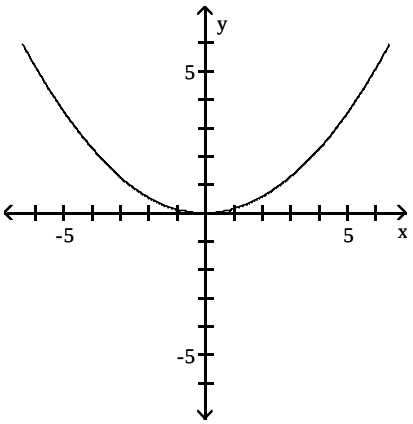
A)



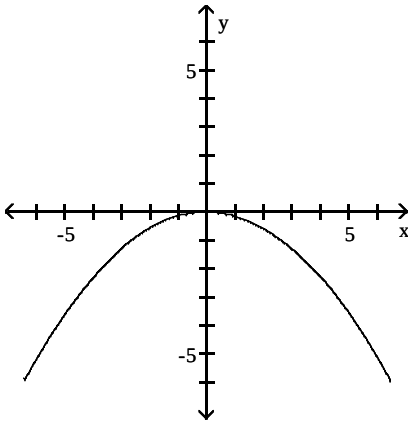
B)



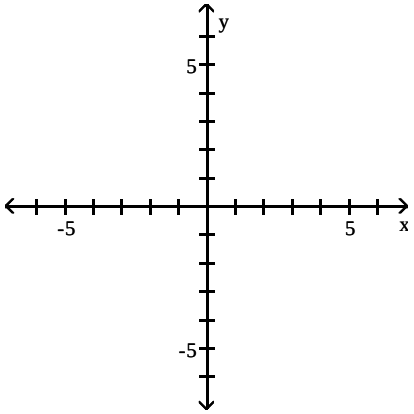
C)



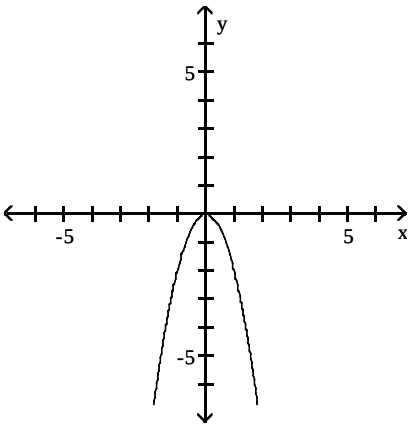
D)



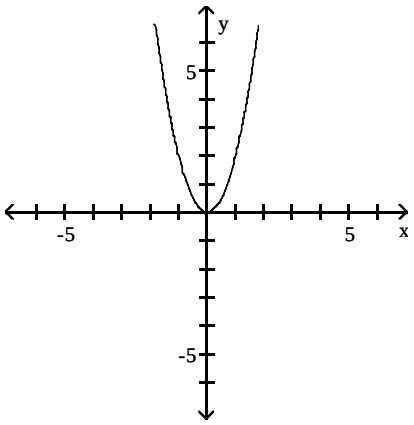
6) $f(x) = \frac{1}{2}x^2$



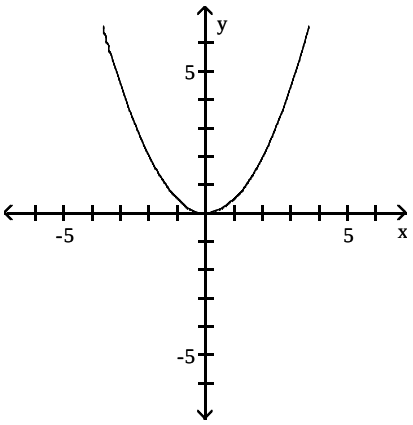
A)



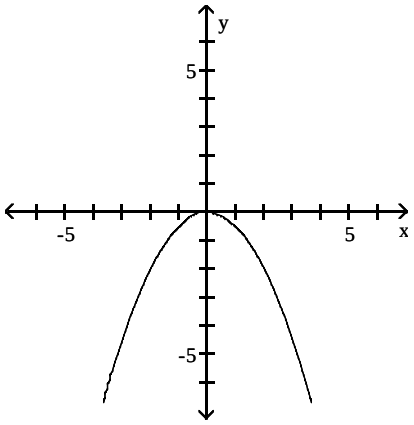
B)



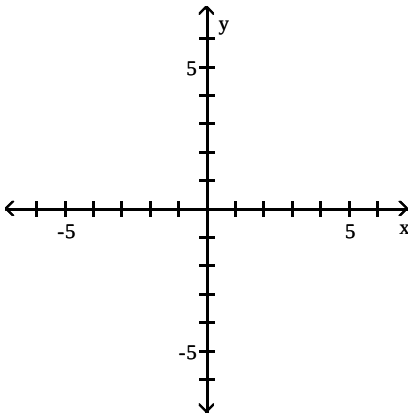
C)



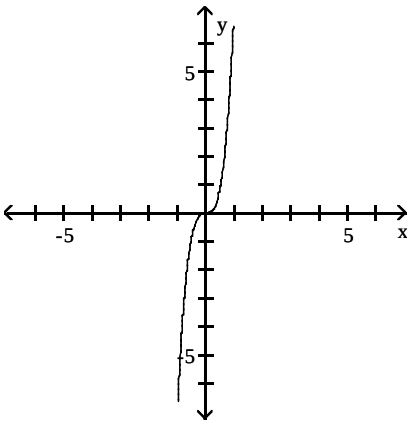
D)



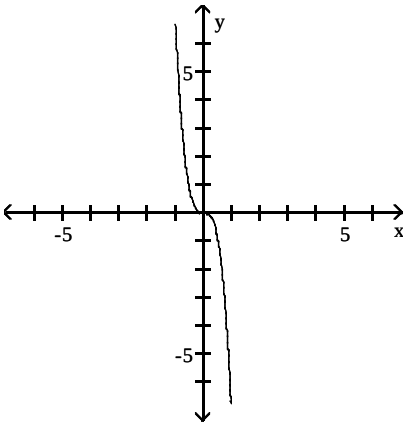
7) $f(x) = 7x^3$



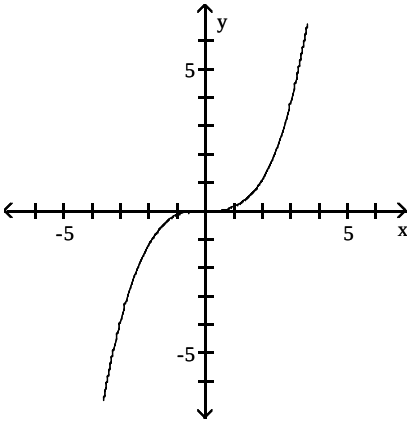
A)



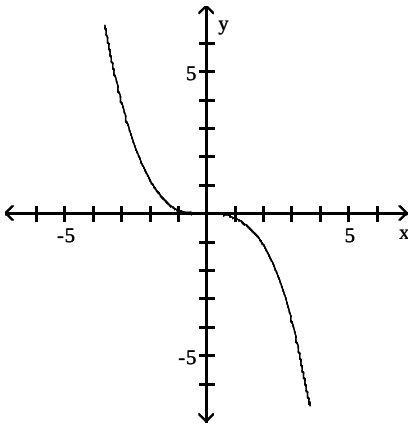
B)



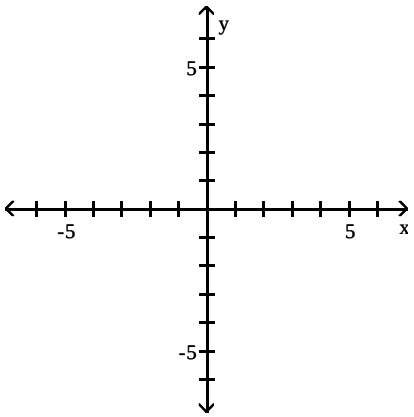
C)



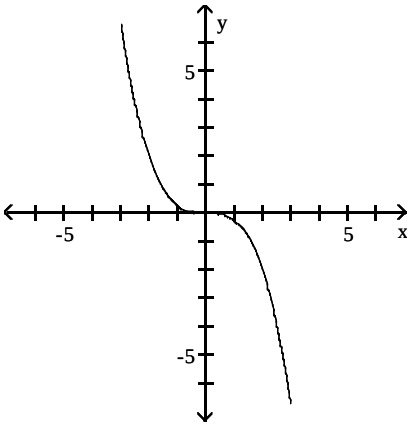
D)



8) $f(x) = \frac{1}{4}x^3$



A)



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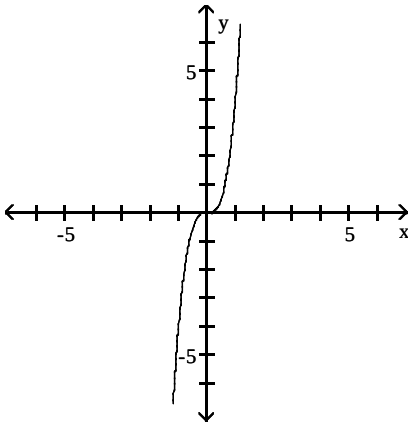
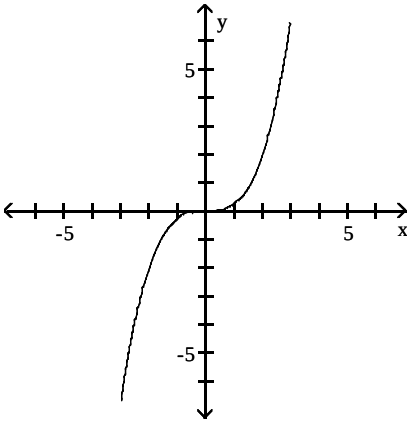
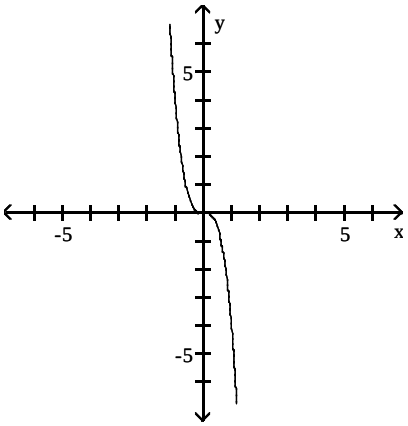


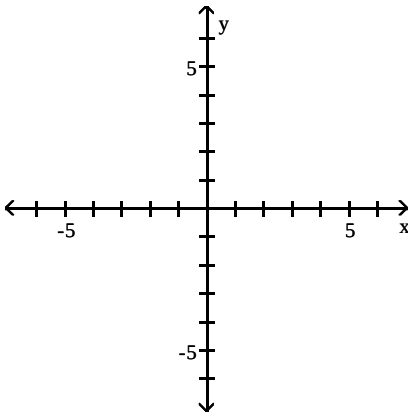
C)



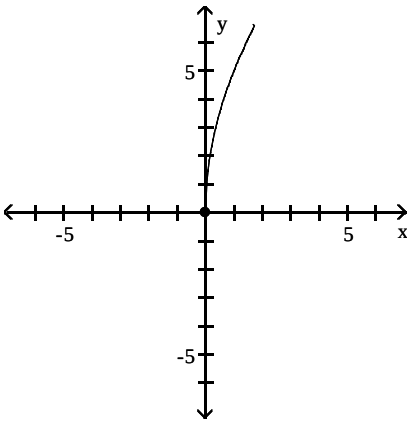
D)



9) $f(x) = 5\sqrt{x}$



A)



