

TEST BANK



Blitzer
PRECALCULUS^{4e}



Ch. 2 Polynomial and Rational Functions

2.1 Complex Numbers

1 Add and Subtract Complex Numbers

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Add or subtract as indicated and write the result in standard form.

1) $(9 - 4i) + (6 + 9i)$

A) $15 + 5i$

B) $15 - 5i$

C) $3 + 13i$

D) $-15 - 5i$

2) $(4 + 5i) - (-8 + i)$

A) $12 + 4i$

B) $12 - 4i$

C) $-4 + 6i$

D) $-12 - 4i$

3) $9i + (-6 - i)$

A) $-6 + 8i$

B) $-6 + 10i$

C) $6 - 8i$

D) $6 - 10i$

4) $5i - (-5 - i)$

A) $5 + 6i$

B) $-5 - 6i$

C) $5 - 4i$

D) $-5 + 4i$

5) $(-5 + 8i) - 9$

A) $-14 + 8i$

B) $14 - 8i$

C) $4 + 8i$

D) $4 - 8i$

6) $3 - (-6 - 9i) - (-7 + 2i)$

A) $16 + 7i$

B) $16 - 7i$

C) $13 - 7i$

D) $13 + 7i$

7) $(-4 + 10i) + (-3 + 2i) + (-6 - 4i)$

A) $-13 + 8i$

B) $-7 + 4i$

C) $-1 + 16i$

D) $-7 + 12i$

2 Multiply Complex Numbers

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find the product and write the result in standard form.

1) $-9i(7i - 2)$

A) $63 + 18i$

B) $-63 + 18i$

C) $18i - 63i^2$

D) $18i + 63i^2$

2) $9i(-4i + 5)$

A) $36 + 45i$

B) $-36 + 45i$

C) $45i - 36i^2$

D) $45i + 36i^2$

3) $(7 + 2i)(4 - 6i)$

A) $40 - 34i$

B) $40 + 34i$

C) $16 + 50i$

D) $-12i^2 - 34i + 28$

4) $(-5 - 3i)(3 + i)$

A) $-12 - 14i$

B) $-18 - 14i$

C) $-12 + 4i$

D) $-18 + 4i$

5) $(4 - 7i)(-5 - 2i)$

A) $-34 + 27i$

B) $-34 - 43i$

C) $-6 + 27i$

D) $-6 - 43i$

6) $(6 + 3i)(6 - 3i)$

A) 45

B) $36 - 9i^2$

C) 27

D) $36 - 9i$

7) $(-7 + i)(-7 - i)$

A) 50

B) -7

C) 49

D) -48

8) $(6 + 9i)^2$

A) $-45 + 108i$

B) $117 + 108i$

C) -45

D) $36 + 108i + 81i^2$

Perform the indicated operations and write the result in standard form.

9) $(7 + 8i)(3 - i) - (2 - i)(2 + i)$

A) $24 + 17i$

B) $34 + 17i$

C) $26 + 17i$

D) $24 + 31i$

10) $(2 + i)^2 - (3 - i)^2$

A) $-5 + 10i$

B) $5 + 10i$

C) -15

D) $-5 - 10i$

Complex numbers are used in electronics to describe the current in an electric circuit. Ohm's law relates the current in a circuit, I , in amperes, the voltage of the circuit, E , in volts, and the resistance of the circuit, R , in ohms, by the formula $E = IR$. Solve the problem using this formula.

11) Find E , the voltage of a circuit, if $I = (3 + 9i)$ amperes and $R = (4 + 3i)$ ohms.

A) $(-15 + 45i)$ volts

B) $(-15 - 45i)$ volts

C) $(45 - 15i)$ volts

D) $(45 + 15i)$ volts

12) Find E , the voltage of a circuit, if $I = (18 + i)$ amperes and $R = (3 + 2i)$ ohms.

A) $(52 + 39i)$ volts

B) $(52 - 39i)$ volts

C) $(18 + 39i)$ volts

D) $(18 - 39i)$ volts

3 Divide Complex Numbers

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Divide and express the result in standard form.

1) $\frac{9}{4 - i}$

A) $\frac{36}{17} + \frac{9}{17}i$

B) $\frac{36}{17} - \frac{9}{17}i$

C) $\frac{12}{5} + \frac{3}{5}i$

D) $\frac{12}{5} - \frac{3}{5}i$

2) $\frac{5}{9 + i}$

A) $\frac{45}{82} - \frac{5}{82}i$

B) $\frac{45}{82} + \frac{5}{82}i$

C) $\frac{9}{16} + \frac{1}{16}i$

D) $\frac{9}{16} - \frac{1}{16}i$

3) $\frac{2i}{1 - i}$

A) $-1 + i$

B) $1 + i$

C) $-1 + 2i$

D) $-1 - i$

4) $\frac{5i}{3 - i}$

A) $-\frac{1}{2} + \frac{3}{2}i$

B) $\frac{1}{2} + \frac{3}{2}i$

C) $-\frac{5}{8} + \frac{15}{8}i$

D) $-\frac{1}{2} - \frac{3}{2}i$

5) $\frac{3i}{4 - 5i}$

A) $-\frac{15}{41} + \frac{12}{41}i$

B) $\frac{12}{41} - \frac{15}{41}i$

C) $\frac{5}{3} + \frac{4}{3}i$

D) $-\frac{4}{3} + \frac{5}{3}i$

6) $\frac{5 + 6i}{6 - 5i}$

A) i

B) $-i$

C) 1

D) -1

7) $\frac{7-3i}{8+6i}$

A) $\frac{19}{50} - \frac{33}{50}i$

B) $\frac{19}{28} - \frac{33}{28}i$

C) $\frac{37}{25} - \frac{9}{25}i$

D) $\frac{37}{14} - \frac{33}{28}i$

8) $\frac{6+3i}{7-5i}$

A) $\frac{27}{74} + \frac{51}{74}i$

B) $\frac{9}{8} + \frac{17}{8}i$

C) $\frac{57}{74} + \frac{9}{74}i$

D) $\frac{19}{8} + \frac{17}{8}i$

9) $\frac{2+3i}{5+2i}$

A) $\frac{16}{29} + \frac{11}{29}i$

B) $\frac{16}{21} + \frac{11}{21}i$

C) $\frac{4}{29} - \frac{19}{29}i$

D) $\frac{4}{21} + \frac{11}{21}i$

10) $\frac{2+6i}{8+6i}$

A) $\frac{13}{25} + \frac{9}{25}i$

B) $\frac{13}{28} + \frac{9}{28}i$

C) $-\frac{4}{5} - \frac{12}{5}i$

D) $-\frac{5}{7} + \frac{9}{28}i$

11) $\frac{9-9i}{5-8i}$

A) $\frac{117}{89} + \frac{27}{89}i$

B) $-3 - \frac{9}{13}i$

C) $-\frac{27}{89} + \frac{117}{89}i$

D) $\frac{9}{13} - \frac{9}{13}i$

4 Perform Operations with Square Roots of Negative Numbers

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Perform the indicated operations and write the result in standard form.

1) $\sqrt{-16} + \sqrt{-64}$

A) $12i$

B) $-12i$

C) $32i$

D) -12

2) $\sqrt{-3} - \sqrt{-169}$

A) $i(\sqrt{3} - 13)$

B) $\sqrt{3}i - 13$

C) $\sqrt{3}i - 13i$

D) $i(\sqrt{3} + 13)$

3) $3\sqrt{-36} + 4\sqrt{-81}$

A) $54i$

B) -54

C) 54

D) $-54i$

4) $3\sqrt{-8} + 5\sqrt{-18}$

A) $21i\sqrt{2}$

B) $-21\sqrt{2}$

C) $21\sqrt{2}$

D) $-21i\sqrt{2}$

5) $(-2 - \sqrt{-64})^2$

A) $-60 + 32i$

B) $68 + 32i$

C) $4 + 64i$

D) $4 - 64i$

6) $(-7 + \sqrt{-4})^2$

A) $45 - 28i$

B) $53 + 28i$

C) $49 + 4i$

D) $49 - 4i$

7) $(\sqrt{5} - \sqrt{-16})(\sqrt{5} + \sqrt{-16})$

A) 21

B) -11

C) $5 - 16i$

D) $5 + 4i$

8) $(4 + \sqrt{-7})(4 + \sqrt{-3})$

A) $(16 - \sqrt{21}) + (4\sqrt{3} + 4\sqrt{7})i$

C) $-5 - 8\sqrt{21}i$

B) $(16 + \sqrt{21}) - 37i$

D) $37 + 168i$

9) $\frac{-5 + \sqrt{-50}}{5}$

A) $-1 + i\sqrt{2}$

B) $-1 - i\sqrt{2}$

C) $1 + i\sqrt{2}$

D) $-1 + i\sqrt{5}$

10) $\frac{-6 - \sqrt{-28}}{2}$

A) $-3 - i\sqrt{7}$

B) $-3 + i\sqrt{7}$

C) $3 + i\sqrt{7}$

D) $-3 - i\sqrt{2}$

11) $\sqrt{-16}(3 - \sqrt{-16})$

A) $16 + 12i$

B) $12i - 16$

C) $12i - 16i^2$

D) $12i + 16i^2$

12) $(\sqrt{-64})(\sqrt{-9})$

A) -24

B) $24i^2$

C) 24

D) $-24i$

5 Solve Quadratic Equations with Complex Imaginary Solutions

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Solve the quadratic equation using the quadratic formula. Express the solution in standard form.

1) $x^2 + x + 2 = 0$

A) $\left\{-\frac{1}{2} \pm i\frac{\sqrt{7}}{2}\right\}$

B) $\left\{\frac{1}{2} \pm i\frac{\sqrt{7}}{2}\right\}$

C) $\left\{\frac{1}{2} \pm \frac{\sqrt{7}}{2}\right\}$

D) $\left\{-\frac{1}{2} \pm \frac{\sqrt{7}}{2}\right\}$

2) $x^2 - 10x + 61 = 0$

A) $\{5 \pm 6i\}$

B) $\{5 \pm 36i\}$

C) $\{5 + 6i\}$

D) $\{-1, 11\}$

3) $2x^2 - 5x + 6 = 0$

A) $\left\{\frac{5}{4} \pm i\frac{\sqrt{23}}{4}\right\}$

B) $\left\{\frac{5}{4} \pm \frac{\sqrt{23}}{4}\right\}$

C) $\left\{-\frac{5}{4} \pm i\frac{\sqrt{23}}{4}\right\}$

D) $\left\{-\frac{5}{4} \pm \frac{\sqrt{23}}{4}\right\}$

4) $16x^2 - 5x + 1 = 0$

A) $\left\{\frac{5}{32} \pm i\frac{\sqrt{39}}{32}\right\}$

B) $\left\{-\frac{5}{32} \pm i\frac{\sqrt{39}}{32}\right\}$

C) $\left\{-\frac{5}{32} \pm \frac{\sqrt{39}}{32}\right\}$

D) $\left\{\frac{5}{32} \pm \frac{\sqrt{39}}{32}\right\}$

5) $5x^2 = -3x - 8$

A) $\left\{-\frac{3}{10} \pm i\frac{\sqrt{151}}{10}\right\}$

B) $\left\{-\frac{3}{10} \pm \frac{\sqrt{151}}{10}\right\}$

C) $\left\{\frac{3}{10} \pm i\frac{\sqrt{151}}{10}\right\}$

D) $\left\{\frac{3}{10} \pm \frac{\sqrt{151}}{10}\right\}$

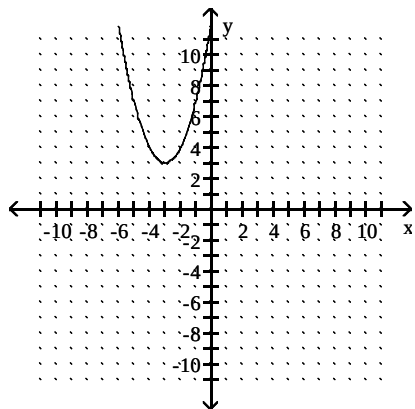
2.2 Quadratic Functions

1 Recognize Characteristics of Parabolas

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

The graph of a quadratic function is given. Determine the function's equation.

1)



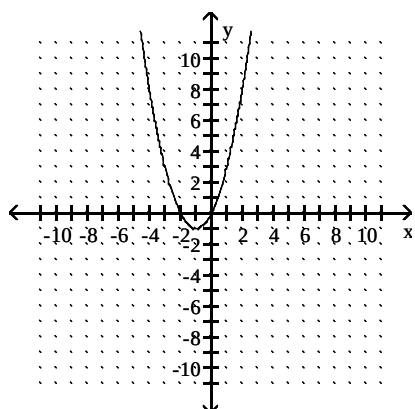
A) $f(x) = (x + 3)^2 + 3$

B) $g(x) = (x + 3)^2 - 3$

C) $h(x) = (x - 3)^2 + 3$

D) $j(x) = (x - 3)^2 - 3$

2)



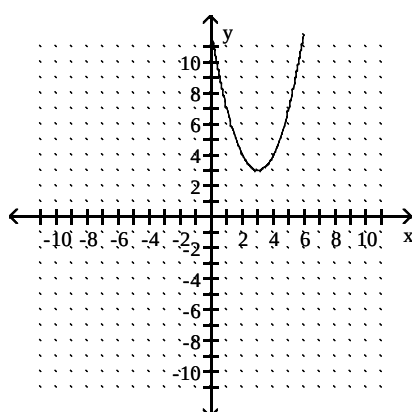
A) $g(x) = (x + 1)^2 - 1$

B) $f(x) = (x + 1)^2 + 1$

C) $h(x) = (x - 1)^2 + 1$

D) $j(x) = (x - 1)^2 - 1$

3)



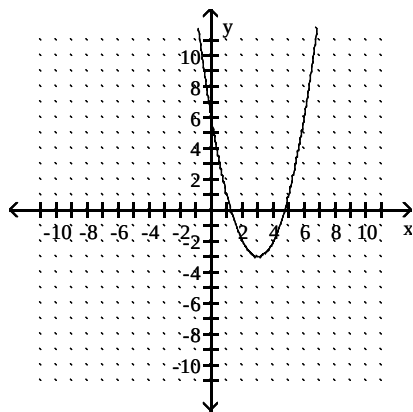
A) $h(x) = (x - 3)^2 + 3$

B) $g(x) = (x + 3)^2 - 3$

C) $f(x) = (x + 3)^2 + 3$

D) $j(x) = (x - 3)^2 - 3$

4)



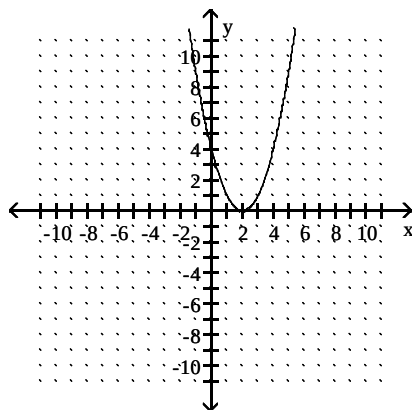
A) $j(x) = (x - 3)^2 - 3$

B) $g(x) = (x + 3)^2 - 3$

C) $h(x) = (x - 3)^2 + 3$

D) $f(x) = (x + 3)^2 + 3$

5)



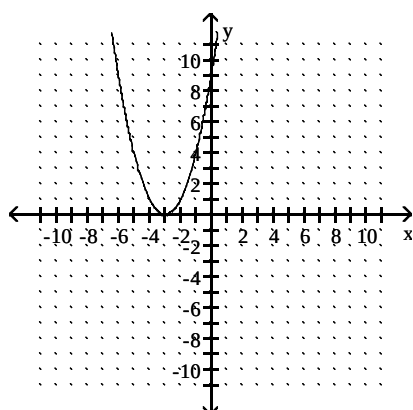
A) $f(x) = x^2 - 4x + 4$

B) $g(x) = x^2 + 4x + 4$

C) $h(x) = x^2 - 2$

D) $j(x) = x^2 + 2$

6)



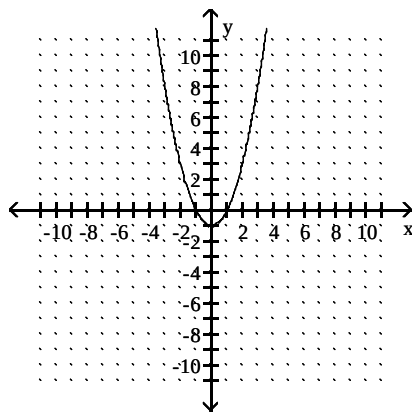
A) $g(x) = x^2 + 6x + 9$

B) $f(x) = x^2 - 6x + 9$

C) $h(x) = x^2 - 3$

D) $j(x) = x^2 + 3$

7)



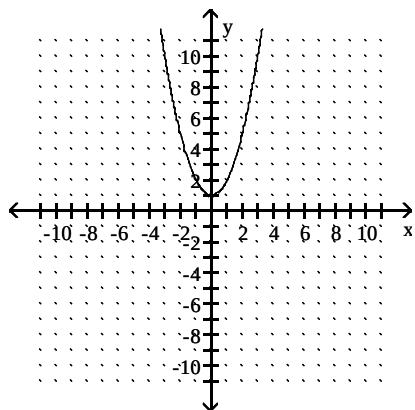
A) $h(x) = x^2 - 1$

B) $g(x) = x^2 + 2x + 1$

C) $f(x) = x^2 - 2x + 1$

D) $j(x) = x^2 + 1$

8)



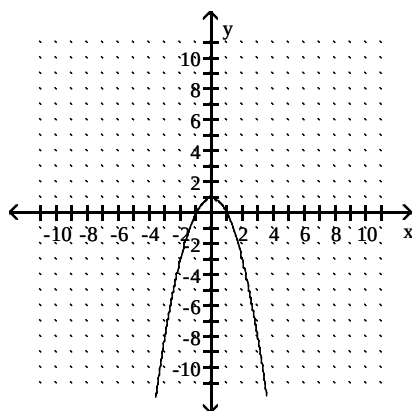
A) $j(x) = x^2 + 1$

B) $g(x) = x^2 + 2x + 1$

C) $h(x) = x^2 - 1$

D) $f(x) = x^2 - 2x + 1$

9)



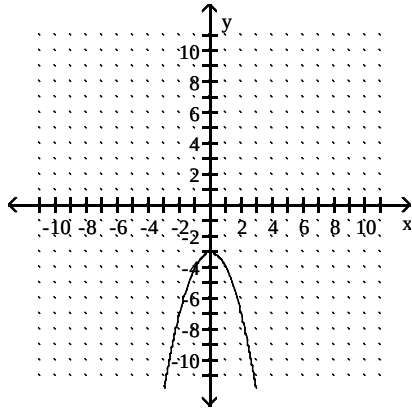
A) $j(x) = -x^2 + 1$

B) $g(x) = -x^2 + 2x + 1$

C) $h(x) = -x^2 - 1$

D) $f(x) = -x^2 - 2x - 1$

10)



A) $h(x) = -x^2 - 3$

B) $g(x) = -x^2 + 6x + 9$

C) $j(x) = -x^2 + 3$

D) $f(x) = -x^2 - 6x - 9$

Find the coordinates of the vertex for the parabola defined by the given quadratic function.

11) $f(x) = (x - 2)^2 - 2$

A) (2, -2)

B) (2, 2)

C) (0, -2)

D) (-2, 0)

12) $f(x) = x^2 + 4$

A) (0, 4)

B) (-4, 0)

C) (0, -4)

D) (4, 0)

13) $f(x) = (x + 3)^2 + 8$

A) (-3, 8)

B) (-8, 3)

C) (8, -9)

D) (8, -3)

14) $f(x) = 7 - (x + 4)^2$

A) (-4, 7)

B) (4, 7)

C) (7, 4)

D) (7, -4)

15) $f(x) = (x + 3)^2 - 5$

A) (-3, -5)

B) (3, 5)

C) (3, -5)

D) (-3, 5)

16) $y + 9 = (x + 3)^2$

A) (-3, -9)

B) (3, -9)

C) (9, -3)

D) (9, 3)

17) $f(x) = 11(x - 4)^2 + 8$

A) (4, 8)

B) (11, 4)

C) (-4, 8)

D) (8, -4)

18) $f(x) = -7(x - 3)^2 - 9$

A) (3, -9)

B) (-9, 3)

C) (-3, -9)

D) (-7, -3)

19) $f(x) = x^2 - 2$

A) (0, -2)

B) (1, 0)

C) (0, 2)

D) (2, 0)

20) $f(x) = x^2 + 14x + 3$

A) (-7, -46)

B) (7, 150)

C) (14, 395)

D) (-7, -144)

21) $f(x) = -x^2 + 12x - 6$

A) (6, 30)

B) (-6, -114)

C) (12, -6)

D) (-6, -42)

22) $f(x) = 8 - x^2 + 2x$

A) (1, 9)

B) (-1, 9)

C) (1, -9)

D) (-1, -9)

23) $f(x) = 2x^2 - 4x - 9$

A) $(1, -11)$

B) $(-1, -3)$

C) $(2, -5)$

D) $(-2, 7)$

Find the axis of symmetry of the parabola defined by the given quadratic function.

24) $f(x) = x^2 + 5$

A) $x = 0$

B) $x = 5$

C) $x = -5$

D) $y = 5$

25) $f(x) = (x + 4)^2 + 5$

A) $x = -4$

B) $x = 4$

C) $y = 5$

D) $y = -5$

26) $f(x) = 8 - (x + 3)^2$

A) $x = -3$

B) $x = 3$

C) $x = 8$

D) $x = -8$

27) $f(x) = (x + 2)^2 - 4$

A) $x = -2$

B) $x = 2$

C) $x = -4$

D) $x = 4$

28) $y + 9 = (x - 3)^2$

A) $x = 3$

B) $x = -3$

C) $y = 9$

D) $y = -9$

29) $f(x) = 11(x - 3)^2 + 7$

A) $x = 3$

B) $x = 11$

C) $x = -3$

D) $x = 7$

30) $f(x) = -7(x - 3)^2 - 8$

A) $x = 3$

B) $x = -8$

C) $x = -3$

D) $x = -7$

31) $f(x) = x^2 - 12x - 8$

A) $x = 6$

B) $x = -6$

C) $x = -12$

D) $x = -44$

32) $f(x) = -x^2 + 14x + 5$

A) $x = 7$

B) $x = -7$

C) $x = 14$

D) $x = 54$

33) $f(x) = -3x^2 + 6x - 6$

A) $x = 1$

B) $x = -1$

C) $x = 2$

D) $x = -3$

Find the range of the quadratic function.

34) $f(x) = x^2 + 2$

A) $[2, \infty)$

B) $(-\infty, 2]$

C) $[-2, \infty)$

D) $[0, \infty)$

35) $f(x) = (x + 4)^2 + 9$

A) $[9, \infty)$

B) $[-9, \infty)$

C) $[4, \infty)$

D) $[-4, \infty)$

36) $f(x) = 8 - (x + 2)^2$

A) $(-\infty, 8]$

B) $[8, \infty)$

C) $(-\infty, 2]$

D) $[-2, \infty)$

37) $f(x) = (x + 8)^2 - 7$

A) $[-7, \infty)$

B) $(-\infty, -8]$

C) $(-\infty, -7]$

D) $[-8, \infty)$

38) $y + 4 = (x - 2)^2$

A) $[-4, \infty)$

B) $(-\infty, -2]$

C) $[4, \infty)$

D) $(-\infty, 4]$

39) $f(x) = 11(x - 3)^2 + 6$

A) $[6, \infty)$

B) $[3, \infty)$

C) $(-\infty, 6]$

D) $[-6, \infty)$

40) $f(x) = -7(x - 3)^2 - 5$

A) $(-\infty, -5]$

B) $(-\infty, 3]$

C) $[-5, \infty)$

D) $[-3, \infty)$

41) $f(x) = x^2 - 10x + 3$

A) $[-22, \infty)$

B) $[-5, \infty)$

C) $(-\infty, -22]$

D) $(-\infty, -72]$

42) $f(x) = -x^2 - 6x + 2$

A) $(-\infty, 11]$

B) $[11, \infty)$

C) $[-3, \infty)$

D) $(-\infty, -3]$

43) $f(x) = 2x^2 + 3x - 9$

A) $[-\frac{81}{8}, \infty)$

B) $(-\infty, -\frac{81}{8}]$

C) $[-\frac{3}{4}, \infty)$

D) $(-\infty, -\frac{3}{4}]$

44) $f(x) = -3x^2 + 3x$

A) $(-\infty, \frac{3}{4}]$

B) $(-\infty, -\frac{3}{4}]$

C) $(-\infty, \frac{1}{2}]$

D) $(-\infty, -\frac{1}{2}]$

Find the x-intercepts (if any) for the graph of the quadratic function.

45) $f(x) = x^2 - 9$

A) $(-3, 0)$ and $(3, 0)$

B) $(-9, 0)$

C) $(3, 0)$

D) No x-intercepts

46) $f(x) = (x - 1)^2 - 1$

A) $(0, 0)$ and $(2, 0)$

B) $(0, 0)$ and $(-2, 0)$

C) $(0, 0)$ and $(-1, 0)$

D) $(-2, 0)$ and $(2, 0)$

47) $y + 9 = (x + 3)^2$

A) $(0, 0)$ and $(-6, 0)$

B) $(0, 0)$ and $(6, 0)$

C) $(6, 0)$ and $(-6, 0)$

D) $(0, 0)$

48) $f(x) = 10 + 7x + x^2$

A) $(-2, 0)$ and $(-5, 0)$

B) $(2, 0)$ and $(5, 0)$

C) $(2, 0)$ and $(-5, 0)$

D) $(-2, 0)$ and $(5, 0)$

49) $f(x) = x^2 + 18x + 70$ Give your answers in exact form.

A) $(-9 \pm \sqrt{11}, 0)$

B) $(9 \pm \sqrt{11}, 0)$

C) $(9 \pm \sqrt{70}, 0)$

D) $(-18 \pm \sqrt{70}, 0)$

50) $f(x) = -x^2 + 17x - 72$

A) $(8, 0)$ and $(9, 0)$

B) $(-8, 0)$ and $(-9, 0)$

C) $(8, 0)$ and $(-9, 0)$

D) No x-intercepts

51) $f(x) = 2x^2 + 15x + 7$

A) $(-7, 0)$ and $(-0.5, 0)$

B) $(-7, 0)$ and $(0.5, 0)$

C) $(-1, 0)$ and $(-3.5, 0)$

D) $(-1, 0)$ and $(3.5, 0)$

52) $f(x) = 2x^2 + 20x + 48$

A) $(-6, 0)$ and $(-4, 0)$

B) $(6, 0)$ and $(4, 0)$

C) $(-6, 0)$ and $(4, 0)$

D) $(6, 0)$ and $(-4, 0)$

53) $6x^2 + 12x + 5 = 0$

Give your answers in exact form.

A) $\left(\frac{-6 \pm \sqrt{6}}{6}, 0\right)$

B) $\left(\frac{-6 \pm \sqrt{6}}{12}, 0\right)$

C) $\left(\frac{-12 \pm \sqrt{6}}{6}, 0\right)$

D) $\left(\frac{-6 \pm \sqrt{66}}{6}, 0\right)$

Find the y-intercept for the graph of the quadratic function.

54) $f(x) = -x^2 - 2x + 8$

A) (0, 8)

B) (8, 0)

C) (0, -4)

D) (0, -8)

55) $y + 4 = (x + 2)^2$

A) (0, 0)

B) (0, 4)

C) (0, -4)

D) (4, 0)

56) $f(x) = 2 + 3x + x^2$

A) (0, 2)

B) (0, 1)

C) (0, -2)

D) (0, 3)

57) $f(x) = x^2 + 3x - 2$

A) (0, -2)

B) (0, 1)

C) (0, 2)

D) (0, 3)

58) $f(x) = (x - 3)^2 - 9$

A) (0, 0)

B) (0, -6)

C) (0, 9)

D) (0, -9)

59) $f(x) = 5x^2 - 3x - 8$

A) (0, -8)

B) (0, 8)

C) $\left(0, \frac{8}{5}\right)$

D) $\left(0, -\frac{8}{5}\right)$

Find the domain and range of the quadratic function whose graph is described.

60) The vertex is (1, 9) and the graph opens up.

A) Domain: $(-\infty, \infty)$
Range: $[9, \infty)$

B) Domain: $[1, \infty)$
Range: $[9, \infty)$

C) Domain: $(-\infty, \infty)$
Range: $(-\infty, 9]$

D) Domain: $(-\infty, \infty)$
Range: $[1, \infty)$

61) The vertex is (-1, 6) and the graph opens down.

A) Domain: $(-\infty, \infty)$
Range: $(-\infty, 6]$

B) Domain: $(-\infty, -1]$
Range: $(-\infty, 6]$

C) Domain: $(-\infty, \infty)$
Range: $[6, \infty)$

D) Domain: $(-\infty, \infty)$
Range: $(-\infty, -1]$

62) The minimum is -10 at $x = -1$.

A) Domain: $(-\infty, \infty)$
Range: $[-10, \infty)$

B) Domain: $[-1, \infty)$
Range: $[-10, \infty)$

C) Domain: $(-\infty, \infty)$
Range: $(-\infty, -10]$

D) Domain: $(-\infty, \infty)$
Range: $[-1, \infty)$

63) The maximum is -8 at $x = 1$

A) Domain: $(-\infty, \infty)$
Range: $(-\infty, -8]$

B) Domain: $(-\infty, 1]$
Range: $(-\infty, -8]$

C) Domain: $(-\infty, \infty)$
Range: $[-8, \infty)$

D) Domain: $(-\infty, \infty)$
Range: $(-\infty, 1]$

Solve the problem.

64) Write an equation in standard form of the parabola that has the same shape as the graph of $f(x) = 11x^2$, but which has its vertex at (3, 9).

A) $f(x) = 11(x - 3)^2 + 9$

B) $f(x) = 11(x + 3)^2 + 9$

C) $f(x) = (11x + 3)^2 + 9$

D) $f(x) = 11(x + 9)^2 + 3$

65) Write an equation in standard form of the parabola that has the same shape as the graph of $f(x) = 5x^2$, but which has a minimum of 6 at $x = 2$.

A) $f(x) = 5(x - 2)^2 + 6$

B) $f(x) = 5(x + 2)^2 + 6$

C) $f(x) = -5(x - 2)^2 + 6$

D) $f(x) = 5(x + 6)^2 - 2$

66) Write an equation in standard form of the parabola that has the same shape as the graph of $f(x) = -7x^2$, but which has a maximum of 5 at $x = 4$.

A) $f(x) = -7(x - 4)^2 + 5$

B) $f(x) = -7(x + 4)^2 + 5$

C) $f(x) = 7(x - 4)^2 + 5$

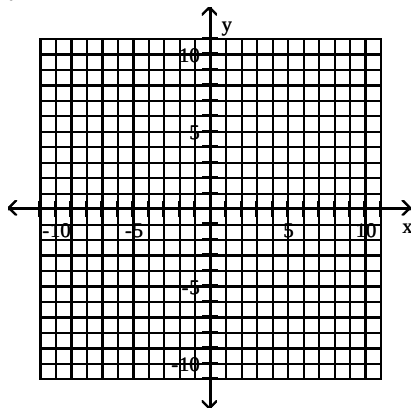
D) $f(x) = -7(x - 4)^2 - 5$

2 Graph Parabolas

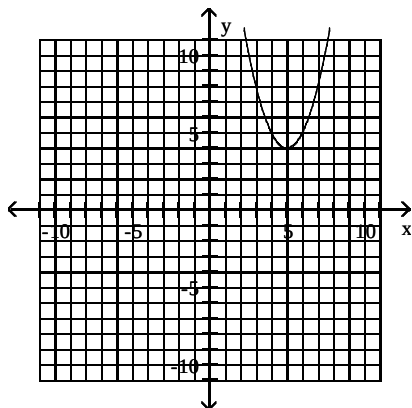
MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Use the vertex and intercepts to sketch the graph of the quadratic function.

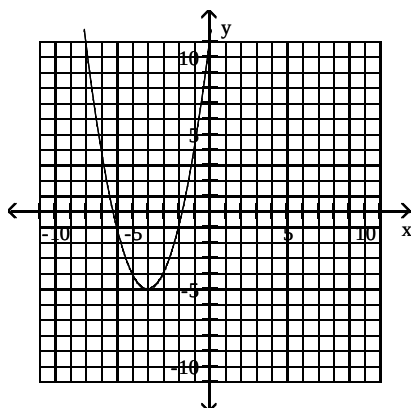
1) $y - 4 = (x - 5)^2$



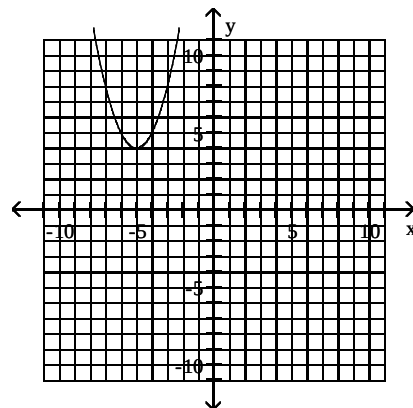
A)



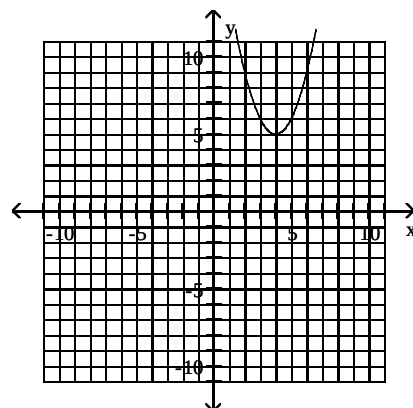
C)



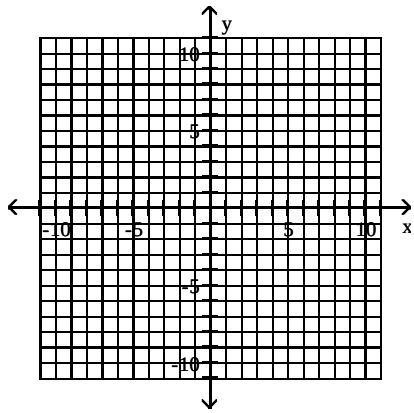
B)



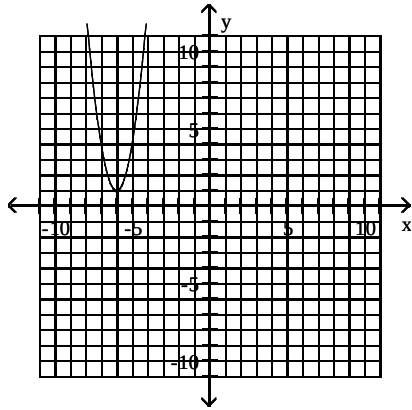
D)



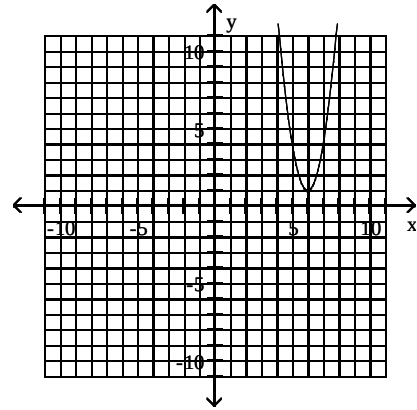
2) $f(x) = 3(x + 6)^2 + 1$



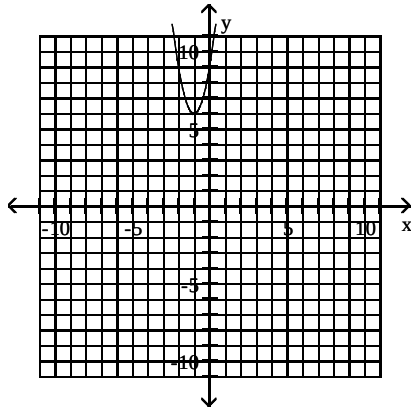
A)



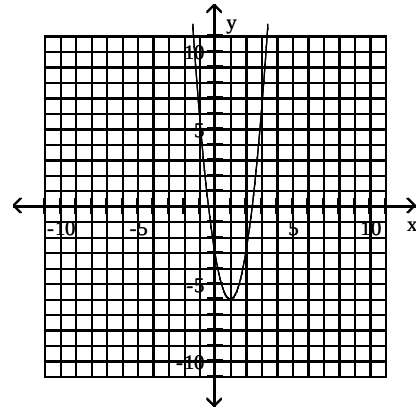
B)



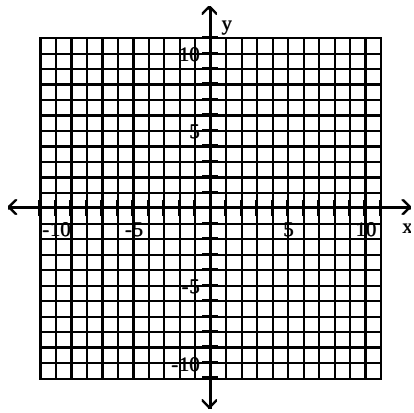
C)



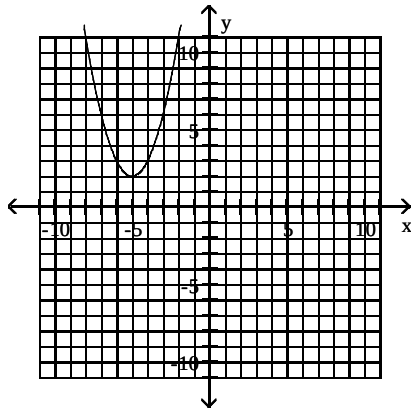
D)



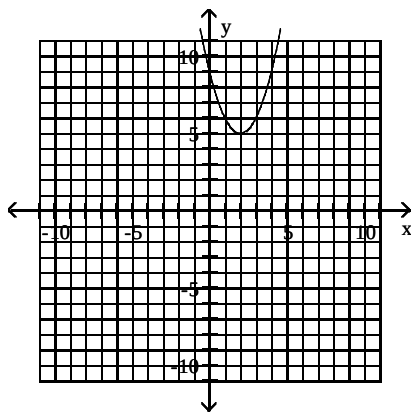
3) $f(x) = (x + 5)^2 + 2$



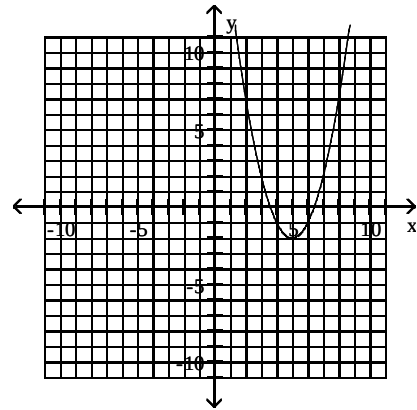
A)



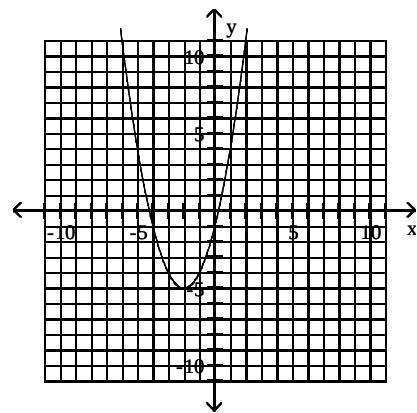
C)



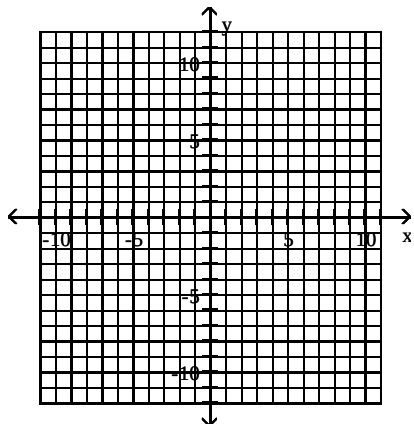
B)



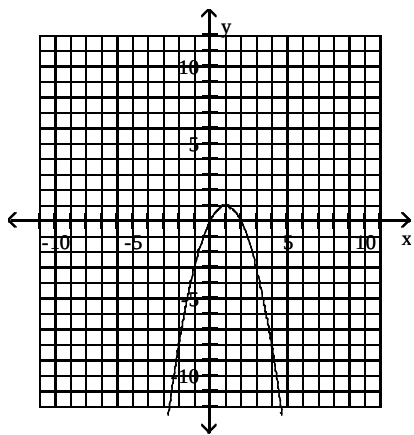
D)



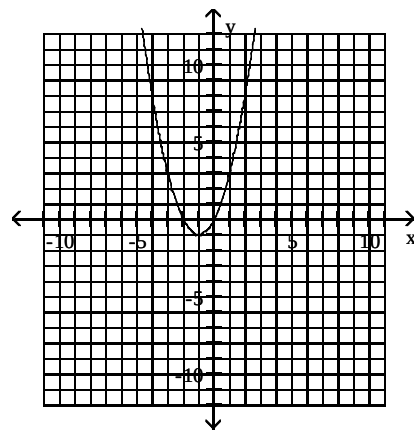
4) $f(x) = 1 - (x - 1)^2$



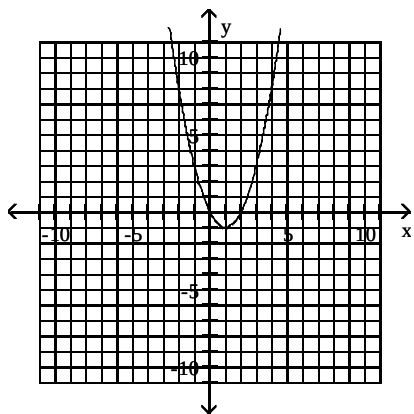
A)



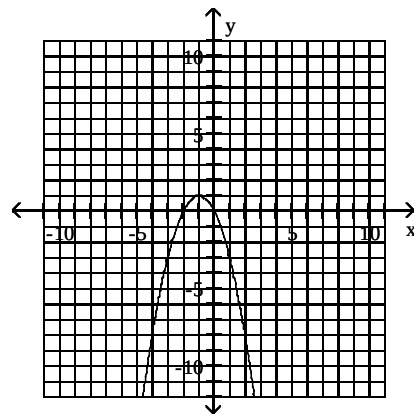
B)



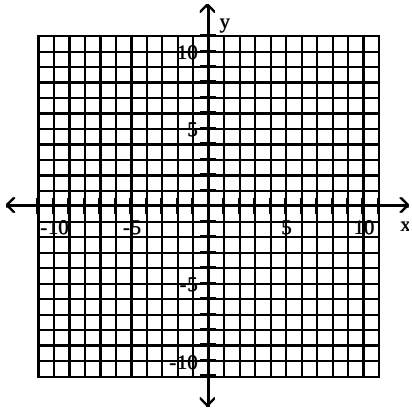
C)



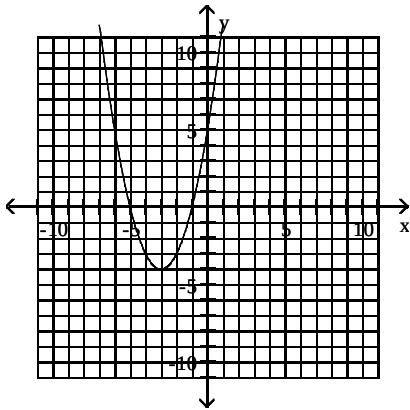
D)



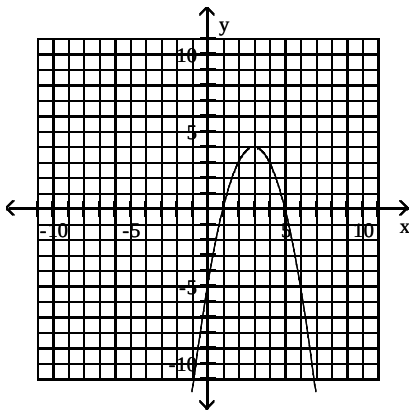
5) $f(x) = x^2 + 6x + 5$



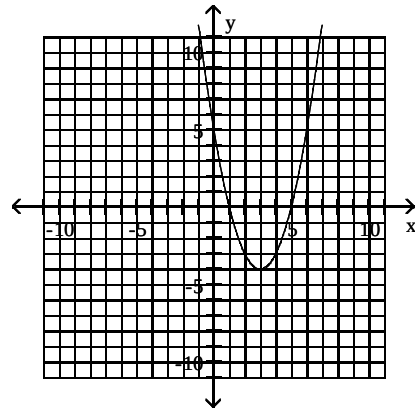
A)



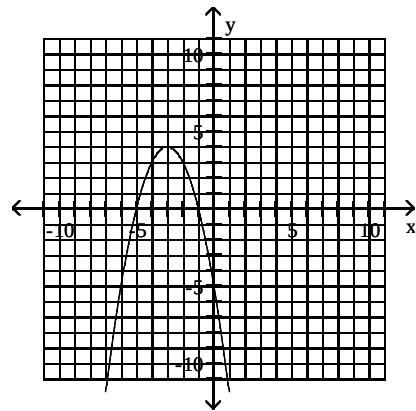
C)



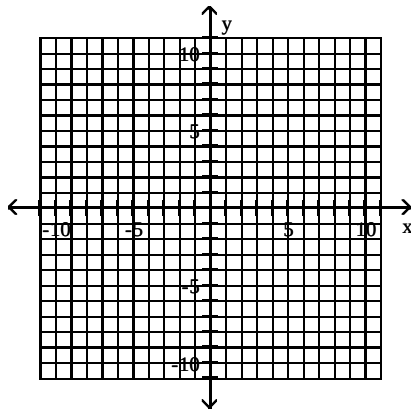
B)



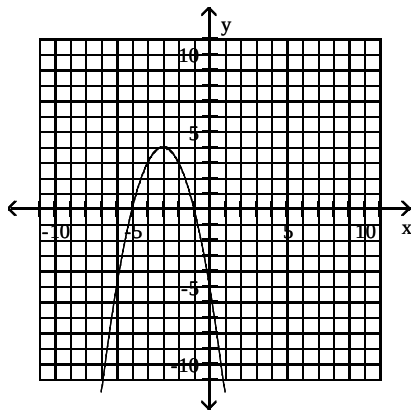
D)



