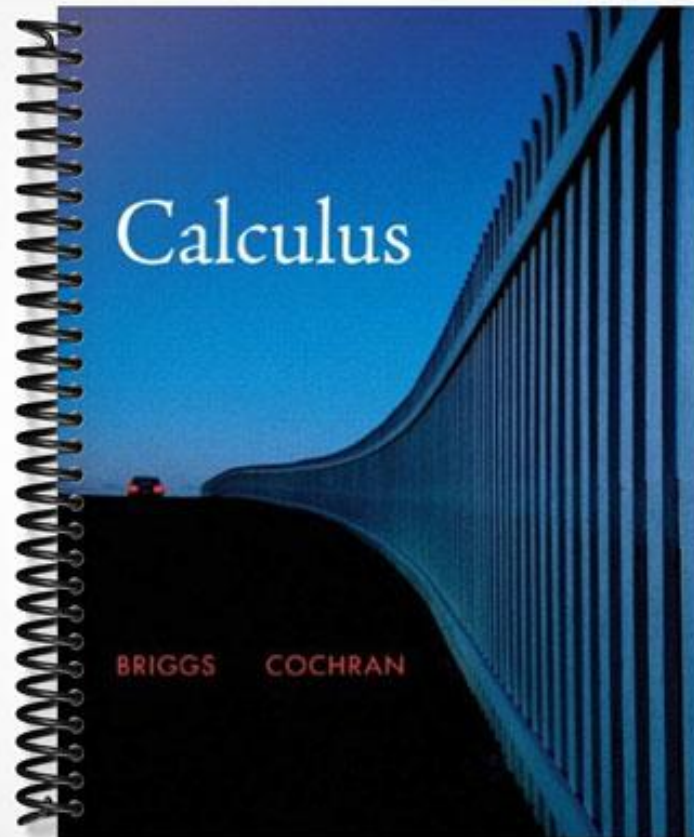


**TEST BANK**



**MULTIPLE CHOICE.** Choose the one alternative that best completes the statement or answers the question.

Find the average velocity of the function over the given interval.

1)  $y = x^2 + 2x, [1, 4]$  1) \_\_\_\_\_  
 A) 7                      B) 6                      C) 8                      D)  $\frac{21}{4}$

2)  $y = 4x^3 - 6x^2 - 6, [6, 8]$  2) \_\_\_\_\_  
 A) 127                      B)  $\frac{829}{4}$                       C) 829                      D) 508

3)  $y = \sqrt{2x}, [2, 8]$  3) \_\_\_\_\_  
 A)  $\frac{1}{3}$                       B)  $\frac{3}{10}$                       C) 2                      D) 7

4)  $y = \frac{3}{x-2}, [4, 7]$  4) \_\_\_\_\_  
 A) 7                      B)  $\frac{3}{10}$                       C) 2                      D)  $\frac{1}{3}$

5)  $y = 4x^2, \left[0, \frac{7}{4}\right]$  5) \_\_\_\_\_  
 A) 2                      B)  $\frac{1}{3}$                       C) 7                      D)  $\frac{3}{10}$

6)  $y = -3x^2 - x, [5, 6]$  6) \_\_\_\_\_  
 A)  $\frac{1}{2}$                       B) -34                      C) -2                      D)  $\frac{1}{6}$

7)  $h(t) = \sin(3t), \left[0, \frac{\pi}{6}\right]$  7) \_\_\_\_\_  
 A)  $\frac{6}{\pi}$                       B)  $\frac{\pi}{6}$                       C)  $\frac{6}{\pi}$                       D)  $\frac{3}{\pi}$

8)  $g(t) = 5 + \tan t, \left[-\frac{\pi}{4}, \frac{\pi}{4}\right]$  8) \_\_\_\_\_  
 A)  $\frac{16}{11}$                       B)  $\frac{4}{\pi}$                       C) 0                      D)  $\frac{4}{\pi}$

Use the table to find the instantaneous velocity of y at the specified value of x.

9)  $x = 1.$

x	y
0	0
0.2	0.02
0.4	0.08
0.6	0.18
0.8	0.32
1.0	0.5
1.2	0.72
1.4	0.98

9)

—  
—  
—  
—

A) 2

B) 1

C) 0.5

D) 1.5

10)  $x = 1$ .