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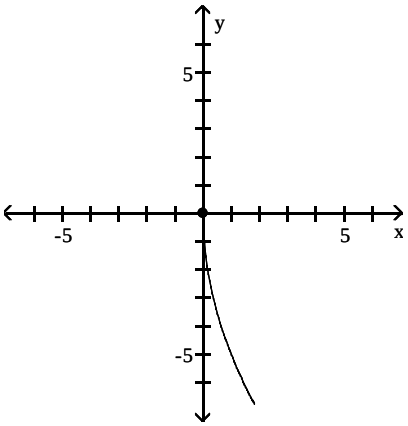

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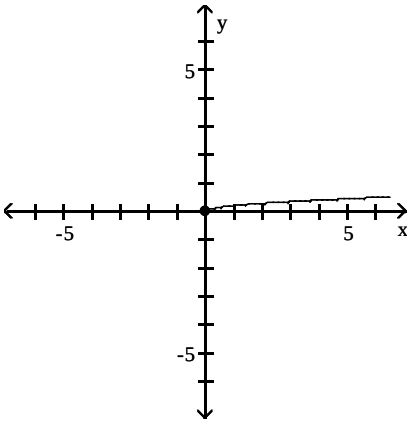
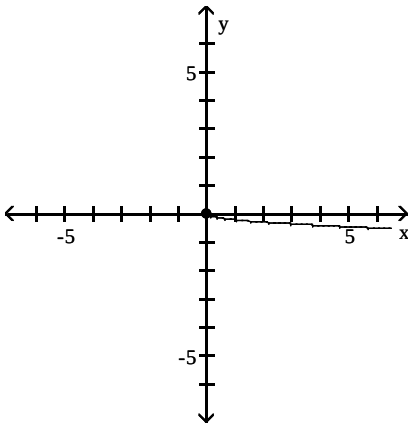
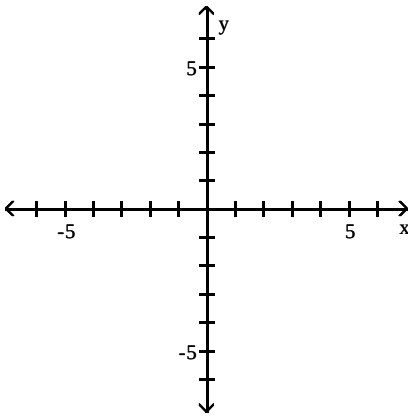


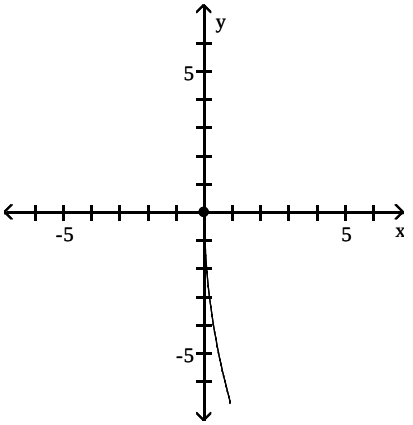
D)



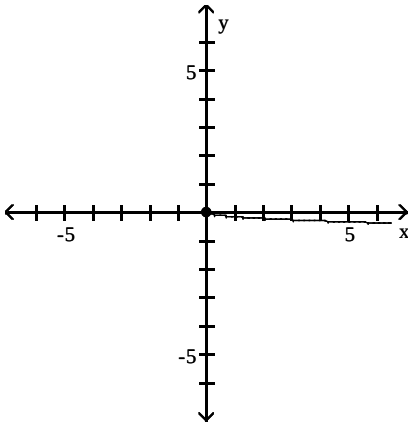
10) $f(x) = \frac{1}{7}\sqrt{x}$



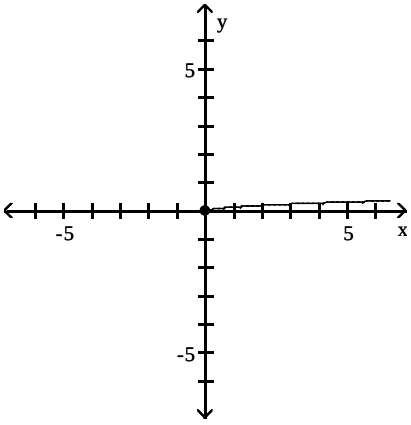
A)



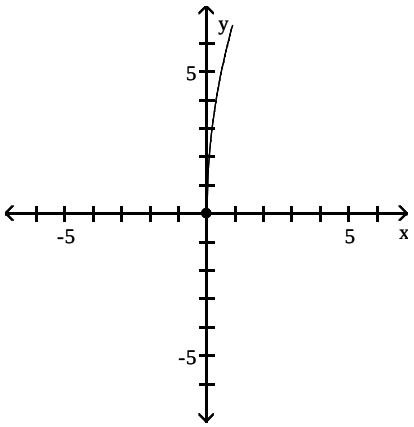
B)



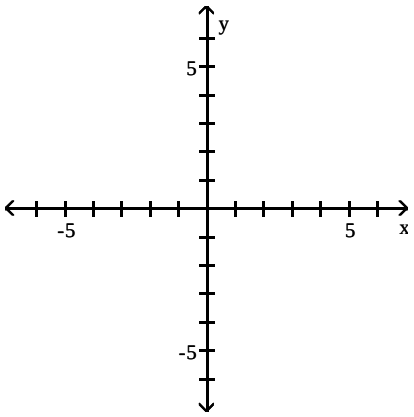
C)



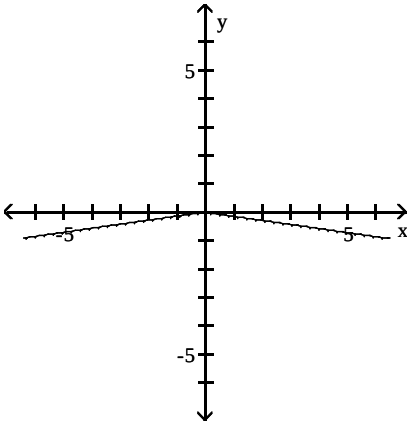
D)



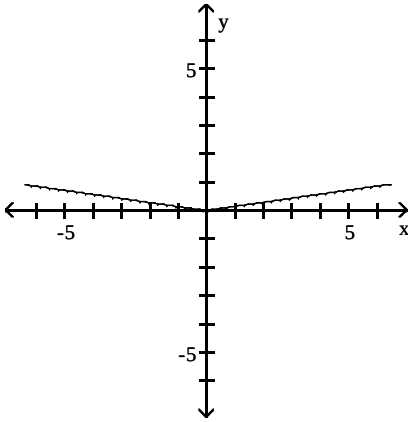
11) $f(x) = 7|x|$



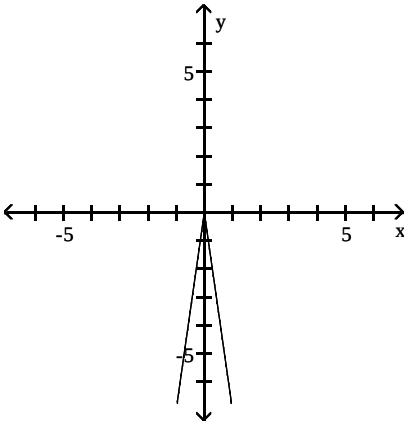
A)



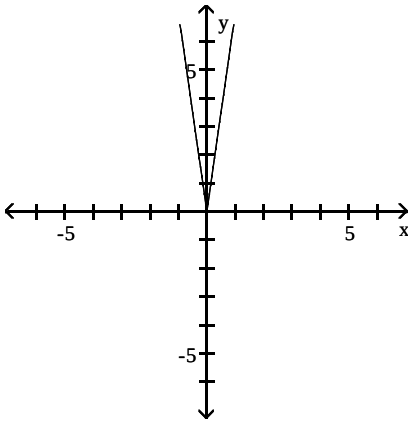
B)



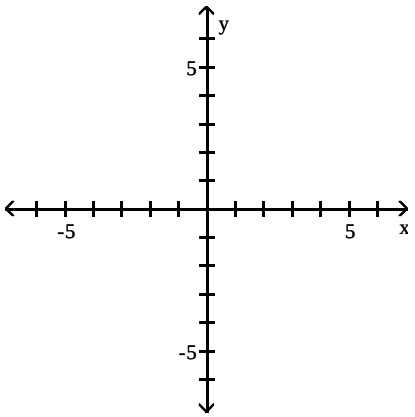
C)



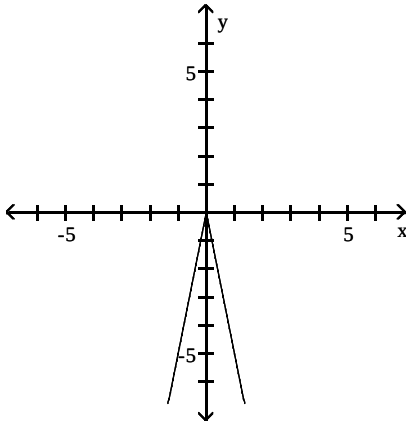
D)



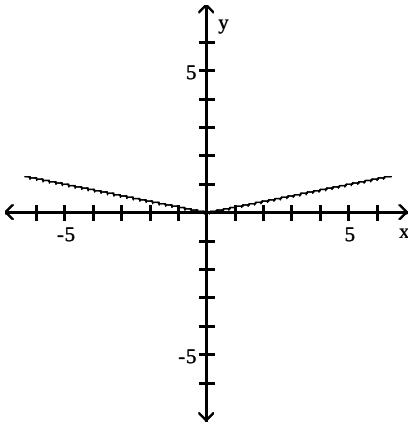
12) $f(x) = \frac{1}{5}|x|$



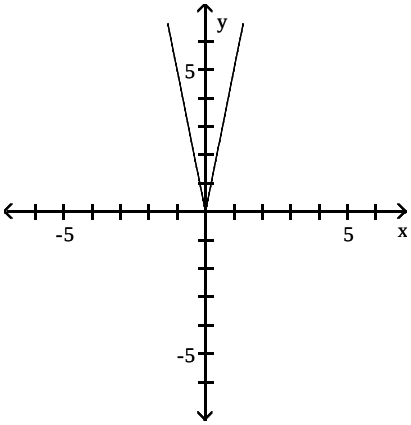
A)



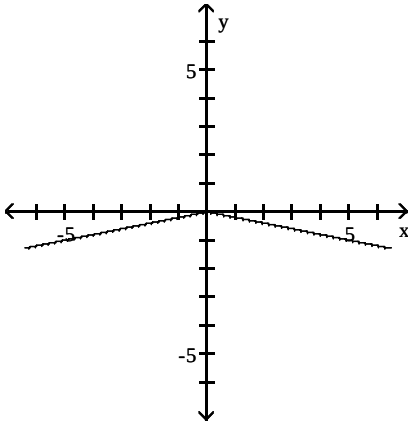
B)



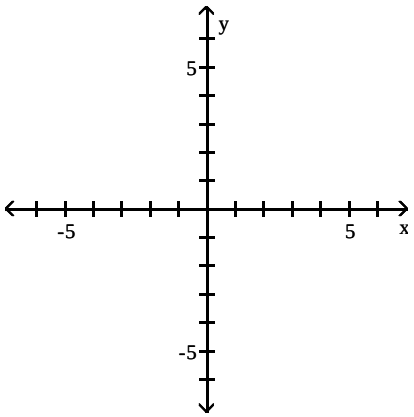
C)



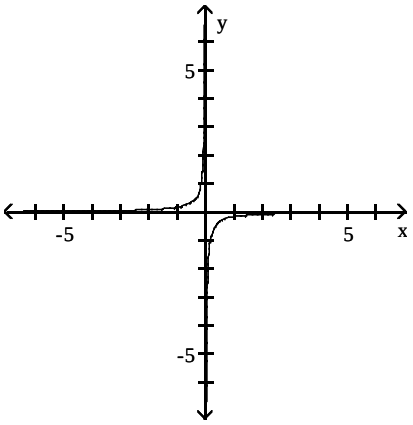
D)