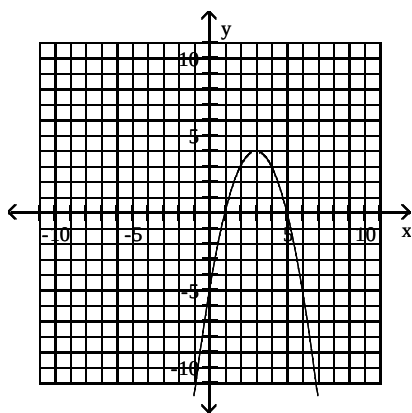
6) $f(x) = -x^2 - 6x - 5$



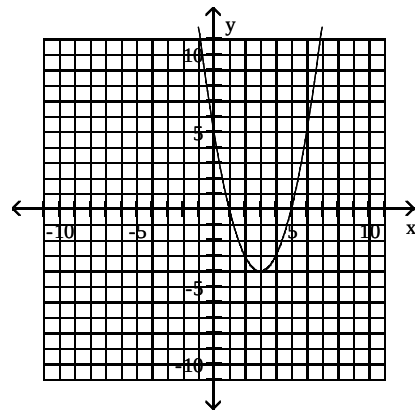
A)



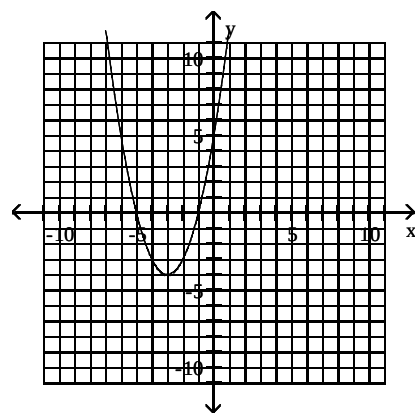
C)



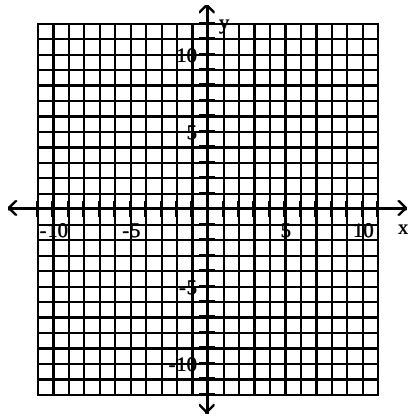
B)



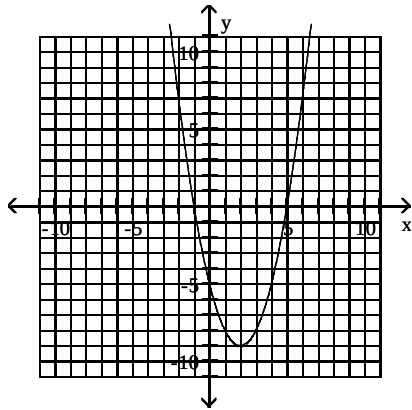
D)



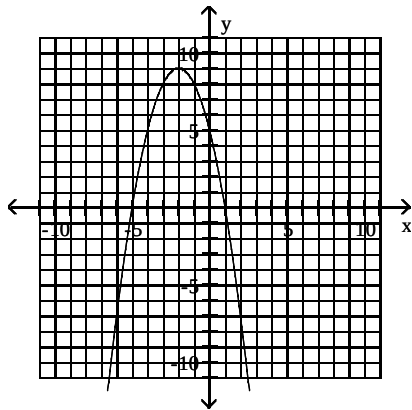
7) $f(x) = x^2 - 4x - 5$



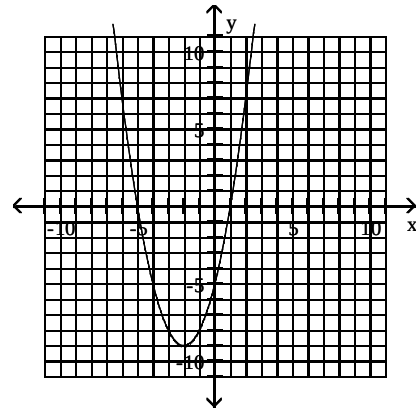
A)



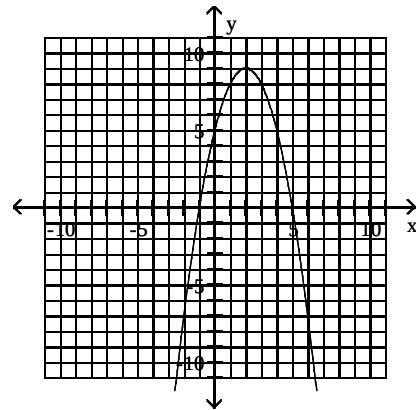
C)



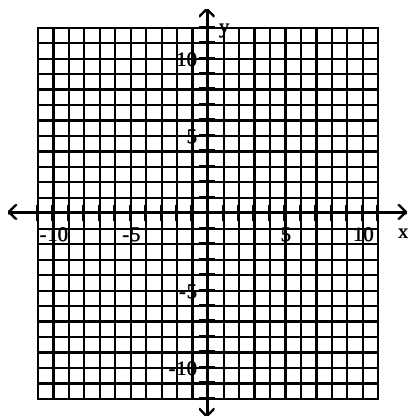
B)



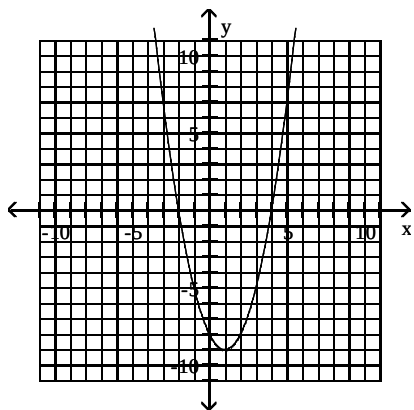
D)



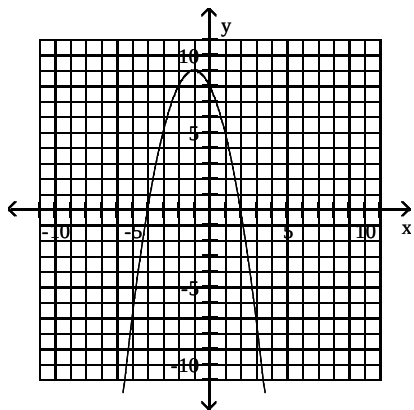
8) $f(x) = -2x - 8 + x^2$



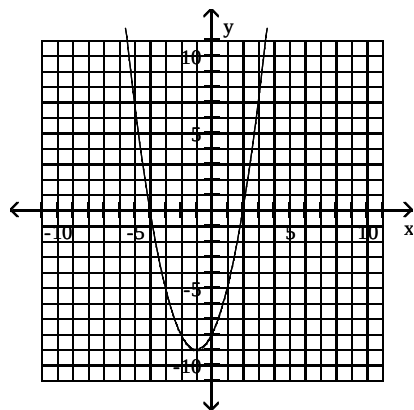
A)



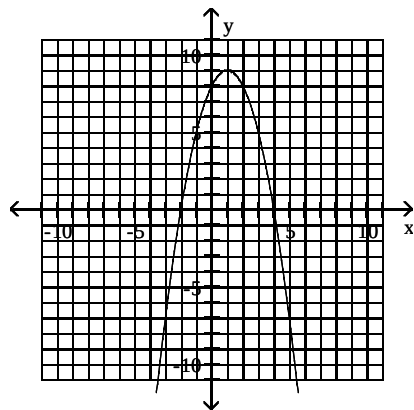
C)



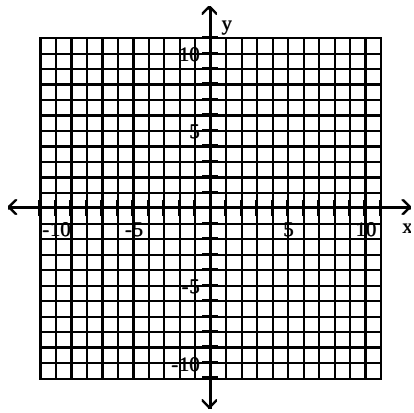
B)



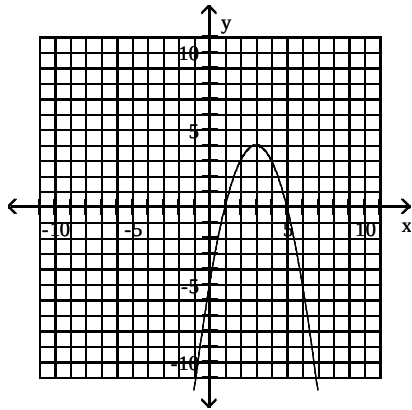
D)



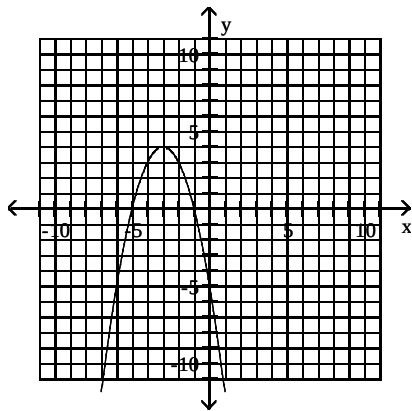
9) $f(x) = -x^2 + 6x - 5$



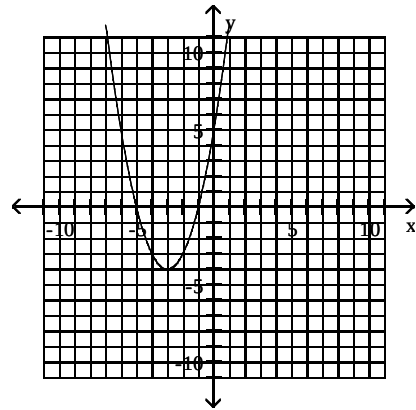
A)



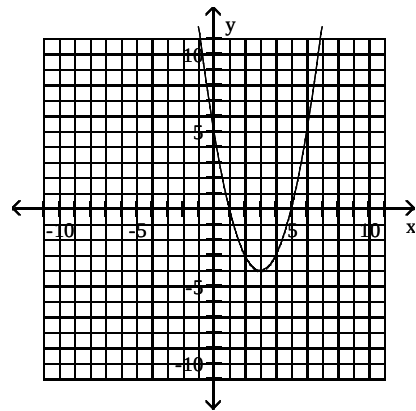
C)



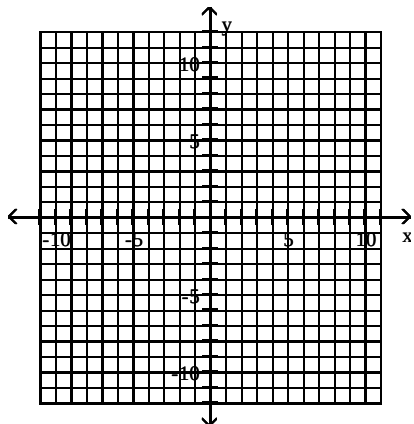
B)



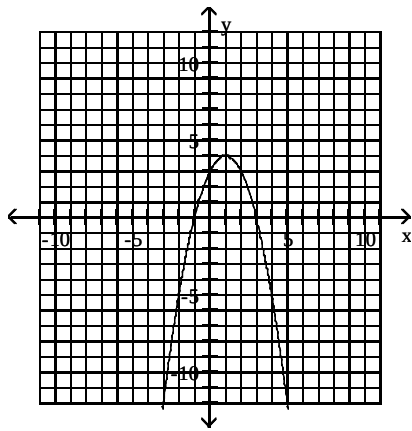
D)



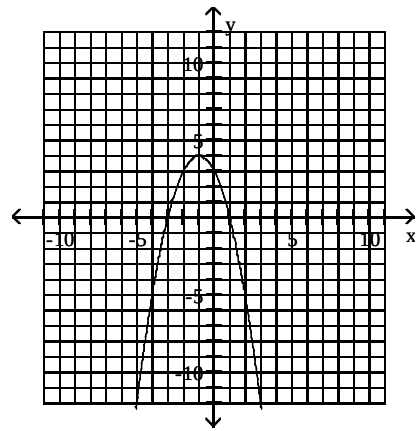
10) $f(x) = 3 - x^2 + 2x$



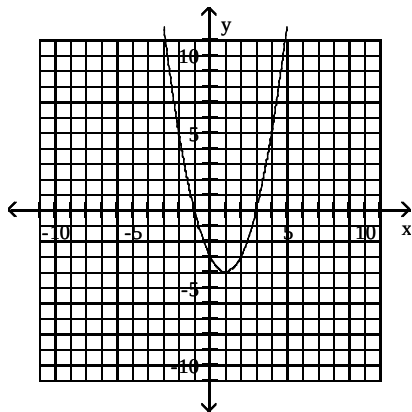
A)



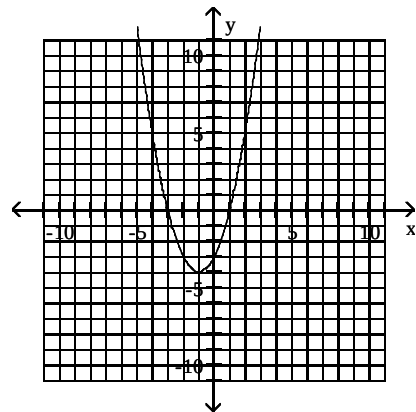
B)



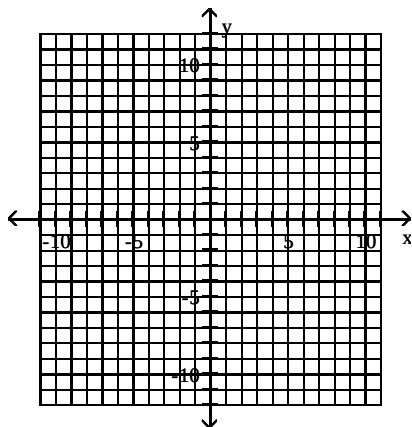
C)



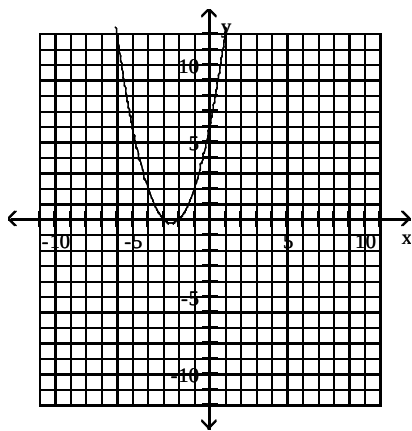
D)



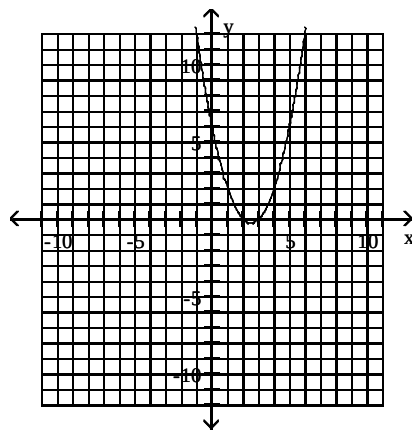
11) $f(x) = 6 + 5x + x^2$



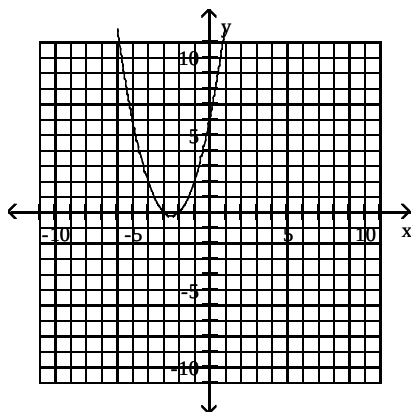
A)



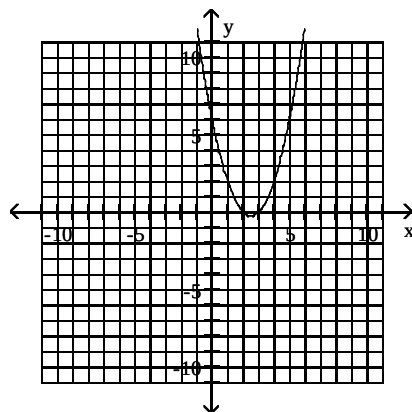
B)



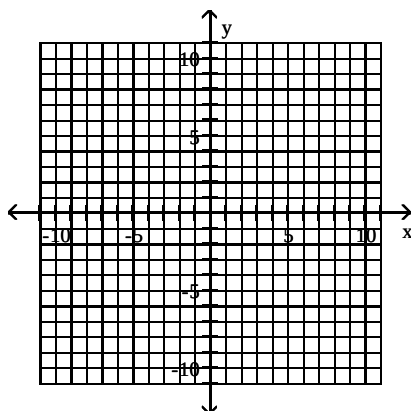
C)



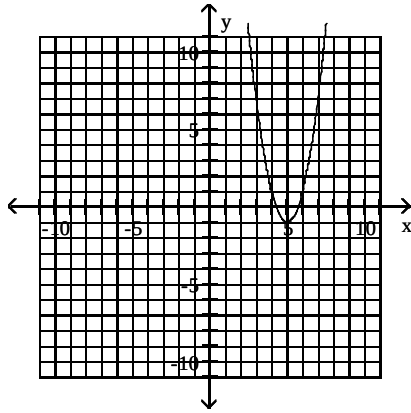
D)



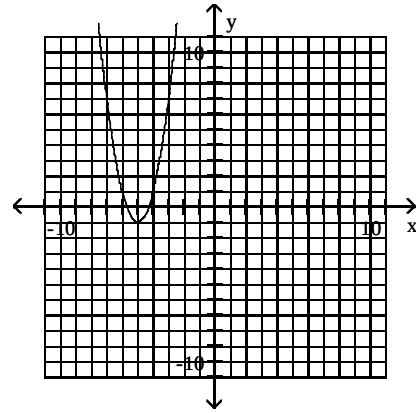
12) $f(x) = 2x^2 - 20x + 49$



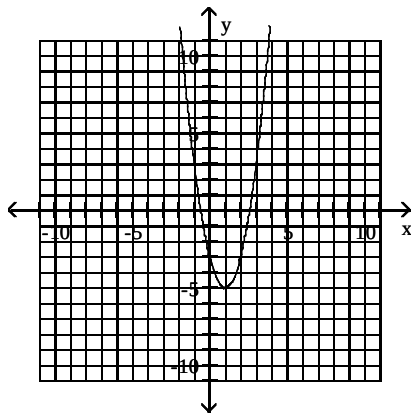
A)



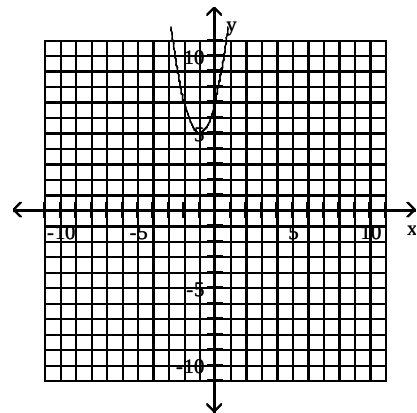
B)



C)



D)



3 Determine a Quadratic Function's Minimum or Maximum Value

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Determine whether the given quadratic function has a minimum value or maximum value. Then find the coordinates of the minimum or maximum point.

1) $f(x) = x^2 - 2x - 6$

- A) minimum; $(1, -7)$ B) maximum; $(1, -7)$ C) minimum; $(-7, 1)$ D) maximum; $(-7, 1)$

2) $f(x) = -x^2 - 2x + 1$

- A) maximum; $(-1, 2)$ B) minimum; $(-1, 2)$ C) minimum; $(2, -1)$ D) maximum; $(2, -1)$

3) $f(x) = 2x^2 + 2x + 1$

- A) minimum; $\left(-\frac{1}{2}, \frac{1}{2}\right)$ B) maximum; $\left(-\frac{1}{2}, \frac{1}{2}\right)$
 C) minimum; $\left(\frac{1}{2}, -\frac{1}{2}\right)$ D) maximum; $\left(\frac{1}{2}, -\frac{1}{2}\right)$

4) $f(x) = 3x^2 + 9x$

- A) minimum; $\left(-\frac{3}{2}, -\frac{27}{4}\right)$ B) maximum; $\left(-\frac{3}{2}, -\frac{27}{4}\right)$
 C) minimum; $\left(\frac{3}{2}, -\frac{27}{4}\right)$ D) maximum; $\left(\frac{3}{2}, -\frac{27}{4}\right)$

5) $f(x) = -5x^2 - 10x$

A) maximum; $(-1, 5)$

B) minimum; $(-1, 5)$

C) minimum; $(1, -5)$

D) maximum; $(1, -5)$

4 Solve Problems Involving a Quadratic Function's Minimum or Maximum Value

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Solve the problem.

- 1) You have 196 feet of fencing to enclose a rectangular region. Find the dimensions of the rectangle that maximize the enclosed area.

A) 49 ft by 49 ft

B) 98 ft by 98 ft

C) 98 ft by 24.5 ft

D) 51 ft by 47 ft

- 2) A developer wants to enclose a rectangular grassy lot that borders a city street for parking. If the developer has 272 feet of fencing and does not fence the side along the street, what is the largest area that can be enclosed?

A) 9248 ft²

B) 18,496 ft²

C) 4624 ft²

D) 13,872 ft²

- 3) You have 332 feet of fencing to enclose a rectangular region. What is the maximum area?

A) 6889 square feet

B) 27,556 square feet

C) 110,224 square feet

D) 6885 square feet

- 4) You have 104 feet of fencing to enclose a rectangular plot that borders on a river. If you do not fence the side along the river, find the length and width of the plot that will maximize the area.

A) length: 52 feet, width: 26 feet

B) length: 78 feet, width: 26 feet

C) length: 52 feet, width: 52 feet

D) length: 26 feet, width: 26 feet

- 5) A rain gutter is made from sheets of aluminum that are 18 inches wide by turning up the edges to form right angles. Determine the depth of the gutter that will maximize its cross-sectional area and allow the greatest amount of water to flow.

A) 4.5 inches

B) 4 inches

C) 5 inches

D) 5.5 inches

- 6) A rectangular playground is to be fenced off and divided in two by another fence parallel to one side of the playground. 288 feet of fencing is used. Find the dimensions of the playground that maximize the total enclosed area.

A) 48 ft by 72 ft

B) 72 ft by 72 ft

C) 24 ft by 108 ft

D) 36 ft by 72 ft

- 7) A rectangular playground is to be fenced off and divided in two by another fence parallel to one side of the playground. 840 feet of fencing is used. Find the maximum area of the playground.

A) 29,400 ft²

B) 44,100 ft²

C) 22,050 ft²

D) 33,075 ft²

- 8) The cost in millions of dollars for a company to manufacture x thousand automobiles is given by the function

$C(x) = 5x^2 - 40x + 144$. Find the number of automobiles that must be produced to minimize the cost.

A) 4 thousand automobiles

B) 8 thousand automobiles

C) 64 thousand automobiles

D) 20 thousand automobiles

- 9) In one U.S. city, the quadratic function $f(x) = 0.0040x^2 - 0.44x + 36.86$ models the median, or average, age, y , at which men were first married x years after 1900. In which year was this average age at a minimum? (Round to the nearest year.) What was the average age at first marriage for that year? (Round to the nearest tenth.)

A) 1955, 24.8 years old

B) 1955, 49 years old

C) 1936, 49 years old

D) 1953, 36 years old

- 10) The profit that the vendor makes per day by selling x pretzels is given by the function

$P(x) = -0.004x^2 + 2.8x - 300$. Find the number of pretzels that must be sold to maximize profit.

A) 350 pretzels

B) 700 pretzels

C) 1.4 pretzels

D) 190 pretzels

- 11) The manufacturer of a CD player has found that the revenue R (in dollars) is $R(p) = -4p^2 + 1550p$, when the unit price is p dollars. If the manufacturer sets the price p to maximize revenue, what is the maximum revenue to the nearest whole dollar?
- A) \$150,156 B) \$300,313 C) \$600,625 D) \$1,201,250
- 12) The owner of a video store has determined that the profits P of the store are approximately given by $P(x) = -x^2 + 90x + 68$, where x is the number of videos rented daily. Find the maximum profit to the nearest dollar.
- A) \$2093 B) \$2025 C) \$4118 D) \$4050
- 13) The owner of a video store has determined that the cost C , in dollars, of operating the store is approximately given by $C(x) = 2x^2 - 18x + 780$, where x is the number of videos rented daily. Find the lowest cost to the nearest dollar.
- A) \$740 B) \$618 C) \$699 D) \$821
- 14) The daily profit in dollars of a specialty cake shop is described by the function $P(x) = -5x^2 + 260x - 2400$, where x is the number of cakes prepared in one day. The maximum profit for the company occurs at the vertex of the parabola. How many cakes should be prepared per day in order to maximize profit?
- A) 26 cakes B) 3380 cakes C) 676 cakes D) 52 cakes
- 15) Among all pairs of numbers whose sum is 32, find a pair whose product is as large as possible.
- A) 16 and 16 B) 8 and 8 C) 18 and 14 D) 31 and 1
- 16) Among all pairs of numbers whose difference is 96, find a pair whose product is as small as possible.
- A) -48 and 48 B) 48 and 48 C) -144 and -48 D) 144 and 48
- 17) An arrow is fired into the air with an initial velocity of 160 feet per second. The height in feet of the arrow t seconds after it was shot into the air is given by the function $h(x) = -16t^2 + 160t$. Find the maximum height of the arrow.
- A) 400 ft B) 80 ft C) 1200 ft D) 720 ft
- 18) A person standing close to the edge on top of a 48-foot building throws a baseball vertically upward. The quadratic function $s(t) = -16t^2 + 64t + 48$ models the ball's height above the ground, $s(t)$, in feet, t seconds after it was thrown. After how many seconds does the ball reach its maximum height? Round to the nearest tenth of a second if necessary.
- A) 2 seconds B) 4.6 seconds C) 112 seconds D) 1.5 seconds
- 19) April shoots an arrow upward into the air at a speed of 64 feet per second from a platform that is 24 feet high. The height of the arrow is given by the function $h(t) = -16t^2 + 64t + 24$, where t is the time in seconds. What is the maximum height of the arrow?
- A) 88 ft B) 20 ft C) 64 ft D) 24 ft
- 20) An object is propelled vertically upward from the top of a 256-foot building. The quadratic function $s(t) = -16t^2 + 192t + 256$ models the ball's height above the ground, $s(t)$, in feet, t seconds after it was thrown. How many seconds does it take until the object finally hits the ground? Round to the nearest tenth of a second if necessary.
- A) 13.2 seconds B) 1.2 seconds C) 6 seconds D) 2 seconds

2.3 Polynomial Functions and Their Graphs

1 Identify Polynomial Functions

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Determine whether the function is a polynomial function.

1) $f(x) = 5x + 2x^5$

A) Yes

B) No

2) $f(x) = \frac{5 - x^2}{2}$

A) Yes

B) No

3) $f(x) = 7 - \frac{1}{x^3}$

A) No

B) Yes

4) $f(x) = \frac{x^5 - 6}{x^4}$

A) No

B) Yes

5) $f(x) = \sqrt[4]{x^5} - x^2 + 3$

A) No

B) Yes

6) $f(x) = 7x^9 + 4x + \frac{9}{x}$

A) No

B) Yes

7) $f(x) = \pi x^4 + 3x^3 + 7$

A) Yes

B) No

8) $f(x) = x^{5/4} - x^4 - 7$

A) No

B) Yes

9) $f(x) = 5x^7 - x^2 + \frac{5}{4}x$

A) Yes

B) No

10) $f(x) = 5x^3 + 2x^2 - 5x^{-4} + 32$

A) No

B) Yes

Find the degree of the polynomial function.

11) $f(x) = -5x + 4x^5$

A) 5

B) 1

C) -5

D) 4

12) $f(x) = \frac{7 - x^3}{9}$

A) 3

B) $-\frac{1}{9}$

C) 0

D) 7

13) $f(x) = \pi x^4 - 7x^3 - 1$

A) 4

B) 3

C) π

D) 1

14) $f(x) = 4x - x^2 + \frac{4}{3}$

A) 2

B) 1

C) 4

D) -1

15) $g(x) = 9x^3 + 9$

A) 3

B) 4

C) 0

D) 9

16) $h(x) = 13x + 4$

A) 1

B) 2

C) 0

D) 13

17) $-13x^4 - 6x^3 - 4x + 5y^5 + 4$

A) 5

B) 4

C) 13

D) -13

18) $f(x) = 7x^4 + 9x^3 - 4$

A) 4

B) 8

C) 9

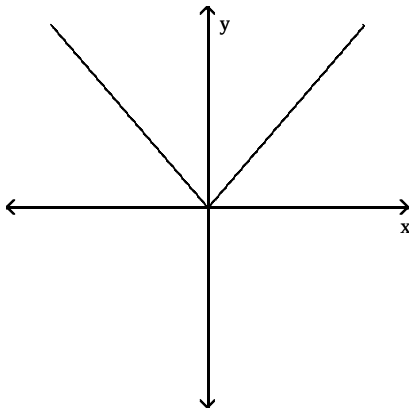
D) 7

2 Recognize Characteristics of Graphs of Polynomial Functions

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Determine whether the graph shown is the graph of a polynomial function.

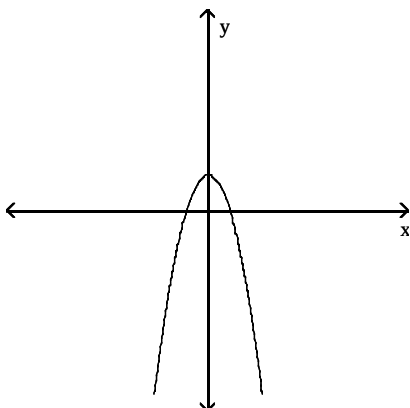
1)



A) not a polynomial function

B) polynomial function

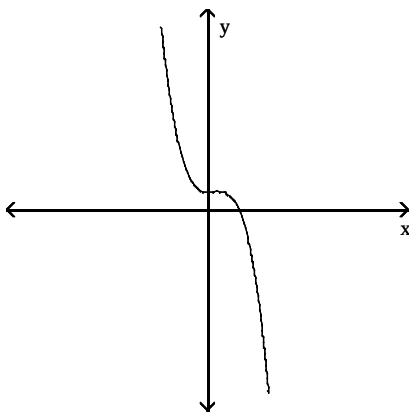
2)



A) polynomial function

B) not a polynomial function

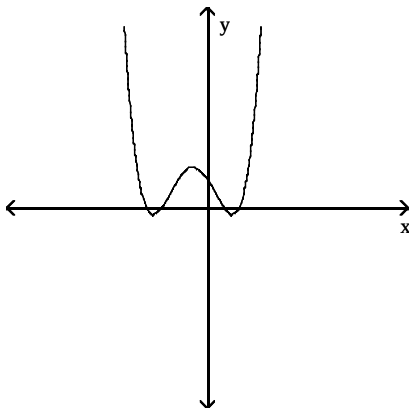
3)



A) polynomial function

B) not a polynomial function

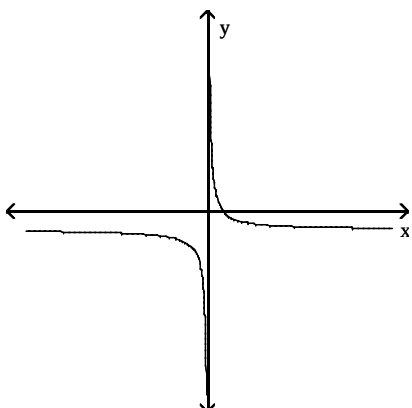
4)



A) polynomial function

B) not a polynomial function

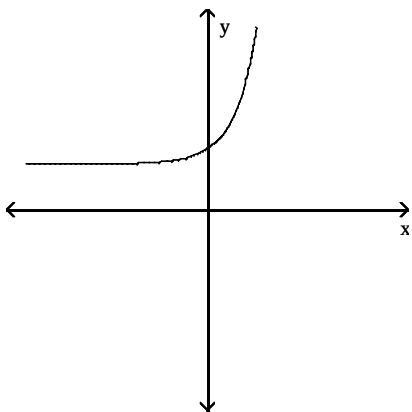
5)



A) not a polynomial function

B) polynomial function

6)



A) not a polynomial function

B) polynomial function

Find the x-intercepts of the polynomial function. State whether the graph crosses the x-axis, or touches the x-axis and turns around, at each intercept.

7) $f(x) = 7x^2 - x^3$

A) 0, touches the x-axis and turns around;
7, crosses the x-axis

B) 0, crosses the x-axis;
 $\sqrt{7}$, crosses the x-axis;
 $-\sqrt{7}$, crosses the x-axis

C) 0, touches the x-axis and turns around;
 $\sqrt{7}$, crosses the x-axis;
 $-\sqrt{7}$, crosses the x-axis

D) 0, touches the x-axis and turns around;
7, touches the x-axis and turns around

8) $f(x) = x^4 - 49x^2$

A) 0, touches the x-axis and turns around;
7, crosses the x-axis;
-7, crosses the x-axis
C) 0, touches the x-axis and turns around;
49, touches the x-axis and turns around

B) 0, crosses the x-axis;
7, crosses the x-axis;
-7, crosses the x-axis
D) 0, touches the x-axis and turns around;
49, crosses the x-axis

9) $x^5 - 19x^3 + 48x = 0$

A) 0, crosses the x-axis;
4, crosses the x-axis;
-4, crosses the x-axis;
 $\sqrt{3}$, crosses the x-axis;
 $-\sqrt{3}$, crosses the x-axis
C) 0, crosses the x-axis;
16, touches the x-axis and turns around;
3, touches the x-axis and turns around

B) 0, touches the x-axis and turns around;
4, crosses the x-axis;
-4, crosses the x-axis;
 $\sqrt{3}$, crosses the x-axis;
 $-\sqrt{3}$, crosses the x-axis
D) 0, touches the x-axis and turns around;
16, touches the x-axis and turns around;
3, touches the x-axis and turns around

10) $x^4 + 4x^3 - 96x^2 = 0$

A) 0, touches the x-axis and turns around;
-12, crosses the x-axis;
8, crosses the x-axis
C) 0, crosses the x-axis;
-12, crosses the x-axis;
8, crosses the x-axis

B) 0, touches the x-axis and turns around;
12, touches the x-axis and turns around;
-8, touches the x-axis and turns around
D) 0, touches the x-axis and turns around;
12, crosses the x-axis;
-8, crosses the x-axis

11) $f(x) = x^3 + 11x^2 + 40x + 48$

- A) -4, touches the x-axis and turns around;
-3, crosses the x-axis.
- C) 4, crosses the x-axis;
-4, crosses the x-axis;
-3, crosses the x-axis.

- B) -4, crosses the x-axis;
-3, touches the x-axis and turns around
- D) 4, crosses the x-axis;
-4, touches the x-axis and turns around;
-3, crosses the x-axis.

12) $f(x) = (x + 1)(x - 4)(x - 1)^2$

- A) -1, crosses the x-axis;
4, crosses the x-axis;
1, touches the x-axis and turns around
- C) 1, crosses the x-axis;
-4, crosses the x-axis;
-1, touches the x-axis and turns around

- B) -1, crosses the x-axis;
4, crosses the x-axis;
1, crosses the x-axis
- D) 1, crosses the x-axis;
-4, touches the x-axis and turns around;
-1, touches the x-axis and turns around

13) $f(x) = -x^2(x + 9)(x^2 - 1)$

- A) 0, touches the x-axis and turns around;
-9, crosses the x-axis;
-1, crosses the x-axis;
1, crosses the x-axis
- C) 0, touches the x-axis and turns around;
-9, crosses the x-axis;
1, touches the x-axis and turns around

- B) 0, crosses the x-axis;
-9, crosses the x-axis;
-1, crosses the x-axis;
1, crosses the x-axis
- D) 0, touches the x-axis and turns around;
9, crosses the x-axis;
-1, touches the x-axis and turns around;
1, touches the x-axis and turns around

14) $f(x) = -x^2(x + 5)(x^2 + 1)$

- A) 0, touches the x-axis and turns around;
-5, crosses the x-axis
- C) 0, touches the x-axis and turns around;
-5, crosses the x-axis;
-1, touches the x-axis and turns around

- B) 0, touches the x-axis and turns around;
5, crosses the x-axis

- D) 0, touches the x-axis and turns around;
-5, crosses the x-axis;
-1, crosses the x-axis;
1, crosses the x-axis;

15) $f(x) = x^2(x - 4)(x - 1)$

- A) 0, touches the x-axis and turns around;
4, crosses the x-axis;
1, crosses the x-axis
- C) 0, crosses the x-axis;
4, crosses the x-axis;
1, crosses the x-axis

- B) 0, touches the x-axis and turns around;
-4, crosses the x-axis;
-1, crosses the x-axis
- D) 0, crosses the x-axis;
4, touches the x-axis and turns around;
1, touches the x-axis and turns around

16) $f(x) = -x^3(x + 3)^2(x - 9)$

- A) 0, crosses the x-axis;
-3, touches the x-axis and turns around;
9, crosses the x-axis
- C) 0, touches the x-axis and turns around;
-3, touches the x-axis and turns around;
9, crosses the x-axis

- B) 0, crosses the x-axis;
3, touches the x-axis and turns around;
-9, crosses the x-axis
- D) 0, touches the x-axis and turns around;
3, crosses the x-axis;
9, crosses the x-axis

17) $f(x) = (x - 2)^2(x^2 - 9)$

- A) 2, touches the x-axis and turns around;
-3, crosses the x-axis;
3, crosses the x-axis
C) 2, touches the x-axis and turns around;
9, touches the x-axis and turns around

- B) 2, touches the x-axis and turns around;
-3, touches the x-axis and turns around;
3, touches the x-axis and turns around
D) -2, touches the x-axis and turns around;
9, crosses the x-axis

Find the y-intercept of the polynomial function.

18) $f(x) = 4x - x^3$

- A) 0 B) 4 C) -1 D) -4

19) $f(x) = -x^2 - 2x + 8$

- A) 8 B) -8 C) 0 D) -1

20) $f(x) = (x + 1)(x - 4)(x - 1)^2$

- A) -4 B) 4 C) 0 D) -1

21) $f(x) = -x^2(x + 5)(x^2 - 1)$

- A) 0 B) -1 C) -5 D) 5

22) $f(x) = -x^2(x + 6)(x^2 + 1)$

- A) 0 B) 1 C) 6 D) -6

23) $f(x) = x^2(x - 4)(x - 5)$

- A) 0 B) -20 C) 20 D) -4

24) $f(x) = -x^2(x + 4)(x - 7)$

- A) 0 B) -7 C) -28 D) 28

25) $f(x) = (x - 3)^2(x^2 - 16)$

- A) -144 B) 144 C) -48 D) 48

Determine whether the graph of the polynomial has y-axis symmetry, origin symmetry, or neither.

26) $f(x) = 9x^2 - x^3$

- A) y-axis symmetry B) origin symmetry C) neither

27) $f(x) = 6 - x^4$

- A) y-axis symmetry B) origin symmetry C) neither

28) $f(x) = x^4 - 16x^2$

- A) y-axis symmetry B) origin symmetry C) neither

29) $f(x) = x^3 - 2x$

- A) origin symmetry B) y-axis symmetry C) neither

30) $f(x) = x^3 + x^2 + 1$

- A) origin symmetry B) y-axis symmetry C) neither

31) $f(x) = x(3 - x^2)$

- A) origin symmetry B) y-axis symmetry C) neither

32) $x^5 - 19x^3 + 48x = 0$

A) origin symmetry

B) y-axis symmetry

C) neither

33) $f(x) = x^3 + 11x^2 + 40x + 48$

A) origin symmetry

B) y-axis symmetry

C) neither

34) $f(x) = (x + 1)(x - 4)(x - 1)^2$

A) y-axis symmetry

B) origin symmetry

C) neither

35) $f(x) = -x^2(x + 5)(x^2 - 1)$

A) origin symmetry

B) y-axis symmetry

C) neither

36) $f(x) = -x^3(x + 4)^2(x - 8)$

A) origin symmetry

B) y-axis symmetry

C) neither

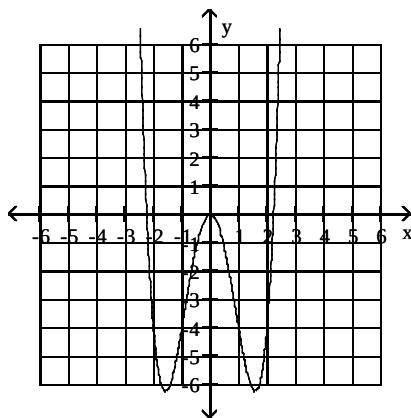
37) $f(x) = (x - 4)^2(x^2 - 25)$

A) origin symmetry

B) y-axis symmetry

C) neither

38)

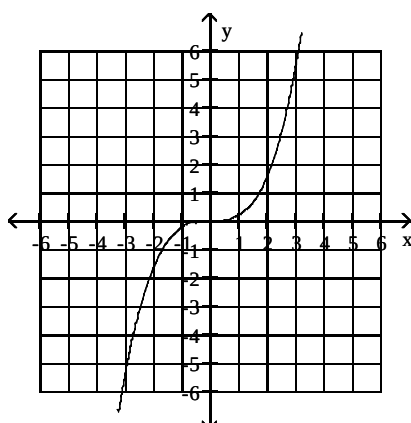


A) y-axis symmetry

B) origin symmetry

C) neither

39)

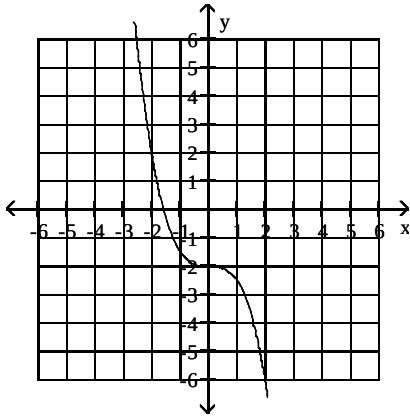


A) origin symmetry

B) y-axis symmetry

C) neither

40)

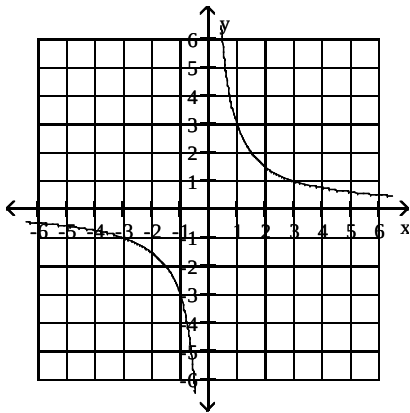


A) origin symmetry

B) y-axis symmetry

C) neither

41)



A) origin symmetry

B) y-axis symmetry

C) neither

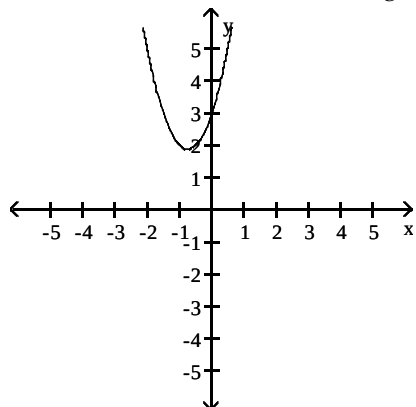
3 Determine End Behavior

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

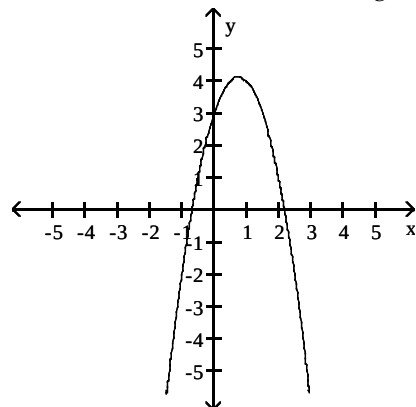
Use the Leading Coefficient Test to determine the end behavior of the polynomial function. Then use this end behavior to match the function with its graph.

1) $f(x) = 2x^2 + 3x + 3$

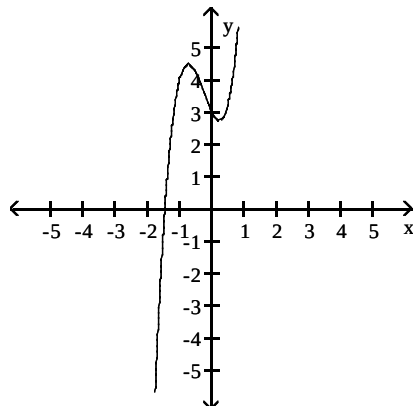
A) rises to the left and rises to the right



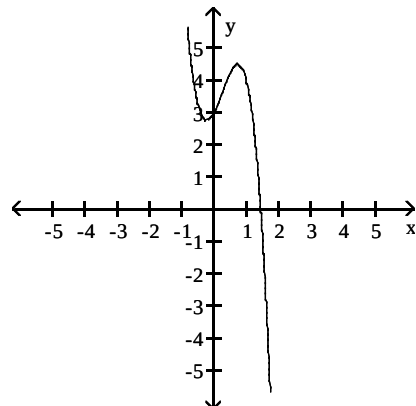
B) falls to the left and falls to the right



C) falls to the left and rises to the right

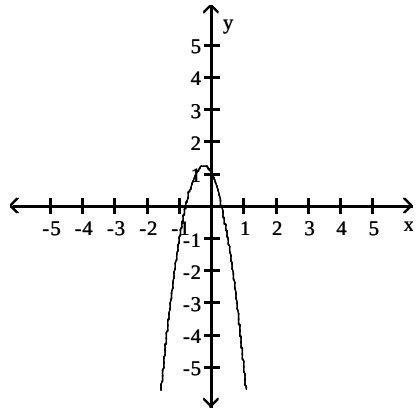


D) rises to the left and falls to the right

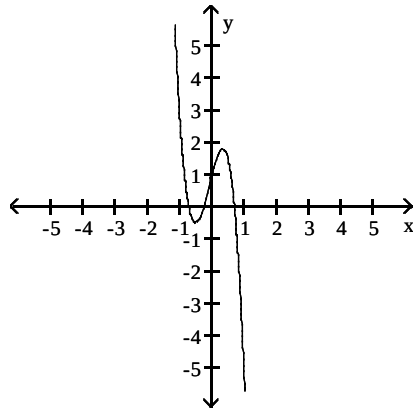


2) $f(x) = -4x^2 - 2x + 1$

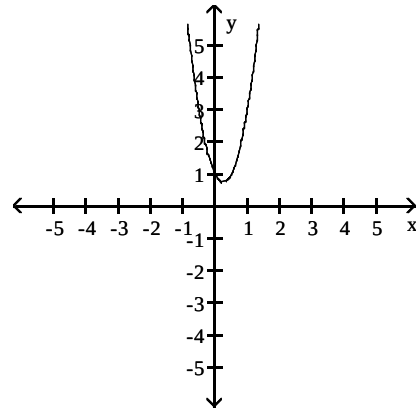
A) falls to the left and falls to the right



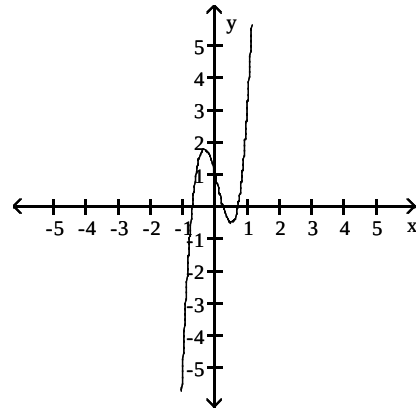
C) rises to the left and falls to the right



B) rises to the left and rises to the right

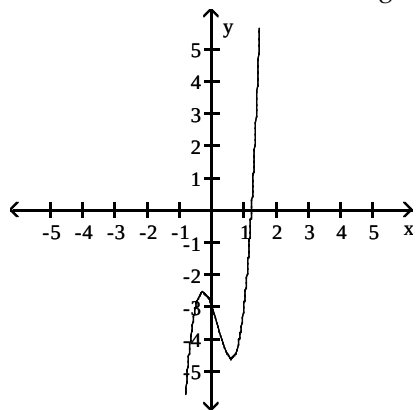


D) falls to the left and rises to the right

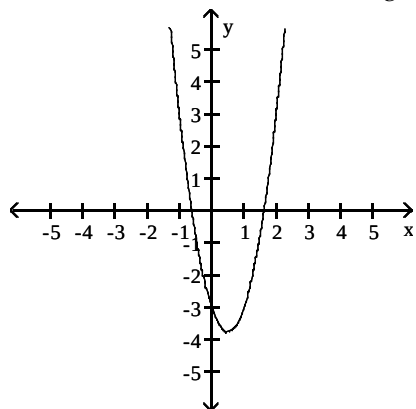


3) $f(x) = 6x^3 - 3x^2 - 3x - 3$

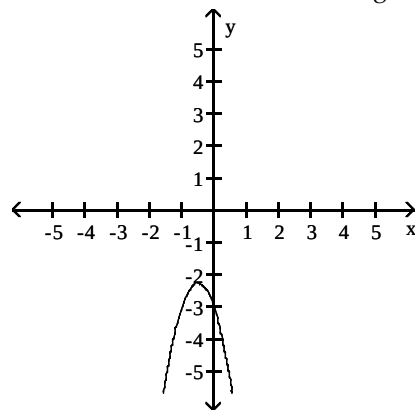
A) falls to the left and rises to the right



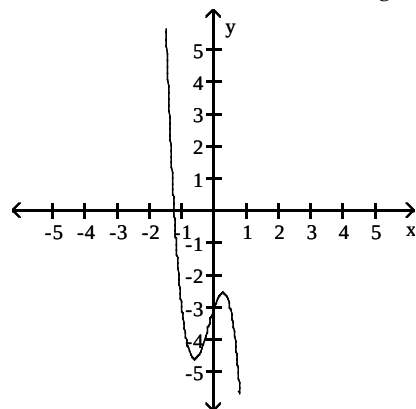
C) rises to the left and rises to the right



B) falls to the left and falls to the right

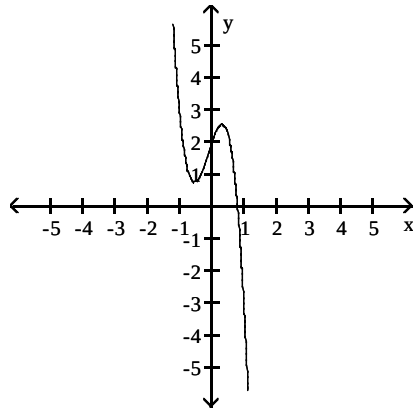


D) rises to the left and falls to the right

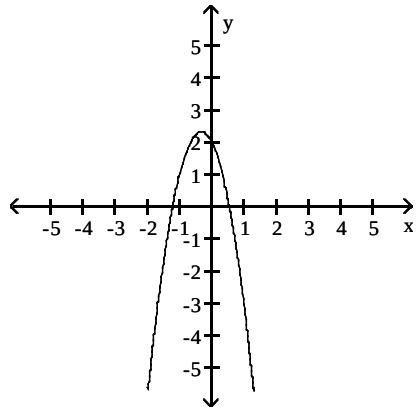


4) $f(x) = -6x^3 - 2x^2 + 3x + 2$

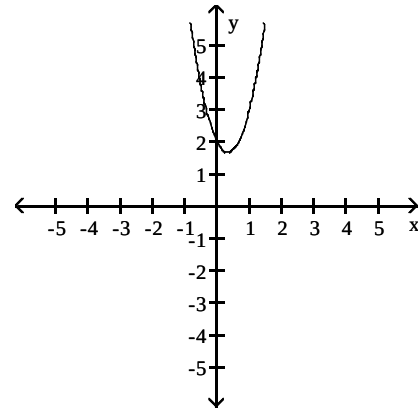
A) rises to the left and falls to the right



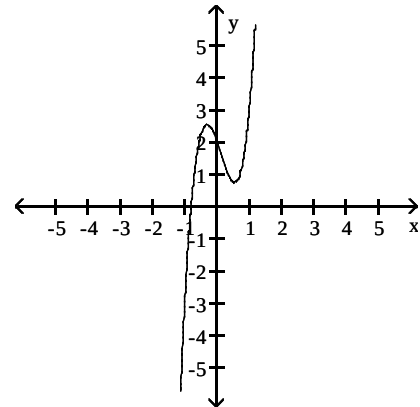
C) falls to the left and falls to the right



B) rises to the left and rises to the right

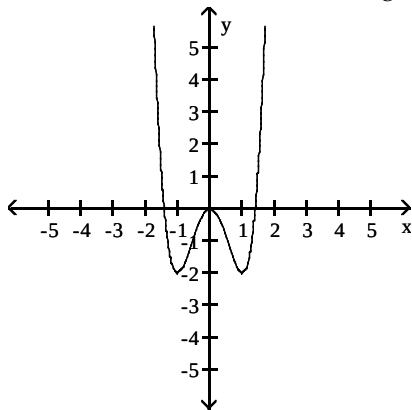


D) falls to the left and rises to the right

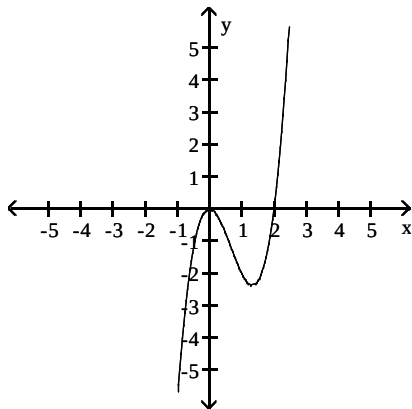


5) $f(x) = 2x^4 - 4x^2$

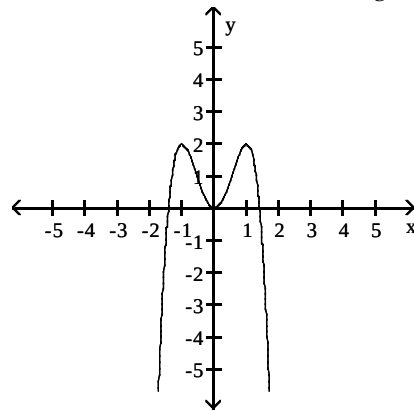
A) rises to the left and rises to the right



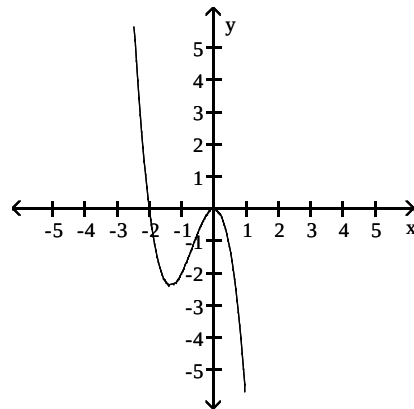
C) falls to the left and rises to the right



B) falls to the left and falls to the right



D) rises to the left and falls to the right



Use the Leading Coefficient Test to determine the end behavior of the polynomial function.

6) $f(x) = 5x^4 + 5x^3 + 3x^2 - 2x - 5$

A) rises to the left and rises to the right

C) falls to the left and rises to the right

B) rises to the left and falls to the right

D) falls to the left and falls to the right

7) $f(x) = -4x^4 + 3x^3 + 4x^2 + 3x + 5$

A) falls to the left and falls to the right

C) falls to the left and rises to the right

B) rises to the left and falls to the right

D) rises to the left and rises to the right

8) $f(x) = 5x^3 + 5x^2 + 3x + 3$

A) falls to the left and rises to the right

C) falls to the left and falls to the right

B) rises to the left and falls to the right

D) rises to the left and rises to the right

9) $f(x) = x^3 - 4x^2 + 4x - 5$

A) falls to the left and rises to the right

C) falls to the left and falls to the right

B) rises to the left and falls to the right

D) rises to the left and rises to the right

10) $f(x) = -3x^3 - 2x^2 + 3x - 3$

A) rises to the left and falls to the right

C) falls to the left and falls to the right

B) falls to the left and rises to the right

D) rises to the left and rises to the right

11) $f(x) = 5x^3 - 5x^2 - x^5$

A) rises to the left and falls to the right

C) falls to the left and falls to the right

B) falls to the left and rises to the right

D) rises to the left and rises to the right

- 12) $f(x) = x - 2x^2 - 2x^3$
 A) rises to the left and falls to the right
 C) falls to the left and falls to the right
 B) falls to the left and rises to the right
 D) rises to the left and rises to the right
- 13) $f(x) = (x - 5)(x - 4)(x - 3)^2$
 A) rises to the left and rises to the right
 C) rises to the left and falls to the right
 B) falls to the left and rises to the right
 D) falls to the left and falls to the right
- 14) $f(x) = (x + 2)(x + 3)(x + 5)^3$
 A) falls to the left and rises to the right
 C) rises to the left and falls to the right
 B) rises to the left and rises to the right
 D) falls to the left and falls to the right
- 15) $f(x) = -5(x^2 + 3)(x + 4)^2$
 A) falls to the left and falls to the right
 C) rises to the left and rises to the right
 B) falls to the left and rises to the right
 D) rises to the left and falls to the right
- 16) $f(x) = x^3(x - 2)(x + 2)^2$
 A) rises to the left and rises to the right
 C) rises to the left and falls to the right
 B) falls to the left and rises to the right
 D) falls to the left and falls to the right
- 17) $f(x) = -x^2(x - 1)(x + 2)$
 A) falls to the left and falls to the right
 C) rises to the left and falls to the right
 B) falls to the left and rises to the right
 D) rises to the left and rises to the right
- 18) $f(x) = -6x^3(x - 4)(x + 2)^2$
 A) falls to the left and falls to the right
 C) rises to the left and falls to the right
 B) falls to the left and rises to the right
 D) rises to the left and rises to the right

Solve the problem.

- 19) A herd of elk is introduced to a wildlife refuge. The number of elk, $N(t)$, after t years is described by the polynomial function $N(t) = -t^3 + 17t + 160$. Use the Leading Coefficient Test to determine the graph's end behavior. What does this mean about what will eventually happen to the elk population?
 A) The elk population in the refuge will die out.
 B) The elk population in the refuge will grow out of control.
 C) The elk population in the refuge will reach a constant amount greater than 0.
 D) The elk population in the refuge will be displaced by "oil" wells.
- 20) The following table shows the number of larceny thefts in a county for the years 1994–1998, where 1 represents 1994, 2 represents 1995, and so on.

Year, x	Larceny Thefts, T
1994, 1	3315.58
1995, 2	3384.96
1996, 3	3421.28
1997, 4	3457.48
1998, 5	3506.5

This data can be approximated using the third-degree polynomial

$$T(x) = -0.51x^3 + 0.53x^2 + 59.36x + 3256.2.$$

Use this function to predict the number of larceny thefts in 2005. Round to the nearest whole number.

- A) 3164 B) 3176 C) -89 D) 2451

- 21) The following table shows the number of fires in a county for the years 1994–1998, where 1 represents 1994, 2 represents 1995, and so on.

Year, x	Fires, T
1994, 1	3747.86
1995, 2	3795.8
1996, 3	3851.56
1997, 4	3891.48
1998, 5	3945.9

This data can be approximated using the third-degree polynomial

$$T(x) = -0.61x^3 + 0.57x^2 + 62.50x + 3685.4.$$

Use the Leading Coefficient Test to determine the end behavior to the right for the graph of T. Will this function be useful in modeling the number of fires over an extended period of time? Explain your answer.

- A) The graph of T decreases without bound to the right. This means that as x increases, the values of T will become more and more negative and the function will no longer model the number of fires.
- B) The graph of T increases without bound to the right. This means that as x increases, the values of T will become large and positive and, since the values of T will become so large, the function will no longer model the number of fires.
- C) The graph of T approaches zero for large values of x. This means that T will not be useful in modeling the number of fires over an extended period.
- D) The graph of T decreases without bound to the right. Since the number of larceny thefts will eventually decrease, the function T will be useful in modeling the number of fires over an extended period of time.

4 Use Factoring to Find Zeros of Polynomial Functions

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find the zeros of the polynomial function.

1) $f(x) = x^3 + x^2 - 42x$

A) $x = 0, x = -7, x = 6$

B) $x = -7, x = 6$

C) $x = 5, x = 6$

D) $x = 0, x = 5, x = 6$

2) $f(x) = x^3 + 2x^2 - x - 2$

A) $x = -1, x = 1, x = -2$

B) $x = 1, x = -2, x = 2$

C) $x = -2, x = 2$

D) $x = 4$

3) $f(x) = x^3 + 8x^2 + 16x$

A) $x = 0, x = -4$

B) $x = 0, x = 4$

C) $x = 1, x = -4$

D) $x = 0, x = 4, x = -4$

4) $f(x) = x^3 + 5x^2 - 4x - 20$

A) $x = -5, x = -2, x = 2$

B) $x = 5, x = -2, x = 2$

C) $x = -2, x = 2$

D) $x = -5, x = 4$

5) $f(x) = 4(x - 4)(x + 2)^4$

A) $x = 4, x = -2,$

B) $x = -4, x = 4$

C) $x = 4, x = 4$

D) $x = -4, x = 2, x = 4$

5 Identify Zeros and Their Multiplicities

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find the zeros for the polynomial function and give the multiplicity for each zero. State whether the graph crosses the x-axis or touches the x-axis and turns around, at each zero.

1) $f(x) = 5(x - 5)(x + 3)^2$

- A) 5, multiplicity 1, crosses x-axis; -3, multiplicity 2, touches x-axis and turns around
- B) -5, multiplicity 1, crosses x-axis; 3, multiplicity 2, touches x-axis and turns around
- C) 5, multiplicity 1, touches x-axis and turns around; -3, multiplicity 2, crosses x-axis
- D) -5, multiplicity 1, touches x-axis and turns around; 3, multiplicity 2, crosses x-axis

2) $f(x) = 3(x + 1)(x + 2)^3$

- A) -1, multiplicity 1, crosses x-axis; -2, multiplicity 3, crosses x-axis
- B) 1, multiplicity 1, crosses x-axis; 2, multiplicity 3, crosses x-axis
- C) -1, multiplicity 1, crosses x-axis; -2, multiplicity 3, touches x-axis and turns around
- D) 1, multiplicity 1, touches x-axis; 2, multiplicity 3, touches x-axis and turns around

3) $f(x) = -2(x + 2)(x + 4)^3$

- A) -2, multiplicity 1, crosses x-axis; -4, multiplicity 3, crosses x-axis
- B) 2, multiplicity 1, crosses x-axis; 4, multiplicity 3, crosses x-axis
- C) -2, multiplicity 1, touches the x-axis and turns around; -4, multiplicity 3, touches x-axis and turns around
- D) 2, multiplicity 1, touches the x-axis and turns around; 4, multiplicity 3, touches x-axis and turns around

4) $f(x) = 4(x^2 + 2)(x + 6)^2$

- A) -6, multiplicity 2, touches the x-axis and turns around
- B) -2, multiplicity 1, crosses the x-axis; -6, multiplicity 2, touches the x-axis and turns around.
- C) -2, multiplicity 1, crosses the x-axis; -6, multiplicity 2, crosses the x-axis
- D) -6, multiplicity 2, crosses the x-axis

5) $f(x) = \frac{1}{5}x^2(x^2 - 5)(x - 5)$

- A) 0, multiplicity 2, touches x-axis and turns around;
5, multiplicity 1, crosses x-axis;
 $\sqrt{5}$, multiplicity 1, crosses x-axis;
 $-\sqrt{5}$, multiplicity 1, crosses x-axis
- B) 0, multiplicity 2, crosses x-axis;
5, multiplicity 1, touches x-axis and turns around;
 $\sqrt{5}$, multiplicity 1, touches x-axis and turns around;
 $-\sqrt{5}$, multiplicity 1, touches x-axis and turns around
- C) 0, multiplicity 2, touches x-axis and turns around;
5, multiplicity 1, crosses x-axis
- D) 0, multiplicity 2, touches x-axis and turns around;
5, multiplicity 1, crosses x-axis
5, multiplicity 2, touches x-axis and turns around

$$6) f(x) = \left(x + \frac{1}{4}\right)^4 (x + 6)^3$$

- A) $-\frac{1}{4}$, multiplicity 4, touches the x-axis and turns around;
 -6 , multiplicity 3, crosses the x-axis.
- B) $-\frac{1}{4}$, multiplicity 4, crosses the x-axis;
 -6 , multiplicity 3, touches the x-axis and turns around
- C) $\frac{1}{4}$, multiplicity 4, touches the x-axis and turns around;
 6 , multiplicity 3, crosses the x-axis.
- D) $\frac{1}{4}$, multiplicity 4, crosses the x-axis;
 6 , multiplicity 3, touches the x-axis and turns around

$$7) f(x) = \left(x + \frac{1}{4}\right)^2 (x^2 + 2)^5$$

- A) $-\frac{1}{4}$, multiplicity 2, touches the x-axis and turns around.
- B) $-\frac{1}{4}$, multiplicity 2, touches the x-axis and turns around;
 -2 , multiplicity 5, crosses the x-axis
- C) $\frac{1}{4}$, multiplicity 2, touches the x-axis and turns around;
 2 , multiplicity 5, crosses the x-axis
- D) $-\frac{1}{4}$, multiplicity 2, crosses the x-axis.

$$8) f(x) = x^3 + x^2 - 42x$$

- A) 0, multiplicity 1, crosses the x-axis
 -7 , multiplicity 1, crosses the x-axis
 6 , multiplicity 1, crosses the x-axis
- B) -7 , multiplicity 2, touches the x-axis and turns around
 6 , multiplicity 1, crosses the x-axis
- C) 0, multiplicity 1, crosses the x-axis
 7 , multiplicity 1, crosses the x-axis
 -6 , multiplicity 1, crosses the x-axis
- D) 0, multiplicity 1, touches the x-axis and turns around;
 -7 , multiplicity 1, touches the x-axis and turns around;
 6 , multiplicity 1, touches the x-axis and turns around

- 9) $f(x) = x^3 + 11x^2 + 39x + 45$
- A) -3, multiplicity 2, touches the x-axis and turns around;
-5, multiplicity 1, crosses the x-axis.
 - B) -3, multiplicity 2, crosses the x-axis;
-5, multiplicity 1, touches the x-axis and turns around
 - C) 3, multiplicity 1, crosses the x-axis;
-3, multiplicity 1, crosses the x-axis;
-5, multiplicity 1, crosses the x-axis.
 - D) 3, multiplicity 1, crosses the x-axis;
-3, multiplicity 2, touches the x-axis and turns around;
-5, multiplicity 1, crosses the x-axis.

- 10) $f(x) = x^3 + 7x^2 - x - 7$
- A) -1, multiplicity 1, crosses the x-axis;
1, multiplicity 1, crosses the x-axis;
-7, multiplicity 1, crosses the x-axis.
 - B) 7, multiplicity 1, crosses the x-axis;
1, multiplicity 1, crosses the x-axis;
-7, multiplicity 1, crosses the x-axis.
 - C) 1, multiplicity 2, touches the x-axis and turns around;
-7, multiplicity 1, crosses the x-axis.
 - D) -1, multiplicity 1, touches the x-axis and turns around;
1, multiplicity 1, touches the x-axis and turns around;
-7, multiplicity 1, touches the x-axis and turns around

Write the equation of a polynomial function with the given characteristics. Use a leading coefficient of 1 or -1 and make the degree of the function as small as possible.

- 11) Crosses the x-axis at -3, 0, and 1; lies above the x-axis between -3 and 0; lies below the x-axis between 0 and 1.

A) $f(x) = x^3 + 2x^2 - 3x$
C) $f(x) = -x^3 - 2x^2 + 3x$

B) $f(x) = x^3 - 2x^2 - 3x$
D) $f(x) = -x^3 + 2x^2 + 3x$

- 12) Crosses the x-axis at -4, 0, and 2; lies below the x-axis between -4 and 0; lies above the x-axis between 0 and 2.

A) $f(x) = -x^3 - 2x^2 + 8x$
C) $f(x) = x^3 + 2x^2 - 8x$

B) $f(x) = -x^3 + 2x^2 + 8x$
D) $f(x) = x^3 - 2x^2 - 8x$

- 13) Touches the x-axis at 0 and crosses the x-axis at 3; lies below the x-axis between 0 and 3.

A) $f(x) = x^3 - 3x^2$

B) $f(x) = x^3 + 3x^2$

C) $f(x) = -x^3 + 3x^2$

D) $f(x) = -x^3 - 3x^2$

- 14) Touches the x-axis at 0 and crosses the x-axis at 3; lies above the x-axis between 0 and 3.

A) $f(x) = -x^3 + 3x^2$

B) $f(x) = x^3 + 3x^2$

C) $f(x) = x^3 - 3x^2$

D) $f(x) = -x^3 - 3x^2$

6 Use the Intermediate Value Theorem

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Use the Intermediate Value Theorem to determine whether the polynomial function has a real zero between the given integers.

- 1) $f(x) = -2x^3 + 10x^2 - 3x - 8$; between 1 and 2

A) $f(1) = -3$ and $f(2) = 10$; yes

C) $f(1) = -3$ and $f(2) = -10$; no

B) $f(1) = 3$ and $f(2) = 10$; no

D) $f(1) = 3$ and $f(2) = -10$; yes

2) $f(x) = 7x^5 - 2x^3 + 5x^2 + 9$; between -2 and -1

A) $f(-2) = -179$ and $f(-1) = 9$; yes

C) $f(-2) = -179$ and $f(-1) = -9$; no

B) $f(-2) = 179$ and $f(-1) = 9$; no

D) $f(-2) = 179$ and $f(-1) = -9$; yes

3) $f(x) = 4x^4 - 10x^2 - 1$; between 1 and 2

A) $f(1) = -7$ and $f(2) = 23$; yes

C) $f(1) = -7$ and $f(2) = -23$; no

B) $f(1) = 7$ and $f(2) = 24$; no

D) $f(1) = 7$ and $f(2) = -23$; yes

4) $f(x) = 2x^4 + 6x^3 - 4x - 1$; between -3 and -2

A) $f(-3) = 11$ and $f(-2) = -9$; yes

C) $f(-3) = -11$ and $f(-2) = -9$; no

B) $f(-3) = 11$ and $f(-2) = 9$; no

D) $f(-3) = -11$ and $f(-2) = 9$; yes

5) $f(x) = 2x^3 + 5x + 9$; between -2 and -1

A) $f(-2) = -17$ and $f(-1) = 2$; yes

C) $f(-2) = 17$ and $f(-1) = 2$; no

B) $f(-2) = -17$ and $f(-1) = -2$; no

D) $f(-2) = 17$ and $f(-1) = -2$; yes

7 Understand the Relationship Between Degree and Turning Points

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Determine the maximum possible number of turning points for the graph of the function.

1) $f(x) = -x^2 - 6x - 7$

A) 1

B) 2

C) 0

D) 3

2) $f(x) = 8x^3 - 8x^2 - 5x - 22$

A) 2

B) 0

C) 8

D) 3

3) $f(x) = x^6 + 8x^7$

A) 6

B) 7

C) 8

D) 1

4) $g(x) = \frac{5}{2}x + 1$

A) 0

B) 2

C) 1

D) 3

5) $f(x) = (x + 2)(x - 1)(7x + 2)$

A) 2

B) 7

C) 3

D) 0

6) $f(x) = x^3(x^3 + 6)(5x + 7)$

A) 6

B) 7

C) 30

D) 3

7) $f(x) = (5x - 5)^2(x^2 - 1)(x + 1)$

A) 4

B) 5

C) 25

D) 2

8) $f(x) = (x - 5)(x + 3)(x + 2)(x - 2)$

A) 3

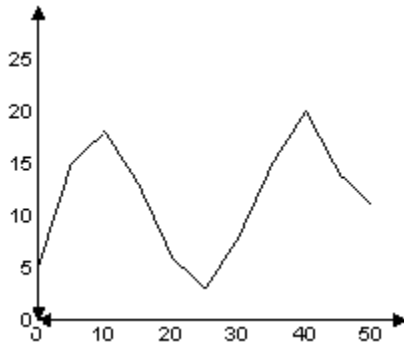
B) 4

C) 0

D) 1

Solve.

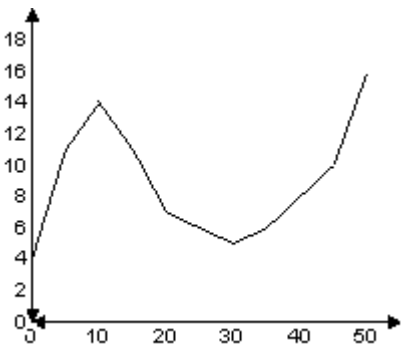
9) Suppose that a polynomial function is used to model the data shown in the graph below.



For what intervals is the function increasing?

- A) 0 through 10 and 25 through 40
- B) 0 through 40
- C) 0 through 10 and 20 through 30
- D) 10 through 25 and 40 through 50

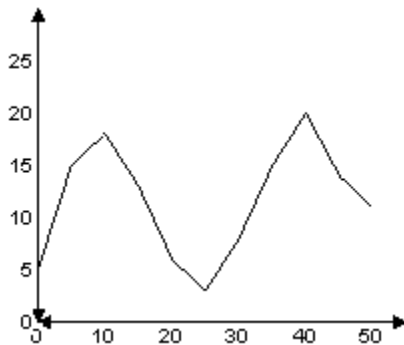
10) Suppose that a polynomial function is used to model the data shown in the graph below.



For what intervals is the function increasing?

- A) 0 through 10 and 30 through 50
- B) 0 through 50
- C) 0 through 20 and 30 through 50
- D) 0 through 10 and 40 through 50

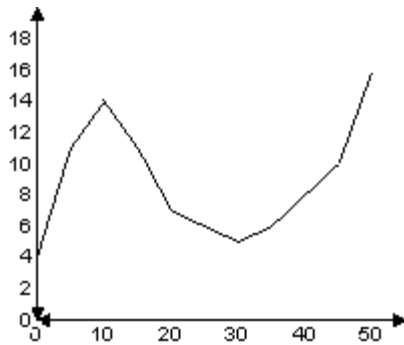
11) Suppose that a polynomial function is used to model the data shown in the graph below.



For what intervals is the function decreasing?

- A) 10 through 25 and 40 through 50
- B) 10 through 50
- C) 10 through 25 and 40 through 45
- D) 0 through 10 and 25 through 40

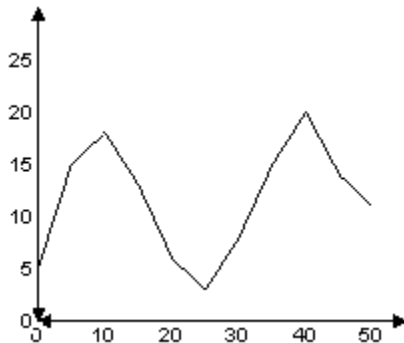
12) Suppose that a polynomial function is used to model the data shown in the graph below.



For what intervals is the function decreasing?

- A) 10 through 30
- B) 0 through 30
- C) 10 through 20 and 30 through 50
- D) 0 through 10 and 30 through 50

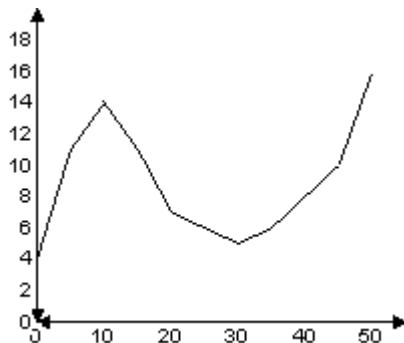
13) Suppose that a polynomial function is used to model the data shown in the graph below.



Determine the degree of the polynomial function of best fit and the sign of the leading coefficient.

- A) Degree 4; negative leading coefficient.
- B) Degree 5; positive leading coefficient.
- C) Degree 5; negative leading coefficient.
- D) Degree 4; positive leading coefficient.

14) Suppose that a polynomial function is used to model the data shown in the graph below.



Determine the degree of the polynomial function of best fit and the sign of the leading coefficient.

- A) Degree 3; positive leading coefficient.
- B) Degree 4; negative leading coefficient.
- C) Degree 3; negative leading coefficient.
- D) Degree 4; positive leading coefficient.

15) The profits (in millions) for a company for 8 years were as follows:

Year, x	Profits, P
1993, 1	1.1
1994, 2	1.7
1995, 3	2.0
1996, 4	1.4
1997, 5	1.3
1998, 6	1.5
1999, 7	1.8
2000, 8	2.1

Which of the following polynomials is the best model for this data?

A) $P(x) = 0.05x^2 - 0.8x + 6$

B) $P(x) = -0.08x^3 + 7x^2 + 1.3x - 0.18$

C) $P(x) = 0.03x^3 - 0.3x^2 + 1.3x + 0.17$

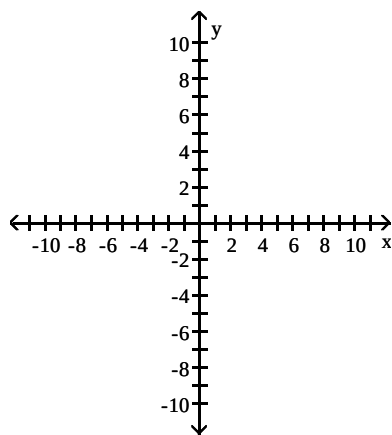
D) $P(x) = -0.03x^4 - 0.3x^2 + 1.3x + 0.17$

8 Graph Polynomial Functions

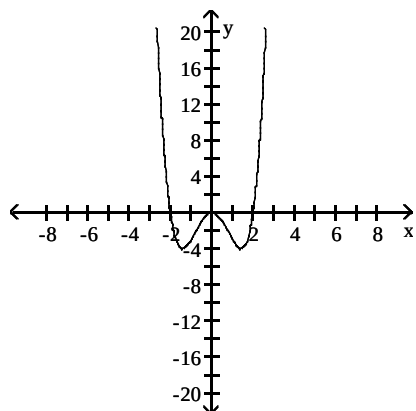
MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Graph the polynomial function.

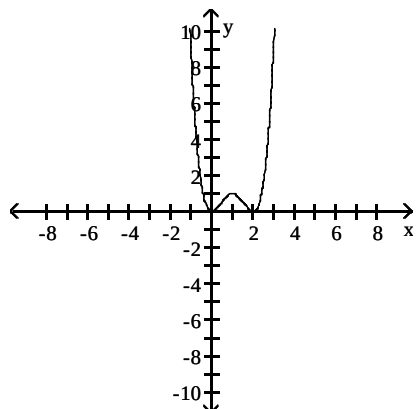
1) $f(x) = x^4 - 4x^2$



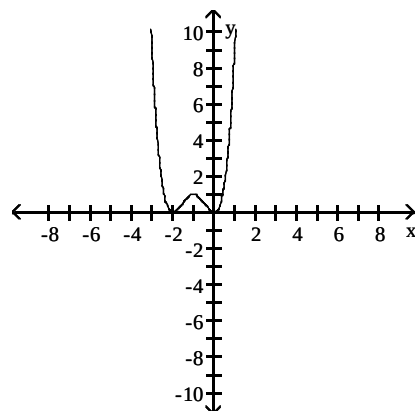
A)



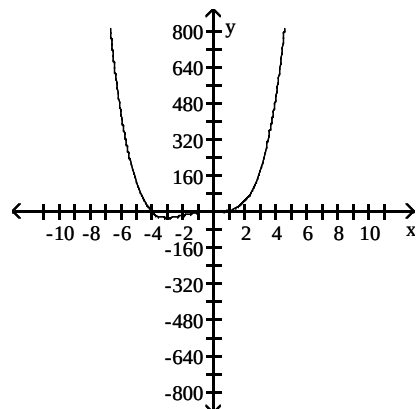
C)



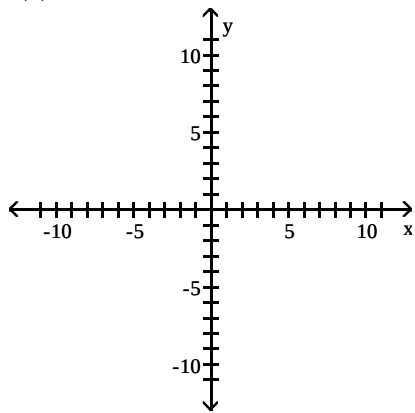
B)



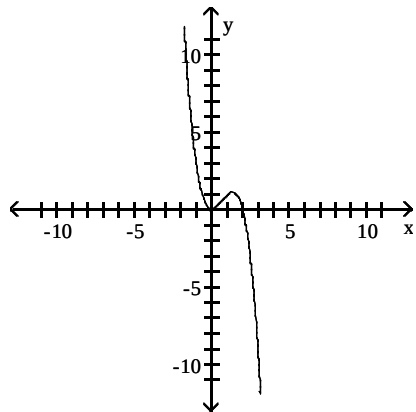
D)



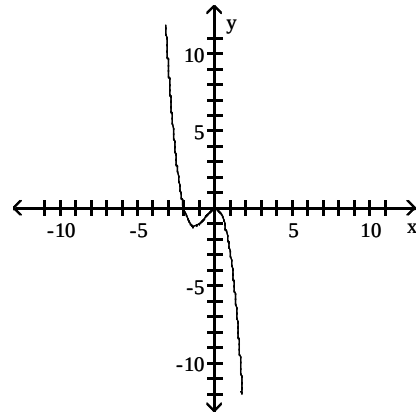
2) $f(x) = 2x^2 - x^3$



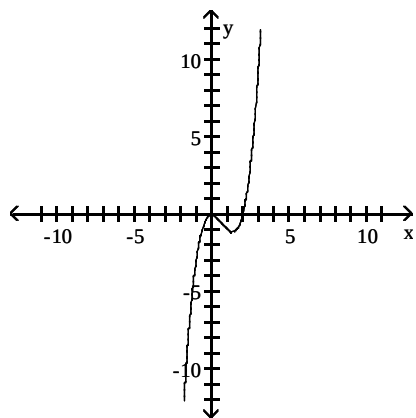
A)



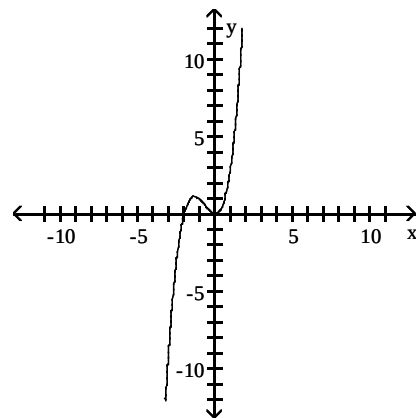
B)



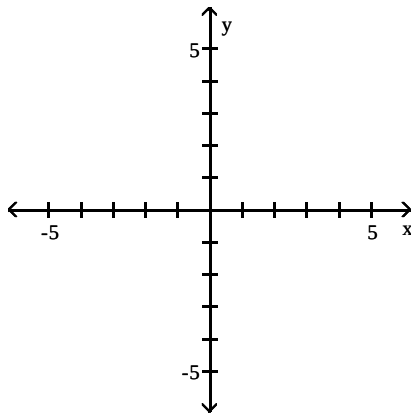
C)



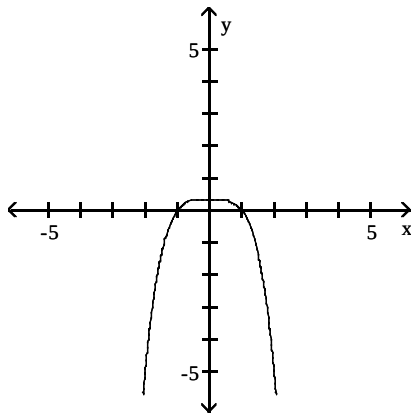
D)



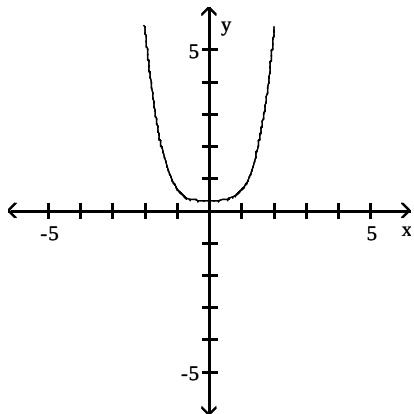
3) $f(x) = \frac{1}{3} - \frac{1}{3}x^4$



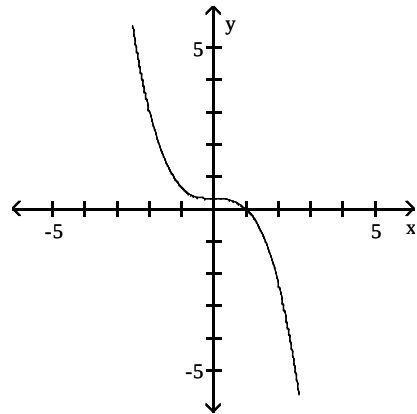
A)



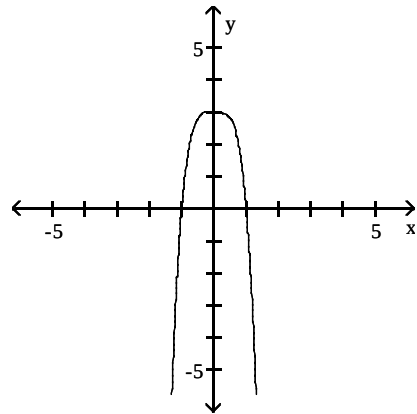
C)



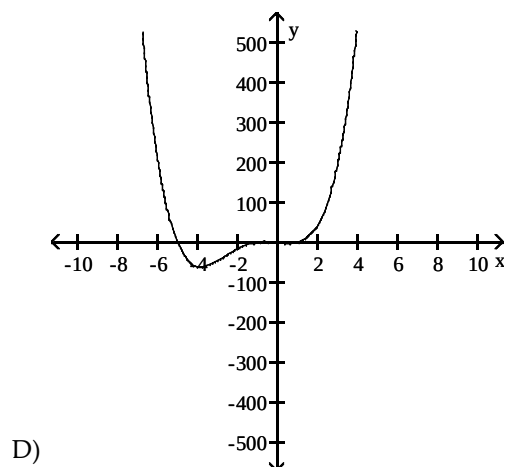
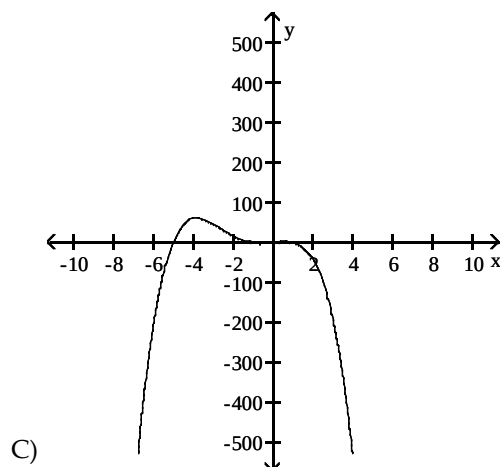
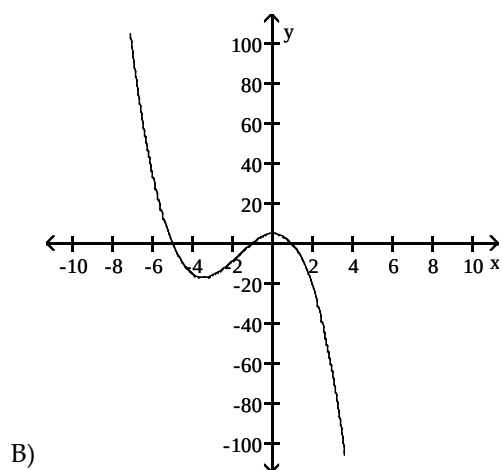
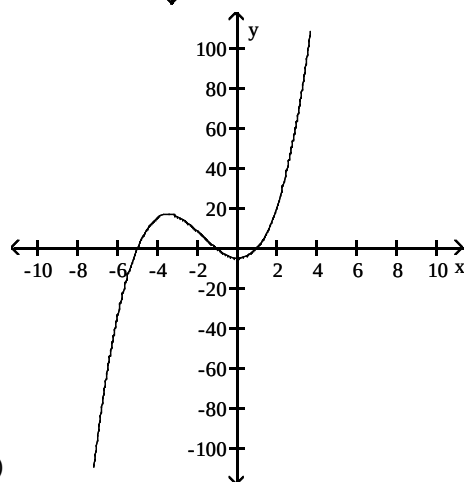
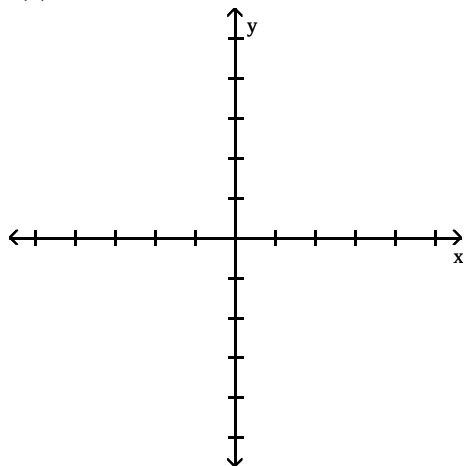
B)



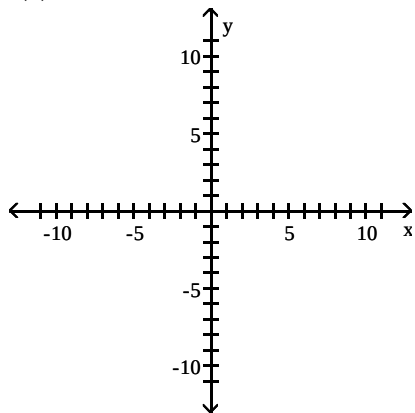
D)



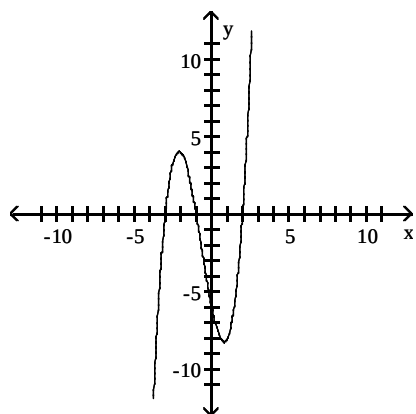
4) $f(x) = x^3 + 5x^2 - x - 5$



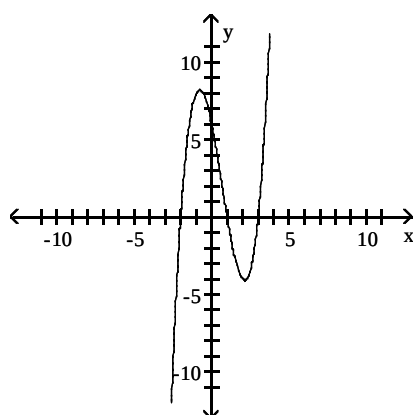
5) $f(x) = x^3 + 2x^2 - 5x - 6$



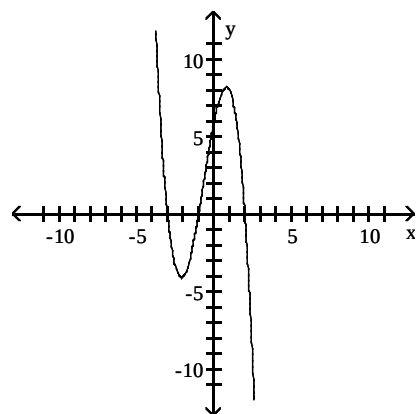
A)



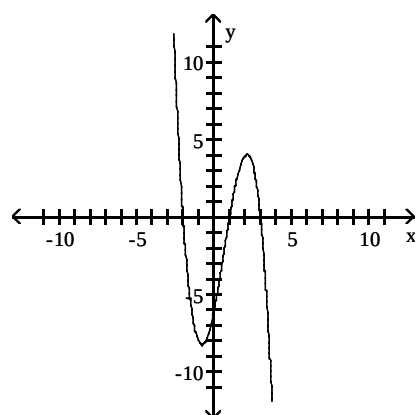
C)



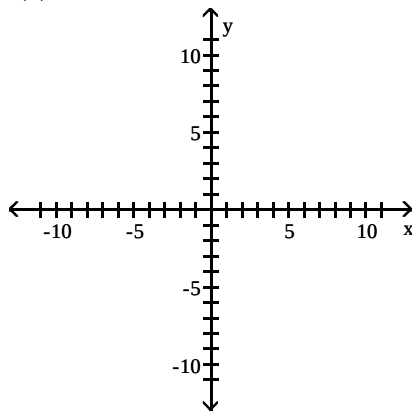
B)



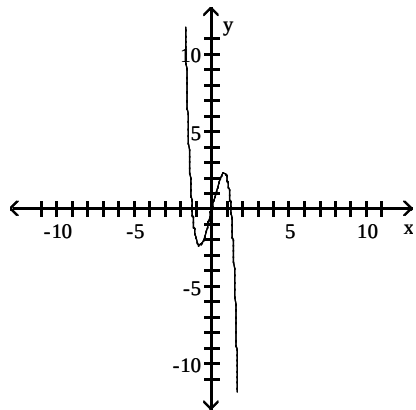
D)