13) $f(x) = \frac{6}{x}$



A)



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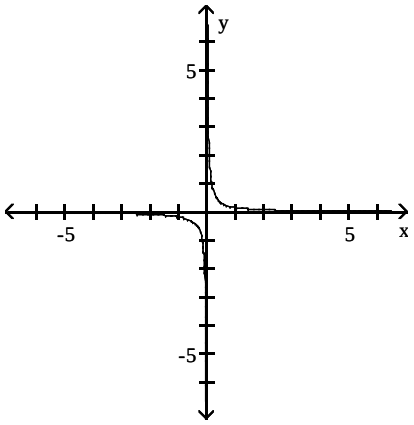
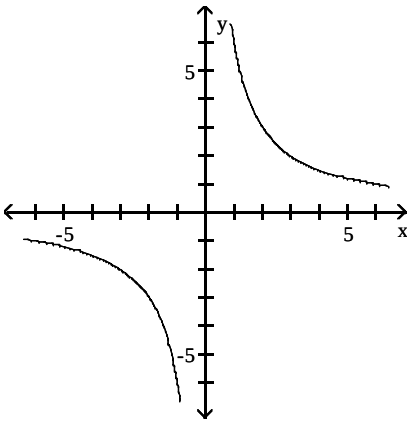
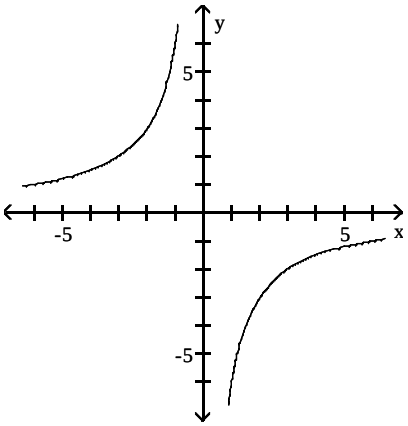


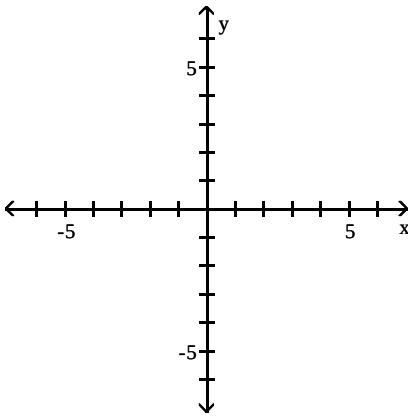
C)



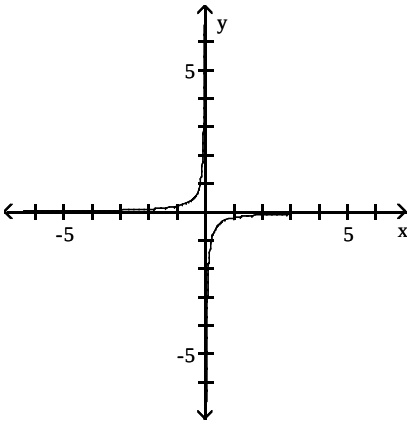
D)



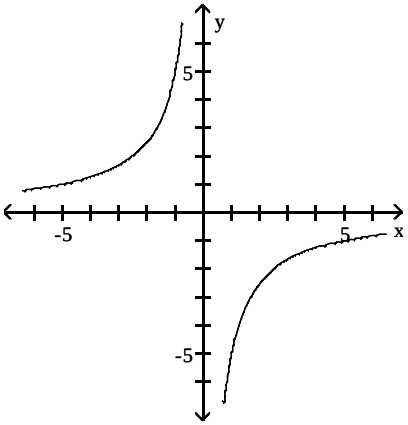
14) $f(x) = \frac{1}{5x}$



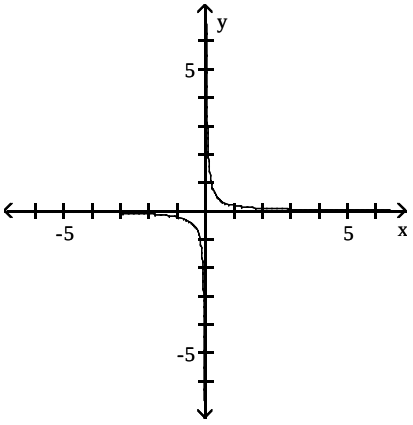
A)



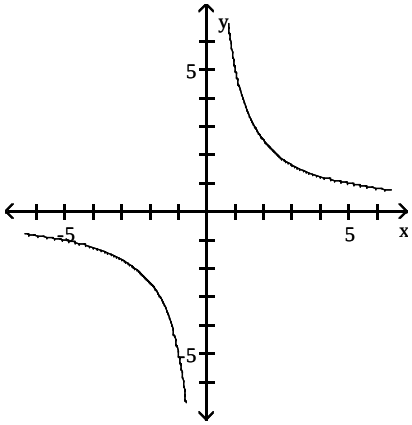
B)



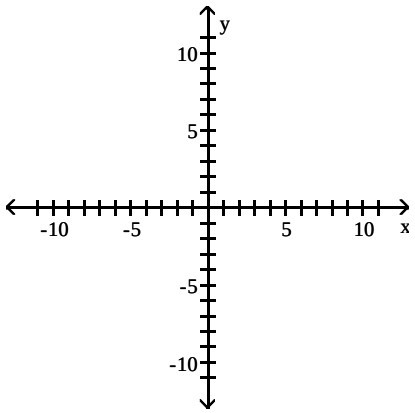
C)



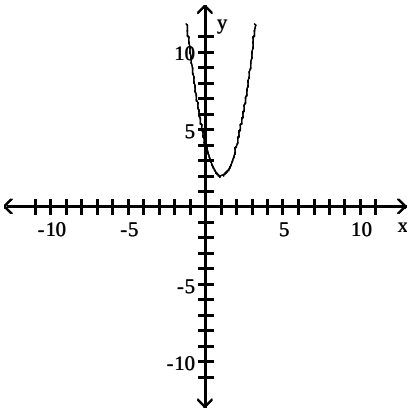
D)



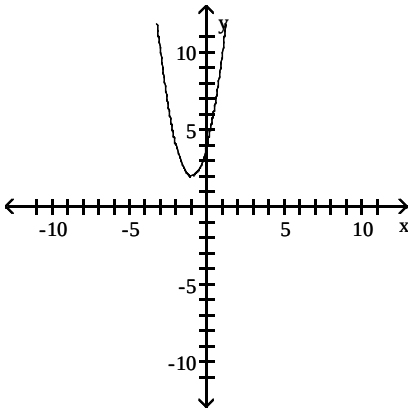
15) $f(x) = 2(x + 1)^2 + 2$



A)



B)



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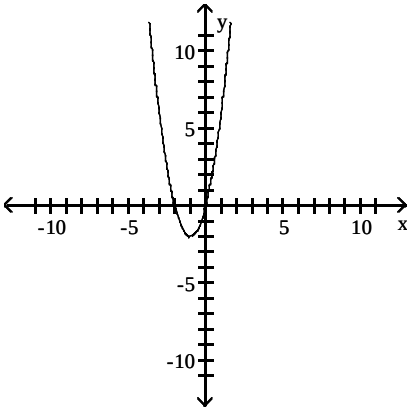
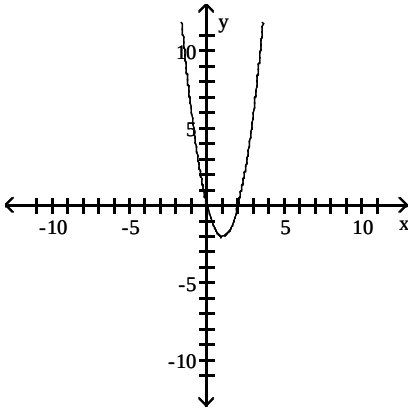
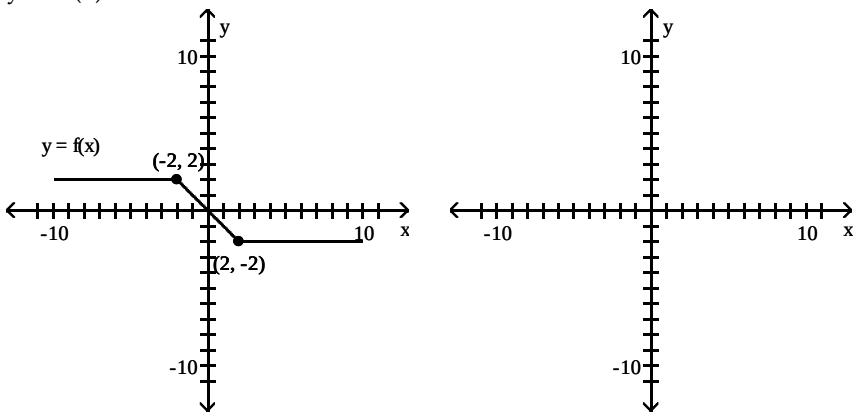


D)

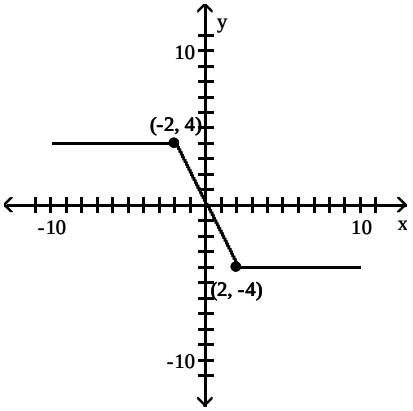


Use the accompanying graph of y = f(x) to sketch the graph of the indicated equation.

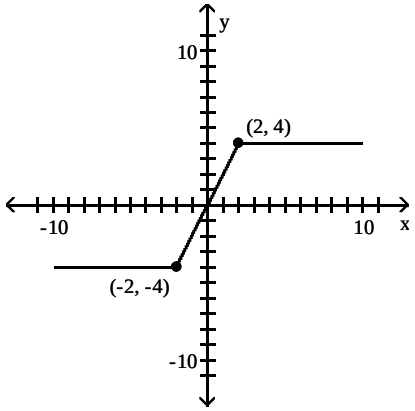
16) y = 2f(x)



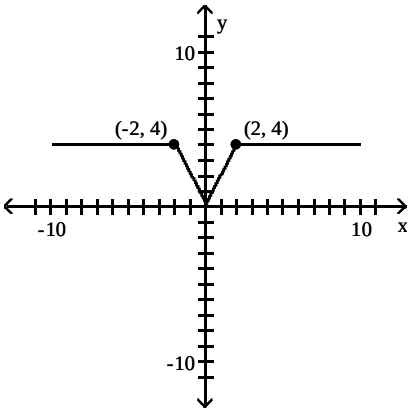
A)



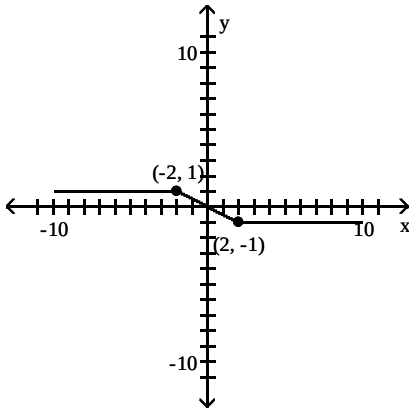
B)



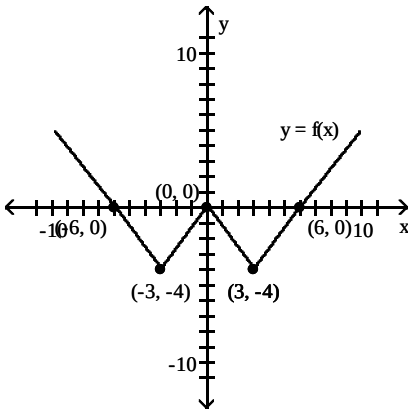
C)