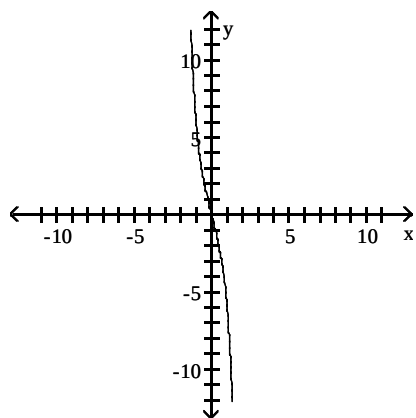
6) $f(x) = 4x - x^3 - x^5$



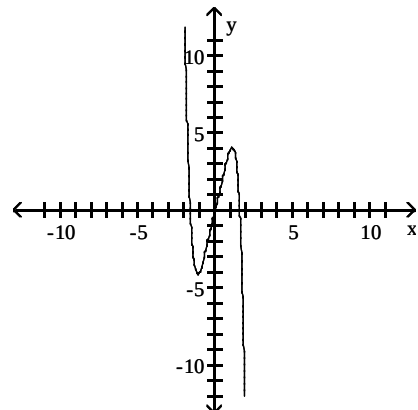
A)



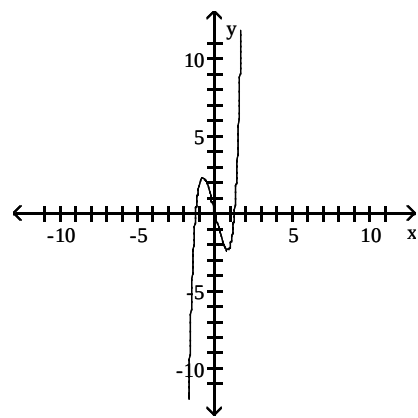
C)



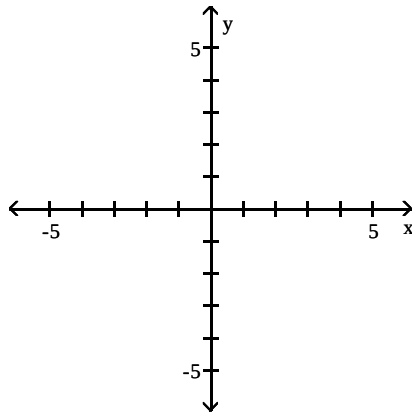
B)



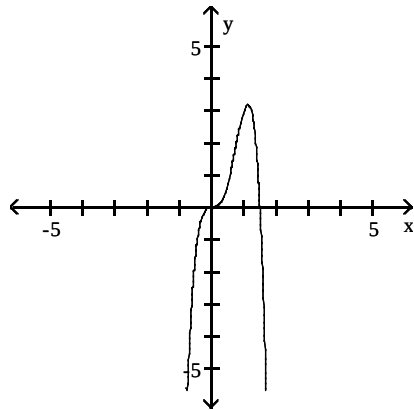
D)



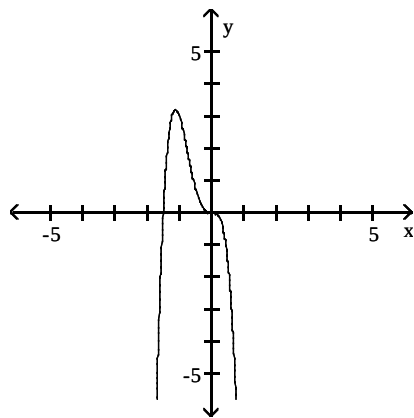
7) $f(x) = -6x^4 + 9x^3$



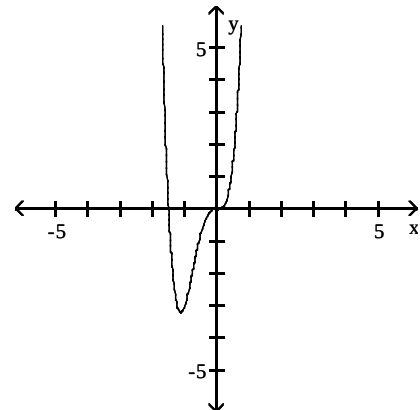
A)



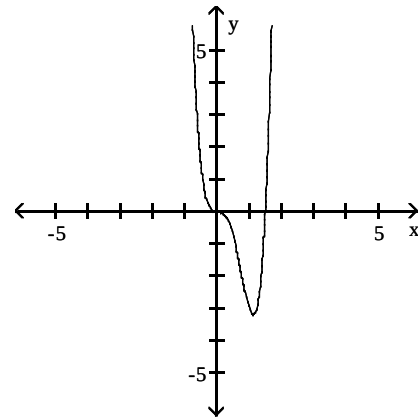
C)



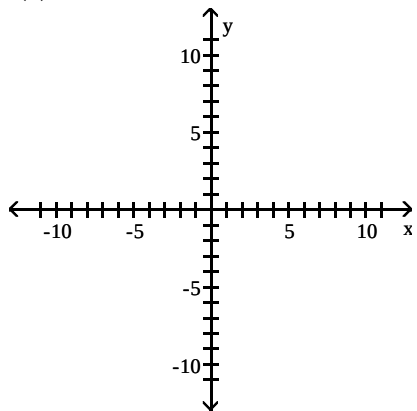
B)



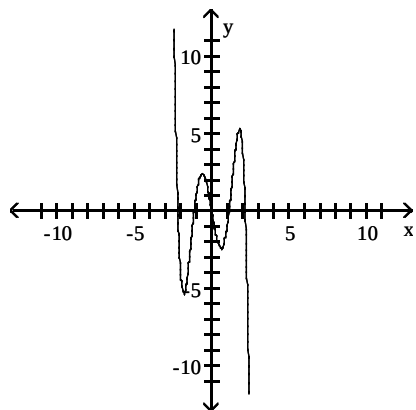
D)



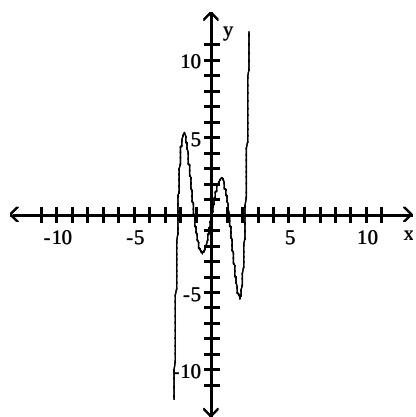
8) $f(x) = 6x^3 - 6x - x^5$



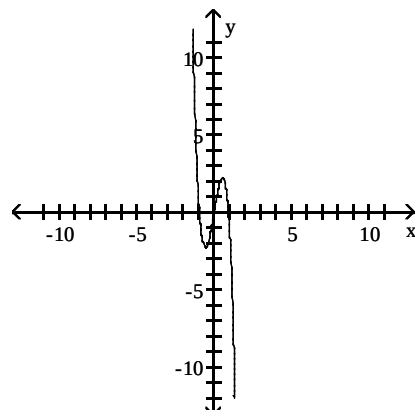
A)



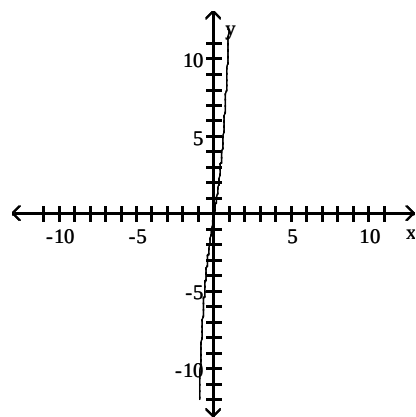
C)



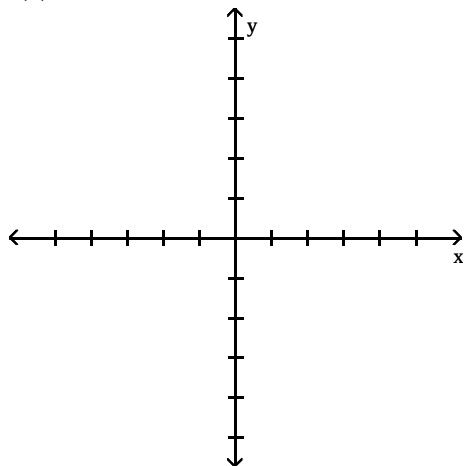
B)



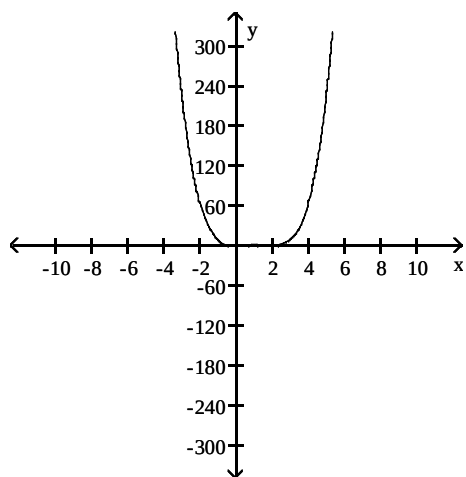
D)



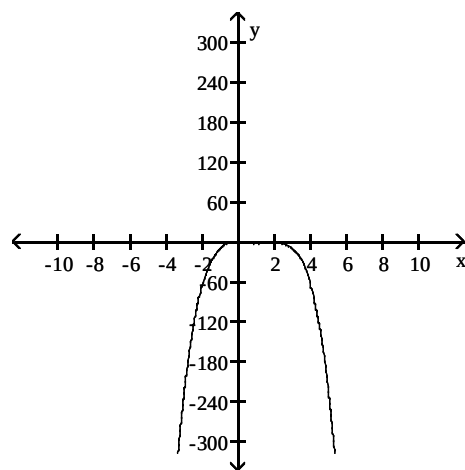
9) $f(x) = x^4 - 4x^3 + 4x^2$



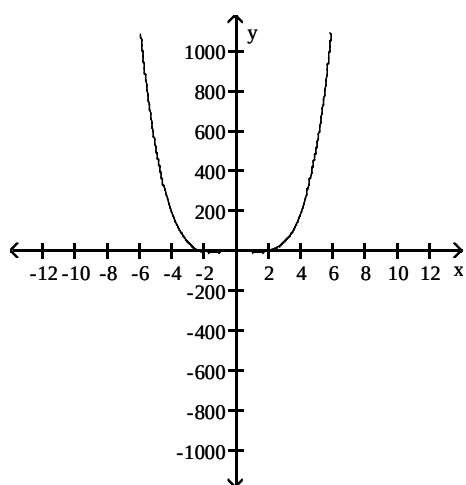
A)



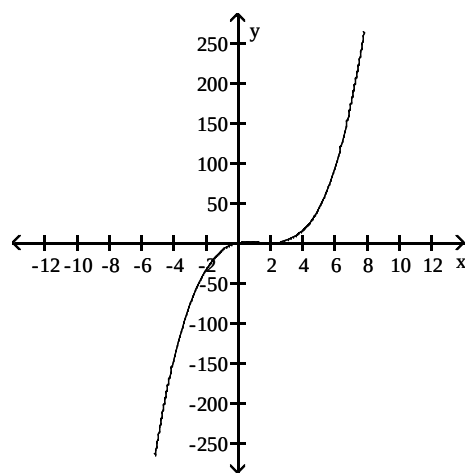
B)



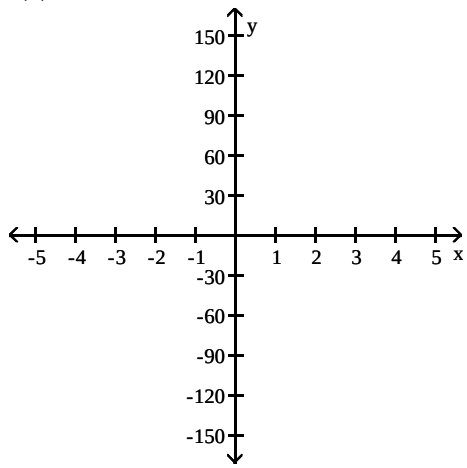
C)



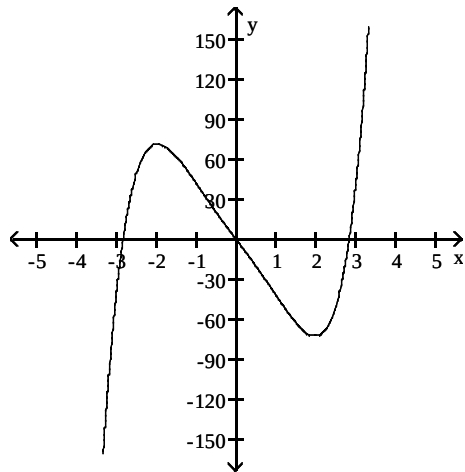
D)



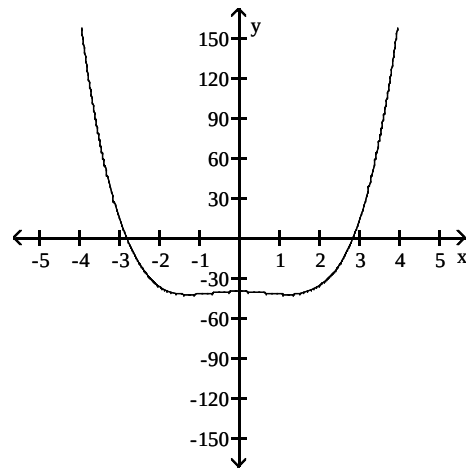
10) $f(x) = x^5 - 3x^3 - 40x$



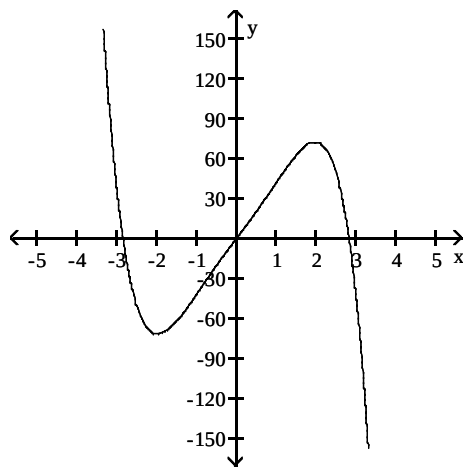
A)



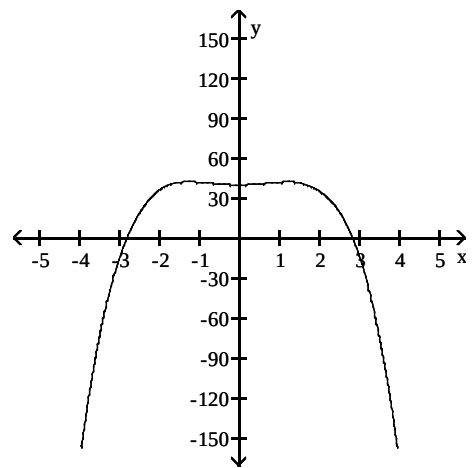
B)



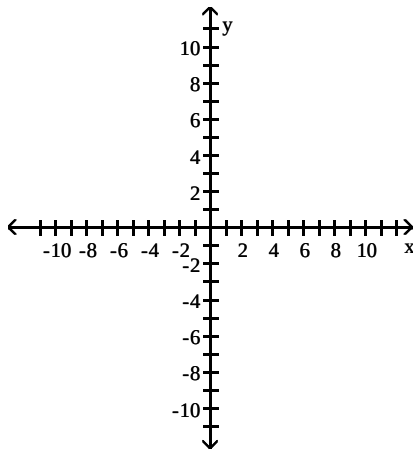
C)



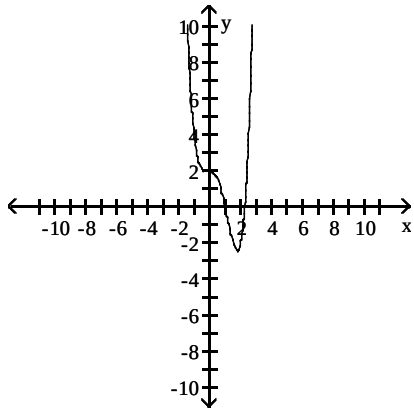
D)



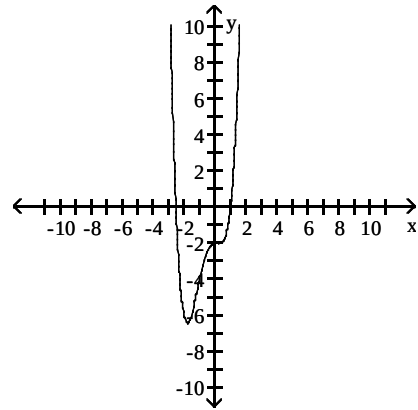
11) $f(x) = x^4 - 2x^3 - x^2 + 2$



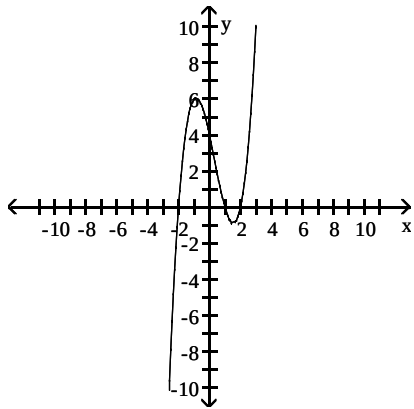
A)



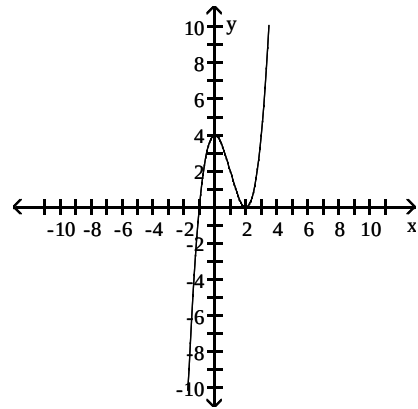
B)



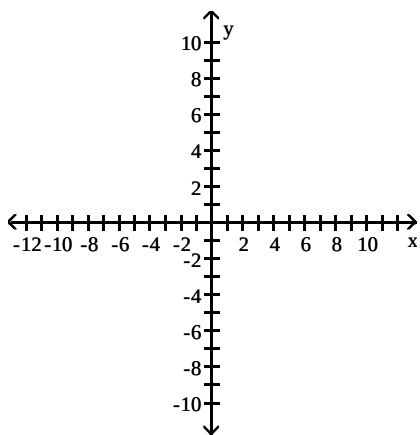
C)



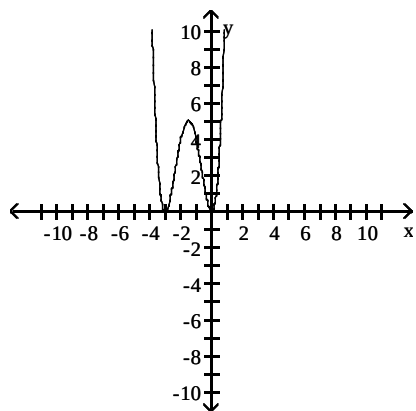
D)



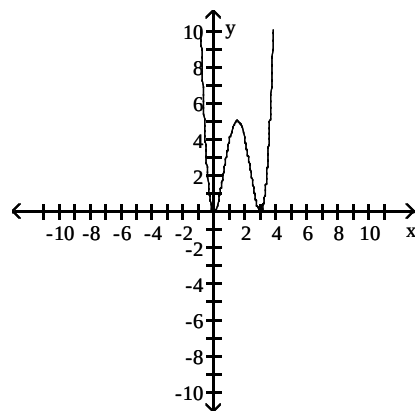
12) $f(x) = x^4 + 6x^3 + 9x^2$



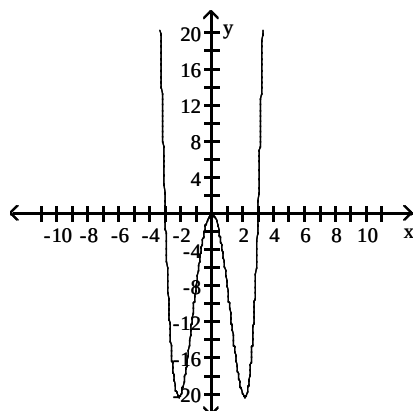
A)



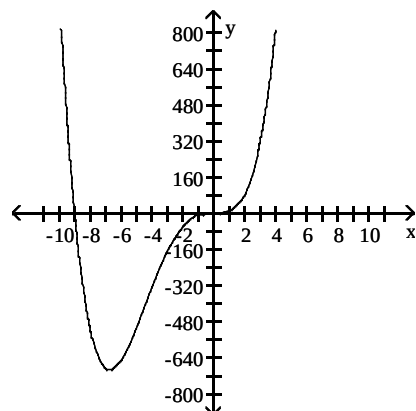
B)



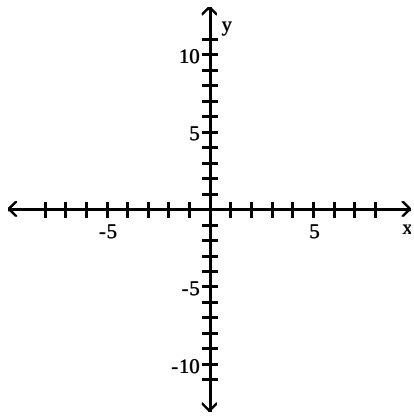
C)



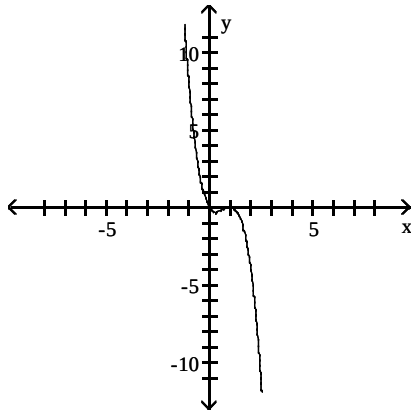
D)



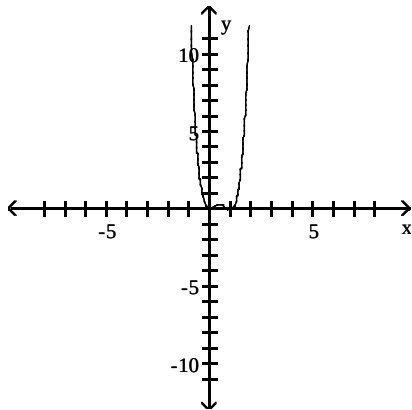
13) $f(x) = -2x(x - 1)^2$



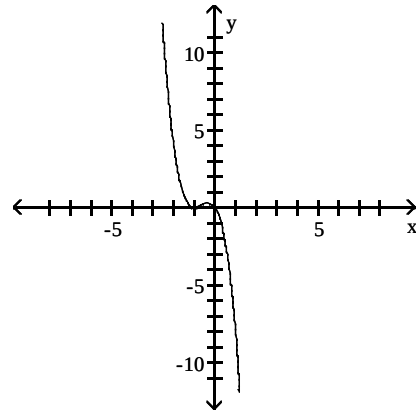
A)



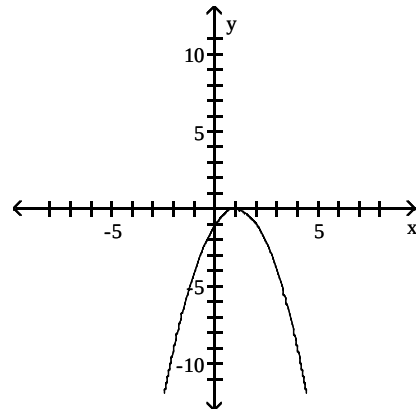
C)



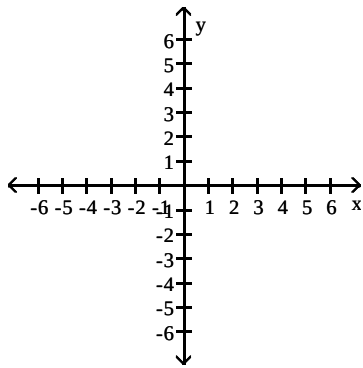
B)



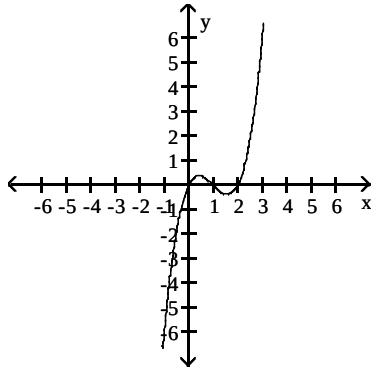
D)



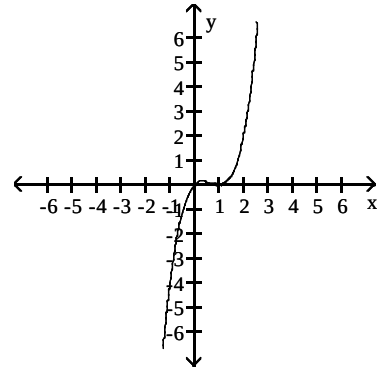
14) $f(x) = x(x - 2)(x - 1)$



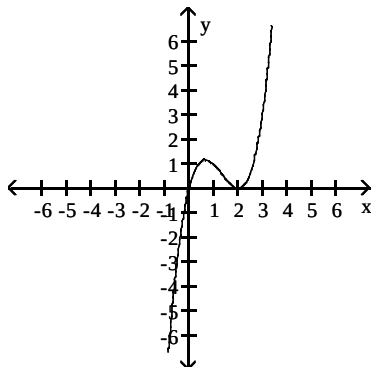
A)



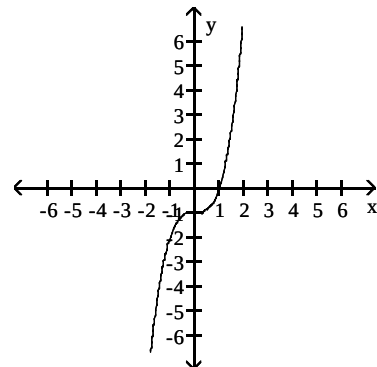
B)



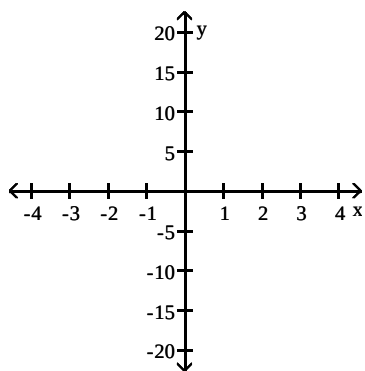
C)



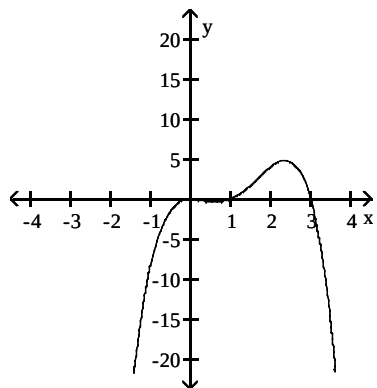
D)



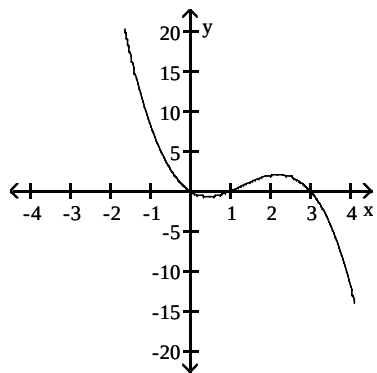
15) $f(x) = -x^2(x - 3)(x - 1)$



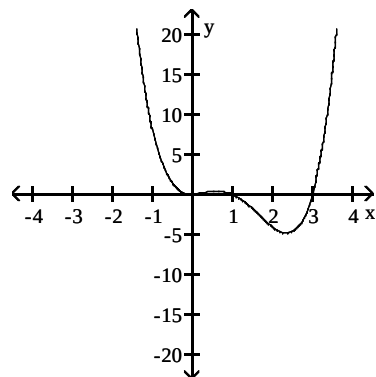
A)



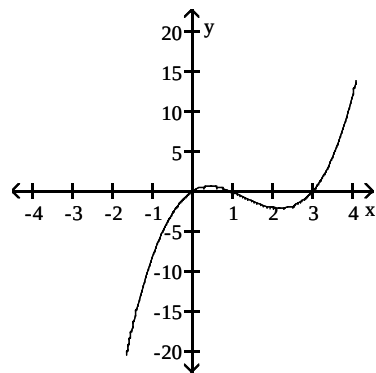
C)



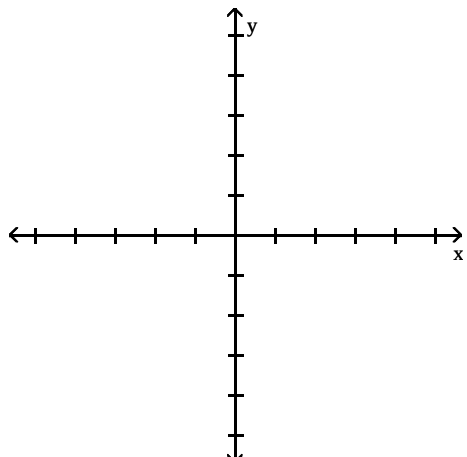
B)

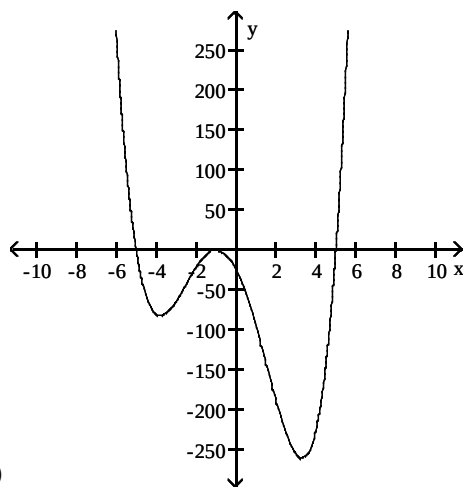


D)

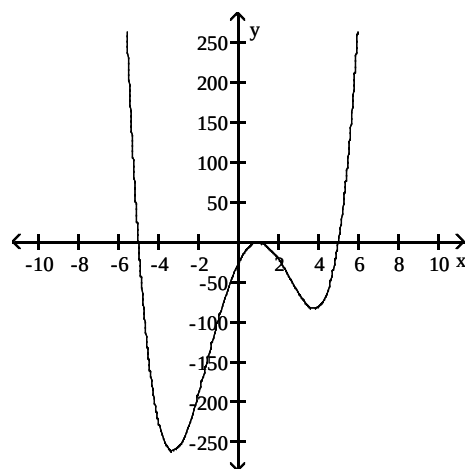


16) $f(x) = (x + 1)^2(x^2 - 25)$

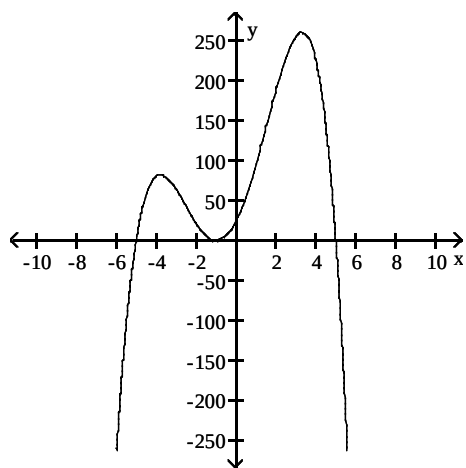




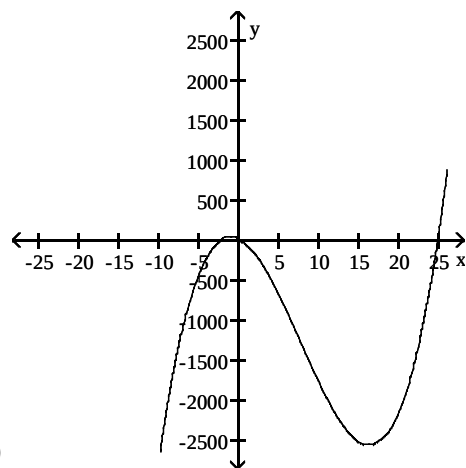
A)



B)

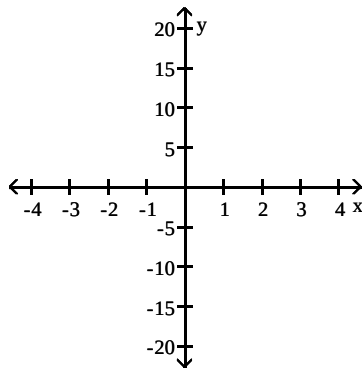


C)

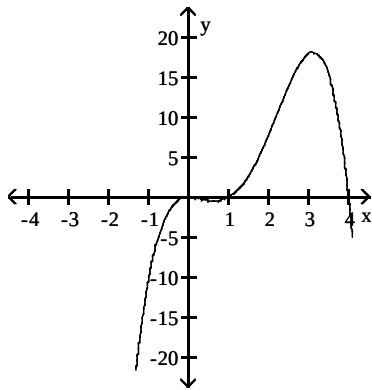


D)

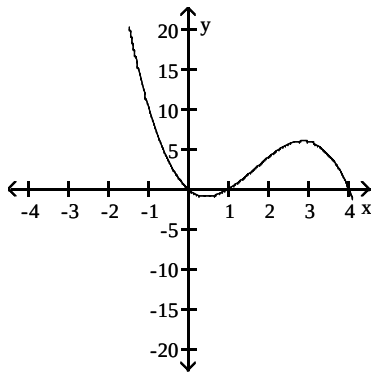
17) $f(x) = -x^2(x - 4)(x - 1)$



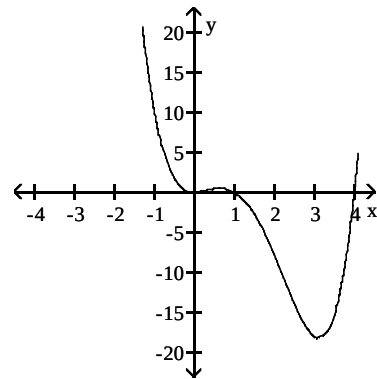
A)



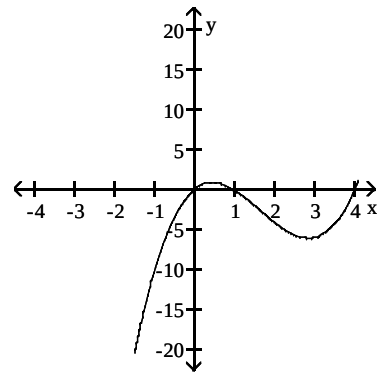
C)



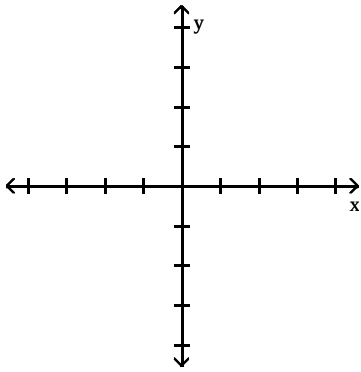
B)



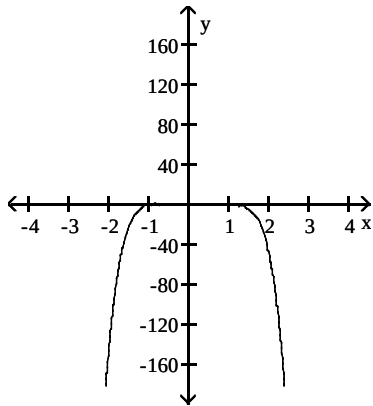
D)



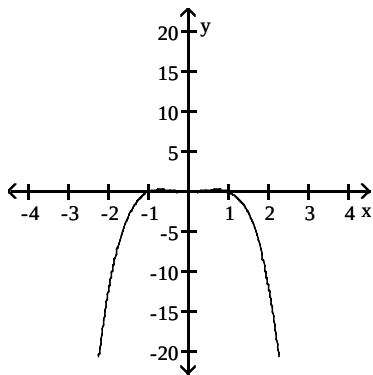
18) $f(x) = -2x^3(x - 1)^2(x + 1)$



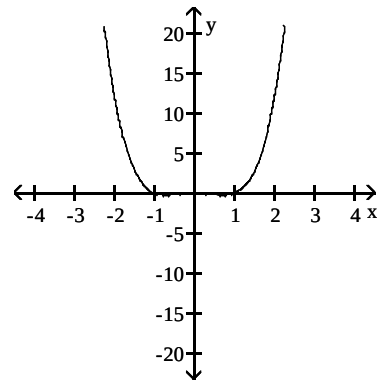
A)



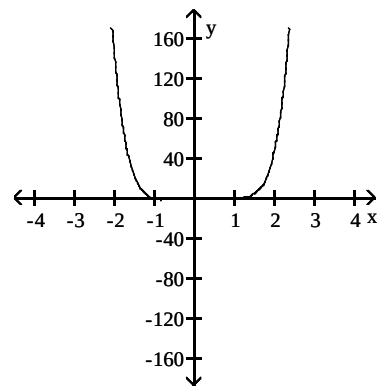
C)



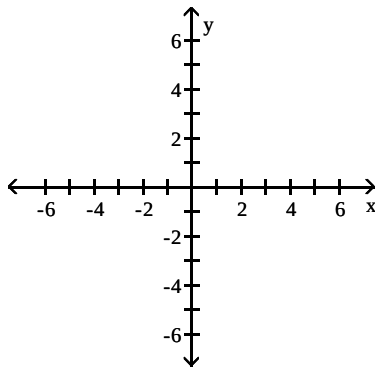
B)



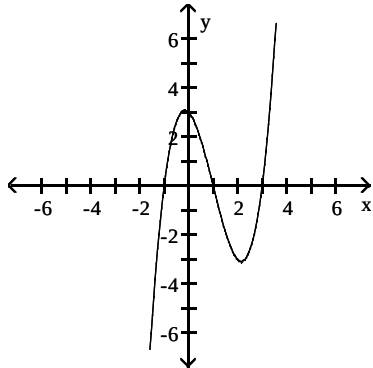
D)



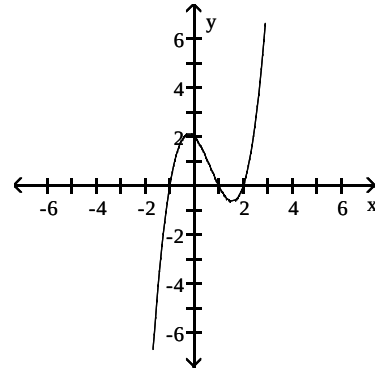
19) $f(x) = (x - 3)(x - 1)(x + 1)$



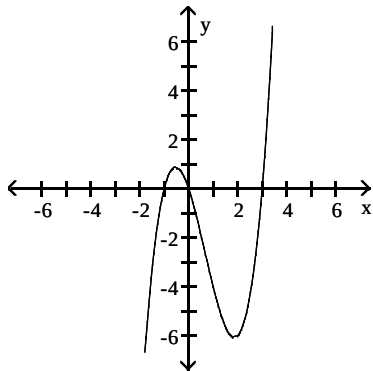
A)



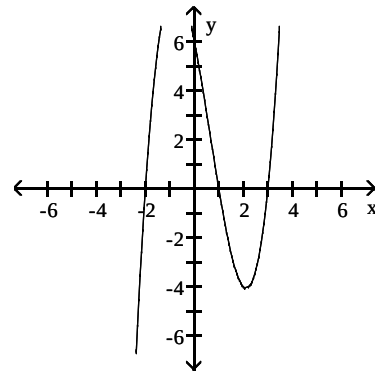
B)



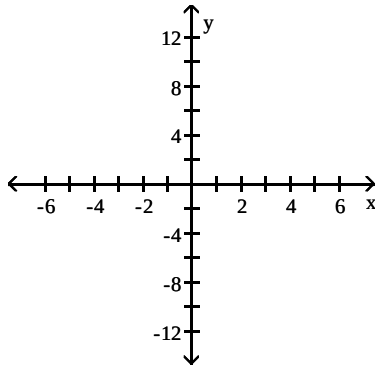
C)



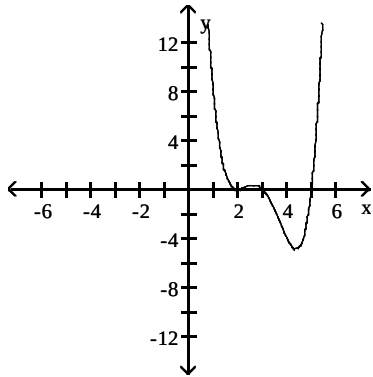
D)



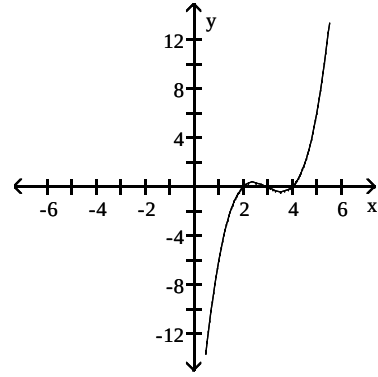
20) $f(x) = (x - 5)(x - 3)(x - 2)^2$



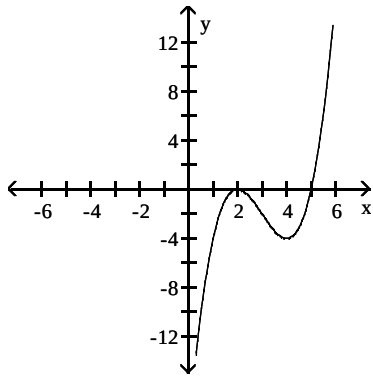
A)



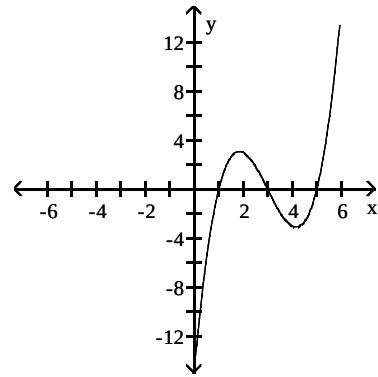
B)



C)



D)

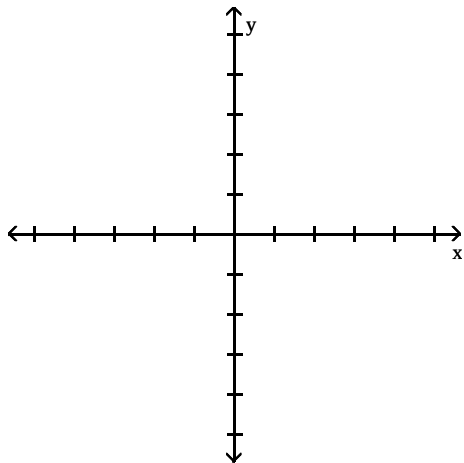


SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

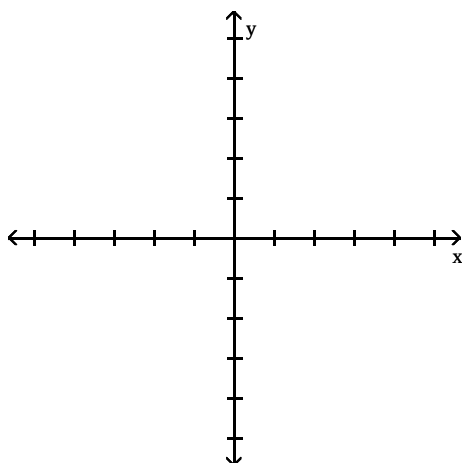
Complete the following:

- (a) Use the Leading Coefficient Test to determine the graph's end behavior.
- (b) Find the x -intercepts. State whether the graph crosses the x -axis or touches the x -axis and turns around at each intercept.
- (c) Find the y -intercept.
- (d) Graph the function.

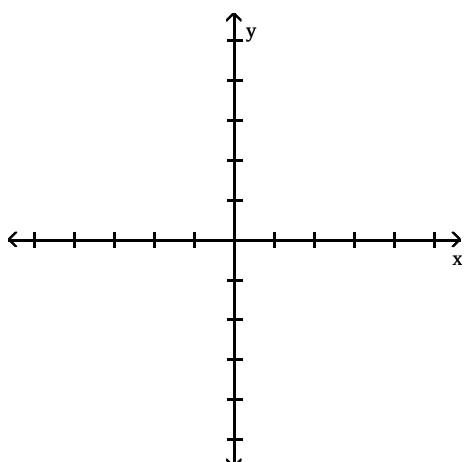
21) $f(x) = x^2(x + 2)$



22) $f(x) = (x + 2)(x - 3)^2$



23) $f(x) = -2(x - 1)(x + 3)^3$



2.4 Dividing Polynomials: Remainder and Factor Theorems

1 Use Long Division to Divide Polynomials

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Divide using long division.

1) $(x^2 + 3x - 10) \div (x - 2)$

A) $x + 5$

B) $x + 3$

C) $x^2 + 5$

D) $x^2 + 3$

2) $(11x^2 + 82x + 35) \div (x + 7)$

A) $11x + 5$

B) $11x - 5$

C) $x + 82$

D) $11x^2 - 82$

3) $(6x^2 + 17x - 45) \div (3x - 5)$

A) $2x + 9$

B) $6x + 9$

C) $x + 9$

D) $9x + 1$

4) $\frac{6m^3 + 5m^2 - 9m + 10}{m + 2}$

A) $6m^2 - 7m + 5$

B) $6m^2 + 7m + 5$

C) $m^2 + 8m + 9$

D) $m^2 + 7m + 6$

5) $\frac{3r^3 - 3r^2 - 1r - 10}{r - 2}$

A) $3r^2 + 3r + 5$

B) $3r^2 - 3r - 5$

C) $3r^2 + 3r + \frac{5}{r - 2}$

D) $r^2 + 5r + 3$

6) $(-6x^3 - 17x^2 - 17x - 4) \div (3x + 1)$

A) $-2x^2 - 5x - 4$

B) $-2x^2 - 4$

C) $x^2 - 5x - 4$

D) $x^2 + 5x + 4$

7) $\frac{3x^3 - 112x + 24}{x - 6}$

A) $3x^2 + 18x - 4$

B) $3x^2 - 94x + \frac{-540}{x - 6}$

C) $3x^2 + 94x + \frac{-540}{x - 6}$

D) $3x^2 - 18x - 4$

8) $(6x^3 - 2) \div (3x - 1)$

A) $2x^2 + \frac{2}{3}x + \frac{2}{9} - \frac{16}{9(3x - 1)}$

B) $2x^2 + \frac{2}{3}x + \frac{2}{9} + \frac{16}{9(3x - 1)}$

C) $2x^2 + \frac{2}{3}x + \frac{2}{9}$

D) $2x^2 - \frac{2}{3}x + \frac{2}{9}$

9) $\frac{-6x^3 + 8x^2 + 23x + 14}{3x + 2}$

A) $-2x^2 + 4x + 5 + \frac{4}{3x + 2}$

B) $-2x^2 + 4x + 5$

C) $-2x^2 + 4x + 5 + \frac{7}{3x + 2}$

D) $x^2 + 5 + \frac{4}{3x + 2}$

$$10) \frac{x^4 + 16}{x - 2}$$

$$A) x^3 + 2x^2 + 4x + 8 + \frac{32}{x - 2}$$

$$C) x^3 + 2x^2 + 4x + 8$$

$$B) x^3 + 2x^2 + 4x + 8 + \frac{16}{x - 2}$$

$$D) x^3 - 2x^2 + 4x - 8 + \frac{32}{x - 2}$$

$$11) (3x^4 - 5x^2 + 15x^3 - 25x) \div (3x + 15)$$

$$A) x^3 - \frac{5}{3}x$$

$$B) x^3 + \frac{5}{3}x$$

$$C) x^3 - 15x + \frac{9x}{3x + 15}$$

$$D) x^3 - \frac{5}{3}x - \frac{50x}{3x + 15}$$

$$12) \frac{8y^4 + 12y^3 - 2y}{2y^2 + y}$$

$$A) 4y^2 + 4y - 2$$

$$C) 4y^2 + 4y - \frac{6y}{2y^2 + y}$$

$$B) 4y^2 + 8y + 4 + \frac{2y}{2y^2 + y}$$

$$D) 4y^2 + 6y - \frac{2y}{2y^2 + y}$$

$$13) (16x^3 + x^2 - 48x - 3) \div (8x^2 - 24)$$

$$A) 2x + \frac{1}{8}$$

$$B) 2x + 8$$

$$C) 2x + \frac{-3}{8x^2 - 24}$$

$$D) 2x + \frac{3}{8x^2 - 24}$$

$$14) (-4x^4 + 28x^3 - 23x^2 - 8x + 12) \div (6 - x)$$

$$A) 4x^3 - 4x^2 - x + 2$$

$$C) 4x^3 - 4x^2 - x - 2 + \frac{24}{6 - x}$$

$$B) 4x^3 - 4x^2 - x - 2$$

$$D) 4x^3 - 4x^2 + x - 2$$

$$15) (-4x^5 - x^3 - 5x^2 + 212x + 35) \div (x^2 - 7)$$

$$A) -4x^3 - 29x - 5 + \frac{9x}{x^2 - 7}$$

$$C) -4x^3 - 29x - 5 + \frac{9x + 70}{x^2 - 7}$$

$$B) -4x^3 - 29x - 5 - \frac{9x}{x^2 - 7}$$

$$D) -4x^3 - 29x + 5 + \frac{9x}{x^2 - 7}$$

$$16) \frac{x^4 + 5x^3 + 3x^2 - 7x - 6}{x^2 + 4x + 1}$$

$$A) x^2 + x - 2 + \frac{-4}{x^2 + 4x + 1}$$

$$C) x^2 + 8x + 36 + \frac{153x + 38}{x^2 + 4x + 1}$$

$$B) x^2 + x - 2$$

$$D) x^2 + 8x + 36$$

$$17) \frac{-10t^4 - 24t^3 - 15t^2 - 45t - 27}{2t^2 + 6t + 3}$$

$$A) -5t^2 + 3t - 9$$

$$B) -5t^2 - 3t - 9$$

$$C) -5t^2 + 3t + 9$$

$$D) -5t^2 + 4t - 9$$

Solve the problem.

18) A rectangle with width $2x + 1$ inches has an area of $2x^4 + 7x^3 - 17x^2 - 58x - 24$ square inches. Write a polynomial that represents its length.

A) $x^3 + 3x^2 - 10x - 24$ inches

B) $x^3 - 10x^2 + 3x - 24$ inches

C) $x^3 + 2x^2 - 8x - 24$ inches

D) $x^3 - 8x^2 + 2x - 24$ inches

19) The width of a rectangle is $x - \frac{1}{3}$ feet and its area is $9x^3 + 9x^2 + 23x - 9$ square feet. Write a polynomial that represents the length of the rectangle.

A) $9x^2 + 12x + 27$ ft

B) $9x^2 - 12x + 27$ ft

C) $9x^2 + 6x + 21$ ft

D) $9x^2 + 12x - 27$ ft

20) Two people are 50 years old and 24 years old, respectively. In x years from now, their ages can be represented by $x + 50$ and $x + 24$. Use long division to find the ratio of the older person's age to the younger person's age in x years.

A) $1 + \frac{26}{x + 24}$

B) $1 + \frac{74}{x + 24}$

C) 2.0833

D) $1 + \frac{74}{x + 50}$

2 Use Synthetic Division to Divide Polynomials

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Divide using synthetic division.

1) $(x^2 + 14x + 48) \div (x + 8)$

A) $x + 6$

B) $x - 40$

C) $x^2 + 6$

D) $x^3 - 40$

2) $(x^2 + 15x + 52) \div (x + 9)$

A) $x + 6 - \frac{2}{x + 9}$

B) $x + 6 + \frac{2}{x + 9}$

C) $\frac{x + 6}{x + 9}$

D) $x + 7$

3) $\frac{3x^2 - 8x + 5}{x - 1}$

A) $3x - 5$

B) $x - 5$

C) $-5x - 1$

D) $-3x + 5$

4) $\frac{-4x^3 - 28x^2 - 21x + 18}{x + 6}$

A) $-4x^2 - 4x + 3$

B) $4x^2 - 6x + 3$

C) $-\frac{2}{3}x^2 - \frac{14}{3}x - \frac{7}{2}$

D) $4x^2 + 6x - 3$

5) $\frac{-3x^3 - 15x^2 + 21x + 18}{x + 6}$

A) $-3x^2 + 3x + 3$

B) $3x^2 - 6x + 3$

C) $-\frac{1}{2}x^2 - \frac{5}{2}x + \frac{7}{2}$

D) $-3x^2 x - \frac{5}{2} + 3$

6) $\frac{x^5 + x^3 + 1}{x + 3}$

A) $x^4 - 3x^3 + 10x^2 - 30x + 90 + \frac{-269}{x + 3}$

B) $x^4 - 3x^3 + 9x^2 - 26x + 78 + \frac{-233}{x + 3}$

C) $x^4 - 2x^2 + \frac{7}{x + 3}$

D) $x^4 - 2 + \frac{7}{x + 3}$

$$7) \frac{x^4 - 3x^3 + x^2 + 7x - 11}{x - 1}$$

$$A) x^3 - 2x^2 - x + 6 - \frac{5}{x - 1}$$

$$C) x^3 + 2x^2 - x + 8 - \frac{5}{x - 1}$$

$$B) x^3 - 2x^2 + x + 8 + \frac{10}{x - 1}$$

$$D) x^3 - 2x^2 + x + 6 + \frac{10}{x - 1}$$

$$8) (x^4 + 1296) \div (x - 6)$$

$$A) x^3 + 6x^2 + 36x + 216 + \frac{2592}{x - 6}$$

$$C) x^3 + 6x^2 + 36x + 216$$

$$B) x^3 + 6x^2 + 36x + 216 + \frac{1296}{x - 6}$$

$$D) x^3 - 6x^2 + 36x - 216 + \frac{2592}{x - 6}$$

$$9) (x^5 - 4x^4 - 9x^3 + x^2 - x + 21) \div (x + 2)$$

$$A) x^4 - 6x^3 + 3x^2 - 5x + 9 + \frac{3}{x + 2}$$

$$C) x^4 - 6x^3 + 3x^2 - 6x + 9 + \frac{6}{x + 2}$$

$$B) x^4 - 6x^3 + 3x^2 - 5x - 9 + \frac{3}{x + 2}$$

$$D) x^4 - 6x^3 + 3x^2 - 6x - 10 + \frac{6}{x + 2}$$

$$10) (5x^5 + 3x^4 + 2x^3 + x^2 - x + 14) \div (x + 1)$$

$$A) 5x^4 - 2x^3 + 4x^2 + 3x + 2 + \frac{12}{x + 1}$$

$$C) 5x^4 - 2x^3 + 4x^2 - 4x + 3 + \frac{18}{x + 1}$$

$$B) 5x^4 - 2x^3 + 4x^2 - 3x - 3 + \frac{12}{x + 1}$$

$$D) 5x^4 - 2x^3 + 4x^2 - 4x - 3 + \frac{18}{x + 1}$$

3 Evaluate a Polynomial Using the Remainder Theorem

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Use synthetic division and the Remainder Theorem to find the indicated function value.

$$1) f(x) = x^4 + 7x^3 + 3x^2 + 9x - 6; f(-4)$$

$$A) -186$$

$$B) 744$$

$$C) 186$$

$$D) -442$$

$$2) f(x) = 2x^3 - 6x^2 - 3x + 15; f(-2)$$

$$A) -19$$

$$B) -13$$

$$C) -10$$

$$D) -31$$

$$3) f(x) = 6x^4 + 5x^3 + 6x^2 - 5x + 48; f(3)$$

$$A) 708$$

$$B) 264$$

$$C) 1152$$

$$D) 1734$$

$$4) f(x) = x^5 + 8x^4 + 2x^3 + 4; f(-2)$$

$$A) 84$$

$$B) -84$$

$$C) 24$$

$$D) 116$$

$$5) f(x) = x^4 + 5x^3 - 6x^2 - 2x - 8; f\left(\frac{1}{2}\right)$$

$$A) -\frac{157}{16}$$

$$B) -\frac{157}{32}$$

$$C) \frac{157}{16}$$

$$D) -\frac{79}{8}$$

4 Use the Factor Theorem to Solve a Polynomial Equation

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Solve the problem.

1) Use synthetic division to divide $f(x) = x^3 + 15x^2 + 71x + 105$ by $x + 7$. Use the result to find all zeros of f .

A) $\{-7, -3, -5\}$

B) $\{-7, 3, 5\}$

C) $\{7, 3, 5\}$

D) $\{7, -3, -5\}$

2) Solve the equation $3x^3 - 28x^2 + 69x - 20 = 0$ given that 5 is a zero of $f(x) = 3x^3 - 28x^2 + 69x - 20$.

A) $\left\{5, 4, \frac{1}{3}\right\}$

B) $\left\{5, -4, -\frac{1}{3}\right\}$

C) $\left\{5, 1, \frac{4}{3}\right\}$

D) $\left\{5, -1, -\frac{4}{3}\right\}$

3) Solve the equation $12x^3 - 65x^2 + 24x + 10 = 0$ given that $\frac{2}{3}$ is a root.

A) $\left\{\frac{2}{3}, -\frac{1}{4}, 5\right\}$

B) $\left\{\frac{2}{3}, \frac{1}{4}, -5\right\}$

C) $\left\{\frac{2}{3}, \frac{5}{4}, -1\right\}$

D) $\left\{\frac{2}{3}, -\frac{5}{4}, 1\right\}$

Use synthetic division to show that the number given to the right of the equation is a solution of the equation, then solve the polynomial equation.

4) $x^3 - 5x^2 + 2x + 8 = 0$; 2

A) $\{4, -1, 2\}$

B) $\{-4, -1, 2\}$

C) $\{4, 1, 2\}$

D) $\{-4, 1, 2\}$

5) $2x^3 + 3x^2 - 14x - 15 = 0$; -3

A) $\left\{\frac{5}{2}, -1, -3\right\}$

B) $\left\{-\frac{5}{2}, -1, -3\right\}$

C) $\left\{\frac{5}{2}, 1, -3\right\}$

D) $\left\{-\frac{1}{2}, 5, -3\right\}$

6) $3x^3 - 10x^2 - 13x + 20 = 0$; 4

A) $\left\{-\frac{5}{3}, 1, 4\right\}$

B) $\left\{\frac{5}{3}, 1, 4\right\}$

C) $\left\{-\frac{5}{3}, -1, 4\right\}$

D) $\left\{\frac{1}{3}, -5, 4\right\}$

7) $5x^3 - 21x^2 + 10x + 24 = 0$; 2

A) $\left\{-\frac{4}{5}, 3, 2\right\}$

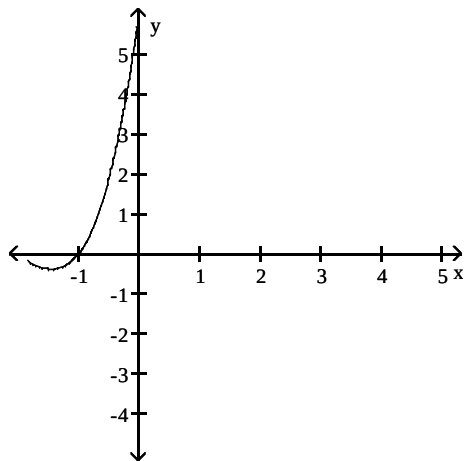
B) $\left\{\frac{4}{5}, 3, 2\right\}$

C) $\left\{-\frac{4}{5}, -3, 2\right\}$

D) $\left\{\frac{3}{5}, -4, 2\right\}$

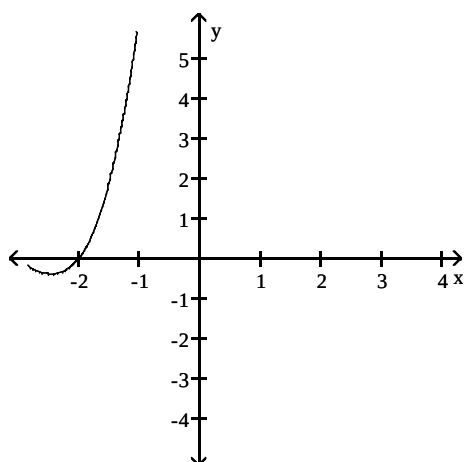
Use the graph or table to determine a solution of the equation. Use synthetic division to verify that this number is a solution of the equation. Then solve the polynomial equation.

8) $x^3 + 6x^2 + 11x + 6 = 0$



- A) -1; The remainder is zero; -1, -2, and -3, or $\{-3, -2, -1\}$
- B) -1; The remainder is zero; 1, -2, and -3, or $\{-3, -2, 1\}$
- C) -1; The remainder is zero; -1, 2, and -3, or $\{-3, -1, 2\}$
- D) -1; The remainder is zero; -1, -2, and 3, or $\{-2, -1, 3\}$

9) $x^3 + 9x^2 + 26x + 24 = 0$



- A) -2; The remainder is zero; -2, -3, and -4, or $\{-4, -3, -2\}$
- B) -2; The remainder is zero; 2, -3, and -4, or $\{-4, -3, 2\}$
- C) -2; The remainder is zero; -2, 3, and -4, or $\{-4, -2, 3\}$
- D) -2; The remainder is zero; -2, -3, and 4, or $\{-3, -2, 4\}$

10) $2x^3 + 11x^2 + 17x + 6 = 0$

x	y1
-2	0
-1	-2
0	6
1	36
2	100
3	210

- A) -2; The remainder is zero; -3, -2, and $-\frac{1}{2}$, or $\left\{-3, -2, -\frac{1}{2}\right\}$
- B) -2; The remainder is zero; 3, -2, and $-\frac{1}{2}$, or $\left\{-2, -\frac{1}{2}, 3\right\}$
- C) -2; The remainder is zero; -3, 2, and $-\frac{1}{2}$, or $\left\{-3, -\frac{1}{2}, 2\right\}$
- D) -2; The remainder is zero; -3, -2, and $\frac{1}{2}$, or $\left\{-3, -2, \frac{1}{2}\right\}$

2.5 Zeros of Polynomial Functions

1 Use the Rational Zero Theorem to Find Possible Rational Zeros

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Use the Rational Zero Theorem to list all possible rational zeros for the given function.

1) $f(x) = x^5 - 4x^2 + 6x + 5$

A) $\pm 1, \pm 5$

B) $\pm 1, \pm \frac{1}{5}$

C) $\pm \frac{1}{4}, \pm \frac{5}{4}, \pm 5$

D) $\pm 5, \pm \frac{1}{5}$

2) $f(x) = x^5 - 2x^2 + 2x + 14$

A) $\pm 1, \pm 7, \pm 2, \pm 14$

B) $\pm 1, \pm \frac{1}{7}, \pm \frac{1}{2}, \pm \frac{1}{14}$

C) $\pm 1, \pm \frac{1}{7}, \pm \frac{1}{2}, \pm \frac{1}{14}, \pm 7, \pm 2, \pm 14$

D) $\pm 1, \pm 7, \pm 2$

3) $f(x) = x^4 + 7x^3 - 5x^2 + 2x - 12$

A) $\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12$

B) $\pm 1, \pm \frac{1}{2}, \pm \frac{1}{3}, \pm \frac{1}{4}, \pm \frac{1}{6}, \pm \frac{1}{12}$

C) $\pm \frac{1}{2}, \pm \frac{1}{3}, \pm \frac{1}{4}, \pm \frac{1}{6}, \pm \frac{1}{12}, \pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12$

D) $\pm \frac{1}{12}, \pm 1, \pm 12$

4) $f(x) = -2x^3 + 4x^2 - 2x + 8$

A) $\pm \frac{1}{2}, \pm 1, \pm 2, \pm 4, \pm 8$

B) $\pm \frac{1}{4}, \pm \frac{1}{2}, \pm 1, \pm 2, \pm 4, \pm 8$

C) $\pm \frac{1}{8}, \pm \frac{1}{4}, \pm \frac{1}{2}, \pm 1, \pm 2, \pm 4, \pm 8$

D) $\pm \frac{1}{2}, \pm 1, \pm 2, \pm 4$

5) $f(x) = 7x^3 - x^2 + 3$

A) $\pm \frac{1}{7}, \pm \frac{3}{7}, \pm 1, \pm 3$

C) $\pm \frac{1}{7}, \pm \frac{3}{7}, \pm 1, \pm 3, \pm 7$

B) $\pm \frac{1}{3}, \pm \frac{7}{3}, \pm 1, \pm 7$

D) $\pm \frac{1}{7}, \pm \frac{1}{3}, \pm 1, \pm 3, \pm 7$

6) $f(x) = 6x^4 + 2x^3 - 4x^2 + 2$

A) $\pm \frac{1}{6}, \pm \frac{1}{3}, \pm \frac{1}{2}, \pm \frac{2}{3}, \pm 1, \pm 2$

C) $\pm \frac{1}{6}, \pm \frac{1}{3}, \pm \frac{1}{2}, \pm 1, \pm 2$

B) $\pm \frac{1}{6}, \pm \frac{1}{3}, \pm \frac{1}{2}, \pm \frac{2}{3}, \pm 1, \pm 2, \pm 3$

D) $\pm \frac{1}{2}, \pm \frac{3}{2}, \pm 1, \pm 2, \pm 3, \pm 6$

7) $f(x) = -4x^4 + 4x^2 - 2x + 6$

A) $\pm \frac{1}{4}, \pm \frac{1}{2}, \pm \frac{3}{4}, \pm \frac{3}{2}, \pm 1, \pm 2, \pm 3, \pm 6$

C) $\pm \frac{1}{4}, \pm \frac{1}{2}, \pm \frac{3}{4}, \pm \frac{3}{2}, \pm 1, \pm 2, \pm 3, \pm 4, \pm 6$

B) $\pm \frac{1}{6}, \pm \frac{1}{2}, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{4}{3}, \pm 1, \pm 2, \pm 4$

D) $\pm \frac{1}{4}, \pm \frac{1}{2}, \pm \frac{2}{3}, \pm \frac{3}{4}, \pm \frac{3}{2}, \pm 1, \pm 2, \pm 3, \pm 6$

8) $f(x) = 2x^5 - 2x^2 + 6x - 1$

A) $\pm 1, \pm \frac{1}{2}$

B) $\pm 1, \pm 2$

C) $\pm 1, \pm 2, \pm \frac{1}{2}$

D) $\pm 2, \pm \frac{1}{2}$

9) $f(x) = 6x^4 + 3x^3 - 3x^2 + 3x - 5$

A) $\pm 1, \pm 5, \pm \frac{1}{2}, \pm \frac{5}{2}, \pm \frac{1}{3}, \pm \frac{5}{3}, \pm \frac{1}{6}, \pm \frac{5}{6}$

C) $\pm 1, \pm 2, \pm 3, \pm 6, \pm \frac{1}{2}, \pm \frac{5}{2}, \pm \frac{1}{3}, \pm \frac{5}{3}, \pm \frac{1}{6}, \pm \frac{5}{6}$

B) $\pm 1, \pm 2, \pm 3, \pm 6, \pm \frac{1}{5}, \pm \frac{2}{5}, \pm \frac{3}{5}, \pm \frac{6}{5}$

D) $\pm 1, \pm 5, \pm \frac{1}{5}, \pm \frac{2}{5}, \pm \frac{3}{5}, \pm \frac{6}{5}$

10) $f(x) = 3x^4 + 7x^3 - 3x^2 + 5x - 12$

A) $\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{4}{3}$

B) $\pm 1, \pm 3, \pm \frac{1}{2}, \pm \frac{3}{2}, \pm \frac{1}{3}, \pm \frac{1}{4}, \pm \frac{3}{4}, \pm \frac{1}{6}, \pm \frac{1}{12}$

C) $\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12, \pm \frac{1}{2}, \pm \frac{3}{2}, \pm \frac{1}{3}, \pm \frac{1}{4}, \pm \frac{3}{4}, \pm \frac{1}{6}, \pm \frac{1}{12}$

D) $\pm 1, \pm 2, \pm 3, \pm 6, \pm 12, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{3}{4}$

2 Find Zeros of a Polynomial Function

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find a rational zero of the polynomial function and use it to find all the zeros of the function.

1) $f(x) = x^3 + 2x^2 - 5x - 6$

A) $\{-3, -1, 2\}$

B) $\{-2, 1, 3\}$

C) $\{-3\}$

D) $\{-1\}$

2) $f(x) = 2x^3 - 9x^2 + 7x + 6$

A) $\left\{-\frac{1}{2}, 2, 3\right\}$

B) $\left\{\frac{1}{2}, 2, -3\right\}$

C) $\left\{\frac{3}{2}, -1, 2\right\}$

D) $\left\{-\frac{3}{2}, -1, -2\right\}$

3) $f(x) = x^3 + 6x^2 - x - 6$

A) $\{1, -1, -6\}$

B) $\{-1, 2, 3\}$

C) $\{1, 2, -3\}$

D) $\{1, -1, 6\}$

4) $f(x) = x^3 - 8x^2 + 16x - 8$

A) $\{2, 3 + \sqrt{5}, 3 - \sqrt{5}\}$

C) $\{-2, 6 + \sqrt{5}, 6 - \sqrt{5}\}$

B) $\{1, -1, 8\}$

D) $\{2, 6 + \sqrt{8}, 6 - \sqrt{8}\}$

5) $f(x) = x^3 + 8x^2 + 25x + 26$

A) $\{-2, -3 + 2i, -3 - 2i\}$

C) $\{2, -3 + \sqrt{2}, -6 - \sqrt{2}\}$

B) $\{-2, 2 + 3i, 2 - 3i\}$

D) $\{-2, 2 + \sqrt{2}, 2 - \sqrt{2}\}$

6) $f(x) = 3x^3 - x^2 - 9x + 3$

A) $\{\frac{1}{3}, \sqrt{3}, -\sqrt{3}\}$

B) $\{-\frac{1}{3}, \sqrt{3}, -\sqrt{3}\}$

C) $\{3, \sqrt{3}, -\sqrt{3}\}$

D) $\{-3, \sqrt{3}, -\sqrt{3}\}$

7) $f(x) = x^4 + 3x^3 - 5x^2 - 9x - 2$

A) $\{-1, 2, -2 + \sqrt{3}, -2 - \sqrt{3}\}$

C) $\{-1, 3, -2 + \sqrt{5}, -2 - \sqrt{5}\}$

B) $\{1, -2, -2 + \sqrt{3}, -2 - \sqrt{3}\}$

D) $\{-1, -2, -2 + \sqrt{5}, -2 - \sqrt{5}\}$

8) $f(x) = x^4 - 9x^3 + 48x^2 - 78x - 136$

A) $\{-1, 4, 3 + 5i, 3 - 5i\}$

C) $\{-1, 4, 3 + 6i, 3 - 6i\}$

B) $\{1, -4, 3 + 5i, 3 - 5i\}$

D) $\{1, -4, 3 + \sqrt{5}, 3 - \sqrt{5}\}$

9) $f(x) = 2x^4 - 17x^3 + 59x^2 - 83x + 39$

A) $\{1, \frac{3}{2}, 3 + 2i, 3 - 2i\}$

C) $\{1, -\frac{3}{2}, 2 + 3i, 2 - 3i\}$

B) $\{-1, -\frac{3}{2}, 2 + 3i, 2 - 3i\}$

D) $\{-1, \frac{3}{2}, 3 + 2i, 3 - 2i\}$

10) $f(x) = 2x^4 + 19x^3 + 71x^2 + 109x + 39$

A) $\{-3, -\frac{1}{2}, -3 + 2i, -3 - 2i\}$

C) $\{-3, +\frac{1}{2}, -2 + 3i, -2 - 3i\}$

B) $\{3, +\frac{1}{2}, -2 + 3i, -2 - 3i\}$

D) $\{3, -\frac{1}{2}, -3 + 2i, -3 - 2i\}$

3 Solve Polynomial Equations

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Solve the polynomial equation. In order to obtain the first root, use synthetic division to test the possible rational roots.

1) $x^3 + 2x^2 - 5x - 6 = 0$

A) $\{-3, -1, 2\}$

B) $\{-2, 1, 3\}$

C) $\{-3\}$

D) $\{-1\}$

2) $4x^3 - 23x^2 + 26x + 8 = 0$

A) $\left\{-\frac{1}{4}, 2, 4\right\}$

B) $\left\{\frac{1}{4}, 2, -4\right\}$

C) $\{1, -1, 2\}$

D) $\{-1, -1, -2\}$

3) $x^3 + 6x^2 - x - 6 = 0$

A) $\{1, -1, -6\}$

B) $\{-1, 2, 3\}$

C) $\{1, 2, -3\}$

D) $\{1, -1, 6\}$

4) $x^3 - 6x^2 + 7x + 2 = 0$

A) $\{2, 2 + \sqrt{5}, 2 - \sqrt{5}\}$

C) $\{-2, 4 + \sqrt{5}, 4 - \sqrt{5}\}$

B) $\{1, -1, -2\}$

D) $\{2, 4 + \sqrt{2}, 4 - \sqrt{2}\}$

5) $x^3 + 7x^2 + 19x + 13 = 0$

A) $\{-1, -3 + 2i, -3 - 2i\}$

C) $\{1, -3 + \sqrt{5}, -6 - \sqrt{5}\}$

B) $\{-1, 2 + 3i, 2 - 3i\}$

D) $\{-1, 2 + \sqrt{5}, 2 - \sqrt{5}\}$

6) $x^3 + 7x^2 - 16x + 18 = 0$

A) $\{1 + i, 1 - i, -9\}$

B) $\{1 + i, 1 - i, 9\}$

C) $\{-9, 9\}$

D) $\{1 + i, 1 - i, 9i\}$

7) $2x^3 - x^2 - 12x + 6 = 0$

A) $\{\frac{1}{2}, \sqrt{6}, -\sqrt{6}\}$

B) $\{-\frac{1}{2}, \sqrt{6}, -\sqrt{6}\}$

C) $\{2, \sqrt{6}, -\sqrt{6}\}$

D) $\{-2, \sqrt{6}, -\sqrt{6}\}$

8) $x^4 + 2x^3 - 10x^2 - 14x - 3 = 0$

A) $\{-1, 3, -2 + \sqrt{3}, -2 - \sqrt{3}\}$

C) $\{-1, 4, -2 + \sqrt{5}, -2 - \sqrt{5}\}$

B) $\{1, -3, -2 + \sqrt{3}, -2 - \sqrt{3}\}$

D) $\{-1, -3, -2 + \sqrt{5}, -2 - \sqrt{5}\}$

9) $x^4 - 5x^3 + 28x^2 - 70x - 104 = 0$

A) $\{-1, 4, 1 + 5i, 1 - 5i\}$

C) $\{-1, 4, 1 + 6i, 1 - 6i\}$

B) $\{1, -4, 1 + 5i, 1 - 5i\}$

D) $\{1, -4, 1 + \sqrt{5}, 1 - \sqrt{5}\}$

10) $2x^4 - 19x^3 + 74x^2 - 127x + 78 = 0$

A) $\{2, \frac{3}{2}, 3 + 2i, 3 - 2i\}$

C) $\{2, -\frac{3}{2}, 2 + 3i, 2 - 3i\}$

B) $\{-2, -\frac{3}{2}, 2 + 3i, 2 - 3i\}$

D) $\{-2, \frac{3}{2}, 3 + 2i, 3 - 2i\}$

11) $3x^4 + 16x^3 + 56x^2 + 56x + 13 = 0$

A) $\{-1, -\frac{1}{3}, -2 + 3i, -2 - 3i\}$

C) $\{-1, +\frac{1}{3}, -3 + 2i, -3 - 2i\}$

B) $\{1, +\frac{1}{3}, -3 + 2i, -3 - 2i\}$

D) $\{1, -\frac{1}{3}, -2 + 3i, -2 - 3i\}$

Solve the problem.

- 12) The concentration, in parts per million, of a particular drug in a patient's blood x hours after the drug is administered is given by the function

$$f(x) = -x^4 + 9x^3 - 27x^2 + 35x$$

How many hours after the drug is administered will it be eliminated from the bloodstream.

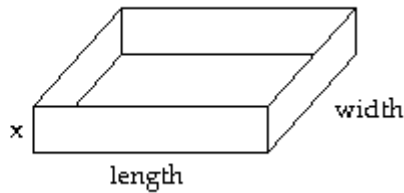
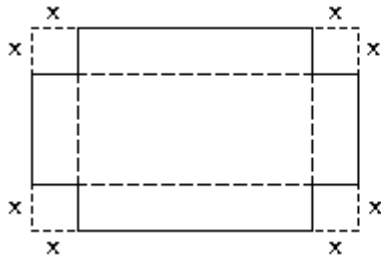
A) 5 hours

B) 7 hours

C) 3 hours

D) 12 hours

- 13) A box with an open top is formed by cutting squares out of the corners of a rectangular piece of cardboard and then folding up the sides. If x represents the length of the side of the square cut from each corner, and if the original piece of cardboard is 16 inches by 9 inches, what size square must be cut if the volume of the box is to be 120 cubic inches?



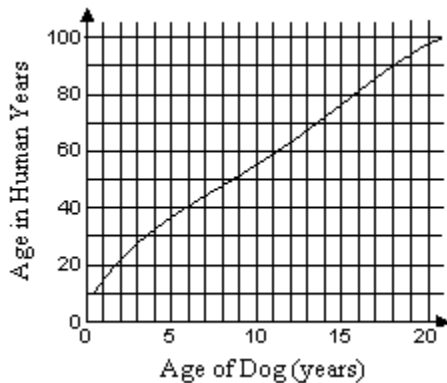
- A) 2 in. by 2 in. square
C) 12 in. by 12 in. square

- B) 3 in. by 3 in. square
D) 5 in. by 5 in. square

- 14) The polynomial function

$$H(x) = -0.001183x^4 + 0.05495x^3 - 0.8523x^2 + 9.054x + 6.748$$

models the age in human years, $H(x)$, of a dog that is x years old, where $x \geq 1$. Using the graph of this function shown below, what is the approximately equivalent dog age for a person who is 30?



A) 3.5 years

B) 4 years

C) 2.5 years

D) 5 years

4 Use the Linear Factorization Theorem to Find Polynomials with Given Zeros

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find an n th degree polynomial function with real coefficients satisfying the given conditions.

- 1) $n = 3$; 3 and i are zeros; $f(2) = 25$

A) $f(x) = -5x^3 + 15x^2 - 5x + 15$

B) $f(x) = 5x^3 - 15x^2 + 5x - 15$

C) $f(x) = 5x^3 - 15x^2 - 5x + 15$

D) $f(x) = -5x^3 + 15x^2 + 5x - 15$

- 2) $n = 3$; -4 and i are zeros; $f(-3) = 60$

A) $f(x) = 6x^3 + 24x^2 + 6x + 24$

B) $f(x) = 6x^3 + 24x^2 - 6x - 24$

C) $f(x) = -6x^3 - 24x^2 - 6x - 24$

D) $f(x) = -6x^3 - 24x^2 + 6x + 24$

- 3) $n = 3$; 2 and $-3 + 3i$ are zeros; leading coefficient is 1

A) $f(x) = x^3 + 4x^2 + 6x - 36$

B) $f(x) = x^3 - 4x^2 + 6x - 36$

C) $f(x) = x^3 + 4x^2 + 15x - 36$

D) $f(x) = x^3 + 5x^2 + 6x - 14$

4) $n = 4$; 3 , $\frac{1}{3}$, and $1 + 2i$ are zeros; $f(1) = 48$

A) $f(x) = -6x^4 + 48x^3 - 114x^2 + 168x - 45$

C) $f(x) = -3x^4 + 48x^3 - 114x^2 + 168x - 45$

B) $f(x) = 3x^4 - 16x^3 + 38x^2 + 168x - 45$

D) $f(x) = -6x^4 + 32x^3 - 76x^2 + 112x - 30$

5) $n = 4$; $2i$, 4 , and -4 are zeros; leading coefficient is 1

A) $f(x) = x^4 - 12x^2 - 64$

C) $f(x) = x^4 + 4x^2 - 64$

B) $f(x) = x^4 + 4x^3 - 12x^2 - 64$

D) $f(x) = x^4 + 4x^2 - 4x - 64$

5 Use Descartes's Rule of Signs

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Use Descartes's Rule of Signs to determine the possible number of positive and negative real zeros for the given function.

1) $f(x) = -5x^7 + x^3 - x^2 + 9$

A) 3 or 1 positive zeros, 2 or 0 negative zeros

C) 2 or 0 positive zeros, 2 or 0 negative zeros

B) 3 or 1 positive zeros, 3 or 1 negative zeros

D) 2 or 0 positive zeros, 3 or 1 negative zeros

2) $f(x) = 7x^3 - 4x^2 + x + 3.5$

A) 2 or 0 positive zeros, 1 negative zero

C) 2 or 0 positive zeros, no negative zeros

B) 3 or 1 positive zeros, 1 negative zero

D) 3 or 1 positive zeros, 2 or 0 negative zeros

3) $f(x) = 6x^5 - 4x^2 + x + 4$

A) 2 or 0 positive zeros, 1 negative zero

C) 2 or 0 positive zeros, 1 or 0 negative zeros

B) 3 or 1 positive zeros, 3 or 1 negative zeros

D) 2 or 0 positive zeros, 2 or 0 negative zeros

4) $f(x) = x^7 + x^4 + x^2 + x + 9$

A) 0 positive zeros, 3 or 1 negative zeros

C) 0 positive zeros, 2 or 0 negative zeros

B) 0 positive zeros, 0 negative zeros

D) 0 positive zeros, 1 negative zero

5) $f(x) = x^5 - 1.5x^4 - 13.76x^3 + 3x^2 + 34.42x - 15.397$

A) 3 or 1 positive zeros, 2 or 0 negative zeros

C) 3 or 1 positive zeros, 3 or 1 negative zeros

B) 2 or 0 positive zeros, 2 or 0 negative zeros

D) 2 or 0 positive zeros, 3 or 1 negative zeros

6) $f(x) = x^2 - 4$

A) 1 positive zero, 1 negative zero

C) 0 positive zeros, 0 negative zeros

B) 1 positive zero, 0 negative zeros

D) 0 positive zeros, 1 negative zero

7) $f(x) = 6x^8 - 9x^7 + x^6 - 3x + 18$

A) 4, 2 or 0 positive zeros, no negative zeros

C) 4, 2 or 0 positive zeros, 1 negative zeros

B) 4 or 2 positive zeros, no negative zeros

D) 4 positive zeros, no negative zeros

8) $f(x) = -7x^9 - 4x^8 - 2x^7 + 6x^6 + x + 8$

A) 1 positive zero, 4, 3 or 1 negative zeros

C) 1 positive zero, 4 or 2 negative zeros

B) 1 positive zero, 2 or 0 negative zeros

D) 1 positive zero, 3 or 1 negative zeros

2.6 Rational Functions and Their Graphs

1 Find the Domains of Rational Functions

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find the domain of the rational function.

1) $h(x) = \frac{8x}{x-9}$

A) $\{x \mid x \neq 9\}$

B) $\{x \mid x \neq -9\}$

C) $\{x \mid x \neq 0\}$

D) all real numbers

2) $g(x) = \frac{8x^2}{(x+9)(x-2)}$

A) $\{x \mid x \neq -9, x \neq 2\}$

B) $\{x \mid x \neq 9, x \neq -2\}$

C) $\{x \mid x \neq -9, x \neq 2, x \neq -8\}$

D) all real numbers

3) $h(x) = \frac{x+8}{x^2-4}$

A) $\{x \mid x \neq -2, x \neq 2\}$

B) $\{x \mid x \neq -2, x \neq 2, x \neq -8\}$

C) $\{x \mid x \neq 0, x \neq 4\}$

D) all real numbers

4) $g(x) = \frac{x+9}{x^2+16}$

A) all real numbers

B) $\{x \mid x \neq -4, x \neq 4, x \neq -9\}$

C) $\{x \mid x \neq 0, x \neq -16\}$

D) $\{x \mid x \neq -4, x \neq 4\}$

5) $h(x) = \frac{x+7}{x^2+36x}$

A) $\{x \mid x \neq 0, x \neq -36\}$

B) $\{x \mid x \neq -6, x \neq 6, x \neq -7\}$

C) all real numbers

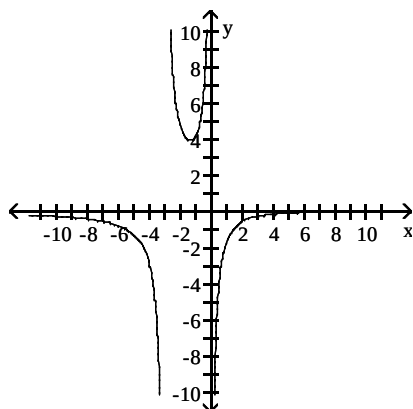
D) $\{x \mid x \neq -6, x \neq 6\}$

2 Use Arrow Notation

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Use the graph of the rational function shown to complete the statement.

1)



As $x \rightarrow -3^+$, $f(x) \rightarrow ?$

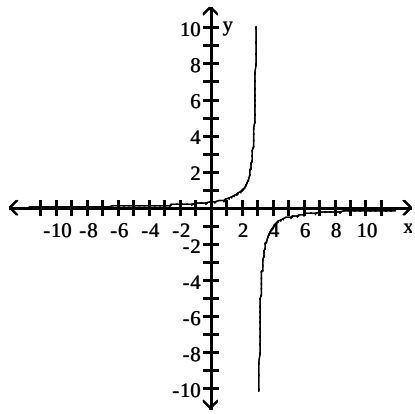
A) $+\infty$

B) $-\infty$

C) 0

D) -3

2)



As $x \rightarrow 3^+$, $f(x) \rightarrow ?$

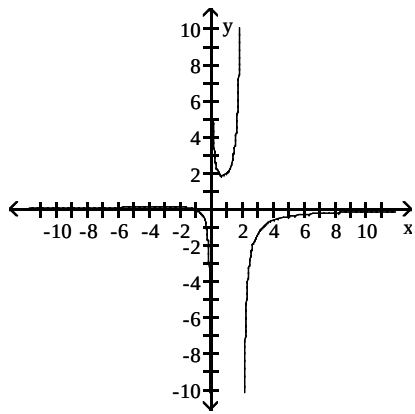
A) $-\infty$

B) $+\infty$

C) 0

D) 3

3)



As $x \rightarrow -\infty$, $f(x) \rightarrow ?$

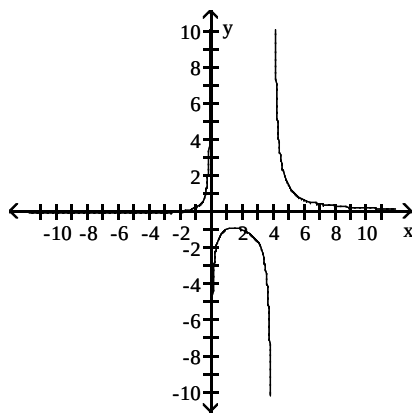
A) 0

B) $+\infty$

C) $-\infty$

D) -1

4)



As $x \rightarrow 4^-$, $f(x) \rightarrow ?$

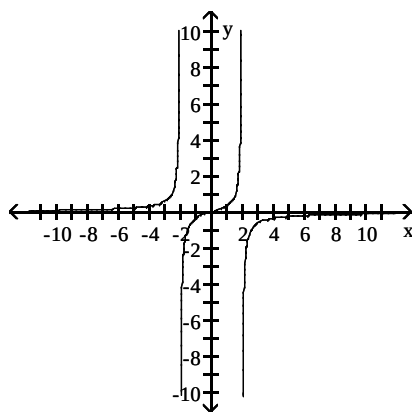
A) $-\infty$

B) $+\infty$

C) 0

D) -4

5)



As $x \rightarrow -2^+$, $f(x) \rightarrow ?$

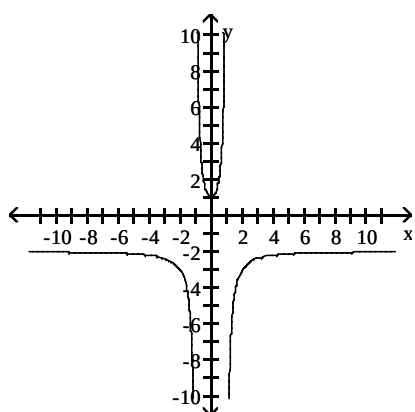
A) $-\infty$

B) $+\infty$

C) 0

D) -2

6)



As $x \rightarrow -1^+$, $f(x) \rightarrow ?$

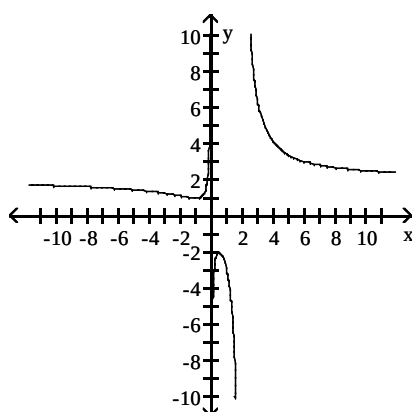
A) $+\infty$

B) $-\infty$

C) 2

D) -1

7)



As $x \rightarrow 2^-$, $f(x) \rightarrow ?$

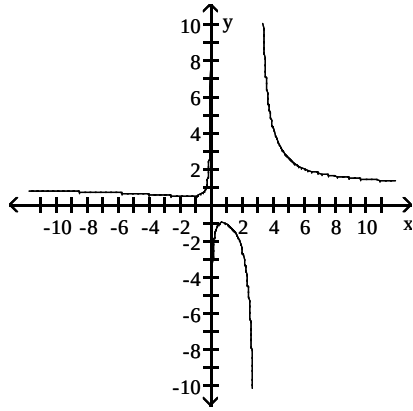
A) $-\infty$

B) $+\infty$

C) 2

D) -2

8)



As $x \rightarrow +\infty$, $f(x) \rightarrow ?$

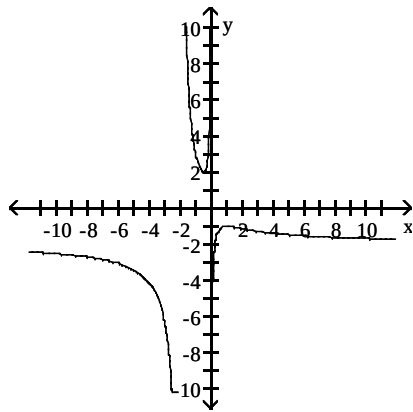
A) 1

B) $+\infty$

C) $-\infty$

D) -1

9)



As $x \rightarrow -2^-$, $f(x) \rightarrow ?$

A) $-\infty$

B) $+\infty$

C) -2

D) 2

3 Identify Vertical Asymptotes

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find the vertical asymptotes, if any, of the graph of the rational function.

1) $f(x) = \frac{x}{x+5}$

A) $x = -5$

C) $x = 0$ and $x = 5$

B) $x = 0$ and $x = -5$

D) no vertical asymptote

2) $f(x) = \frac{x-4}{x(x-4)}$

A) $x = 0$ and $x = 4$

C) $x = 4$ and $x = 4$

B) $x = 4$

D) no vertical asymptote

3) $h(x) = \frac{x}{x(x-5)}$

A) $x = 0$ and $x = 5$

C) $x = 0$ and $x = -5$

B) $x = 5$

D) no vertical asymptote

$$4) f(x) = \frac{x}{x^2 + 1}$$

A) $x = -1$

C) $x = 1$

B) $x = -1, x = 1$

D) no vertical asymptote

$$5) g(x) = \frac{x}{x^2 - 16}$$

A) $x = 4, x = -4$

C) $x = 4$

B) $x = 4, x = -4, x = 0$

D) no vertical asymptote

$$6) h(x) = \frac{x + 1}{x^2 - 1}$$

A) $x = 1$

C) $x = 1, x = -1$

B) $x = -1$

D) no vertical asymptote

$$7) \frac{x - 81}{x^2 - 8x + 15}$$

A) $x = 5, x = 3$

C) $x = 5, x = 3, x = -81$

B) $x = -5, x = -3$

D) $x = -81$

4 Identify Horizontal Asymptotes

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find the horizontal asymptote, if any, of the graph of the rational function.

$$1) f(x) = \frac{8x}{2x^2 + 1}$$

A) $y = 0$

C) $y = \frac{1}{4}$

B) $y = 4$

D) no horizontal asymptote

$$2) g(x) = \frac{10x^2}{2x^2 + 1}$$

A) $y = 5$

C) $y = \frac{1}{5}$

B) $y = 0$

D) no horizontal asymptote

$$3) h(x) = \frac{10x^3}{5x^2 + 1}$$

A) $y = 2$

C) $y = \frac{1}{2}$

B) $y = 0$

D) no horizontal asymptote

$$4) f(x) = \frac{8x}{8x + 9}$$

A) $y = 1$

C) $y = 0$

B) $y = -\frac{9}{8}$

D) no horizontal asymptote

$$5) h(x) = \frac{-3x + 5}{3x - 1}$$

A) $y = -1$

C) $y = -3$

B) $y = -5$

D) no horizontal asymptote

$$6) g(x) = \frac{3x^2 - 7x - 5}{2x^2 - 4x + 9}$$

A) $y = \frac{3}{2}$

C) $y = \frac{7}{4}$

B) $y = 0$

D) no horizontal asymptote

$$7) f(x) = \frac{-9x}{3x^3 + x^2 + 1}$$

A) $y = 0$

C) $y = -\frac{1}{3}$

B) $y = -3$

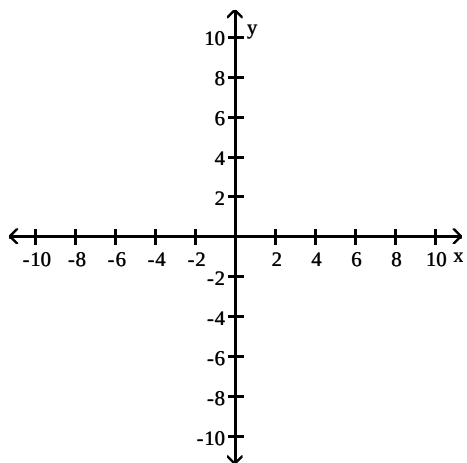
D) no horizontal asymptote

5 Use Transformations to Graph Rational Functions

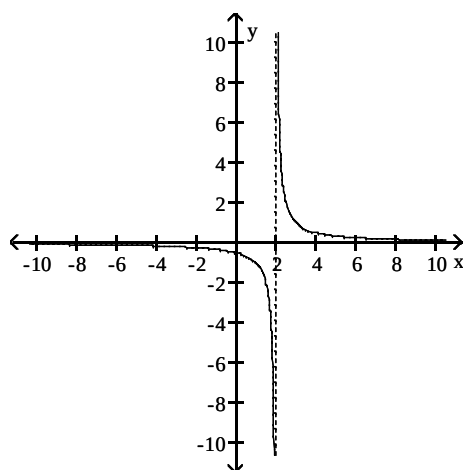
MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Use transformations of $f(x) = \frac{1}{x}$ or $f(x) = \frac{1}{x^2}$ to graph the rational function.