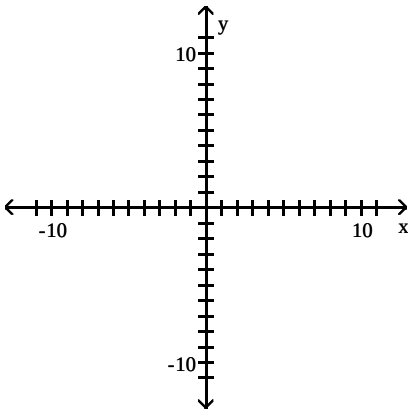
D)



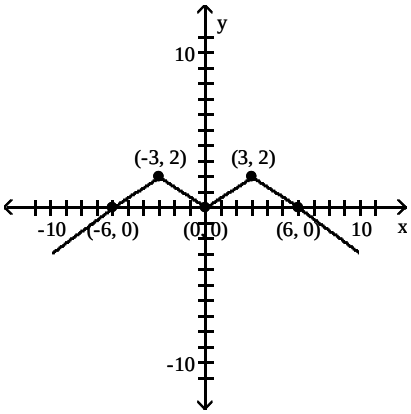
17) $y = -\frac{1}{2}f(x)$



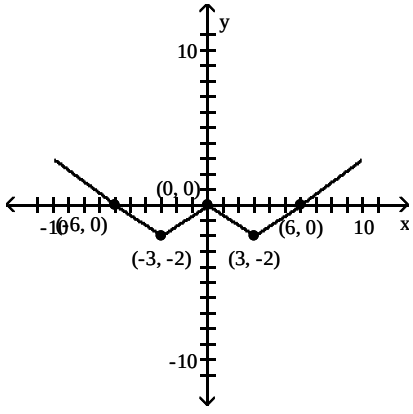
A)



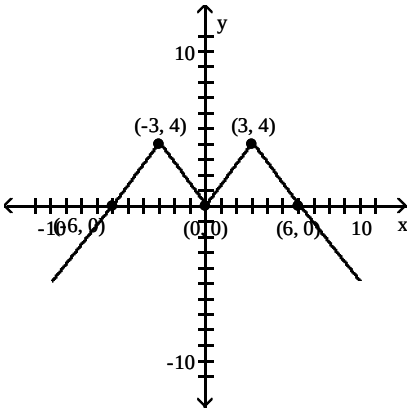
B)

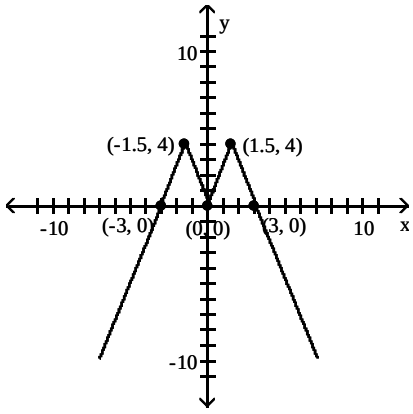


C)

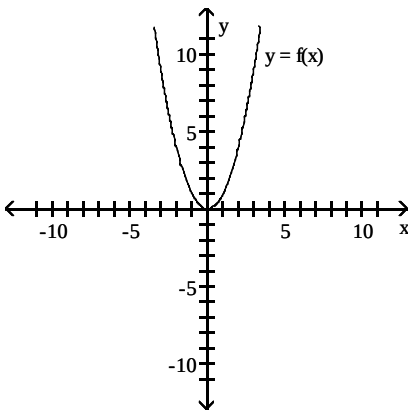


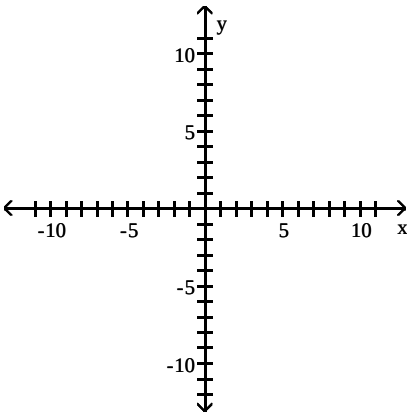
D)



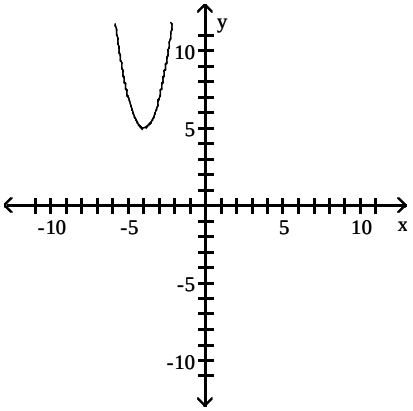


18) $y = -2f(x + 5) + 4$

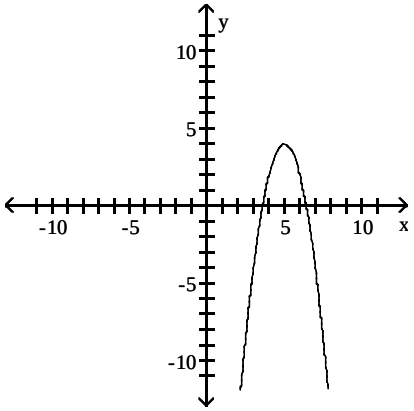




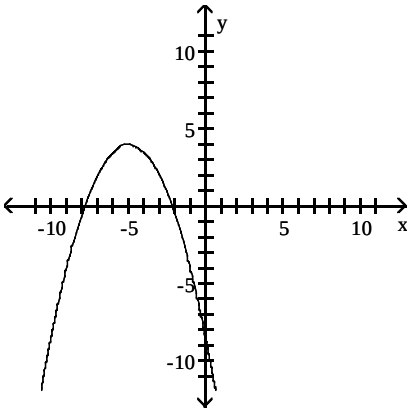
A)



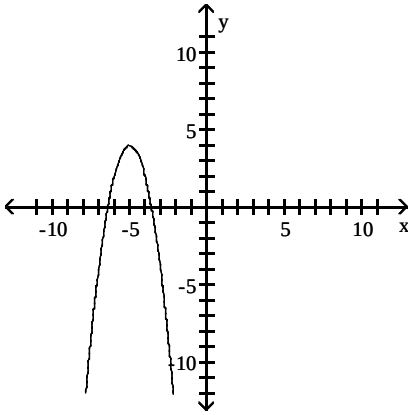
B)



C)



D)

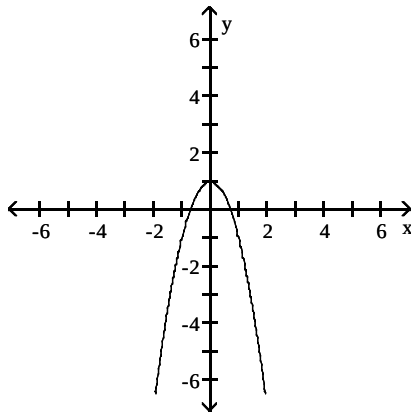


3 Graph Functions Using Reflections about the x–Axis and the y–Axis

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Match the correct function to the graph.

1)



A) $y = -2x^2$ B) $y = 1 - x^2$ C) $y = -2x^2 + 1$ D) $y = -2x^2 - 1$

Suppose the point (2, 4) is on the graph of y = f(x). Find a point on the graph of the given function.

2) The reflection of the graph of y = f(x) across the x–axis

A) (2, –4) B) (–2, –4) C) (–2, 4) D) (2, 4)

3) The reflection of the graph of y = f(x) across the y–axis

A) (2, 4) B) (2, –4) C) (–2, –4) D) (–2, 4)

Solve the problem.

4) Suppose that the x–intercepts of the graph of y = f(x) are 3 and 9. What are the x–intercepts of y = f(–x)?

A) –3 and –9 B) 3 and 9 C) 3 and –9 D) –3 and 9

5) Suppose that the function y = f(x) is decreasing on the interval (5, 7). What can be said about the graph of y = –f(x)?

A) increasing on (–5, –7) B) increasing on (5, 7)
C) decreasing on (5, 7) D) decreasing on (–5, –7)

Find the function.

6) Find the function that is finally graphed after the following transformations are applied to the graph of $y = |x|$. The graph is shifted right 3 units, stretched by a factor of 3, shifted vertically down 2 units, and finally reflected across the x–axis.

A) $y = -3|x - 3| - 2$ B) $y = -(3|x - 3| - 2)$ C) $y = 3|-x - 3| - 2$ D) $y = -(3|x + 3| - 2)$

7) Find the function that is finally graphed after the following transformations are applied to the graph of $y = \sqrt{x}$. The graph is shifted up 2 units, reflected about the y–axis, and finally shifted right 8 units.

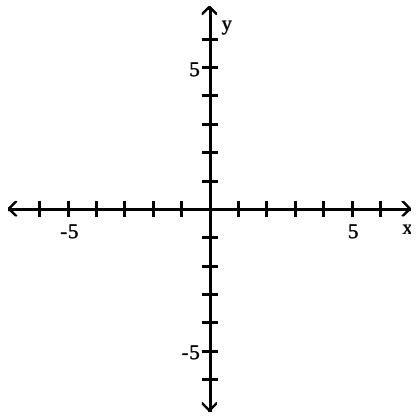
A) $y = -\sqrt{x - 8} + 2$ B) $y = \sqrt{-x + 8} - 2$ C) $y = \sqrt{-x + 8} + 2$ D) $y = \sqrt{-x - 8} - 2$

8) Find the function that is finally graphed after the following transformations are applied to the graph of $y = |x|$. The graph is shifted down 4 units, reflected about the y–axis, and finally shifted right 7 units.

A) $y = |-x + 7| - 4$ B) $y = |-x - 7| + 4$ C) $y = -|x - 7| - 4$ D) $y = |-x + 7| + 4$

Graph the function by starting with the graph of the basic function and then using the techniques of shifting, compressing, stretching, and/or reflecting.

9) $f(x) = -x^2$



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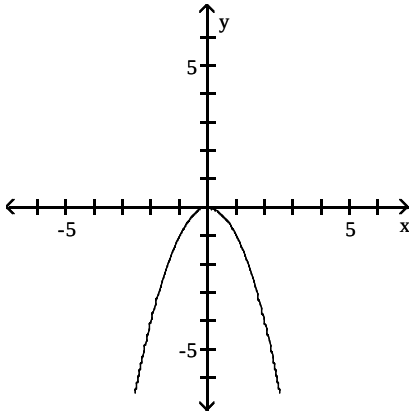

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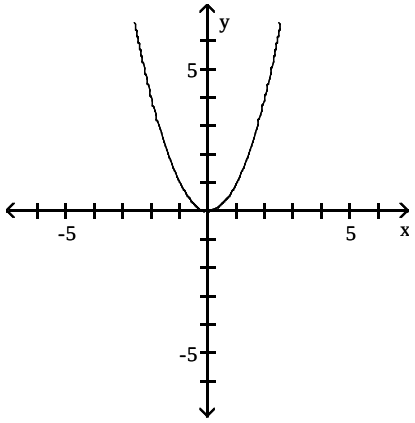

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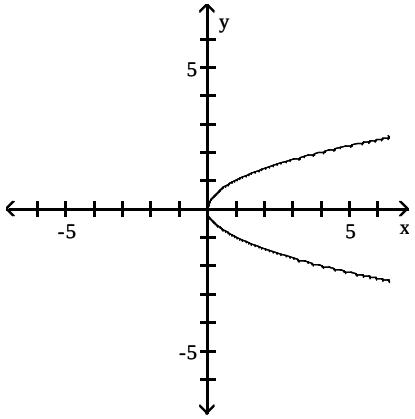