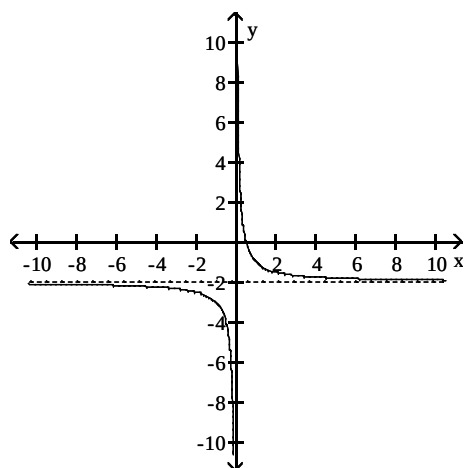
1) $g(x) = \frac{1}{x-2}$



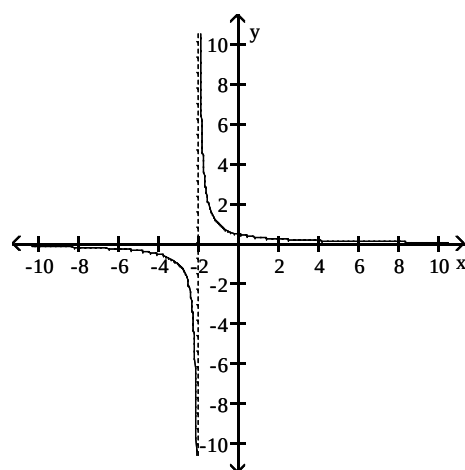
A)



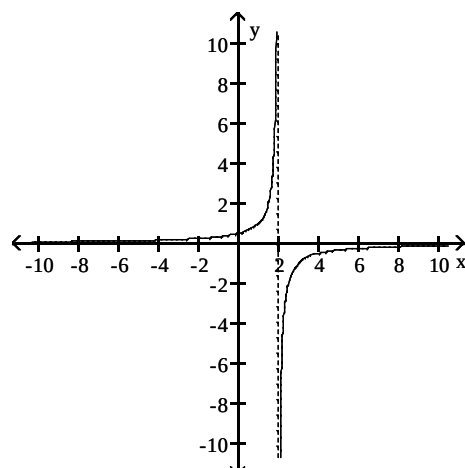
C)



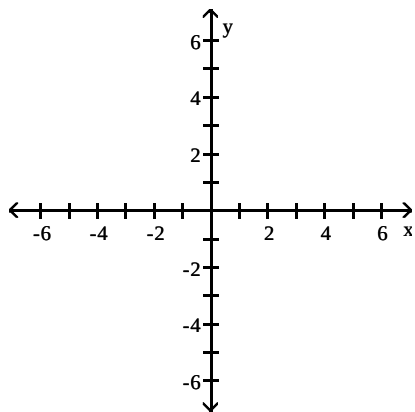
B)



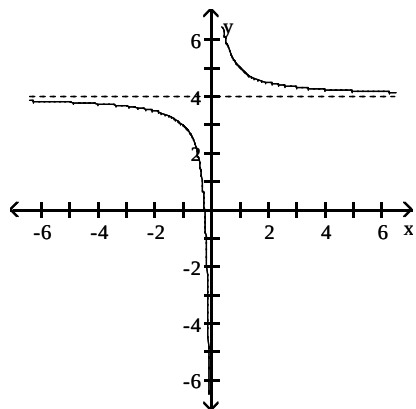
D)



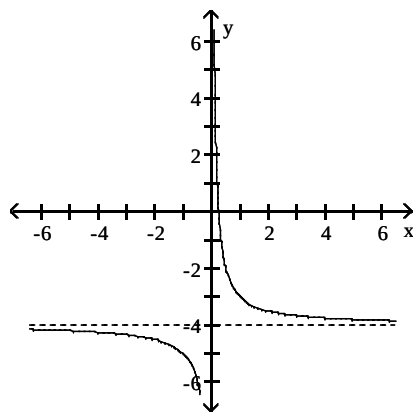
2) $f(x) = \frac{1}{x} + 4$



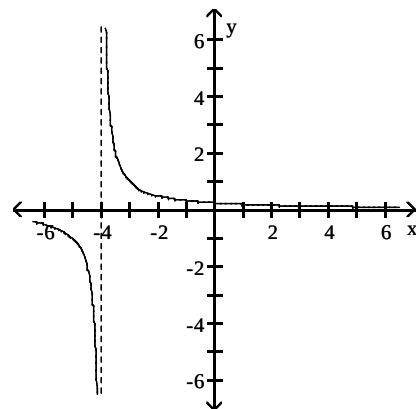
A)



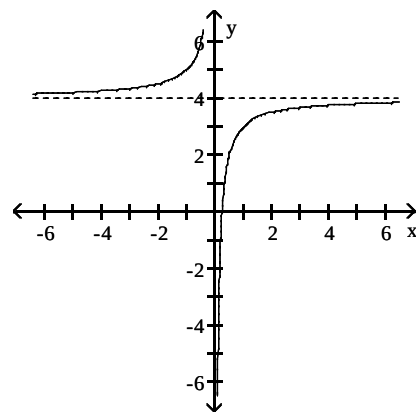
C)



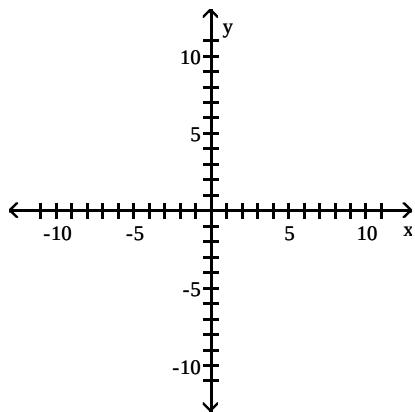
B)



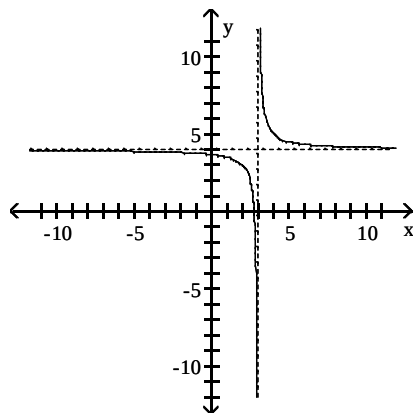
D)



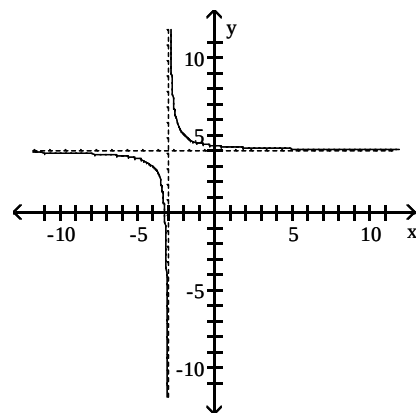
3) $f(x) = \frac{1}{x-3} + 4$



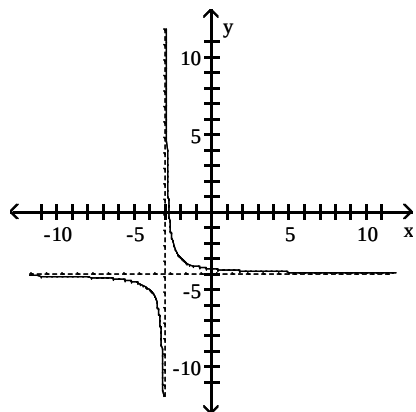
A)



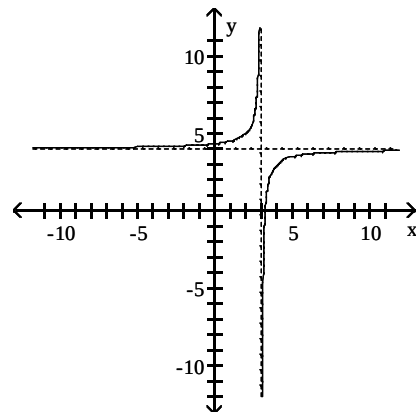
B)



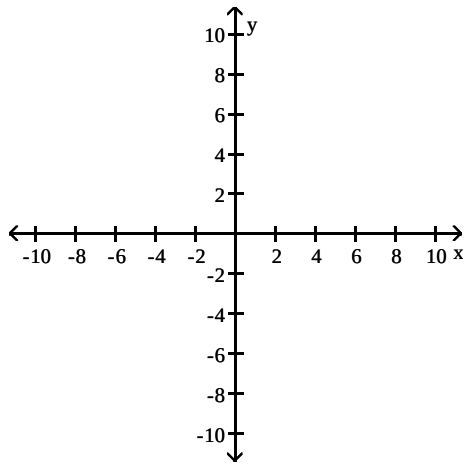
C)



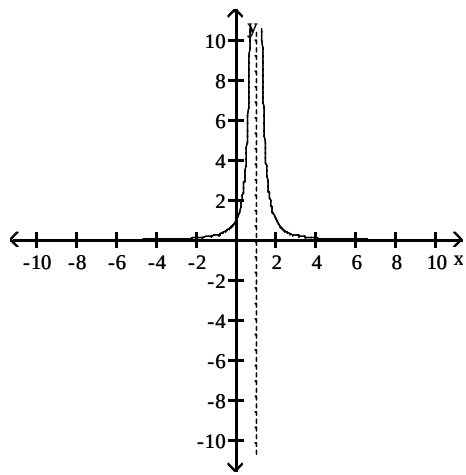
D)



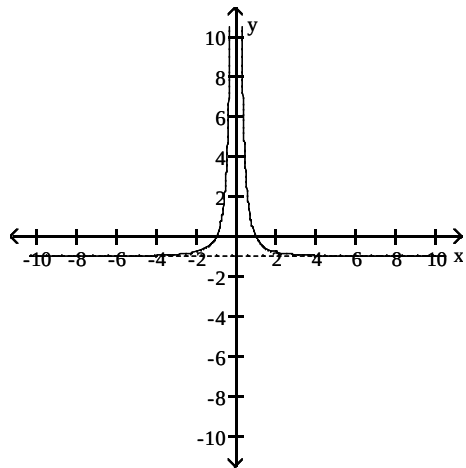
4) $f(x) = \frac{1}{(x-1)^2}$



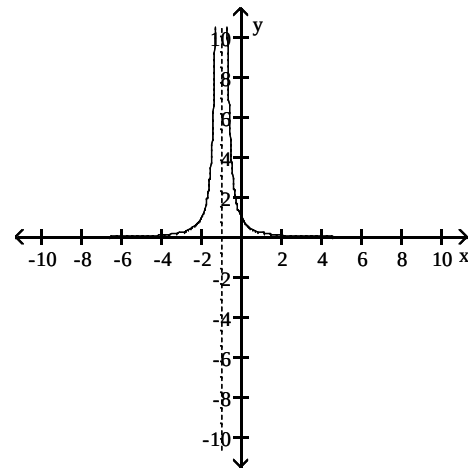
A)



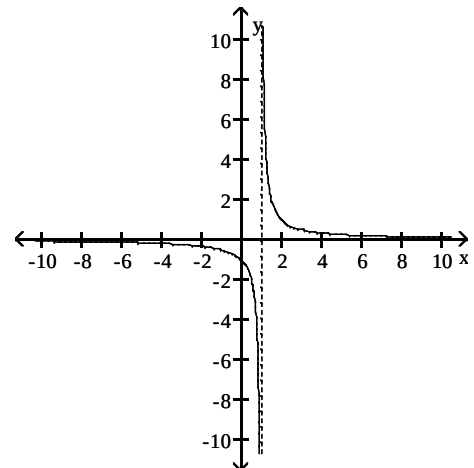
C)



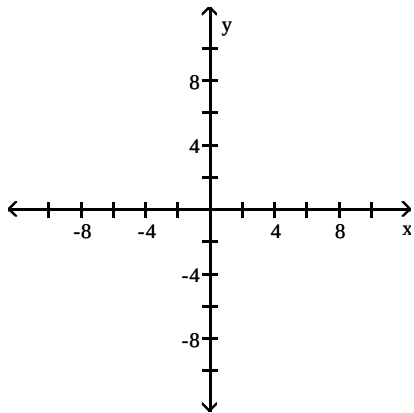
B)



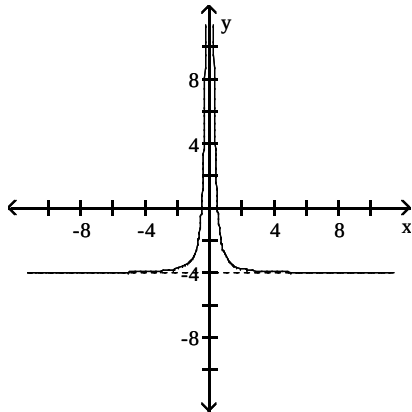
D)



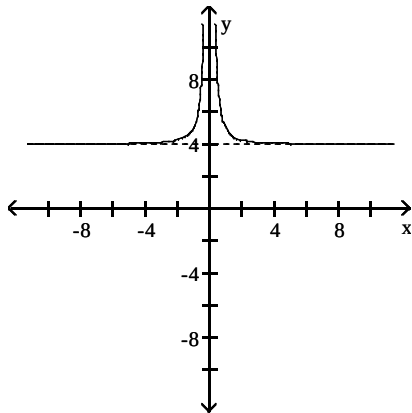
5) $f(x) = \frac{1}{x^2} - 4$



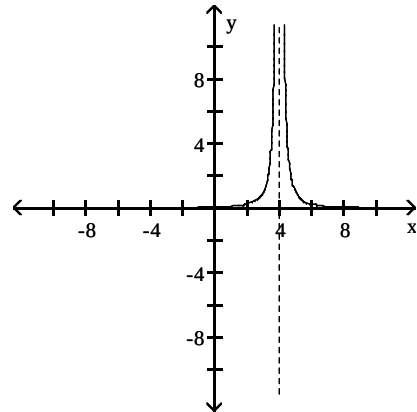
A)



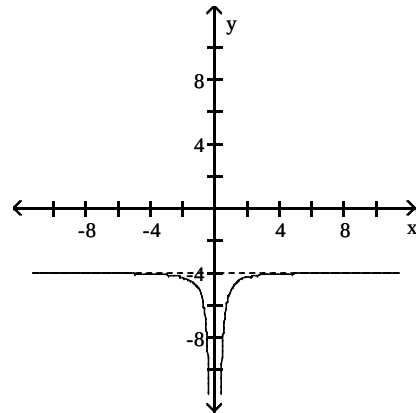
C)



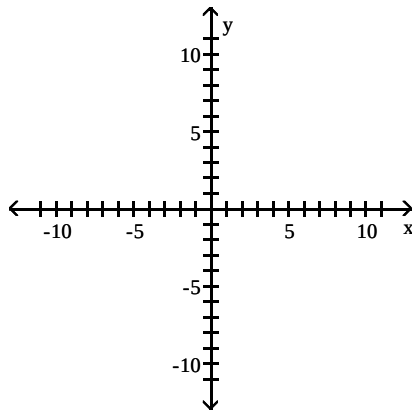
B)



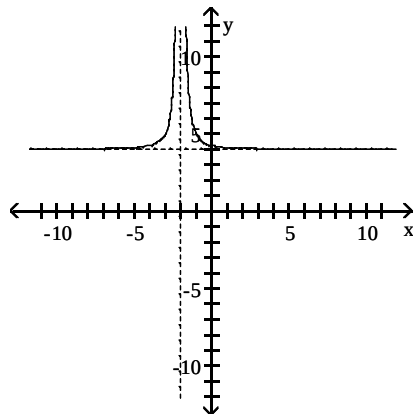
D)



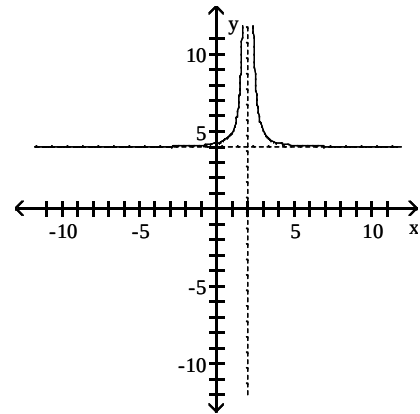
6) $f(x) = \frac{1}{(x+2)^2} + 4$



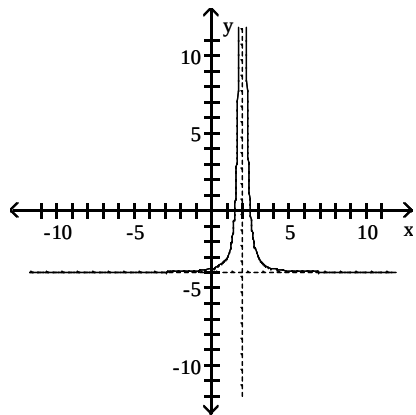
A)



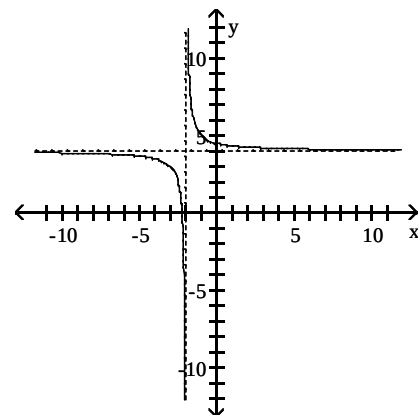
B)



C)



D)

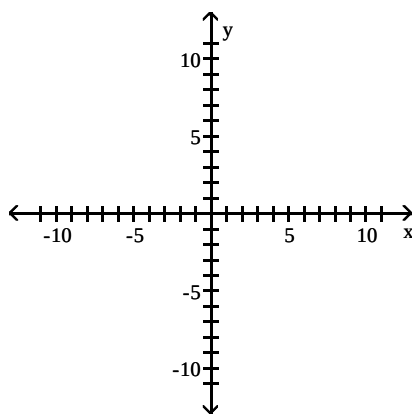


6 Graph Rational Functions

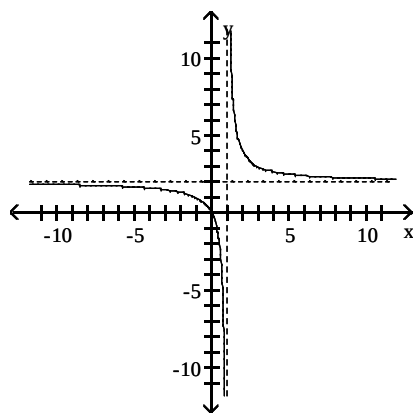
MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Graph the rational function.

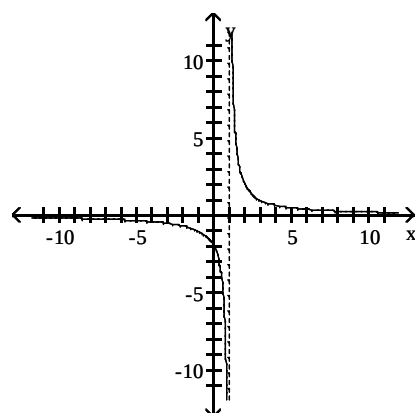
1) $f(x) = \frac{2x}{x-1}$



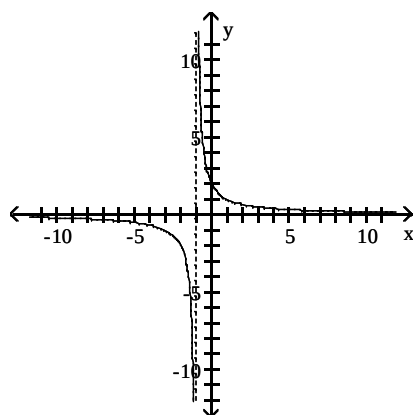
A)



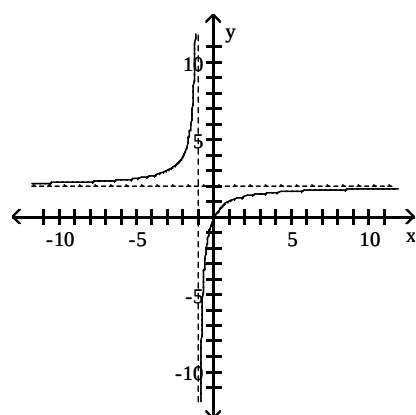
B)



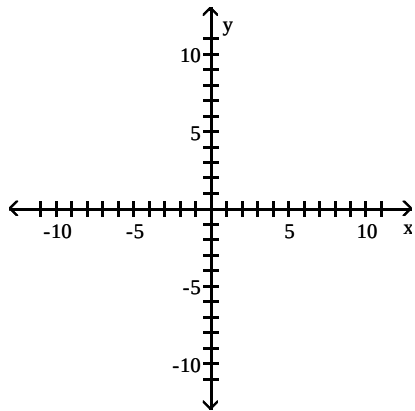
C)



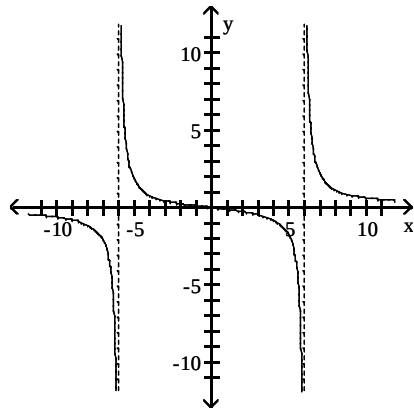
D)



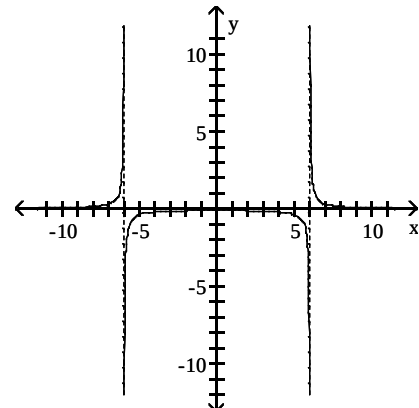
2) $f(x) = \frac{4x}{x^2 - 36}$



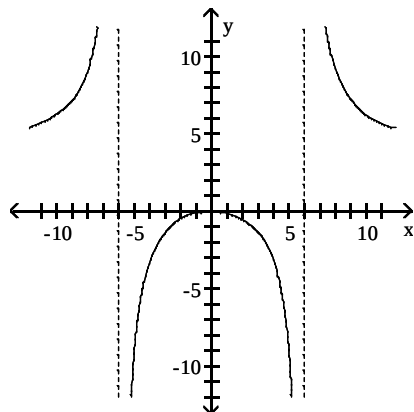
A)



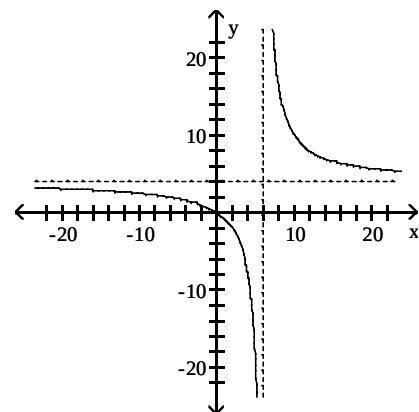
B)



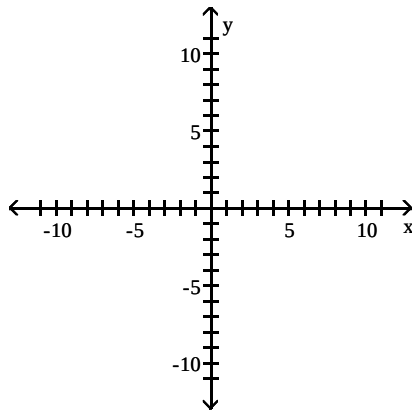
C)



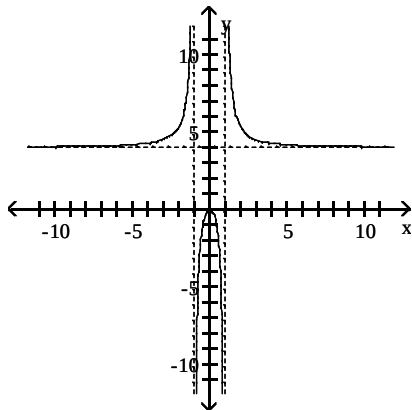
D)



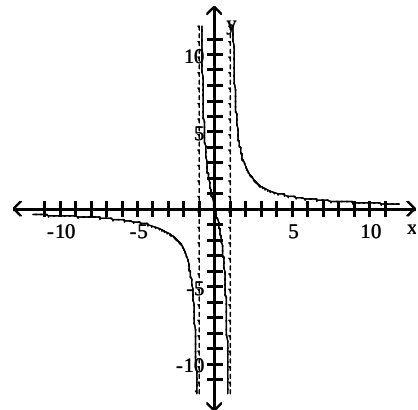
$$3) f(x) = \frac{4x^2}{x^2 - 1}$$



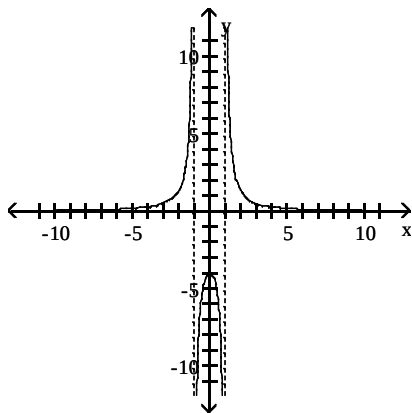
A)



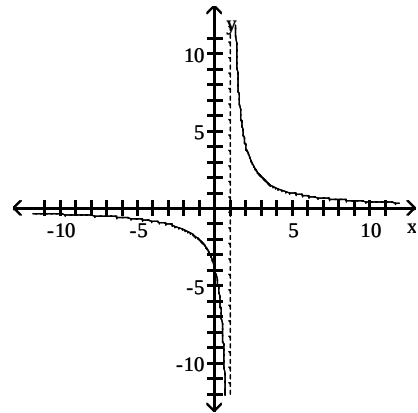
B)



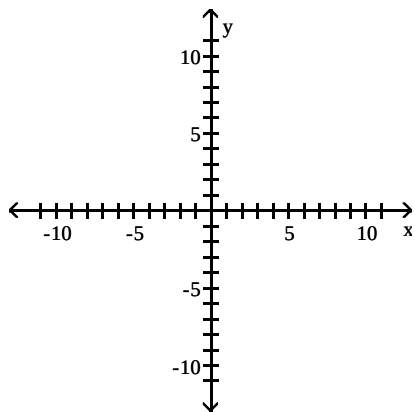
C)



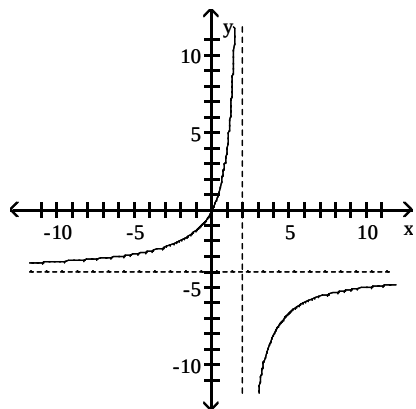
D)



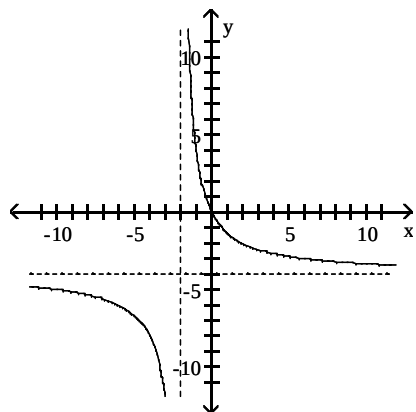
4) $f(x) = \frac{-4x}{x-2}$



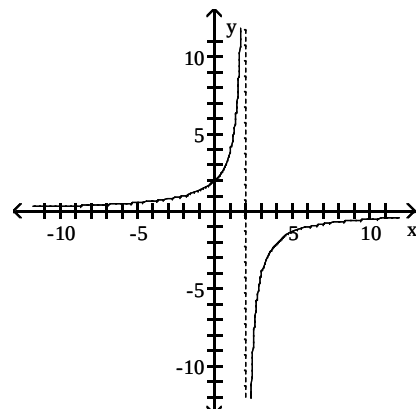
A)



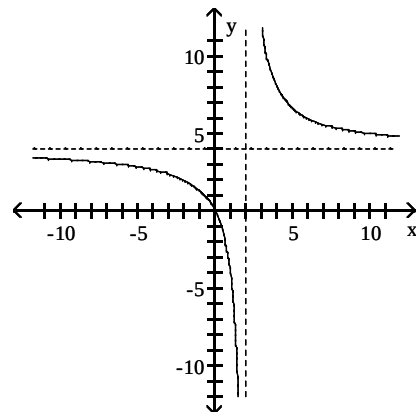
C)



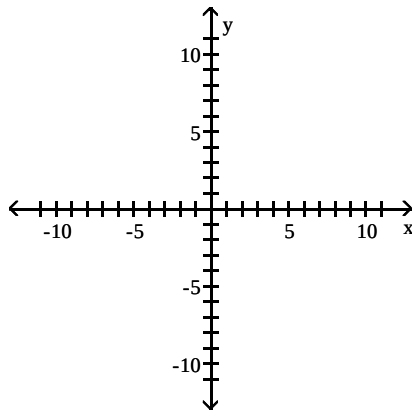
B)



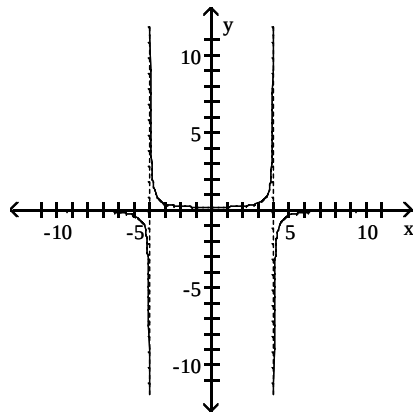
D)



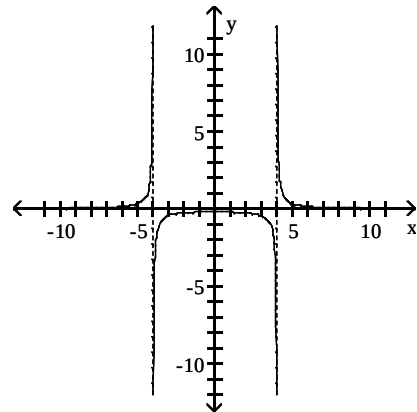
5) $f(x) = -\frac{3}{x^2 - 16}$



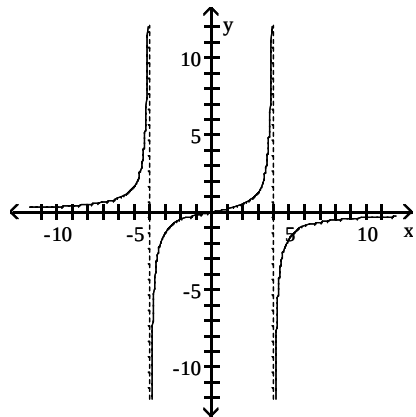
A)



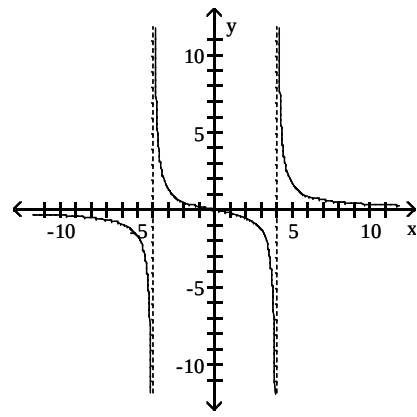
B)



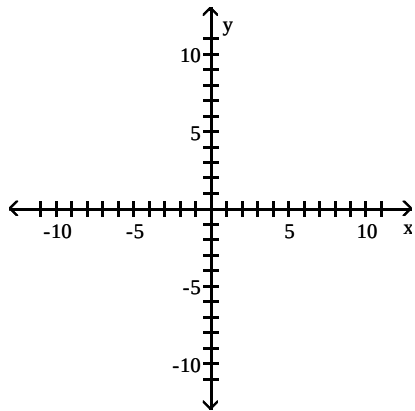
C)



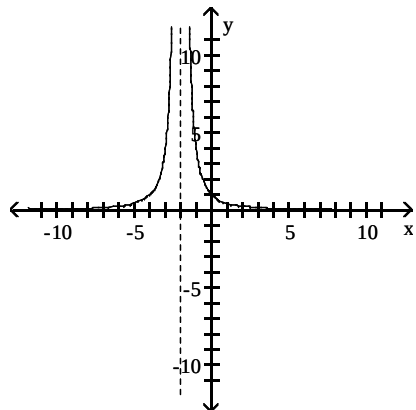
D)



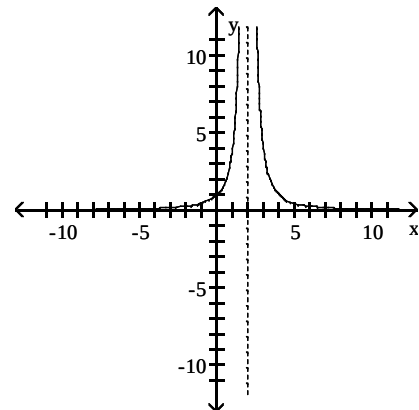
6) $f(x) = \frac{4}{x^2 + 4x + 4}$



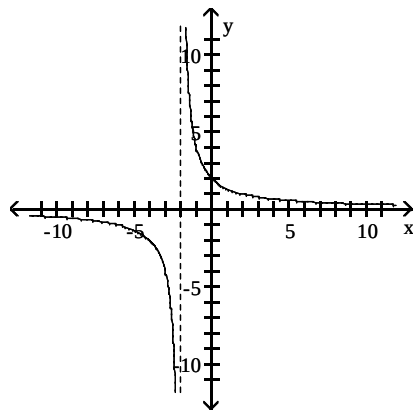
A)



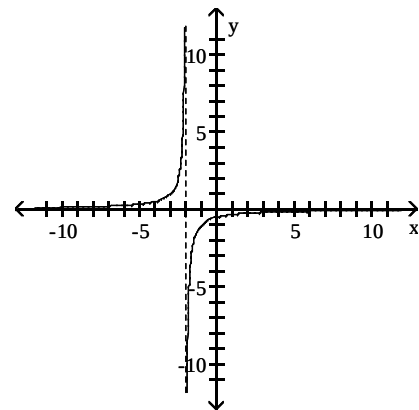
B)



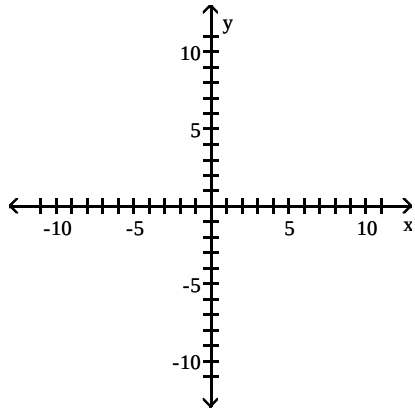
C)



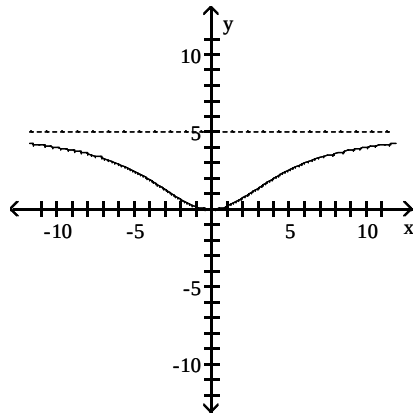
D)



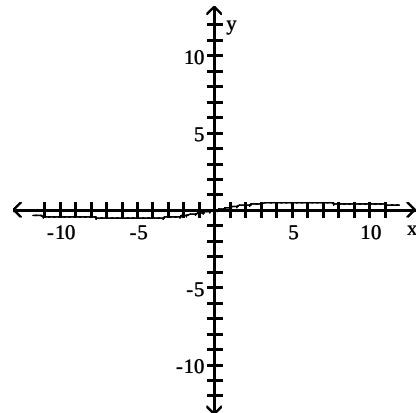
7) $f(x) = \frac{5x^2}{x^2 + 25}$



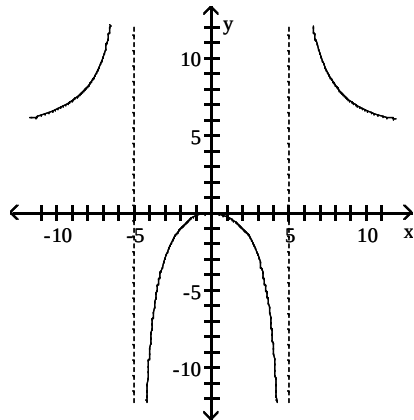
A)



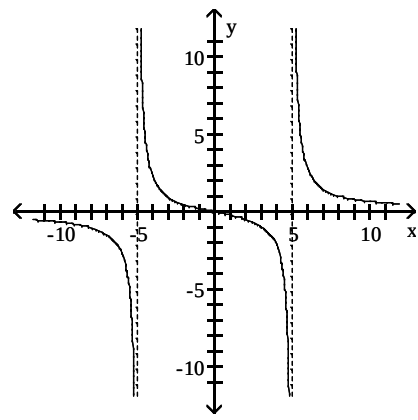
B)



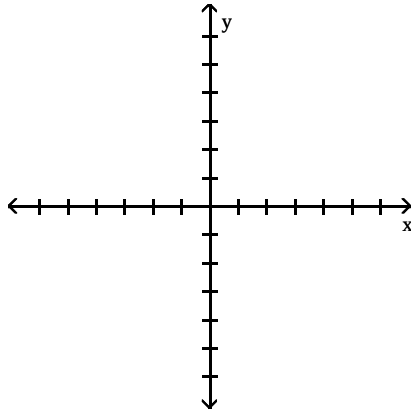
C)



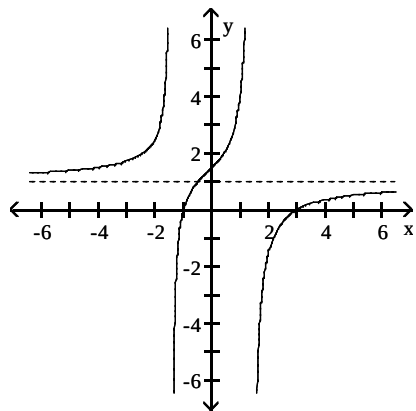
D)



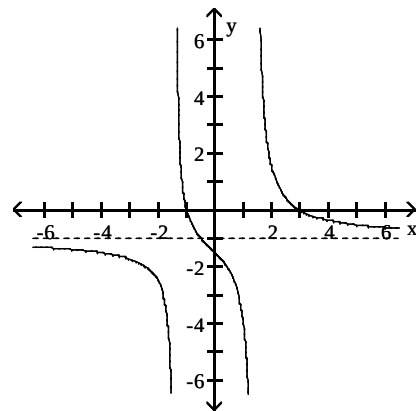
8) $f(x) = \frac{x^2 - 2x - 3}{x^2 - 2}$



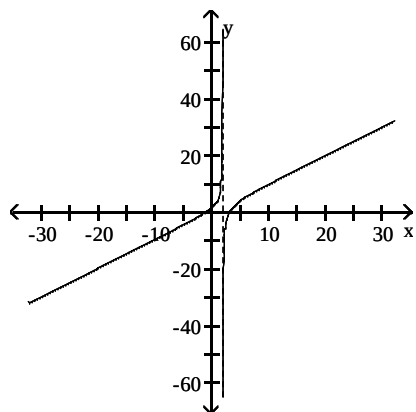
A)



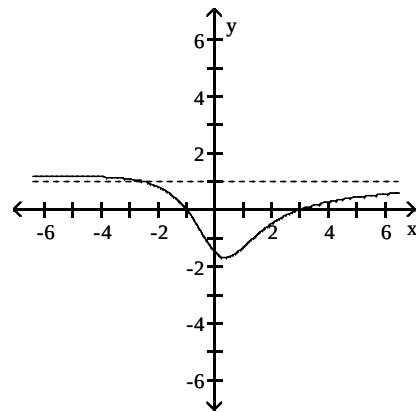
B)



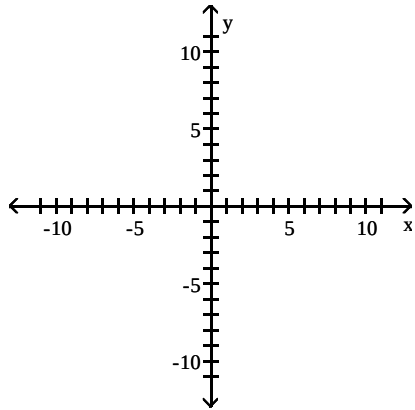
C)



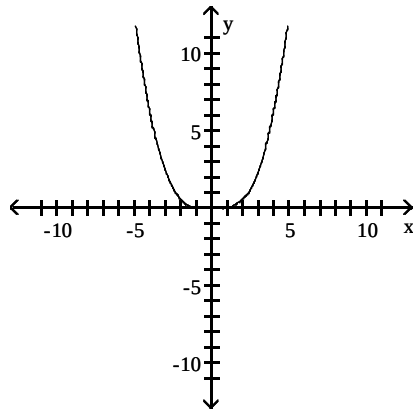
D)



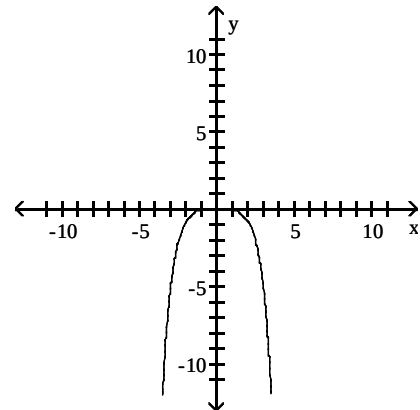
9) $f(x) = \frac{x^4}{x^2 + 25}$



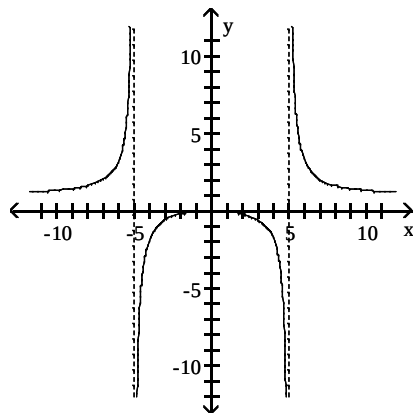
A)



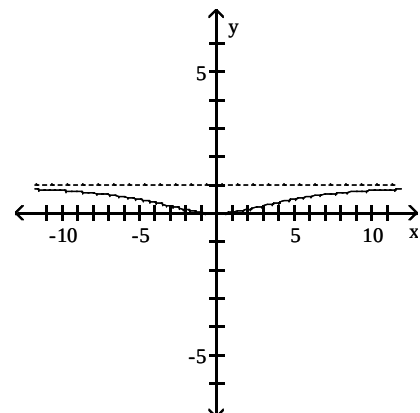
B)



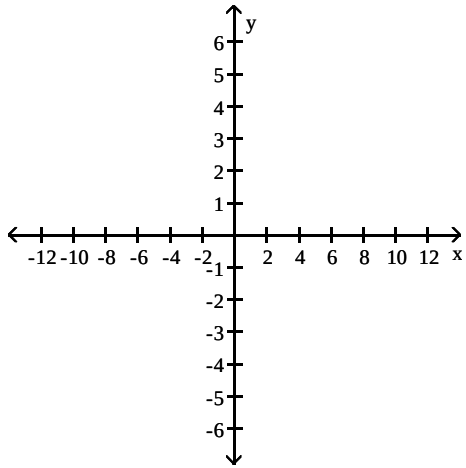
C)



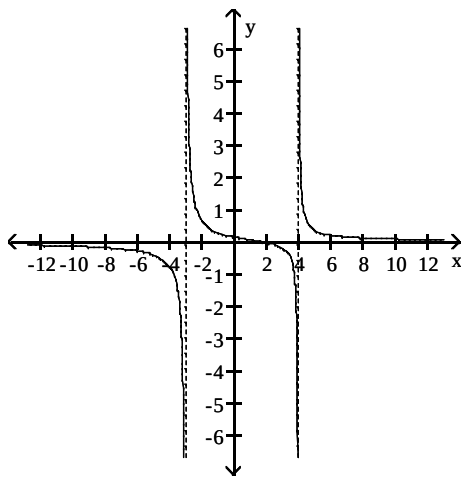
D)



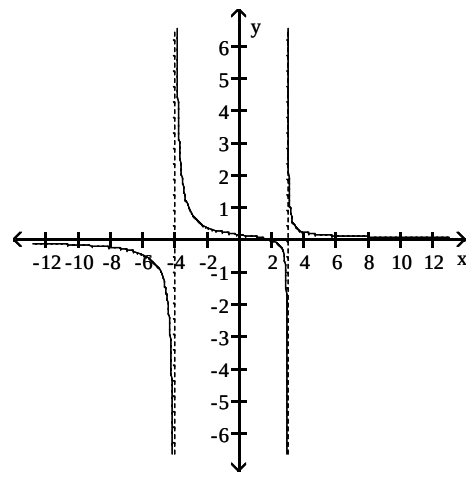
10) $f(x) = \frac{x-2}{x^2-x-12}$



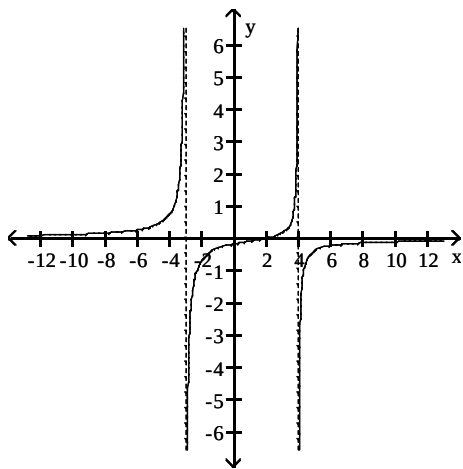
A)