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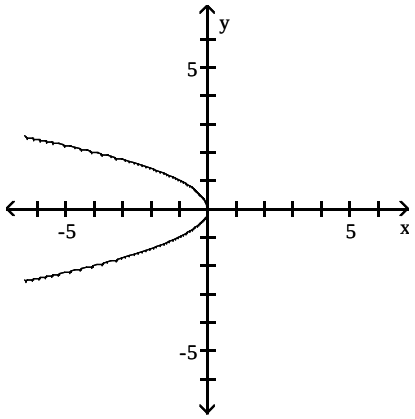
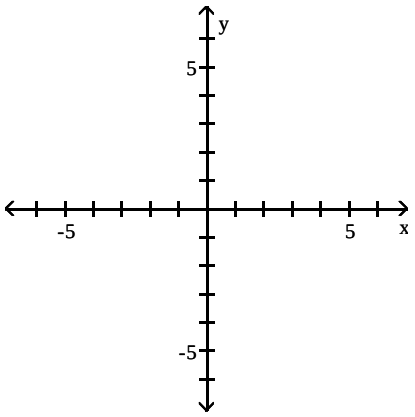


10) $f(x) = (-x)^2$



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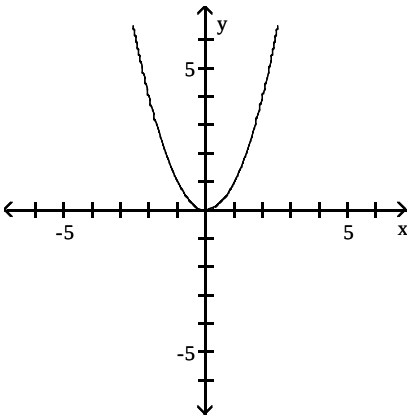

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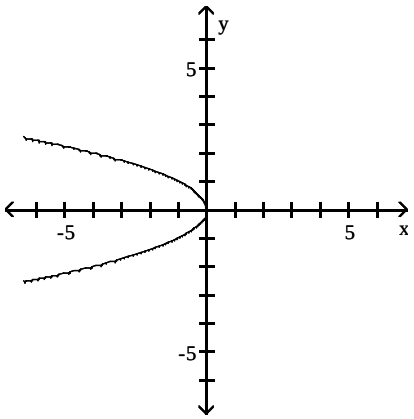

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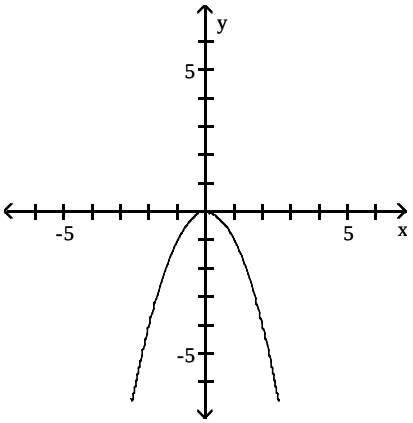

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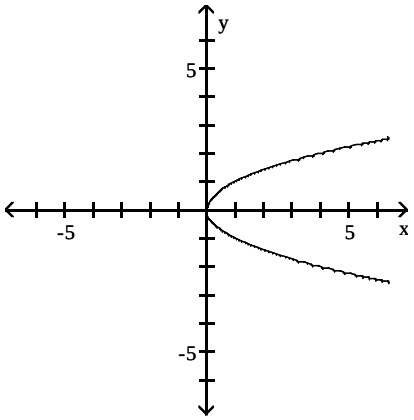
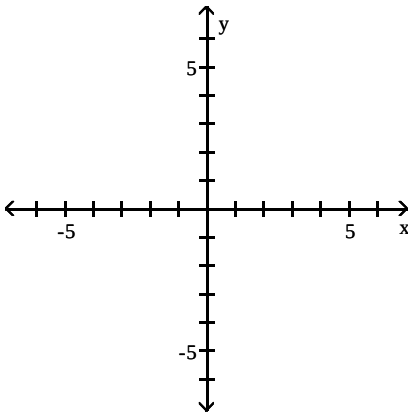


11) $f(x) = -x^3$



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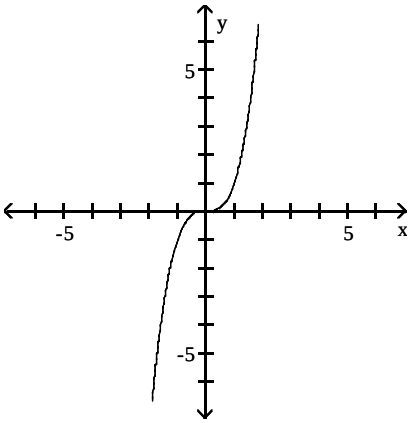

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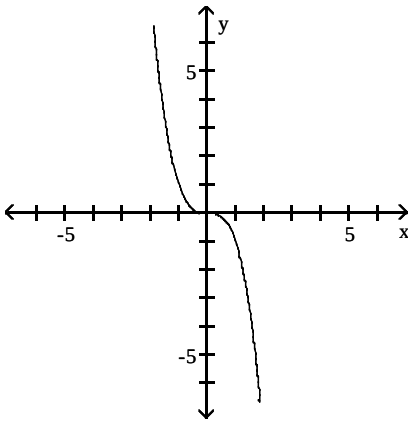

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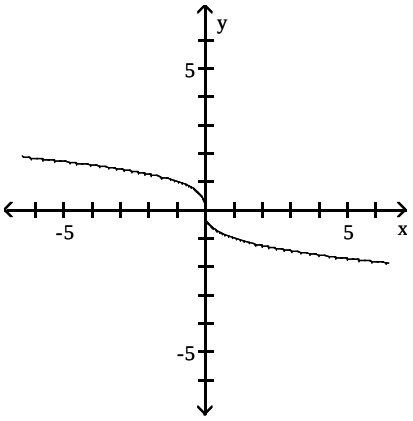

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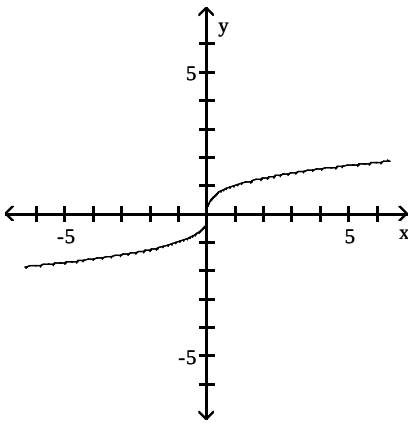
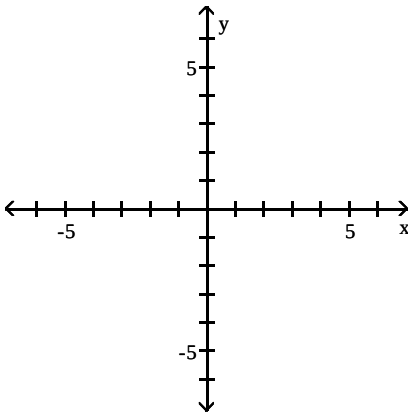


12) $f(x) = (-x)^3$



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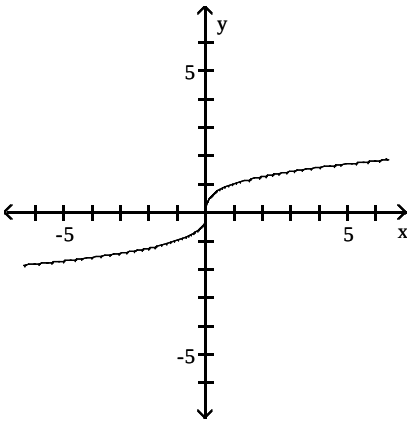

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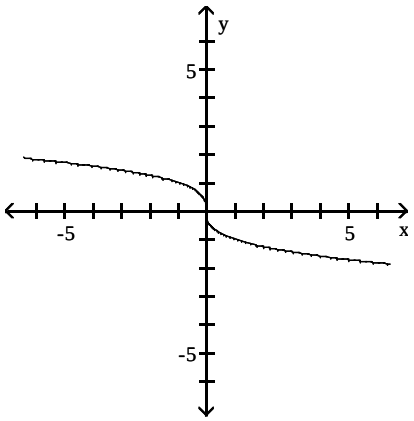

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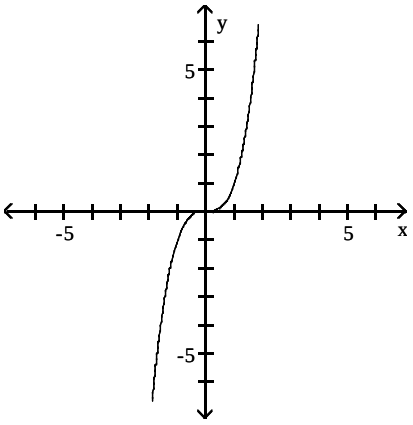

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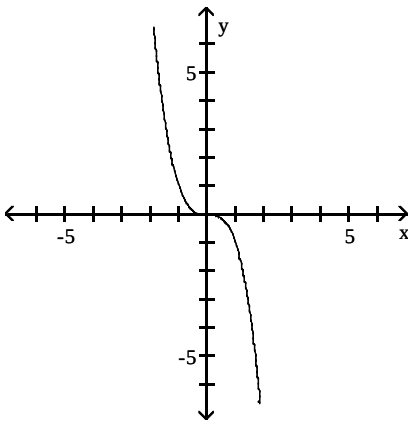
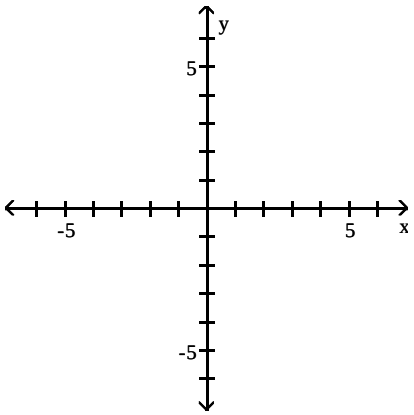


13) $f(x) = -\sqrt{x}$



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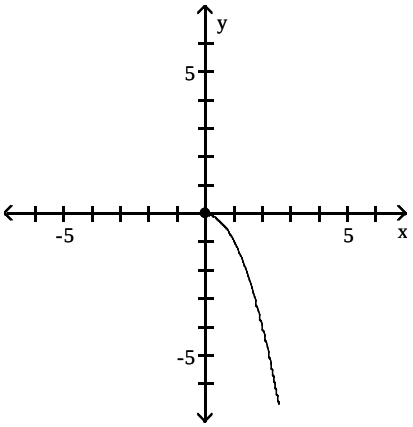

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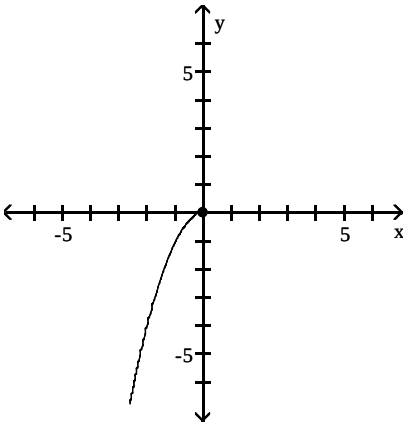

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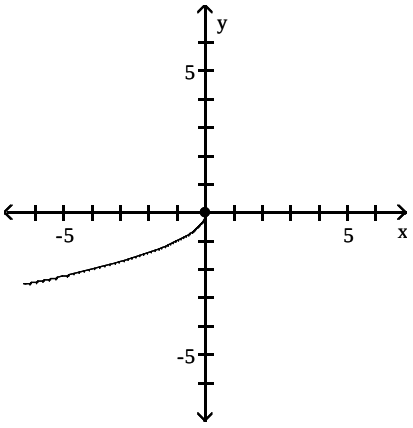