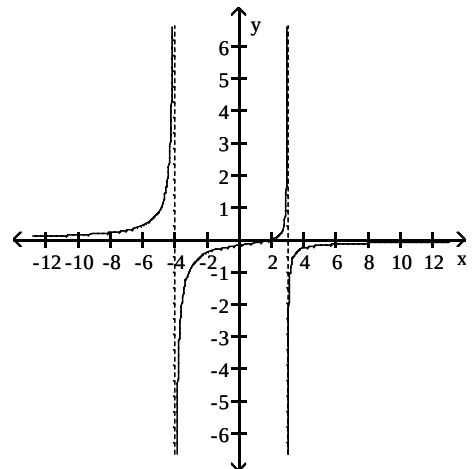
B)



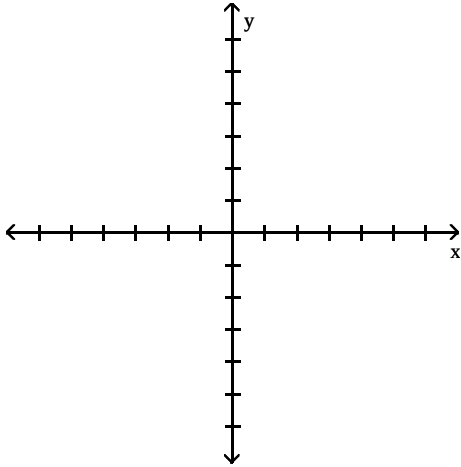
C)



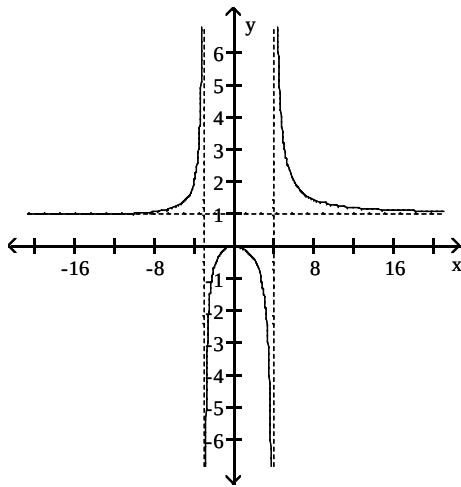
D)



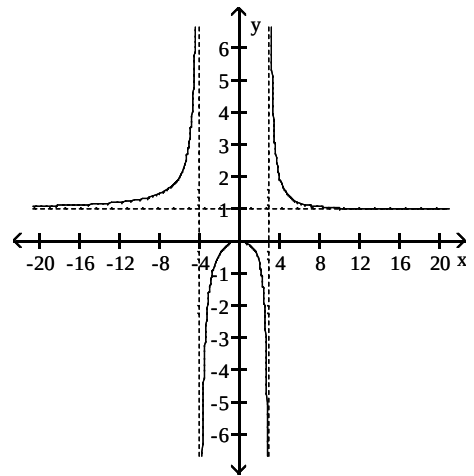
11) $f(x) = \frac{x^2}{x^2 - x - 12}$



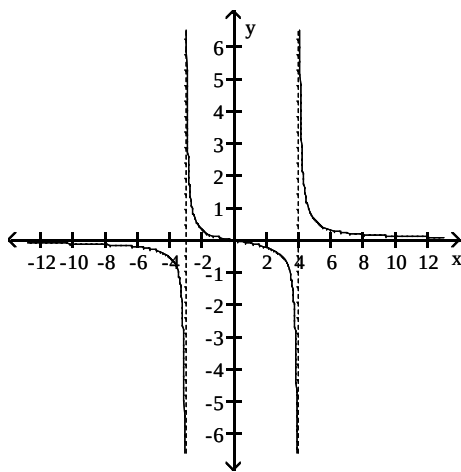
A)



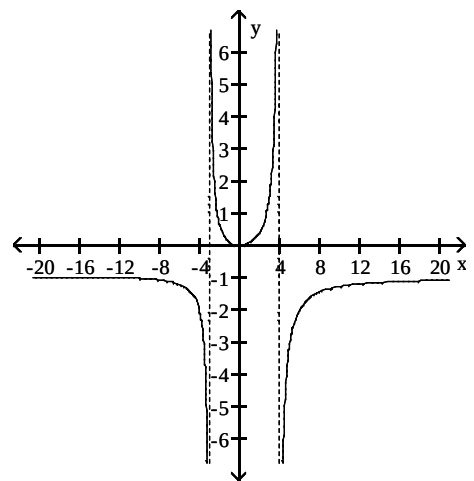
B)



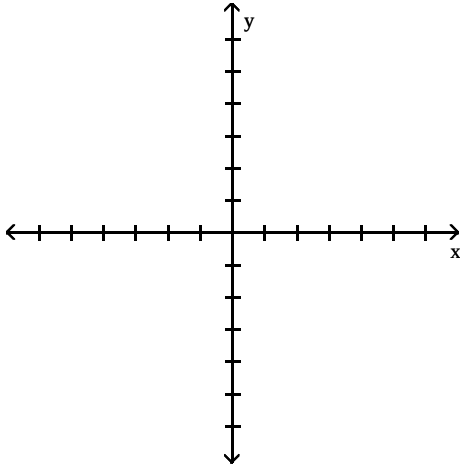
C)



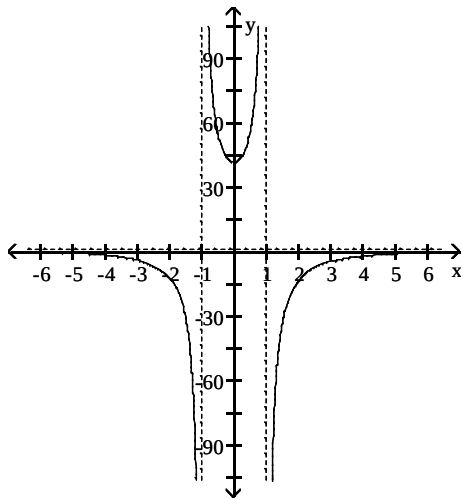
D)



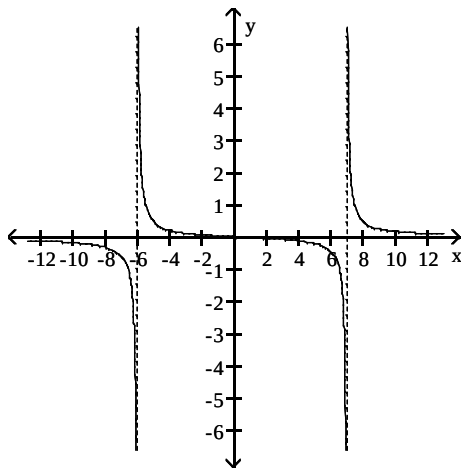
12) $f(x) = \frac{x^2 - x - 42}{x^2 - 1}$



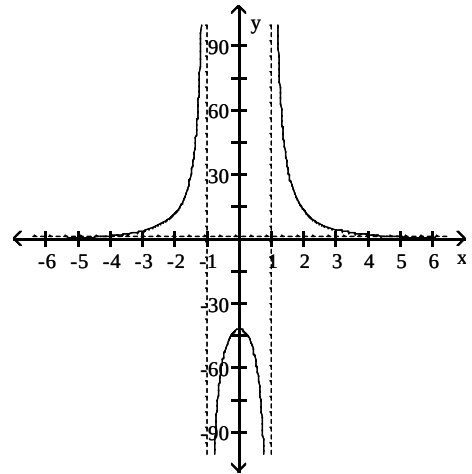
A)



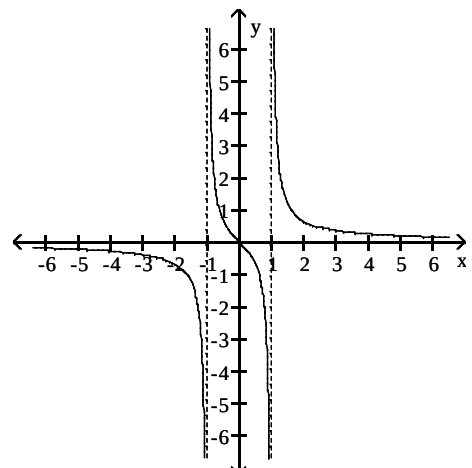
C)



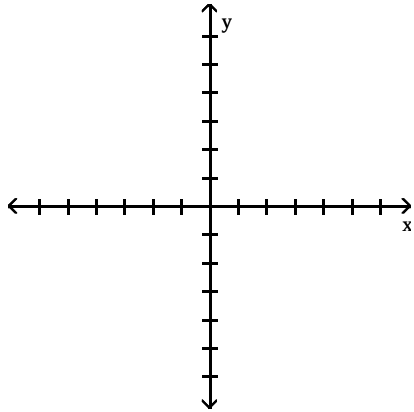
B)



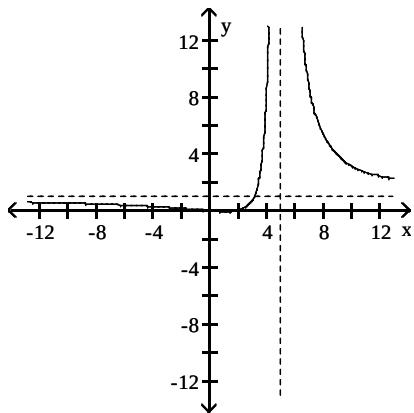
D)



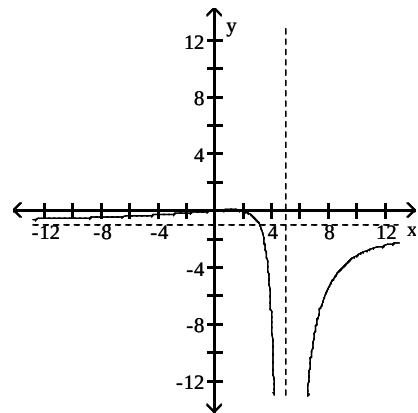
13) $f(x) = \frac{x^2 - 2x}{(x - 5)^2}$



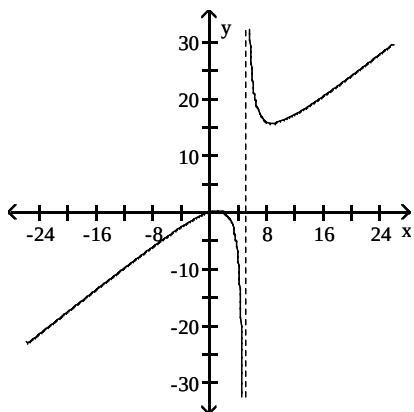
A)



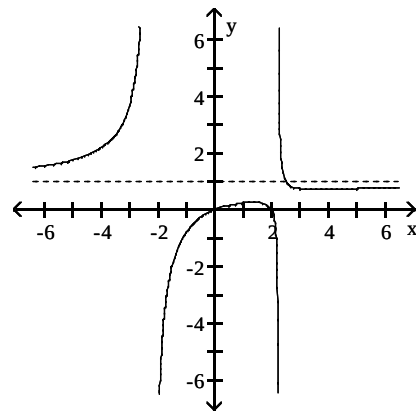
B)



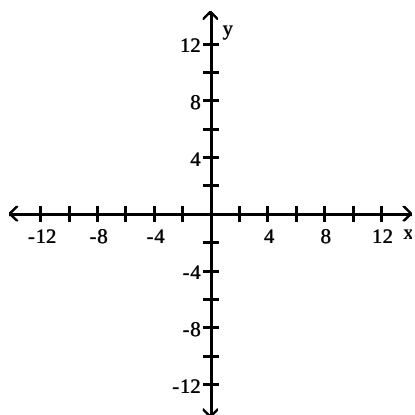
C)



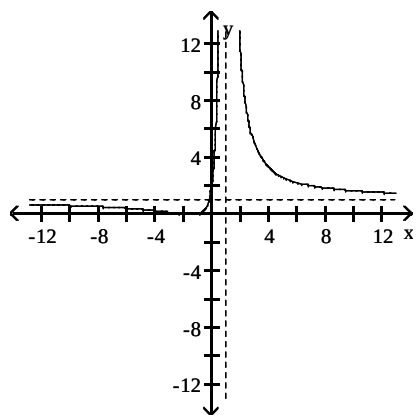
D)



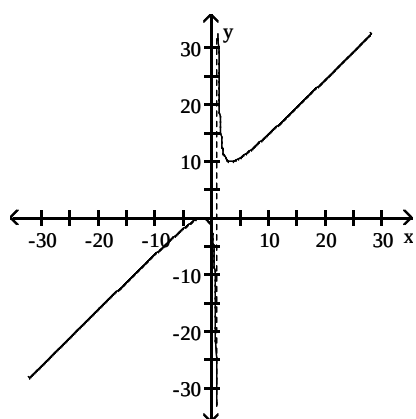
14) $f(x) = \frac{x^2 + 3x + 2}{(x - 1)^2}$



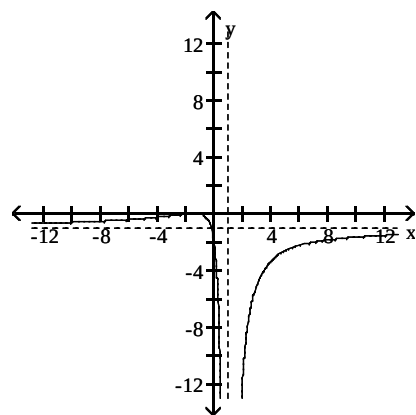
A)



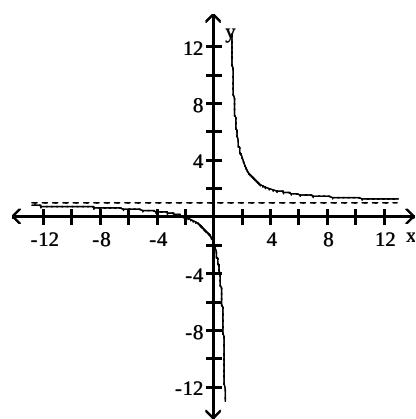
C)



B)



D)



Find the indicated intercept(s) of the graph of the function.

15) x-intercepts of $f(x) = \frac{x - 9}{x^2 + 2x - 3}$

A) (9, 0)

B) (3, 0)

C) (2, 0)

D) none

16) x-intercepts of $f(x) = \frac{x^2 + 7}{x^2 + 2x + 9}$

A) (9, 0)

B) $(\sqrt{7}, 0), (-\sqrt{7}, 0)$

C) (7, 0)

D) none

17) x-intercepts of $f(x) = \frac{x+7}{x^2+5x-3}$

A) $(-7, 0)$

B) $(7, 0)$

C) $\left(\frac{7}{3}, 0\right)$

D) none

18) x-intercepts of $f(x) = \frac{x^2+8x}{x^2+5x-2}$

A) $(0, 0)$ and $(-8, 0)$

B) $(-8, 0)$

C) $(0, 0)$ and $(8, 0)$

D) $(8, 0)$

19) x-intercepts of $f(x) = \frac{(x-8)(2x+9)}{x^2+3x-6}$

A) $(8, 0)$ and $\left(-\frac{9}{2}, 0\right)$

B) $(-8, 0)$ and $\left(\frac{9}{2}, 0\right)$

C) $(8, 0)$ and $(-9, 0)$

D) none

20) y-intercept of $f(x) = \frac{x-11}{x^2+7x-11}$

A) $(0, 1)$

B) $(0, 11)$

C) $(0, -1)$

D) none

21) y-intercept of $f(x) = \frac{x^2-11x}{x^2+7x-6}$

A) $(0, 0)$

B) $\left(0, \frac{11}{6}\right)$

C) $(0, 11)$

D) $\left(0, -\frac{6}{11}\right)$

22) y-intercept of $f(x) = \frac{x^2-7}{x^2+4x-6}$

A) $\left(0, \frac{7}{6}\right)$

B) $(0, 7)$

C) $\left(0, -\frac{6}{7}\right)$

D) none

23) y-intercept of $f(x) = \frac{x^2-5x+1}{13x}$

A) $\left(0, \frac{1}{13}\right)$

B) $(0, 1)$

C) $(0, -13)$

D) none

Solve the problem.

24) Is there y-axis symmetry for the rational function $f(x) = \frac{-6x^2}{-4x^4-5}$?

A) Yes

B) No

25) Is there y-axis symmetry for the rational function $f(x) = \frac{2x^2}{4x^3-16}$?

A) Yes

B) No

26) Is there y-axis symmetry for the rational function $f(x) = \frac{-3x^2-3x-4}{8x+10}$?

A) Yes

B) No

27) Is there origin symmetry for the rational function $f(x) = \frac{-5x}{-3x^2 + 9}$?

A) Yes

B) No

28) Is there origin symmetry for the rational function $f(x) = \frac{-6x^2 + 11}{2x}$?

A) Yes

B) No

29) Is there origin symmetry for the rational function $f(x) = \frac{-9x^2 - 2}{-6x^2 + 11}$?

A) Yes

B) No

7 Identify Slant Asymptotes

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Find the slant asymptote, if any, of the graph of the rational function.

1) $f(x) = \frac{x^2 - 4}{x}$

A) $y = x$

C) $x = 0$

B) $y = x - 4$

D) no slant asymptote

2) $f(x) = \frac{x^2 + 7x - 7}{x - 2}$

A) $y = x + 9$

C) $y = x$

B) $y = x + 7$

D) no slant asymptote

3) $f(x) = \frac{6x^2}{9x^2 + 5}$

A) $y = 6x$

C) $y = x + \frac{2}{3}$

B) $y = x + 6$

D) no slant asymptote

4) $f(x) = \frac{x^2 - 3x + 2}{x + 5}$

A) $y = x - 8$

C) $x = y + 3$

B) $y = x + 5$

D) no slant asymptote

5) $f(x) = \frac{x^3 + 3}{x^2 - 25}$

A) $y = x$

C) $y = x - 25$

B) $y = x + 3$

D) no slant asymptote

6) $h(x) = \frac{x^3 - 3}{x^2 + 6x}$

A) $y = x - 6$

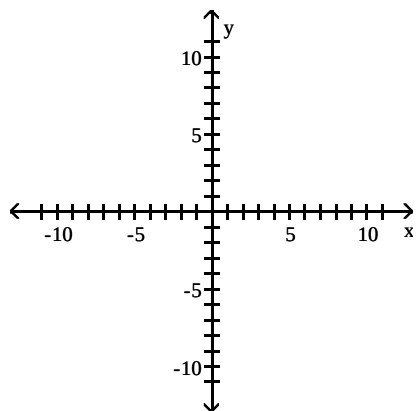
B) $y = x + 6$

C) $y = x - 3$

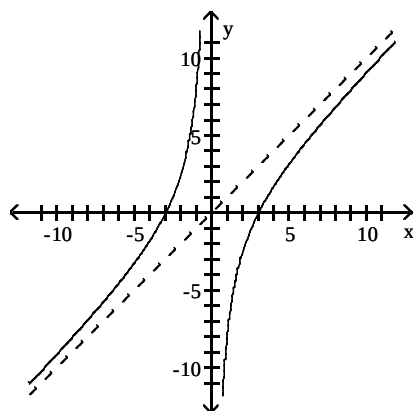
D) $y = x$

Graph the function.

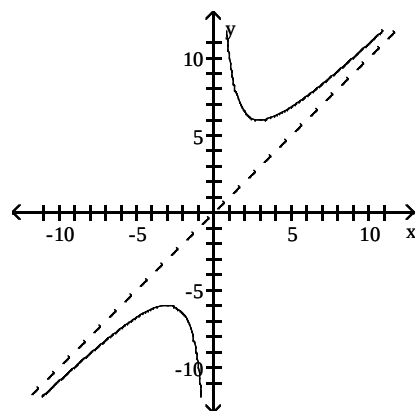
$$7) f(x) = \frac{x^2 - 9}{x}$$



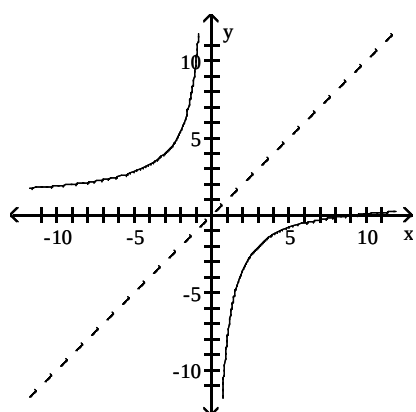
A)



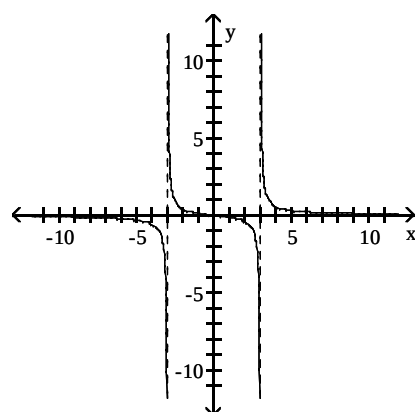
B)



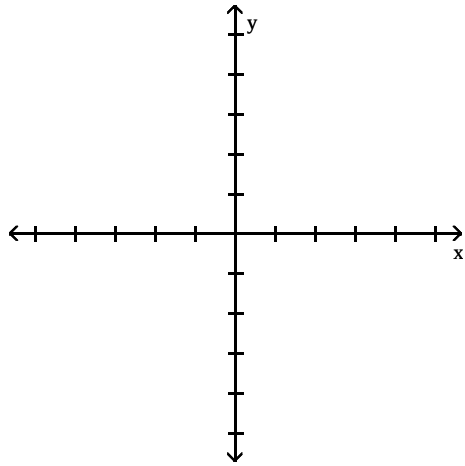
C)



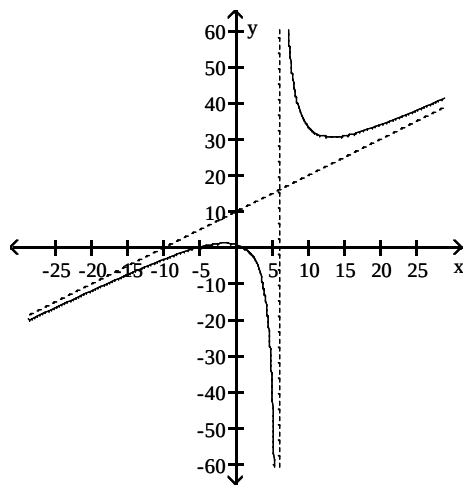
D)



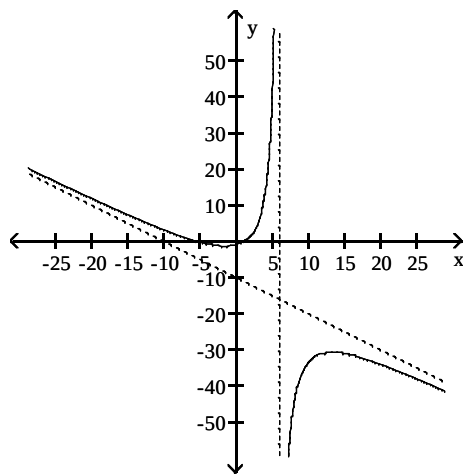
8) $f(x) = \frac{x^2 + 4x - 6}{x - 6}$



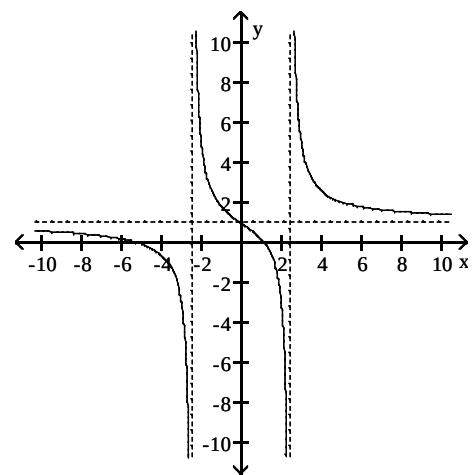
A)



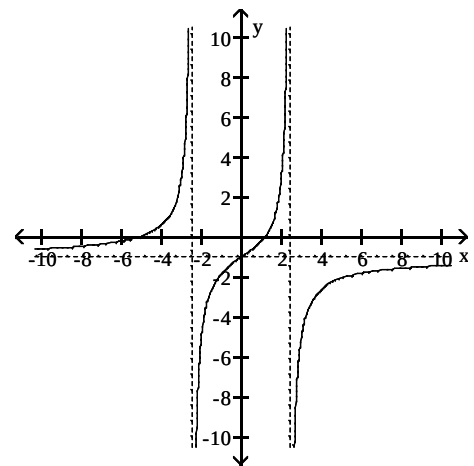
C)



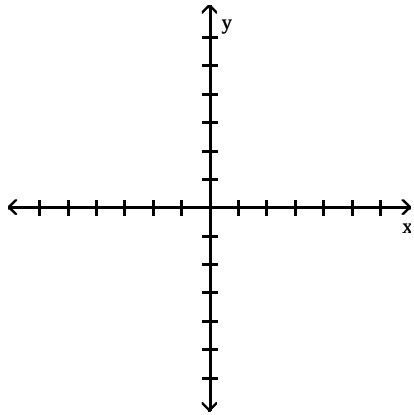
B)



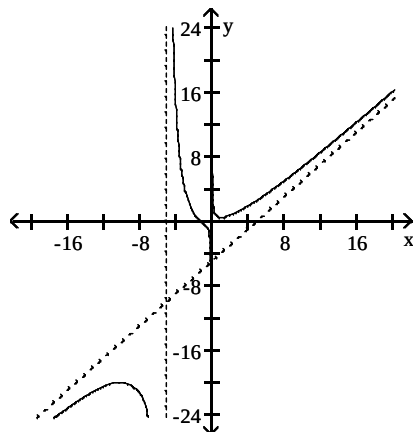
D)



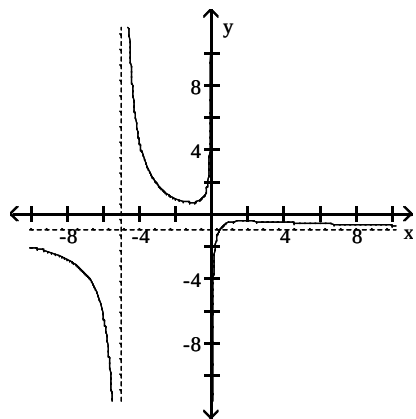
9) $f(x) = \frac{x^3 + 2}{x^2 + 5x}$



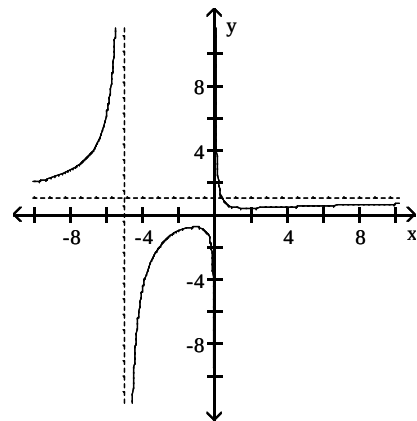
A)



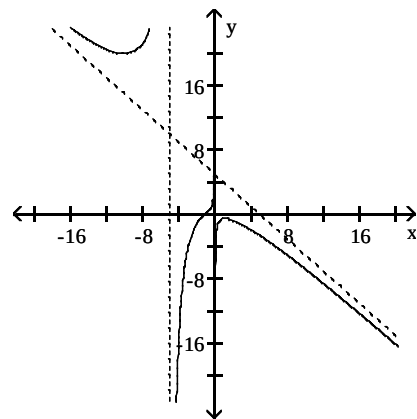
C)



B)



D)



8 Solve Applied Problems Involving Rational Functions

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Solve the problem.

- 1) A company that produces radios has costs given by the function $C(x) = 20x + 15,000$, where x is the number of radios manufactured and $C(x)$ is measured in dollars. The average cost to manufacture each radio is given by

$$\bar{C}(x) = \frac{20x + 15,000}{x}.$$

Find $\bar{C}(200)$. (Round to the nearest dollar, if necessary.)

- A) \$95 B) \$75 C) \$28 D) \$30

- 2) A company that produces inflatable rafts has costs given by the function $C(x) = 25x + 20,000$, where x is the number of inflatable rafts manufactured and $C(x)$ is measured in dollars. The average cost to manufacture each inflatable raft is given by

$$\bar{C}(x) = \frac{25x + 20,000}{x}.$$

What is the horizontal asymptote for the function $\bar{C}$? Describe what this means in practical terms.

- A) $y = 25$; \$25 is the least possible cost for producing each inflatable raft.
B) $y = 20,000$; 20,000 is the maximum number of inflatable rafts the company can produce.
C) $y = 25$; 25 is the minimum number of inflatable rafts the company can produce.
D) $y = 20,000$; \$20,000 is the least possible cost for running the company.

- 3) A drug is injected into a patient and the concentration of the drug is monitored. The drug's concentration, $C(t)$, in milligrams after t hours is modeled by

$$C(t) = \frac{4t}{3t^2 + 2}.$$

What is the horizontal asymptote for this function? Describe what this means in practical terms.

- A) $y = 0$; 0 is the final amount, in milligrams, of the drug that will be left in the patient's bloodstream.
B) $y = 1.33$; 1.33 is the final amount, in milligrams, of the drug that will be left in the patient's bloodstream.
C) $y = 0.80$; After 0.80 hours, the concentration of the drug is at its greatest.
D) $y = 1.33$; After 1.33 hours, the concentration of the drug is at its greatest.

- 4) A drug is injected into a patient and the concentration of the drug is monitored. The drug's concentration, $C(t)$, in milligrams per liter after t hours is modeled by

$$C(t) = \frac{4t}{3t^2 + 4}.$$

Estimate the drug's concentration after 2 hours. (Round to the nearest hundredth.)

- A) 0.50 milligrams per liter B) 0.55 milligrams per liter
C) 0.80 milligrams per liter D) 0.85 milligrams per liter

- 5) The rational function

$$C(x) = \frac{140x}{100 - x}, \quad 0 \leq x < 100$$

describes the cost, C , in millions of dollars, to inoculate $x\%$ of the population against a particular strain of the flu. Determine the difference in cost between inoculating 65% of the population and inoculating 40% of the population. (Round to the nearest tenth, if necessary.)

- A) \$166.7 million B) \$1.3 million C) \$166.6 million D) \$1.4 million

Write a rational function that models the problem's conditions.

- 6) A plane flies a distance of 2300 miles in still air. The next day, the plane makes the return trip, however due to a tailwind, the average velocity on the return trip is 27 miles per hour faster than the average velocity on the outgoing trip. Express the total time required to complete the round trip, T , as a function of the average velocity on the outgoing trip, x .

A) $T(x) = \frac{2300}{x} + \frac{2300}{x + 27}$

B) $T(x) = \frac{2300}{x} + \frac{2300}{x - 27}$

C) $T(x) = \frac{x}{2300} + \frac{x + 27}{2300}$

D) $T(x) = 2300x + 2300(x + 27)$

- 7) An athlete is training for a triathlon. One morning she runs a distance of 4 miles and cycles a distance of 31 miles. Her average velocity cycling is three times that while running. Express the total time for running and cycling, T , as a function of the average velocity while running, x .

A) $T(x) = \frac{4}{x} + \frac{31}{3x}$

B) $T(x) = \frac{4}{x} + \frac{31}{x + 3}$

C) $T(x) = \frac{x}{4} + \frac{3x}{31}$

D) $T(x) = \frac{31}{x} + \frac{4}{3x}$

- 8) The area of a rectangular rug is 370 square feet. Express the perimeter of the rug, P , as a function of the length of the rug, x .

A) $P(x) = 2x + \frac{740}{x}$

B) $P(x) = 2x + \frac{370}{x}$

C) $P(x) = 2x + \frac{x}{740}$

D) $P(x) = x(370 - x)$

- 9) The area of a rectangular photograph is 59 square inches. It is to be mounted on a rectangular card with a border of 1 inch at each side, 2 inches at the top, and 2 inches at the bottom. Express the total area of the photograph and the border, A , as a function of the width of the photograph, x .

A) $A(x) = 67 + 4x + \frac{118}{x}$

B) $A(x) = 63 + 4x + \frac{118}{x}$

C) $A(x) = 67 + 2x + \frac{236}{x}$

D) $A(x) = 67 + 4x + \frac{x}{118}$

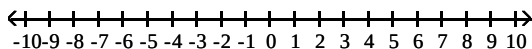
2.7 Polynomial and Rational Inequalities

1 Solve Polynomial Inequalities

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

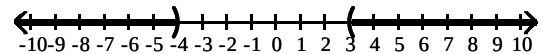
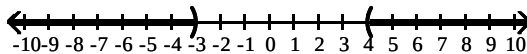
Solve the polynomial inequality and graph the solution set on a number line. Express the solution set in interval notation.

1) $(x - 4)(x + 3) > 0$



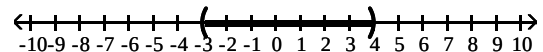
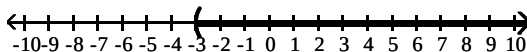
A) $(-\infty, -3) \cup (4, \infty)$

B) $(-\infty, -4) \cup (3, \infty)$

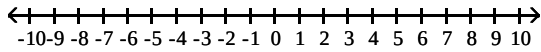


C) $(-3, \infty)$

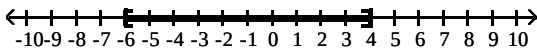
D) $(-3, 4)$



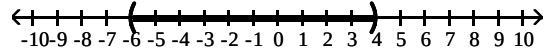
2) $(x + 6)(x - 4) \leq 0$



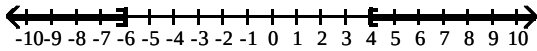
A) $[-6, 4]$



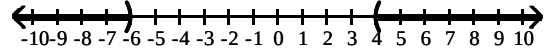
B) $(-6, 4)$



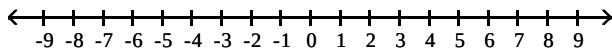
C) $(-\infty, -6] \cup [4, \infty)$



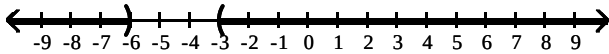
D) $(-\infty, -6) \cup (4, \infty)$



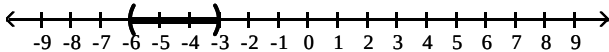
3) $x^2 + 9x + 18 > 0$



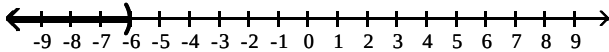
A) $(-\infty, -6) \cup (-3, \infty)$



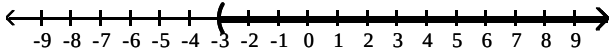
B) $(-6, -3)$



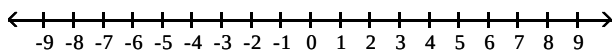
C) $(-\infty, -6)$



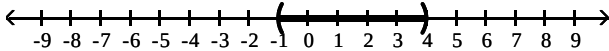
D) $(-3, \infty)$



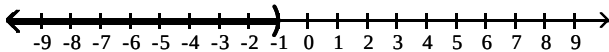
4) $x^2 - 3x - 4 < 0$



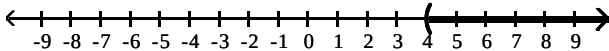
A) $(-1, 4)$



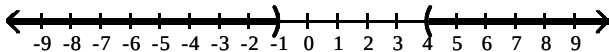
B) $(-\infty, -1)$



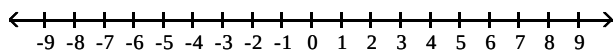
C) $(4, \infty)$



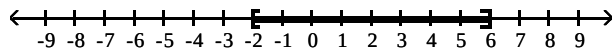
D) $(-\infty, -1) \cup (4, \infty)$



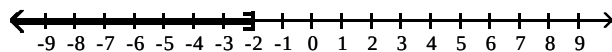
5) $x^2 - 4x - 12 \leq 0$



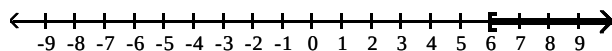
A) $[-2, 6]$



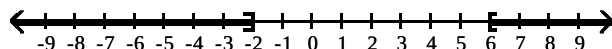
B) $(-\infty, -2]$



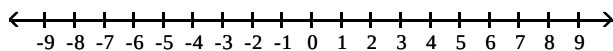
C) $[6, \infty)$



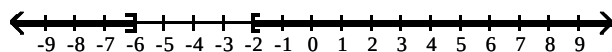
D) $(-\infty, -2] \cup [6, \infty)$



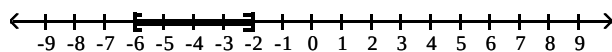
6) $x^2 + 8x + 12 \geq 0$



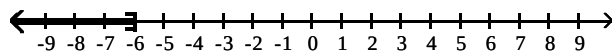
A) $(-\infty, -6] \cup [-2, \infty)$



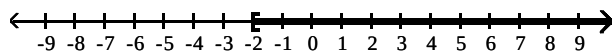
B) $[-6, -2]$



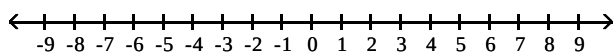
C) $(-\infty, -6]$



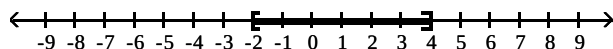
D) $[-2, \infty)$



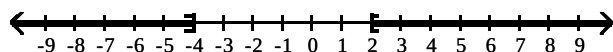
7) $x^2 - 2x \leq 8$



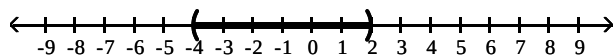
A) $[-2, 4]$



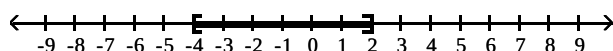
B) $(-\infty, -4] \cup [2, \infty)$



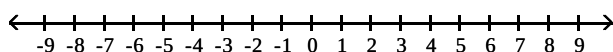
C) $(-4, 2)$



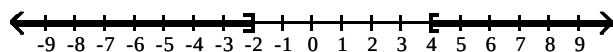
D) $[-4, 2]$



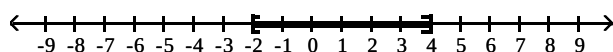
8) $x^2 - 2x \geq 8$



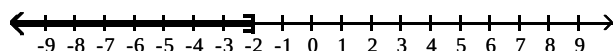
A) $(-\infty, -2] \cup [4, \infty)$



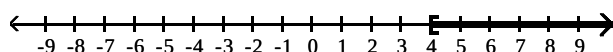
B) $[-2, 4]$



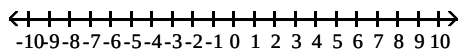
C) $(-\infty, -2]$



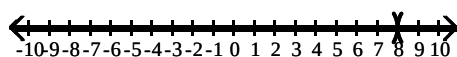
D) $[4, \infty)$



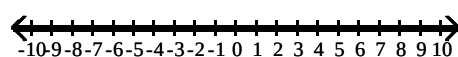
9) $x^2 - 16x + 64 > 0$



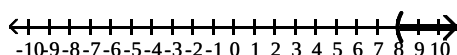
A) $(-\infty, 8) \cup (8, \infty)$



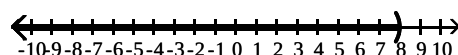
B) $(-\infty, \infty)$



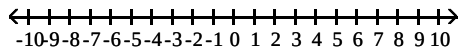
C) $(8, \infty)$



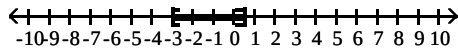
D) $(-\infty, 8)$



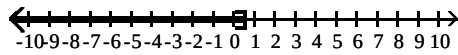
10) $2x^2 + 5x - 3 \leq 0$



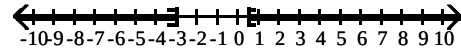
A) $\left[-3, \frac{1}{2}\right]$



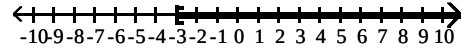
C) $\left[-\infty, \frac{1}{2}\right]$



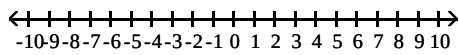
B) $(-\infty, -3] \cup \left[\frac{1}{2}, \infty\right)$



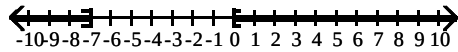
D) $[-3, \infty)$



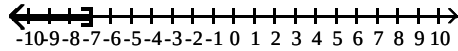
11) $x^2 + 7x \geq 0$



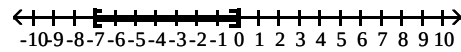
A) $(-\infty, -7] \cup [0, \infty)$



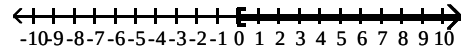
C) $(-\infty, -7]$



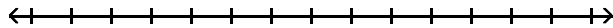
B) $[-7, 0]$



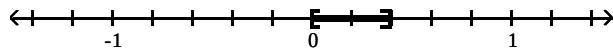
D) $[0, \infty]$



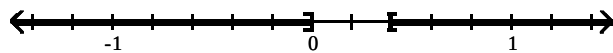
12) $13x^2 - 5x \leq 0$



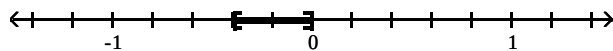
A) $\left[0, \frac{5}{13}\right]$



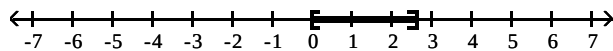
B) $(-\infty, 0] \cup \left[\frac{5}{13}, \infty\right)$



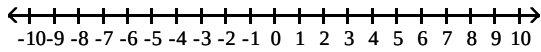
C) $\left[-\frac{5}{13}, 0\right]$



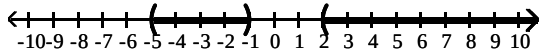
D) $\left[0, \frac{13}{5}\right]$



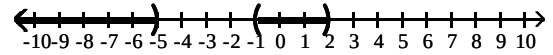
13) $(x + 5)(x + 1)(x - 2) > 0$



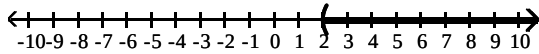
A) $(-5, -1) \cup (2, \infty)$



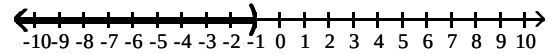
B) $(-\infty, -5) \cup (-1, 2)$



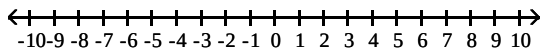
C) $(2, \infty)$



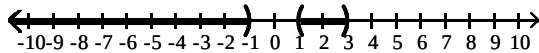
D) $(-\infty, -1)$



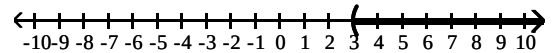
14) $(x + 1)(x - 1)(x - 3) < 0$



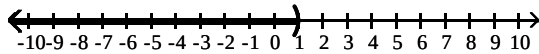
A) $(-\infty, -1) \cup (1, 3)$



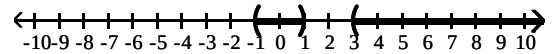
B) $(3, \infty)$



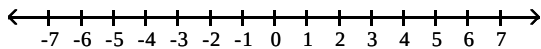
C) $(-\infty, 1)$



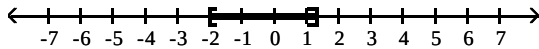
D) $(-1, 1) \cup (3, \infty)$



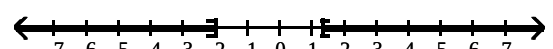
15) $(3x - 4)(x + 2) \leq 0$



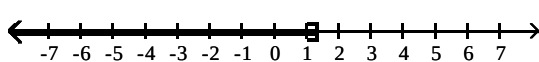
A) $\left[-2, \frac{4}{3}\right]$



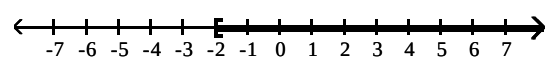
B) $(-\infty, -2] \cup \left[\frac{4}{3}, \infty\right)$



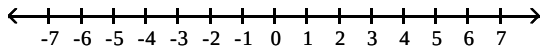
C) $\left(-\infty, \frac{4}{3}\right]$



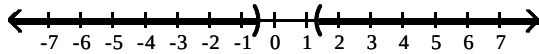
D) $[-2, \infty)$



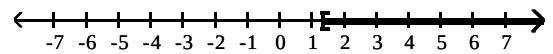
16) $(2x + 1)(3x - 4) > 0$



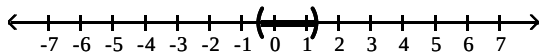
A) $\left(-\infty, -\frac{1}{2}\right) \cup \left(\frac{4}{3}, \infty\right)$



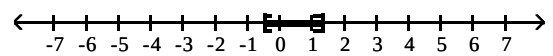
B) $\left(\frac{4}{3}, \infty\right)$



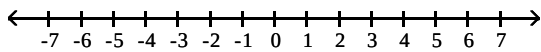
C) $\left[-\frac{1}{2}, \frac{4}{3}\right]$



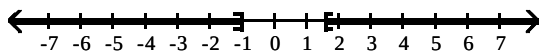
D) $\left[-\frac{1}{2}, \frac{4}{3}\right]$



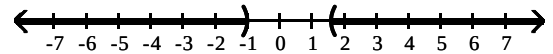
17) $5x^2 - 3x \geq 8$



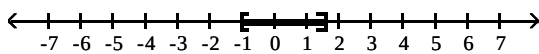
A) $(-\infty, -1] \cup \left[\frac{8}{5}, \infty\right)$



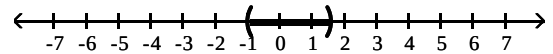
B) $(-\infty, -1) \cup \left[\frac{8}{5}, \infty\right)$



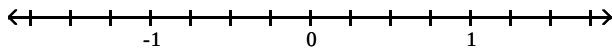
C) $\left[-1, \frac{8}{5}\right]$



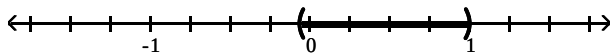
D) $\left[-1, \frac{8}{5}\right)$



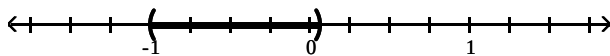
18) $16x^2 < 15x + 1$



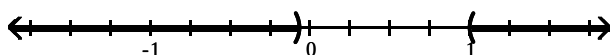
A) $\left(-\frac{1}{16}, 1\right)$



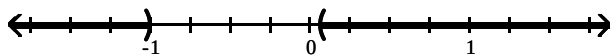
B) $\left[-1, \frac{1}{16}\right)$



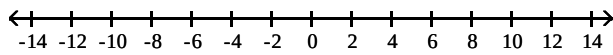
C) $\left(-\infty, -\frac{1}{16}\right) \cup (1, \infty)$



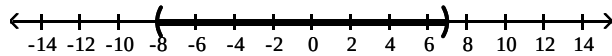
D) $(-\infty, -1) \cup \left[\frac{1}{16}, \infty\right)$



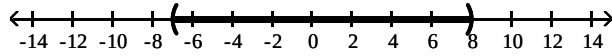
19) $x < 56 - x^2$



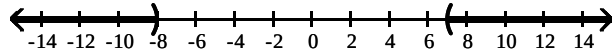
A) $(-8, 7)$



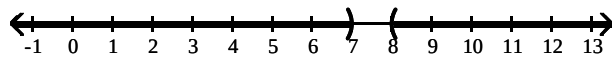
B) $(-7, 8)$



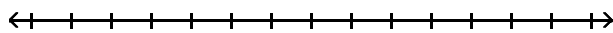
C) $(-\infty, -8) \cup (7, \infty)$



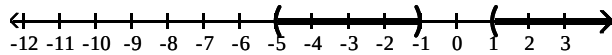
D) $(-\infty, 7) \cup (8, \infty)$



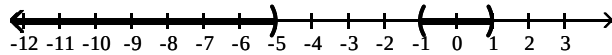
20) $x^3 + 5x^2 - x - 5 > 0$



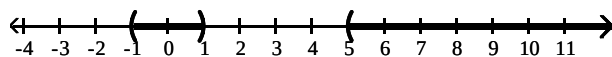
A) $(-5, -1) \cup (1, \infty)$



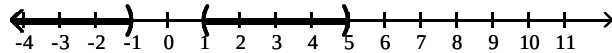
B) $(-\infty, -5) \cup (-1, 1)$



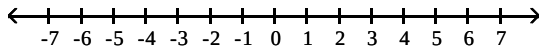
C) $(-1, 1) \cup (5, \infty)$



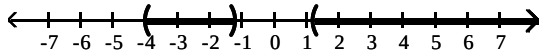
D) $(-\infty, -1) \cup (1, 5)$



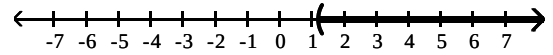
21) $25x^3 + 100x^2 - 36x - 144 > 0$



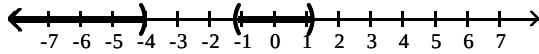
A) $\left(-4, -\frac{6}{5}\right) \cup \left(\frac{6}{5}, \infty\right)$



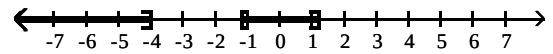
B) $\left(\frac{6}{5}, \infty\right)$



C) $(-\infty, -4) \cup \left(-\frac{6}{5}, \frac{6}{5}\right)$



D) $(-\infty, -4] \cup \left[-\frac{6}{5}, \frac{6}{5}\right]$

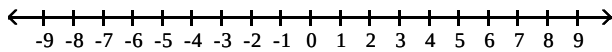


2 Solve Rational Inequalities

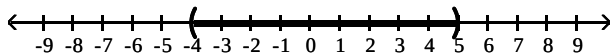
MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Solve the rational inequality and graph the solution set on a real number line. Express the solution set in interval notation.