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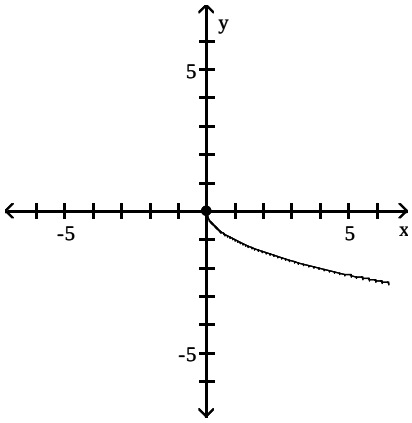
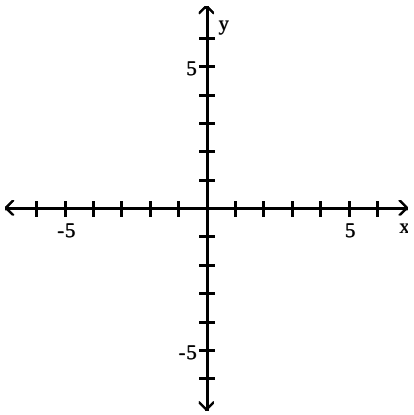
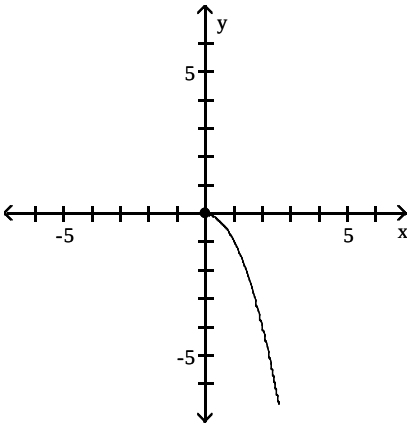


14) $f(x) = \sqrt{-x}$



A)



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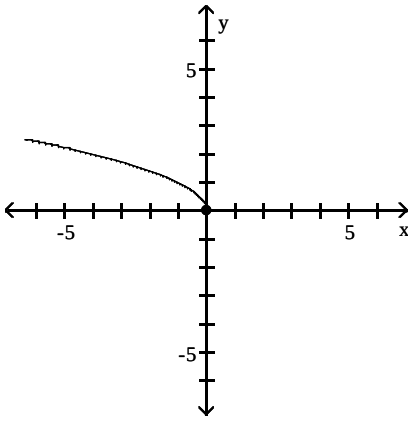

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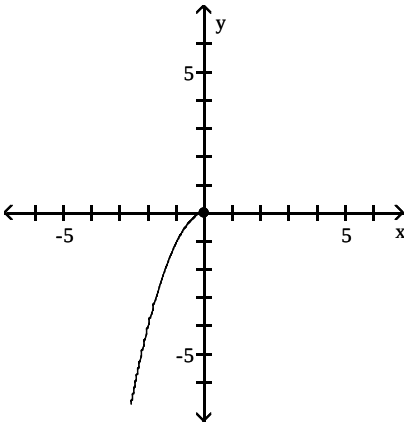

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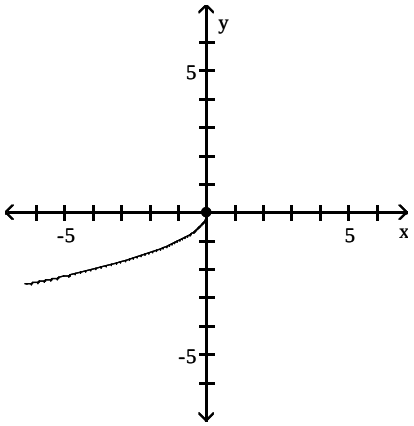
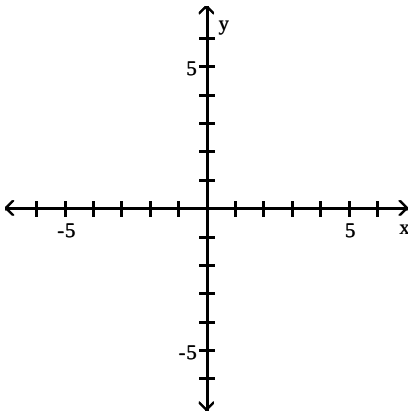
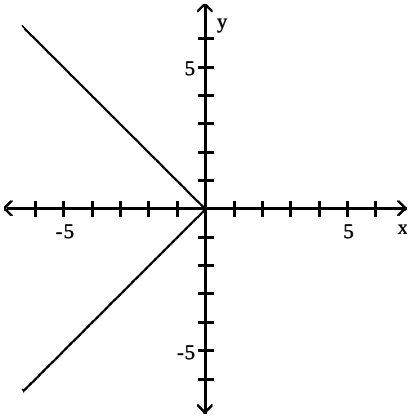


15) $f(x) = -|x|$



A)



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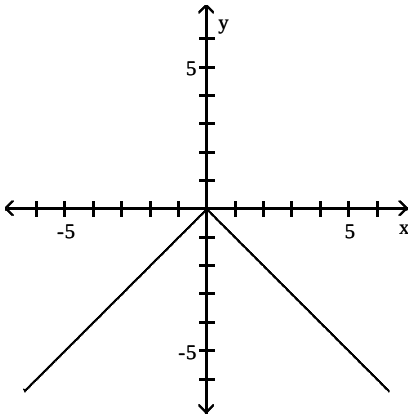

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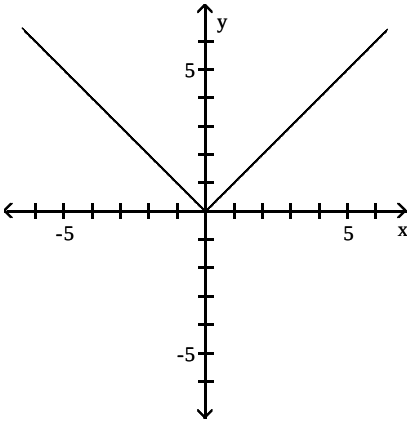

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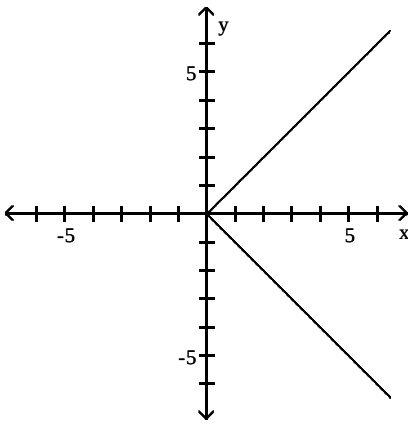
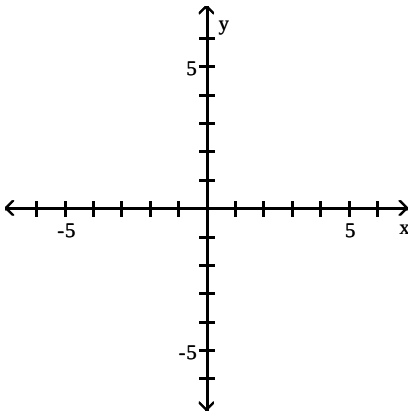
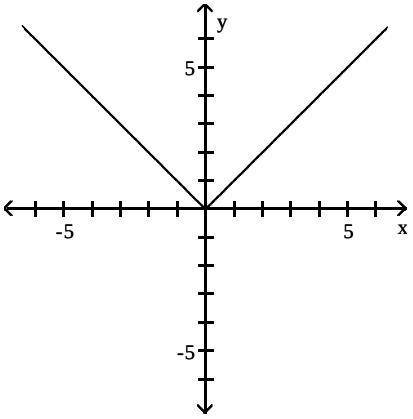


16) f(x) = |−x|



A)



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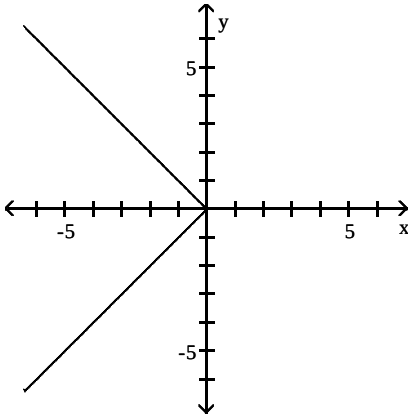

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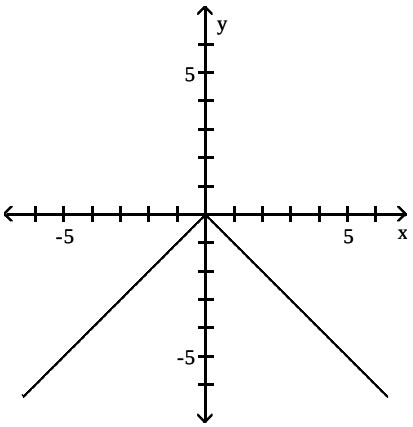
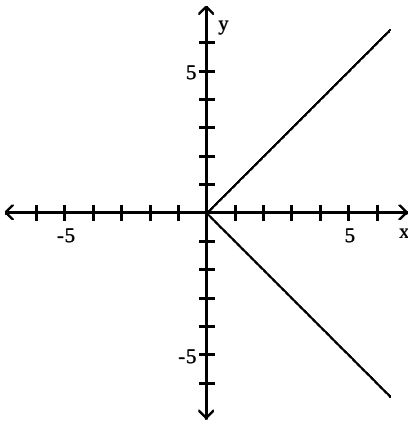
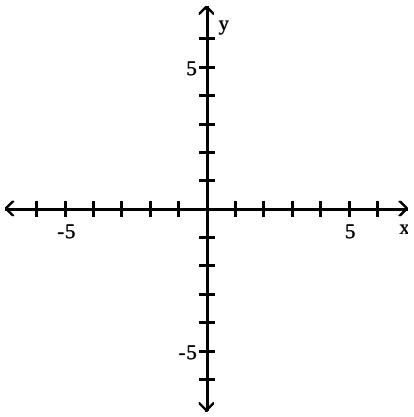


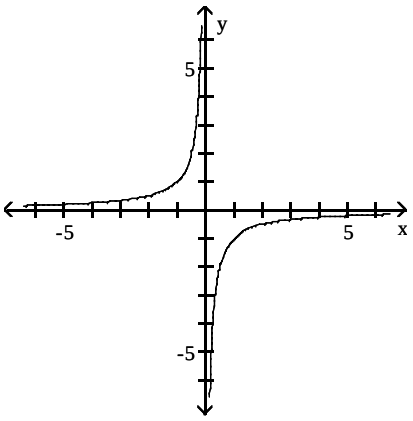
D)



17) $f(x) = -\frac{1}{x}$



A)



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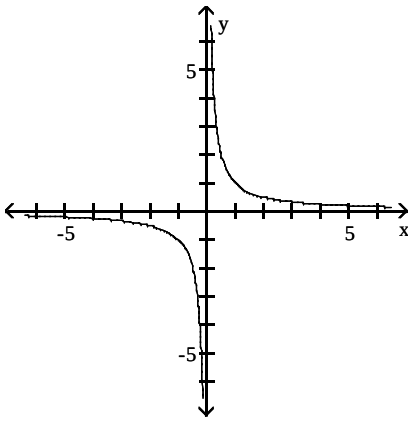