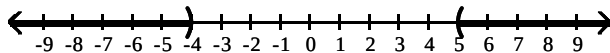
1) $\frac{x-5}{x+4} < 0$



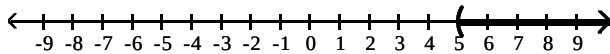
A) $(-4, 5)$



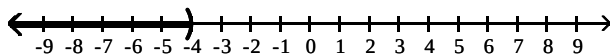
B) $(-\infty, -4)$ or $(5, \infty)$



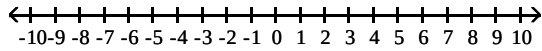
C) $(5, \infty)$



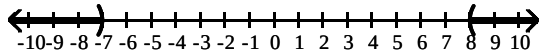
D) $(-\infty, -4)$



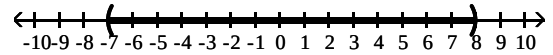
$$2) \frac{x-8}{x+7} > 0$$



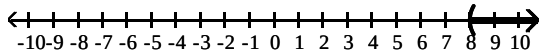
A) $(-\infty, -7)$ or $(8, \infty)$



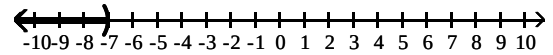
B) $(-7, 8)$



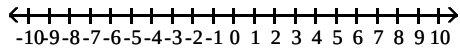
C) $(8, \infty)$



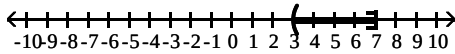
D) $(-\infty, -7)$



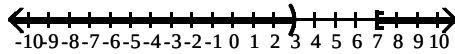
$$3) \frac{-x+7}{x-3} \geq 0$$



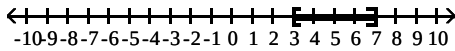
A) $(3, 7)$



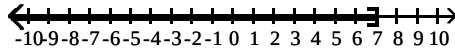
B) $(-\infty, 3)$ or $[7, \infty)$



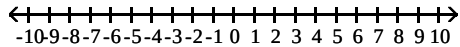
C) $[3, 7]$



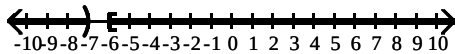
D) $(-\infty, 7]$



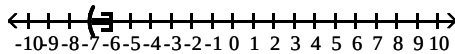
$$4) \frac{-x-6}{x+7} \leq 0$$



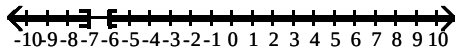
A) $(-\infty, -7)$ or $[-6, \infty)$



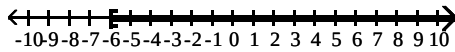
B) $(-7, -6]$



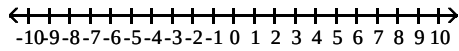
C) $(-\infty, -7]$ or $[-6, \infty)$



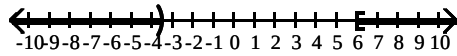
D) $[-6, \infty)$



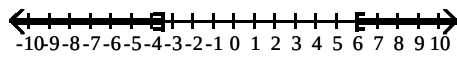
5) $\frac{12 - 2x}{2x + 7} \leq 0$



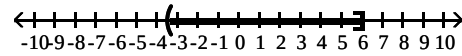
A) $\left(-\infty, -\frac{7}{2}\right)$ or $[6, \infty)$



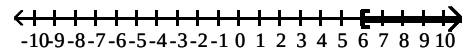
C) $\left(-\infty, -\frac{7}{2}\right]$ or $[6, \infty)$



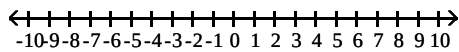
B) $\left[-\frac{7}{2}, 6\right]$



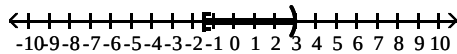
D) $[6, \infty)$



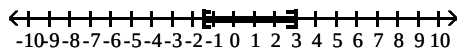
6) $\frac{2x + 3}{15 - 5x} \geq 0$



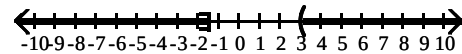
A) $\left[-\frac{3}{2}, 3\right]$



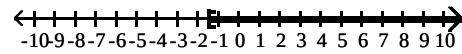
C) $\left[-\frac{3}{2}, 3\right)$



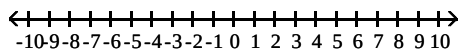
B) $\left(-\infty, -\frac{3}{2}\right]$ or $(3, \infty)$



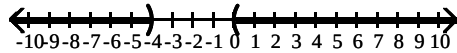
D) $\left[-\frac{3}{2}, \infty\right)$



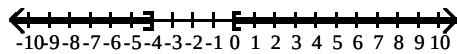
7) $\frac{x}{x + 4} > 0$



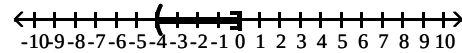
A) $(-\infty, -4)$ or $(0, \infty)$



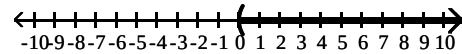
C) $(-\infty, -4]$ or $[0, \infty)$



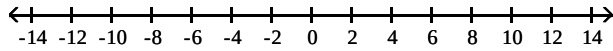
B) $(-4, 0]$



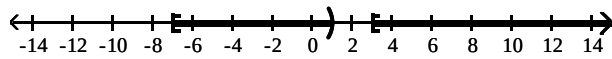
D) $(0, \infty)$



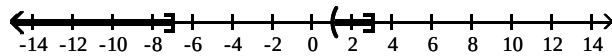
8) $\frac{(x+7)(x-3)}{x-1} \geq 0$



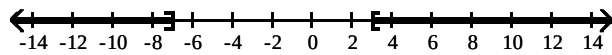
A) $[-7, 1) \cup [3, \infty)$



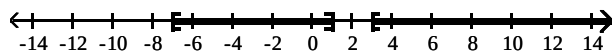
B) $(-\infty, -7] \cup (1, 3]$



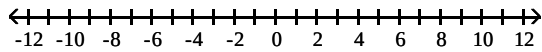
C) $(-\infty, -7] \cup [3, \infty)$



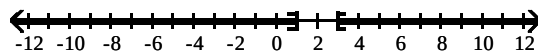
D) $[-7, 1) \cup [3, \infty)$



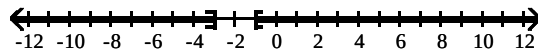
9) $\frac{(x-1)(3-x)}{(x-2)^2} \leq 0$



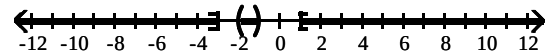
A) $(-\infty, 1] \cup [3, \infty)$



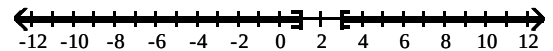
C) $(-\infty, -3] \cup (-1, \infty)$



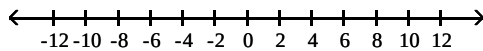
B) $(-\infty, -3] \cup (-2, -1) \cup [1, \infty)$



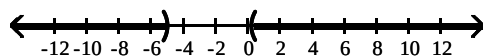
D) $(-\infty, 1) \cup (3, \infty)$



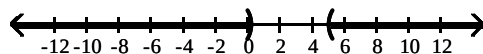
10) $\frac{x+26}{x+5} < 5$



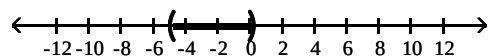
A) $(-\infty, -5) \text{ or } (\frac{1}{4}, \infty)$



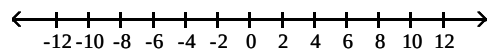
C) $(-\infty, \frac{1}{4}) \text{ or } (5, \infty)$



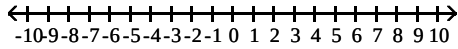
B) $(-5, \frac{1}{4})$



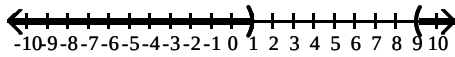
D) $\emptyset$



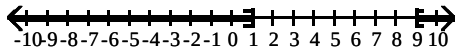
11) $\frac{8}{x-1} < 1$



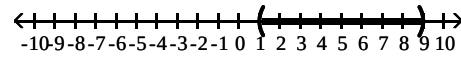
A) $(-\infty, 1)$ or $(9, \infty)$



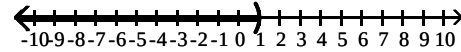
C) $(-\infty, 1]$ or $[9, \infty)$



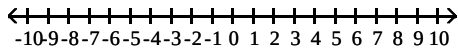
B) $(1, 9)$



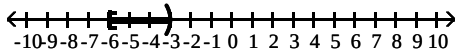
D) $(-\infty, 1)$



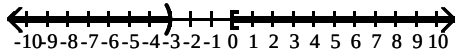
12) $\frac{x}{x+3} \geq 2$



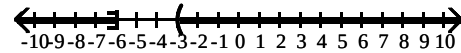
A) $[-6, -3]$



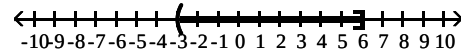
C) $(-\infty, -3)$ or $[0, \infty)$



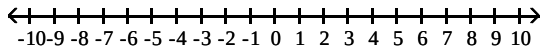
B) $(-\infty, -6]$ or $(-3, \infty)$



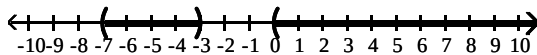
D) $(-3, 6]$



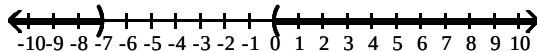
13) $\frac{4x}{x+7} < x$



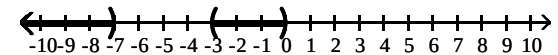
A) $(-7, -3) \cup (0, \infty)$



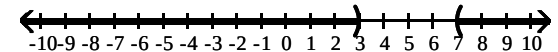
C) $(-\infty, -7) \cup (0, \infty)$



B) $(-\infty, -7) \cup (-3, 0)$



D) $(-\infty, 3) \cup (7, \infty)$



3 Solve Problems Modeled by Polynomial or Rational Inequalities

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Solve the problem.

- 1) The average cost per unit, y , of producing x units of a product is modeled by $y = \frac{300,000 + 0.25x}{x}$. Describe the

company's production level so that the average cost of producing each unit does not exceed \$1.75.

- A) At least 200,000 units
B) Not more than 200,000 units
C) At least 300,000 units
D) Not more than 300,000 units

- 2) The total profit function $P(x)$ for a company producing x thousand units is given by $P(x) = -2x^2 + 22x - 48$. Find the values of x for which the company makes a profit. [Hint: The company makes a profit when $P(x) > 0$.]
- A) x is between 3 thousand units and 8 thousand units
 - B) x is greater than 3 thousand units
 - C) x is less than 8 thousand units
 - D) x is less than 3 thousand units or greater than 8 thousand units
- 3) A number minus the product of 4 and its reciprocal is less than zero. Find the numbers which satisfy this condition.
- A) any number less than -2 or between 0 and 2
 - B) any number between 0 and 2
 - C) any number between -2 and 2
 - D) any number less than 2
- 4) The sum of 36 times a number and the reciprocal of the number is positive. Find the numbers which satisfy this condition.
- A) any number greater than 0
 - B) any number greater than $\frac{1}{6}$
 - C) any number between $-\frac{1}{6}$ and $\frac{1}{6}$
 - D) any number between 0 and $\frac{1}{6}$
- 5) An arrow is fired straight up from the ground with an initial velocity of 128 feet per second. Its height, $s(t)$, in feet at any time t is given by the function $s(t) = -16t^2 + 128t$. Find the interval of time for which the height of the arrow is greater than 156 feet.
- A) between $\frac{3}{2}$ and $\frac{13}{2}$ sec
 - B) after $\frac{3}{2}$ sec
 - C) before $\frac{13}{2}$ sec
 - D) before $\frac{3}{2}$ sec or after $\frac{13}{2}$ sec
- 6) A ball is thrown vertically upward with an initial velocity of 96 feet per second. The distance in feet of the ball from the ground after t seconds is $s = 96t - 16t^2$. For what interval of time is the ball more than 80 above the ground?
- A) between 1 and 5 seconds
 - B) between 0.5 and 5.5 seconds
 - C) between 4 and 8 seconds
 - D) between 2.5 and 3.5 seconds
- 7) A ball is thrown vertically upward with an initial velocity of 96 feet per second. The distance in feet of the ball from the ground after t seconds is $s = 96t - 16t^2$. For what intervals of time is the ball less than 80 above the ground (after it is tossed until it returns to the ground)?
- A) between 0 and 1 seconds and between 5 and 6 seconds
 - B) between 1 and 5 seconds
 - C) between 0 and 0.5 seconds and between 5.5 and 6 seconds
 - D) between 0 and 2.5 seconds and between 3.5 and 6 seconds
- 8) The revenue achieved by selling x graphing calculators is figured to be $x(43 - 0.2x)$ dollars. The cost of each calculator is \$23. How many graphing calculators must be sold to make a profit (revenue - cost) of at least \$471.20?
- A) between 38 and 62 calculators
 - B) between 13 and 37 calculators
 - C) between 39 and 37 calculators
 - D) between 40 and 60 calculators
- 9) The revenue achieved by selling x graphing calculators is figured to be $x(42 - 0.5x)$ dollars. The cost of each calculator is \$18. How many graphing calculators must be sold to make a profit (revenue - cost) of at least \$283.50?
- A) between 21 and 27 calculators
 - B) between 27 and 33 calculators
 - C) between 22 and 26 calculators
 - D) between 23 and 25 calculators

- 10) You drive 126 miles along a scenic highway and then take a 39-mile bike ride. Your driving rate is 5 times your cycling rate. Suppose you have no more than a total of 6 hours for driving and cycling. Let x represent your cycling rate in miles per hour. Write a rational inequality that can be used to determine the possible values of x . Do not simplify and do not solve the inequality.

A) $\frac{126}{5x} + \frac{39}{x} \leq 6$ B) $\frac{126}{x} + \frac{39}{5x} \leq 6$ C) $\frac{5x}{126} + \frac{x}{39} \leq 6$ D) $\frac{126}{5x} + \frac{39}{x} \geq 6$

- 11) You drive 120 miles along a scenic highway and then take a 29-mile bike ride. Your driving rate is 3 times your cycling rate. Suppose you have no more than a total of 5 hours for driving and cycling. Let x represent your cycling rate in miles per hour. Use a rational inequality to determine the possible values of x .

A) $x \geq 13.8$ mph B) $x \leq 13.8$ mph C) $x \geq 25.9$ mph D) $x \leq 84.1$ mph

- 12) The perimeter of a rectangle is 58 feet. Describe the possible lengths of a side if the area of the rectangle is to be greater than 180 square feet.

- A) The length of the rectangle must lie between 9 and 20 ft
 B) The length of the rectangle must be greater than 20 ft
 C) The length of the rectangle must be greater than 20 ft or less than 9 ft
 D) The length of the rectangle must lie between 1 and 180 ft

2.8 Modeling Using Variation

1 Solve Direct Variation Problems

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Write an equation that expresses the relationship. Use k as the constant of variation.

- 1) d varies directly as y .

A) $d = ky$ B) $d = \frac{k}{y}$ C) $k = dy$ D) $y = \frac{k}{d}$

- 2) g varies directly as the square of h .

A) $g = kh^2$ B) $g = \frac{k}{h^2}$ C) $g = k\sqrt{h}$ D) $g = \frac{k}{\sqrt{h}}$

Determine the constant of variation for the stated condition.

- 3) s varies directly as r , and $s = 60$ when $r = 5$.

A) $k = 12$ B) $k = 10$ C) $k = \frac{1}{12}$ D) $k = 55$

- 4) y varies directly as x , and $y = 7$ when $x = 56$.

A) $k = \frac{1}{8}$ B) $k = 10$ C) $k = 8$ D) $k = 49$

- 5) b varies directly as a^2 , and $b = 80$ when $a = 4$.

A) $k = 5$ B) $k = 80$ C) $k = \frac{1}{5}$ D) $k = 76$

If y varies directly as x , find the direct variation equation for the situation.

- 6) $y = 6$ when $x = 30$

A) $y = \frac{1}{5}x$ B) $y = 5x$ C) $y = x + 24$ D) $y = \frac{1}{6}x$

7) $y = 6$ when $x = 15$

A) $y = \frac{2}{5}x$

B) $y = \frac{5}{2}x$

C) $y = x - 9$

D) $y = 3x$

8) $y = 8$ when $x = \frac{1}{3}$

A) $y = 24x$

B) $y = \frac{1}{24}x$

C) $y = x + \frac{23}{3}$

D) $y = \frac{1}{8}x$

9) $y = 1.6$ when $x = 0.4$

A) $y = 4x$

B) $y = 0.4x$

C) $y = x + 1.2$

D) $y = 0.25x$

10) $y = 0.5$ when $x = 2$

A) $y = 0.25x$

B) $y = 0.5x$

C) $y = x - 1.5$

D) $y = 4x$

Solve the problem.

11) y varies directly as z and $y = 195$ when $z = 13$. Find y when $z = 17$.

A) 255

B) 289

C) 225

D) 169

12) If y varies directly as x , and $y = 7$ when $x = 6$, find y when $x = 48$.

A) 56

B) $\frac{7}{8}$

C) $\frac{288}{7}$

D) $\frac{8}{7}$

13) If y varies directly as x , and $y = 300$ when $x = 175$, find y when $x = 70$.

A) 120

B) 750

C) $\frac{245}{6}$

D) $\frac{6}{245}$

14) y varies directly as z^2 and $y = 45$ when $z = 3$. Find y when $z = 6$.

A) 180

B) 15

C) 90

D) 18

15) If y varies directly as the square of x , and $y = 280$ when $x = 6$, find y when $x = 12$.

A) 1120

B) 560

C) 70

D) 140

16) If y varies directly as the cube of x , and $y = 8$ when $x = 20$, find y when $x = 25$.

A) $\frac{125}{8}$

B) 10

C) $\frac{32}{5}$

D) $\frac{512}{125}$

17) If y varies directly as the square root of x , and $y = 2$ when $x = 49$, find y when $x = 16$.

A) $\frac{8}{7}$

B) $\frac{32}{49}$

C) $\frac{7}{2}$

D) $\frac{49}{8}$

18) The amount of water used to take a shower is directly proportional to the amount of time that the shower is in use. A shower lasting 16 minutes requires 6.4 gallons of water. Find the amount of water used in a shower lasting 5 minutes.

A) 2 gallons

B) 20.48 gallons

C) 12.5 gallons

D) 1.28 gallons

19) If the resistance in an electrical circuit is held constant, the amount of current flowing through the circuit is directly proportional to the amount of voltage applied to the circuit. When 2 volts are applied to a circuit, 10 milliamperes of current flow through the circuit. Find the new current if the voltage is increased to 9 volts.

A) 45 milliamperes

B) 18 milliamperes

C) 36 milliamperes

D) 50 milliamperes

- 20) The amount of gas that a helicopter uses is directly proportional to the number of hours spent flying. The helicopter flies for 2 hours and uses 30 gallons of fuel. Find the number of gallons of fuel that the helicopter uses to fly for 4 hours.
- A) 60 gallons B) 8 gallons C) 64 gallons D) 75 gallons
- 21) The distance that an object falls when it is dropped is directly proportional to the square of the amount of time since it was dropped. An object falls 156.8 meters in 4 seconds. Find the distance the object falls in 5 seconds.
- A) 245 meters B) 49 meters C) 196 meters D) 20 meters
- 22) For a resistor in a direct current circuit that does not vary its resistance, the power that a resistor must dissipate is directly proportional to the square of the voltage across the resistor. The resistor must dissipate $\frac{1}{16}$ watt of power when the voltage across the resistor is 7 volts. Find the power that the resistor must dissipate when the voltage across it is 14 volts.
- A) $\frac{1}{4}$ watt B) $\frac{1}{8}$ watt C) $\frac{49}{16}$ watts D) $\frac{7}{16}$ watt

2 Solve Inverse Variation Problems

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Write an equation that expresses the relationship. Use k as the constant of variation.

- 1) s varies inversely as t.

A) $s = \frac{k}{t}$ B) $s = \frac{t}{k}$ C) $s = kt$ D) $ks = t$

- 2) g varies inversely as the square of m.

A) $g = \frac{k}{m^2}$ B) $g = \frac{m^2}{k}$ C) $g = \frac{k}{\sqrt{m}}$ D) $g = \frac{\sqrt{m}}{k}$

If y varies inversely as x, find the inverse variation equation for the situation.

- 3) $y = 3$ when $x = 4$

A) $y = \frac{12}{x}$ B) $y = \frac{3}{4}x$ C) $y = \frac{x}{12}$ D) $y = \frac{1}{12x}$

- 4) $y = 70$ when $x = 3$

A) $y = \frac{210}{x}$ B) $y = \frac{70}{3}x$ C) $y = \frac{x}{210}$ D) $y = \frac{1}{210x}$

- 5) $y = 54$ when $x = \frac{1}{6}$

A) $y = \frac{9}{x}$ B) $y = 324x$ C) $y = \frac{x}{9}$ D) $y = \frac{1}{9x}$

- 6) $y = \frac{1}{2}$ when $x = 6$

A) $y = \frac{3}{x}$ B) $y = \frac{1}{12}x$ C) $y = \frac{x}{3}$ D) $y = \frac{1}{3x}$

- 7) $y = 0.8$ when $x = 0.5$

A) $y = \frac{0.4}{x}$ B) $y = 1.6x$ C) $y = 2.5x$ D) $y = \frac{2.5}{x}$

Solve the problem.

- 8) x varies inversely as v , and $x = 48$ when $v = 8$. Find x when $v = 64$.
A) $x = 6$ B) $x = 64$ C) $x = 48$ D) $x = 8$
- 9) x varies inversely as y^2 , and $x = 4$ when $y = 10$. Find x when $y = 2$.
A) $x = 100$ B) $x = 80$ C) $x = 16$ D) $x = 5$

Solve.

- 10) When the temperature stays the same, the volume of a gas is inversely proportional to the pressure of the gas. If a balloon is filled with 132 cubic inches of a gas at a pressure of 14 pounds per square inch, find the new pressure of the gas if the volume is decreased to 66 cubic inches.
A) 28 pounds per square inch B) $\frac{33}{7}$ pounds per square inch
C) 14 pounds per square inch D) 26 pounds per square inch
- 11) The amount of time it takes a swimmer to swim a race is inversely proportional to the average speed of the swimmer. A swimmer finishes a race in 50 seconds with an average speed of 3 feet per second. Find the average speed of the swimmer if it takes 37.5 seconds to finish the race.
A) 4 feet per second B) 5 feet per second C) 6 feet per second D) 3 feet per second
- 12) If the force acting on an object stays the same, then the acceleration of the object is inversely proportional to its mass. If an object with a mass of 9 kilograms accelerates at a rate of 9 meters per second per second by a force, find the rate of acceleration of an object with a mass of 3 kilograms that is pulled by the same force.
A) 27 meters per second per second B) 3 meters per second per second
C) 18 meters per second per second D) 24 meters per second per second
- 13) If the voltage, V , in an electric circuit is held constant, the current, I , is inversely proportional to the resistance, R . If the current is 140 milliamperes when the resistance is 4 ohms, find the current when the resistance is 28 ohms.
A) 20 milliamperes B) 980 milliamperes C) 973 milliamperes D) 80 milliamperes
- 14) While traveling at a constant speed in a car, the centrifugal acceleration passengers feel while the car is turning is inversely proportional to the radius of the turn. If the passengers feel an acceleration of 10 feet per second per second when the radius of the turn is 70 feet, find the acceleration the passengers feel when the radius of the turn is 140 feet.
A) 5 feet per second per second B) 6 feet per second per second
C) 7 feet per second per second D) 8 feet per second per second

Write an equation that expresses the relationship. Use k as the constant of variation.

- 15) The intensity I of light varies inversely as the square of the distance D from the source. If the intensity of illumination on a screen 20 ft from a light is 3.5 foot-candles, find the intensity on a screen 50 ft from the light.
A) 0.56 foot-candles B) 1.4 foot-candles C) 8.75 foot-candles D) 21.88 foot-candles
- 16) The weight of a body above the surface of the earth is inversely proportional to the square of its distance from the center of the earth. What is the effect on the weight when the distance is multiplied by 8?
A) The weight is divided by 64 B) The weight is divided by 8
C) The weight is multiplied by 64 D) The weight is multiplied by 8

3 Solve Combined Variation Problems

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Write an equation that expresses the relationship. Use k for the constant of proportionality.

1) q varies directly as r and inversely as s.

A) $q = \frac{kr}{s}$

B) $q = \frac{ks}{r}$

C) $qrs = k$

D) $q + r - s = k$

2) q varies directly as r and inversely as the square of s.

A) $q = \frac{kr}{s^2}$

B) $q = \frac{ks^2}{r}$

C) $qrs^2 = k$

D) $q + r - s^2 = k$

3) r varies directly as the square of s and inversely as the cube of t.

A) $r = \frac{ks^2}{t^3}$

B) $rs^2t^3 = k$

C) $r = \frac{kt^3}{s^2}$

D) $r + s^2 - t^3 = k$

4) x varies directly as the square of y and inversely as z.

A) $x = \frac{ky^2}{z}$

B) $x = \frac{kz}{y^2}$

C) $x = k + y^2 - z^2$

D) $x = ky^2z$

5) p varies jointly as q and r and inversely as the square root of a.

A) $p = \frac{kqr}{\sqrt{a}}$

B) $p = \frac{kq}{r\sqrt{a}}$

C) $p = \frac{k(q+r)}{\sqrt{a}}$

D) $p = \frac{qr}{k\sqrt{a}}$

6) p varies directly as a and inversely as the difference between q and r.

A) $p = \frac{ka}{q-r}$

B) $p = \frac{a}{k(q-r)}$

C) $p = ka(q-r)$

D) $p = \frac{k}{a(q-r)}$

Determine the constant of variation for the stated condition.

7) h varies directly as f and inversely as g, and h = 4 when f = 28 and g = 28.

A) $k = 4$

B) $k = \frac{1}{4}$

C) $k = 1$

D) $k = 7$

8) z varies directly as x and inversely as y, and z = 5 when x = 135 and y = 45.

A) $k = \frac{5}{3}$

B) $k = \frac{3}{5}$

C) $k = 45$

D) $k = 9$

Find the variation equation for the variation statement.

9) h varies directly as f and inversely as g; h = 2 when f = 16 and g = 56

A) $h = \frac{7f}{g}$

B) $h = \frac{f}{7g}$

C) $h = 7fg$

D) $h = \frac{7}{fg}$

Solve the problem.

10) y varies directly as x and inversely as the square of z. y = 81 when x = 81 and z = 3. Find y when x = 62 and z = 2.

A) 139.5

B) 93

C) 27.56

D) 279

11) y varies jointly as a and b and inversely as the square root of c. y = 70 when a = 7, b = 10, and c = 9. Find y when a = 5, b = 3, and c = 4.

A) 22.5

B) 7.5

C) 11.25

D) 90

- 12) The volume V of a given mass of gas varies directly as the temperature T and inversely as the pressure P . A measuring device is calibrated to give $V = 250.8 \text{ in}^3$ when $T = 570^\circ$ and $P = 25 \text{ lb/in}^2$. What is the volume on this device when the temperature is 310° and the pressure is 10 lb/in^2 ?
- A) $V = 341 \text{ in}^3$ B) $V = 31 \text{ in}^3$ C) $V = 351 \text{ in}^3$ D) $V = 331 \text{ in}^3$
- 13) The time in hours it takes a satellite to complete an orbit around the earth varies directly as the radius of the orbit (from the center of the earth) and inversely as the orbital velocity. If a satellite completes an orbit 820 miles above the earth in 11 hours at a velocity of 22,000 mph, how long would it take a satellite to complete an orbit if it is at 1400 miles above the earth at a velocity of 36,000 mph? (Use 3960 miles as the radius of the earth.) Round your answer to the nearest hundredth of an hour.
- A) 7.54 hours B) 11.48 hours C) 1.97 hours D) 75.38 hours
- 14) The pressure of a gas varies jointly as the amount of the gas (measured in moles) and the temperature and inversely as the volume of the gas. If the pressure is 1134 kPa (kiloPascals) when the number of moles is 6, the temperature is 270° Kelvin, and the volume is 480 cc, find the pressure when the number of moles is 5, the temperature is 330° K, and the volume is 300 cc.
- A) 1848 B) 1792 C) 924 D) 952
- 15) Body-mass index, or BMI, takes both weight and height into account when assessing whether an individual is underweight or overweight. BMI varies directly as one's weight, in pounds, and inversely as the square of one's height, in inches. In adults, normal values for the BMI are between 20 and 25. A person who weighs 182 pounds and is 70 inches tall has a BMI of 26.11. What is the BMI, to the nearest tenth, for a person who weighs 120 pounds and who is 65 inches tall?
- A) 20 B) 20.3 C) 19.6 D) 19.3

4 Solve Problems Involving Joint Variation

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Write an equation that expresses the relationship. Use k as the constant of variation.

- 1) a varies jointly as y and the square of h .

A) $a = kyh^2$

B) $a = \frac{ky}{h^2}$

C) $a = kykh^2$

D) $a = \frac{kh^2}{y}$

- 2) d varies jointly as m and n .

A) $d = kmn$

B) $d = \frac{km}{n}$

C) $d = kmkn$

D) $d = \frac{kn}{m}$

- 3) w varies jointly as x and the cube of y .

A) $w = kxy^3$

B) $wxy^3 = k$

C) $w = k + x + y^3$

D) $w + x + y^3 = k$

- 4) r varies jointly as the square of s and the square of t .

A) $r = ks^2t^2$

B) $rs^2t^2 = k$

C) $r = k + s^2 + t^2$

D) $r + s^2 + t^2 = k$

- 5) a varies jointly as m and the sum of p and z .

A) $a = km(p + z)$

B) $a = \frac{km}{(p + z)}$

C) $a = km + p + z$

D) $a = k(mp + z)$

- 6) d varies jointly as b and the difference between p and h .

A) $d = kb(p - h)$

B) $d = \frac{kb}{(p - h)}$

C) $d = kb + p - h$

D) $d = k(bp - h)$

Find the variation equation for the variation statement.

7) z varies jointly as y and the cube of x ; $z = 144$ when $x = 2$ and $y = -3$

A) $y = -6x^3y$

B) $y = -6xy^3$

C) $y = 6x^3y$

D) $y = 6xy^3$

Determine the constant of variation for the stated condition.

8) c varies jointly as a and b , and $c = 90$ when $a = 60$ and $b = 24$.

A) $k = \frac{1}{16}$

B) $k = \frac{1}{24}$

C) $k = 16$

D) $k = 24$

9) c varies jointly as a and b , and $c = 560$ when $a = 20$ and $b = 7$.

A) $k = 4$

B) $k = \frac{1}{5}$

C) $k = \frac{1}{4}$

D) $k = 5$

10) h varies jointly as f and g , and $h = 112$ when $f = 42$, and $g = 24$.

A) $k = \frac{1}{9}$

B) $k = \frac{1}{24}$

C) $k = 9$

D) $k = 24$

Solve the problem.

11) t varies jointly as r and s . Find t when $r = 30$, $s = 11$, and $k = 5$.

A) $t = 1650$

B) $t = 330$

C) $t = 66$

D) $t = \frac{11}{6}$

12) y varies jointly as x and z . $y = 3.9$ when $x = 65$ and $z = 6$. Find y when $x = 50$ and $z = 8$.

A) 4

B) 400

C) 40

D) 8

13) f varies jointly as q^2 and h , and $f = 144$ when $q = 4$ and $h = 3$. Find f when $q = 2$ and $h = 5$.

A) $f = 60$

B) $f = 30$

C) $f = 12$

D) $f = 15$

14) f varies jointly as q^2 and h , and $f = -64$ when $q = 4$ and $h = 2$. Find f when $q = 2$ and $h = 6$.

A) $f = -48$

B) $f = -24$

C) $f = -8$

D) $f = -12$

15) f varies jointly as q^2 and h , and $f = 36$ when $q = 3$ and $h = 2$. Find q when $f = 160$ and $h = 5$.

A) $q = 4$

B) $q = 2$

C) $q = 3$

D) $q = 5$

16) f varies jointly as q^2 and h , and $f = 36$ when $q = 3$ and $h = 2$. Find h when $f = 192$ and $q = 4$.

A) $h = 6$

B) $h = 2$

C) $h = 3$

D) $h = 4$

17) The amount of paint needed to cover the walls of a room varies jointly as the perimeter of the room and the height of the wall. If a room with a perimeter of 35 feet and 10-foot walls requires 3.5 quarts of paint, find the amount of paint needed to cover the walls of a room with a perimeter of 65 feet and 10-foot walls.

A) 6.5 quarts

B) 650 quarts

C) 65 quarts

D) 13 quarts

18) The power that a resistor must dissipate is jointly proportional to the square of the current flowing through the resistor and the resistance of the resistor. If a resistor needs to dissipate 196 watts of power when 7 amperes of current is flowing through the resistor whose resistance is 4 ohms, find the power that a resistor needs to dissipate when 4 amperes of current are flowing through a resistor whose resistance is 2 ohms.

A) 32 watts

B) 8 watts

C) 16 watts

D) 56 watts

- 19) While traveling in a car, the centrifugal force a passenger experiences as the car drives in a circle varies jointly as the mass of the passenger and the square of the speed of the car. If a passenger experiences a force of 259.2 newtons when the car is moving at a speed of 60 kilometers per hour and the passenger has a mass of 80 kilograms, find the force a passenger experiences when the car is moving at 30 kilometers per hour and the passenger has a mass of 100 kilograms.
- A) 81 newtons B) 90 newtons C) 72 newtons D) 99 newtons
- 20) The amount of simple interest earned on an investment over a fixed amount of time is jointly proportional to the principle invested and the interest rate. A principle investment of \$2000.00 with an interest rate of 2% earned \$160.00 in simple interest. Find the amount of simple interest earned if the principle is \$2300.00 and the interest rate is 7%.
- A) \$644.00 B) \$64,400.00 C) \$184.00 D) \$560.00
- 21) The voltage across a resistor is jointly proportional to the resistance of the resistor and the current flowing through the resistor. If the voltage across a resistor is 12 volts for a resistor whose resistance is 4 ohms and when the current flowing through the resistor is 3 amperes, find the voltage across a resistor whose resistance is 7 ohms and when the current flowing through the resistor is 5 amperes.
- A) 35 volts B) 20 volts C) 15 volts D) 21 volts
- 22) The pressure of a gas varies jointly as the amount of the gas (measured in moles) and the temperature and inversely as the volume of the gas. If the pressure is 1350 kPa (kiloPascals) when the number of moles is 7, the temperature is 300° Kelvin, and the volume is 560 cc, find the pressure when the number of moles is 10, the temperature is 290° K, and the volume is 600 cc.
- A) 1740 B) 1560 C) 870 D) 960

Ch. 2 Polynomial and Rational Functions

Answer Key

2.1 Complex Numbers

1 Add and Subtract Complex Numbers

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A

2 Multiply Complex Numbers

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A

3 Divide Complex Numbers

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A

4 Perform Operations with Square Roots of Negative Numbers

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A

5 Solve Quadratic Equations with Complex Imaginary Solutions

- 1) A
- 2) A
- 3) A

4) A

5) A

2.2 Quadratic Functions

1 Recognize Characteristics of Parabolas

1) A

2) A

3) A

4) A

5) A

6) A

7) A

8) A

9) A

10) A

11) A

12) A

13) A

14) A

15) A

16) A

17) A

18) A

19) A

20) A

21) A

22) A

23) A

24) A

25) A

26) A

27) A

28) A

29) A

30) A

31) A

32) A

33) A

34) A

35) A

36) A

37) A

38) A

39) A

40) A

41) A

42) A

43) A

44) A

45) A

46) A

47) A

48) A

49) A

50) A

- 51) A
- 52) A
- 53) A
- 54) A
- 55) A
- 56) A
- 57) A
- 58) A
- 59) A
- 60) A
- 61) A
- 62) A
- 63) A
- 64) A
- 65) A
- 66) A

2 Graph Parabolas

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A

3 Determine a Quadratic Function's Minimum or Maximum Value

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A

4 Solve Problems Involving a Quadratic Function's Minimum or Maximum Value

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A
- 15) A
- 16) A
- 17) A
- 18) A

19) A

20) A

2.3 Polynomial Functions and Their Graphs

1 Identify Polynomial Functions

1) A

2) A

3) A

4) A

5) A

6) A

7) A

8) A

9) A

10) A

11) A

12) A

13) A

14) A

15) A

16) A

17) A

18) A

2 Recognize Characteristics of Graphs of Polynomial Functions

1) A

2) A

3) A

4) A

5) A

6) A

7) A

8) A

9) A

10) A

11) A

12) A

13) A

14) A

15) A

16) A

17) A

18) A

19) A

20) A

21) A

22) A

23) A

24) A

25) A

26) C

27) A

28) A

29) A

30) C

31) A

- 32) A
- 33) C
- 34) C
- 35) C
- 36) C
- 37) C
- 38) A
- 39) A
- 40) C
- 41) A

3 Determine End Behavior

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A
- 15) A
- 16) A
- 17) A
- 18) A
- 19) A
- 20) A
- 21) A

4 Use Factoring to Find Zeros of Polynomial Functions

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A

5 Identify Zeros and Their Multiplicities

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A

6 Use the Intermediate Value Theorem

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A

7 Understand the Relationship Between Degree and Turning Points

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A
- 15) C

8 Graph Polynomial Functions

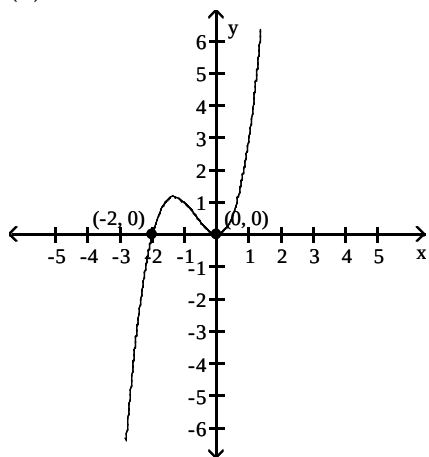
- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A
- 15) A
- 16) A
- 17) A
- 18) A
- 19) A
- 20) A

21) (a) falls to the left and rises to the right

(b) x-intercepts: $(0, 0)$, touches x-axis and turns; $(-2, 0)$, crosses x-axis

(c) y-intercept: $(0, 0)$

(d)

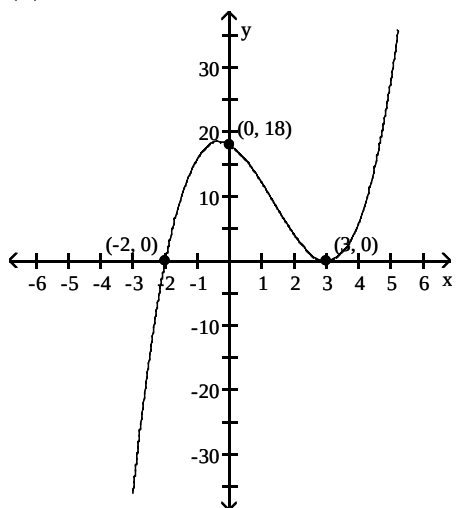


22) (a) falls to the left and rises to the right

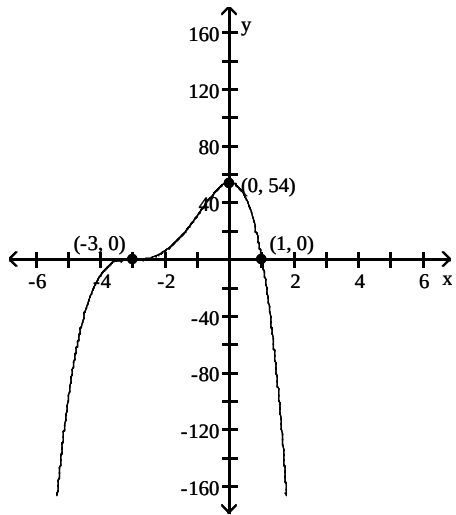
(b) x-intercepts: $(3, 0)$, touches x-axis and turns; $(-2, 0)$, crosses x-axis

(c) y-intercept: $(0, 18)$

(d)



- 23) (a) falls to the left and to the right
 (b) x-intercepts: $(-3, 0)$, crosses x-axis; $(1, 0)$, crosses x-axis
 (c) y-intercept: $(0, 54)$
 (d)



2.4 Dividing Polynomials: Remainder and Factor Theorems

1 Use Long Division to Divide Polynomials

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A
- 15) A
- 16) A
- 17) A
- 18) A
- 19) A
- 20) A

2 Use Synthetic Division to Divide Polynomials

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A

3 Evaluate a Polynomial Using the Remainder Theorem

- 1) A

- 2) A
- 3) A
- 4) A
- 5) A

4 Use the Factor Theorem to Solve a Polynomial Equation

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A

2.5 Zeros of Polynomial Functions

1 Use the Rational Zero Theorem to Find Possible Rational Zeros

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A

2 Find Zeros of a Polynomial Function

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A

3 Solve Polynomial Equations

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A

4 Use the Linear Factorization Theorem to Find Polynomials with Given Zeros

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A

5 Use Descartes's Rule of Signs

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A

2.6 Rational Functions and Their Graphs

1 Find the Domains of Rational Functions

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A

2 Use Arrow Notation

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A

3 Identify Vertical Asymptotes

- 1) A
- 2) A
- 3) A
- 4) D
- 5) A
- 6) A
- 7) A

4 Identify Horizontal Asymptotes

- 1) A
- 2) A
- 3) D
- 4) A
- 5) A
- 6) A
- 7) A

5 Use Transformations to Graph Rational Functions

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A

6) A

6 Graph Rational Functions

1) A

2) A

3) A

4) A

5) A

6) A

7) A

8) A

9) A

10) A

11) A

12) A

13) A

14) A

15) A

16) D

17) A

18) A

19) A

20) A

21) A

22) A

23) D

24) A

25) B

26) B

27) A

28) A

29) B

7 Identify Slant Asymptotes

1) A

2) A

3) D

4) A

5) A

6) A

7) A

8) A

9) A

8 Solve Applied Problems Involving Rational Functions

1) A

2) A

3) A

4) A

5) A

6) A

7) A

8) A

9) A

2.7 Polynomial and Rational Inequalities

1 Solve Polynomial Inequalities

1) A

- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A
- 15) A
- 16) A
- 17) A
- 18) A
- 19) A
- 20) A
- 21) A

2 Solve Rational Inequalities

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A

3 Solve Problems Modeled by Polynomial or Rational Inequalities

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A

2.8 Modeling Using Variation

1 Solve Direct Variation Problems

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A

- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A
- 15) A
- 16) A
- 17) A
- 18) A
- 19) A
- 20) A
- 21) A
- 22) A

2 Solve Inverse Variation Problems

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A
- 15) A
- 16) A

3 Solve Combined Variation Problems

- 1) A
- 2) A
- 3) A
- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A
- 15) A

4 Solve Problems Involving Joint Variation

- 1) A
- 2) A
- 3) A

- 4) A
- 5) A
- 6) A
- 7) A
- 8) A
- 9) A
- 10) A
- 11) A
- 12) A
- 13) A
- 14) A
- 15) A
- 16) A
- 17) A
- 18) A
- 19) A
- 20) A
- 21) A
- 22) A