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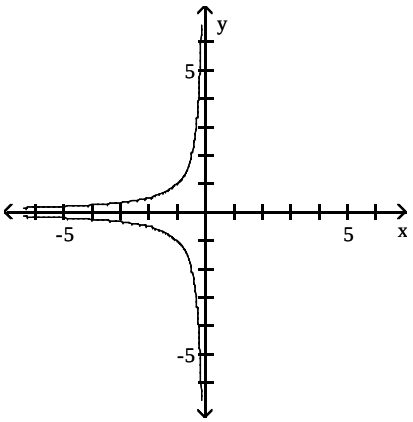
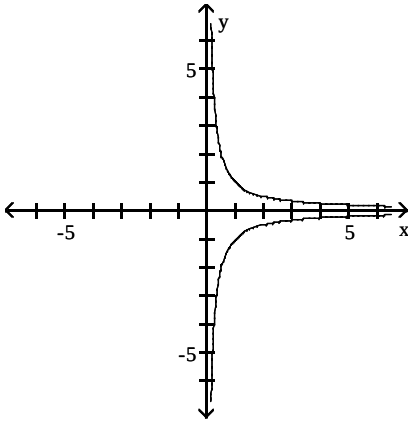
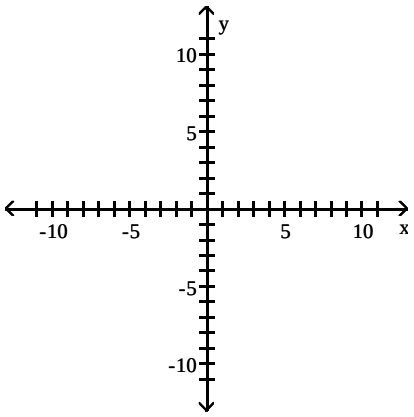


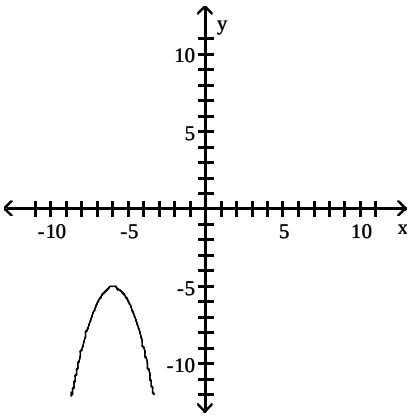
D)



18) $f(x) = -(x + 6)^2 - 5$



A)



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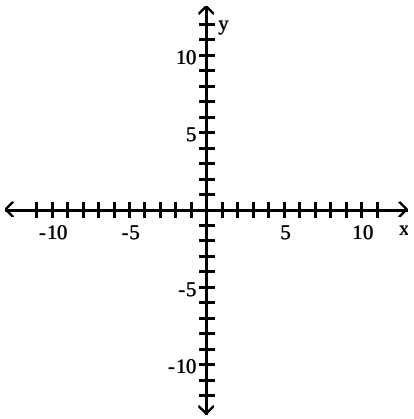
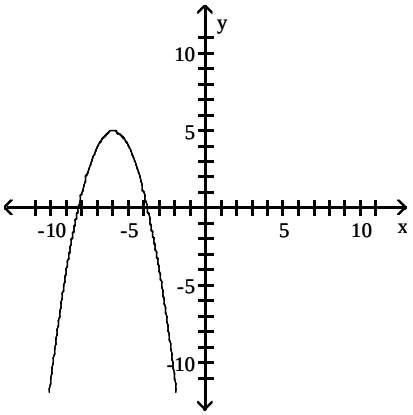
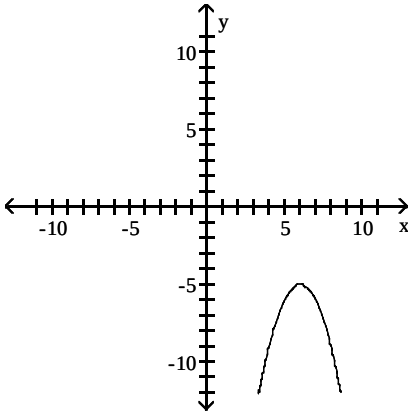


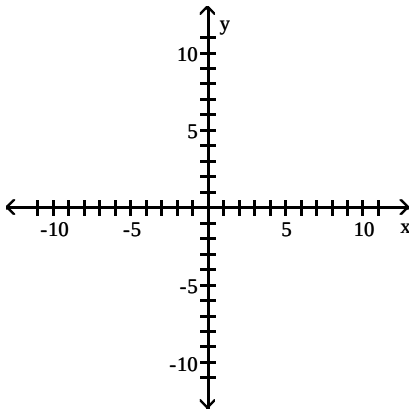
C)



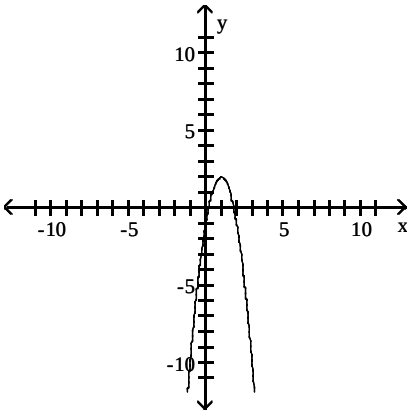
D)



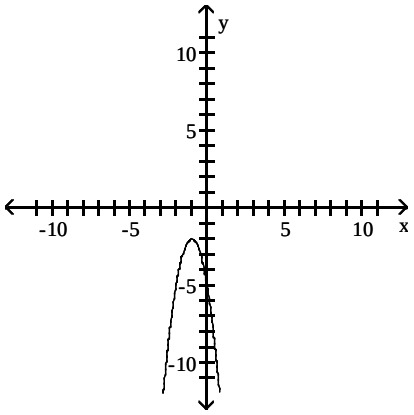
19) $f(x) = -3(x + 1)^2 - 2$



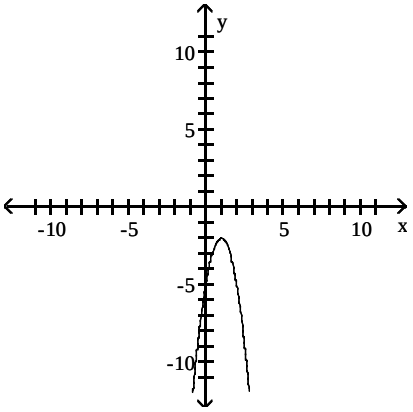
A)



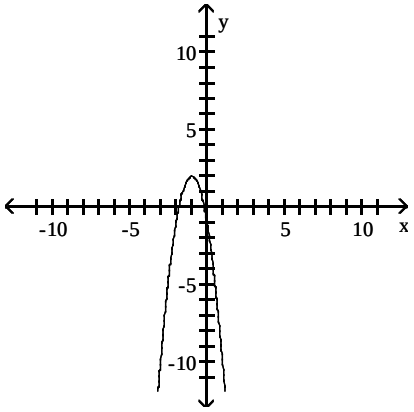
B)



C)



D)



2.6 Mathematical Models: Building Functions

1 Build and Analyze Functions

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Solve the problem.

1) Elissa wants to set up a rectangular dog run in her backyard. She has 34 feet of fencing to work with and wants to use it all. If the dog run is to be x feet long, express the area of the dog run as a function of x.

A) $A(x) = 18x - x^2$ B) $A(x) = 17x - x^2$ C) $A(x) = 19x^2 - x$ D) $A(x) = 16x - x^2$

2) Bob wants to fence in a rectangular garden in his yard. He has 70 feet of fencing to work with and wants to use it all. If the garden is to be x feet wide, express the area of the garden as a function of x.

A) $A(x) = 35x - x^2$ B) $A(x) = 36x - x^2$ C) $A(x) = 37x^2 - x$ D) $A(x) = 34x - x^2$

3) Sue wants to put a rectangular garden on her property using 74 meters of fencing. There is a river that runs through her property so she decides to increase the size of the garden by using the river as one side of the rectangle. (Fencing is then needed only on the other three sides.) Let x represent the length of the side of the rectangle along the river. Express the garden's area as a function of x.

A) $A(x) = 38x - 2x^2$ B) $A(x) = 37x - \frac{1}{2}x^2$ C) $A(x) = 36x - \frac{1}{4}x^2$ D) $A(x) = 37x^2 - x$

4) A farmer has 1000 yards of fencing to enclose a rectangular garden. Express the area A of the rectangle as a function of the width x of the rectangle. What is the domain of A?

A) $A(x) = -x^2 + 500x;\ \{x \mid 0 < x < 1000\}$ B) $A(x) = -x^2 + 1000x;\ \{x \mid 0 < x < 1000\}$

C) $A(x) = x^2 + 500x;\ \{x \mid 0 < x < 500\}$ D) $A(x) = -x^2 + 500x;\ \{x \mid 0 < x < 500\}$

5) A rectangular sign is being designed so that the length of its base, in feet, is 2 feet less than 4 times the height, h. Express the area of the sign as a function of h.

A) $A(h) = -2h + 4h^2$ B) $A(h) = 2h - 2h^2$ C) $A(h) = -2h^2 + 2h$ D) $A(h) = -2h + h^2$

6) A rectangle that is x feet wide is inscribed in a circle of radius 37 feet. Express the area of the rectangle as a function of x.

A) $A(x) = x^2\sqrt{2738 - x^2}$ B) $A(x) = x(5476 - x^2)$

C) $A(x) = x\sqrt{5476 - x^2}$ D) $A(x) = x\sqrt{4107 - x}$

7) A wire of length 9x is bent into the shape of a square. Express the area A of the square as a function of x.

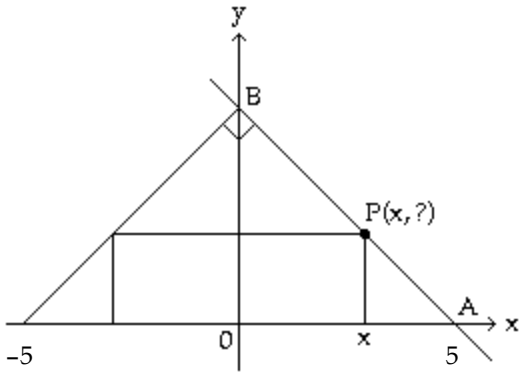
A) $A(x) = \frac{81}{16}x^2$ B) $A(x) = \frac{1}{16}x^2$ C) $A(x) = \frac{9}{4}x^2$ D) $A(x) = \frac{81}{8}x^2$

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

8) A right triangle has one vertex on the graph of $y = x^2$ at (x, y), another at the origin, and the third on the (positive) y–axis at (0, y). Express the area A of the triangle as a function of x.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

9) The figure shown here shows a rectangle inscribed in an isosceles right triangle whose hypotenuse is 10 units long. Express the area A of the rectangle in terms of x.



A) $A(x) = 2x(x - 5)$ B) $A(x) = x(5 - x)$ C) $A(x) = 2x^2$ D) $A(x) = 2x(5 - x)$

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

10) A wire 20 feet long is to be cut into two pieces. One piece will be shaped as a square and the other piece will be shaped as an equilateral triangle. Express the total area A enclosed by the pieces of wire as a function of the length x of a side of the equilateral triangle. What is the domain of A?

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

11) A farmer's silo is the shape of a cylinder with a hemisphere as the roof. If the height of the silo is 78 feet and the radius of the hemisphere is r feet, express the volume of the silo as a function of r.

A) $V(r) = 78\pi r^2 + \frac{8}{3}\pi r^3$

B) $V(r) = \pi(78 - r)r^2 + \frac{2}{3}\pi r^3$

C) $V(r) = \pi(78 - r)r^3 + \frac{4}{3}\pi r^2$

D) $V(r) = \pi(78 - r) + \frac{4}{3}\pi r^2$

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

12) The volume V of a square–based pyramid with base sides s and height h is $V = \frac{1}{3}s^2h$. If the height is half of the length of a base side, express the volume V as a function of s.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

13) A farmer's silo is the shape of a cylinder with a hemisphere as the roof. If the radius of the hemisphere is 10 feet and the height of the silo is h feet, express the volume of the silo as a function of h.

A) $V(h) = 100\,\pi(h - 10) + \frac{2000}{3}\pi$

B) $V(h) = 100\,\pi(h^2 - 10) + \frac{5000}{3}\pi$

C) $V(h) = 100\,\pi h + \frac{4000}{3}\pi h^2$

D) $V(h) = 4100\,\pi(h - 10) + \frac{500}{7}\pi$

14) From a 20–inch by 20–inch piece of metal, squares are cut out of the four corners so that the sides can then be folded up to make a box. Let x represent the length of the sides of the squares, in inches, that are cut out. Express the volume of the box as a function of x.

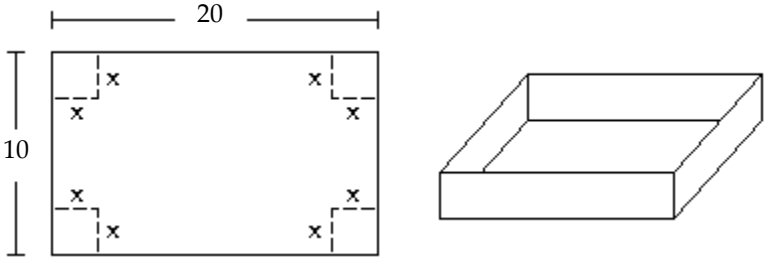
A) $V(x) = 2x^3 - 60x^2 + 20x$

B) $V(x) = 4x^3 - 80x^2$

C) $V(x) = 4x^3 - 80x^2 + 400x$

D) $V(x) = 2x^3 - 60x^2$

15) A box with an open top is to be constructed from a rectangular piece of cardboard with dimensions 10 inches by 20 inches by cutting out equal squares of side x at each corner and then folding up the sides as in the figure. Express the volume V of the box as a function of x.



A) $V(x) = x(10 - x)(20 - x)$

B) $V(x) = (10 - 2x)(20 - 2x)$

C) $V(x) = x(10 - 2x)(20 - 2x)$

D) $V(x) = (10 - x)(20 - x)$

16) A rectangular box with volume 220 cubic feet is built with a square base and top. The cost is \$1.50 per square foot for the top and the bottom and \$2.00 per square foot for the sides. Let x represent the length of a side of the base. Express the cost the box as a function of x.

A) $C(x) = 3x^2 + \frac{880}{x}$

B) $C(x) = 4x + \frac{1760}{x^2}$

C) $C(x) = 2x^2 + \frac{1760}{x}$

D) $C(x) = 3x^2 + \frac{1760}{x}$

17) The price p and the quantity x sold of a certain product obey the demand equation:

$$p = -\frac{1}{4}x + 400, \{x \mid 0 \le x \le 400\}$$

What is the revenue to the nearest dollar when 300 units are sold?

A) \$97,500 B) \$160,000 C) \$10,000 D) \$142,500

18) Let P = (x, y) be a point on the graph of $y = \sqrt{x}$. Express the distance d from P to the point (1, 0) as a function of x.

A) $d(x) = x^2 - x + 1$ B) $d(x) = x^2 + 2x + 2$

C) $d(x) = \sqrt{x^2 - x + 1}$ D) $d(x) = \sqrt{x^2 + 2x + 2}$

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

19) The price p and x, the quantity of a certain product sold, obey the demand equation

$$p = -\frac{1}{10}x + 100, \{x \mid 0 \le x \le 1000\}$$

a) Express the revenue R as a function of x.
b) What is the revenue if 450 units are sold?
c) Graph the revenue function using a graphing utility.
d) What quantity x maximizes revenue? What is the maximum revenue?
e) What price should the company charge to maximize revenue?

20) Two boats leave a dock at the same time. One boat is headed directly east at a constant speed of 35 knots (nautical miles per hour), and the other is headed directly south at a constant speed of 22 knots. Express the distance d between the boats as a function of the time t.

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

21) A rocket is shot straight up in the air from the ground at a rate of 49 feet per second. The rocket is tracked by a range finder that is 482 feet from the launch pad. Let d represent the distance from the rocket to the range finder and t represent the time, in seconds, since "blastoff". Express d as a function of t.

A) $d(t) = 482^2 + (49t)^2$ B) $d(t) = \sqrt{49^2 + (482t)^2}$

C) $d(t) = \sqrt{482^2 + (49t)^2}$ D) $d(t) = 482 + 49t^2$

Ch. 2 Functions and Their Graphs
Answer Key

2.1 Functions

1 Determine Whether a Relation Represents a Function

1) B
2) C
3) A
4) B
5) C
6) B
7) A
8) A
9) A
10) A
11) B
12) B
13) B
14) B
15) A
16) A
17) B
18) A
19) A

2 Find the Value of a Function

1) C
2) A
3) B
4) A
5) A
6) A
7) C
8) D
9) D
10) C
11) D
12) B
13) D
14) D
15) A
16) C
17) B
18) B
19) D
20) B
21) C
22) A

3 Find the Domain of a Function Defined by an Equation

1) D
2) D
3) B
4) B
5) B
6) A

7) A

4 Form the Sum, Difference, Product, and Quotient of Two Functions

1) A
2) C
3) A
4) D
5) D
6) A
7) B
8) B
9) A
10) B
11) D
12) C
13) C
14) C
15) B
16) C
17) D
18) A
19) C
20) C
21) A
22) C
23) B
24) B
25) D
26) D
27) C
28) B

2.2 The Graph of a Function

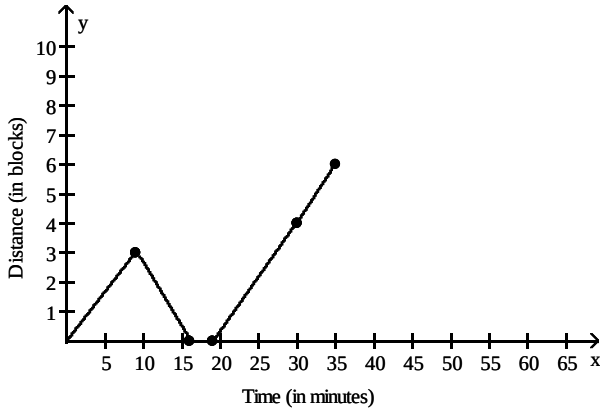
1 Identify the Graph of a Function

1) D
2) A
3) A
4) C
5) D
6) C
7) D

2 Obtain Information from or about the Graph of a Function

1) D
2) A
3) B
4) C
5) B
6) D
7) B
8) A
9) D
10) D
11) C
12) C
13) A
14) B

15) A
16) A
17) A
18) B
19) A
20) B
21) C
22) C
23) D
24) D
25) B
26) D
27) A



28)

29) B
30) B

2.3 Properties of Functions

1 Determine Even and Odd Functions from a Graph

1) A
2) A
3) C
4) C
5) B
6) B
7) B
8) A

2 Identify Even and Odd Functions from the Equation

1) B
2) A
3) A
4) C
5) B
6) C
7) A
8) A
9) B
10) B
11) B

3 Use a Graph to Determine Where a Function Is Increasing, Decreasing, or Constant

1) C
2) B
3) C

4) A
5) C
6) B
7) A
8) A
9) B
10) A
11) B
12) A
13) B
14) C
15) B
16) D

4 Use a Graph to Locate Local Maxima and Local Minima

1) C
2) C
3) C
4) C
5) A
6) A

5 Use a Graph to Locate the Absolute Maximum and the Absolute Minimum

1) A
2) B
3) A
4) C

6 Use Graphing Utility to Approximate Local Maxima/Minima and to Determine Where Function Is Incrs/Decrs

1) A
2) local maximum at (0, 6)
   local minimum at (2.67, −3.48)
   increasing on (−1, 0) and (2.67, 4)
   decreasing on (0, 2.67)
3) local maximum at (0, 0)
   local minimum at (0.74, −0.33)
   increasing on (−2, 0) and (0.74, 2)
   decreasing on (0, 0.74)
4) local maximum at (2.34, 1.61)
   local minimum at (−1.9, −9.82)
   increasing on (−1.9, 2.34)
   decreasing on (−4, −1.9) and (2.34, 5)
5) local maximum at (0, 5)
   local minima at (−2.55, 1.17) and (1.05, 4.65)
   increasing on (−2.55, 0) and (1.05, 2)
   decreasing on (−4, −2.55) and (0, 1.05)
6) C
7) D
8) B
9) B
10) A
11) B
12) C
13) C
14) C
15) D
16) A

7 Find the Average Rate of Change of a Function

1) B
2) C
3) D
4) D
5) A
6) C
7) C
8) D
9) B
10) D
11) C
12) A
13) C
14) B
15) D
16) B
17) C
18) C
19) C
20) B

2.4 Library of Functions; Piecewise–defined Functions

1 Graph the Functions Listed in the Library of Functions

1) D
2) D
3) A
4) B
5) D
6) C
7) C
8) C
9) D
10) C
11) B
12) D
13) B
14) A
15) A
16) C

2 Graph Piecewise–defined Functions

1) C
2) D
3) D
4) C
5) D
6) A
7) B
8) C
9) A
10) B
11) C
12) C
13) D
14) C

15) D
16) A
17) $25.52
$42.69
$C(x) = \begin{cases} 8.8 + 0.6686x & \text{if } 0 \le x \le 25 \\ 4.0475 + 0.8587x & \text{if } x > 25 \end{cases}$
18) $39.70
$49.69
$C(x) = \begin{cases} 4.93 + 0.11589x & \text{if } 0 \le x \le 300 \\ -0.266 + 0.13321x & \text{if } x > 300 \end{cases}$
19) $18.00
$24.25
$65.50
20) 6.0°C
21) $27.50
$32.50;
$C(x) = \begin{cases} 20 & \text{if } 0 \le x \le 100 \\ 12.5 + 0.075x & \text{if } 100 < x \le 200 \\ 7.5 + 0.1x & \text{if } x > 200 \end{cases}$

2.5 Graphing Techniques: Transformations

1 Graph Functions Using Vertical and Horizontal Shifts

1) B
2) B
3) D
4) C
5) B
6) A
7) A
8) C
9) B
10) C
11) D
12) B
13) B
14) C
15) A
16) D
17) B
18) A
19) A
20) A
21) C
22) C
23) D
24) D
25) A
26) D
27) B
28) A
29) D
30) A
31) A
32) B
33) D

34) B
35) B
36) A

2 Graph Functions Using Compressions and Stretches

1) D
2) B
3) D
4) A
5) B
6) C
7) A
8) C
9) A
10) C
11) D
12) B
13) C
14) C
15) B
16) A
17) A
18) D

3 Graph Functions Using Reflections about the x–Axis and the y–Axis

1) C
2) A
3) D
4) A
5) B
6) B
7) C
8) A
9) A
10) A
11) B
12) D
13) D
14) B
15) B
16) A
17) A
18) A
19) B

2.6 Mathematical Models: Building Functions

1 Build and Analyze Functions

1) B
2) A
3) B
4) D
5) A
6) C
7) A
8) $A(x) = \frac{1}{2}x^3$
9) D

10) $A(x) = \frac{4\sqrt{3}+9}{16}x^2 - \frac{15}{2}x + 25;\ \{x \mid 0 \le x \le \frac{20}{3}\}$

11) B

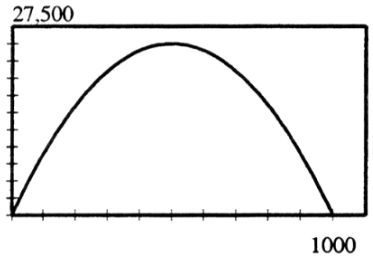
12) $V(s) = \frac{1}{6}s^3$

13) A
14) C
15) C
16) D
17) A
18) C

19) a. $R(x) = -\frac{1}{10}x^2 + 100x$

b. R(450) = $24,750.00

c.



d. 500; $25,000.00

e. $50.00

20) $d(t) = \sqrt{1709t}$

21) C