10) \_\_\_\_\_

x	y
0	0
0.2	0.01
0.4	0.04
0.6	0.09
0.8	0.16
1.0	0.25
1.2	0.36
1.4	0.49

A) 2

B) 1.5

C) 0.5

D) 1

11)  $x = 1$ .

11) \_\_\_\_\_

x	y
0	0
0.2	0.12
0.4	0.48
0.6	1.08
0.8	1.92
1.0	3
1.2	4.32
1.4	5.88

A) 8

B) 6

C) 2

D) 4

12)  $x = 2$ .

12) \_\_\_\_\_

x	y
0	10
0.5	38
1.0	58
1.5	70
2.0	74
2.5	70
3.0	58
3.5	38
4.0	10

A) -8

B) 0

C) 8

D) 4

13)  $x = 1$ .

x	y
0.900	-0.05263
0.990	-0.00503
0.999	-0.0005
1.000	0.0000
1.001	0.0005
1.010	0.00498
1.100	0.04762

—  
—

- A) -0.5                      B) 0.5                      C) 1                      D) 0

**Find the slope of the curve for the given value of x.**

14)  $y = x^2 + 5x, x = 4$  14) \_\_\_\_\_

- A)  $\frac{1}{20}$                       B) slope is 13  
slope is  
C)  $\frac{4}{25}$                       D) slope is -39  
slope is -

15)  $y = x^2 + 11x - 15, x = 1$  15) \_\_\_\_\_

- A)  $\frac{1}{20}$                       B) slope is -39  
slope is  
C)  $\frac{4}{25}$                       D) slope is 13  
slope is -

16)  $y = x^3 - 9x, x = 1$  16) \_\_\_\_\_

- A) slope is 3                      B) slope is -6  
C) slope is -3                      D) slope is 1

17)  $y = x^3 - 2x^2 + 4, x = 1$  17) \_\_\_\_\_

- A) slope is 0                      B) slope is -1  
C) slope is -1                      D) slope is 1

18)  $y = -4 - x^3, x = -1$  18) \_\_\_\_\_

- A) slope is -1                      B) slope is 0  
C) slope is -3                      D) slope is 3

**Solve the problem.**

19)  $\lim_{x \rightarrow 0^-} f(x) = L_1, \lim_{x \rightarrow 0^+} f(x) = L_2, \text{ and } L_1 \neq L_2, \text{ which of the}$  19) \_\_\_\_\_

following statements is true?

- I.  $\lim_{x \rightarrow 0} f(x) = L_1$   
II.  $\lim_{x \rightarrow 0} f(x) = L_2$   
III.  $\lim_{x \rightarrow 0} f(x)$  does not exist.

- A) II                      B) I                      C) none                      D) III

20)

Given  $\lim_{x \rightarrow 0^-}$

$f(x) = L_1$ , 20) —  
 $\lim_{x \rightarrow 0^+} f(x) = L_1$ , —  
 and  $L_1 = L_2$ , which  
 of the  
 following  
 statements  
 is  
 false?

I.

$$\lim_{x \rightarrow 0} f(x) = L_1$$

II.

$$\lim_{x \rightarrow 0} f(x) = L_2$$

I.

$$\lim_{x \rightarrow 0} f(x)$$

does not exist.

- A) I                      B) none                      C) II                      D) III

21) If  $\lim_{x \rightarrow 0} f(x) = L$ , which of the following expressions are true?

21) \_\_\_\_\_

I.  $\lim_{x \rightarrow 0^-} f(x)$  does not exist.

II.  $\lim_{x \rightarrow 0^+} f(x)$  does not exist.

III.  $\lim_{x \rightarrow 0^-} f(x) = L$

IV.  $\lim_{x \rightarrow 0^+} f(x) = L$

- A) III and IV only                      B) I and IV only  
 C) II and III only                      D) I and II only

22) What conditions, when present, are sufficient to conclude that a function  $f(x)$  has a limit as  $x$  approaches some value of  $a$ ?

22) \_\_\_\_\_

A) The limit of  $f(x)$  as  $x \rightarrow a$  from the left exists, the limit of  $f(x)$  as  $x \rightarrow a$  from the right exists, and these two limits are the same.

B)  $f(a)$  exists, the limit of  $f(x)$  as  $x \rightarrow a$  from the left exists, and the limit of  $f(x)$  as  $x \rightarrow a$  from the right exists.

C) The limit of  $f(x)$  as  $x \rightarrow a$  from the left exists, the limit of  $f(x)$  as

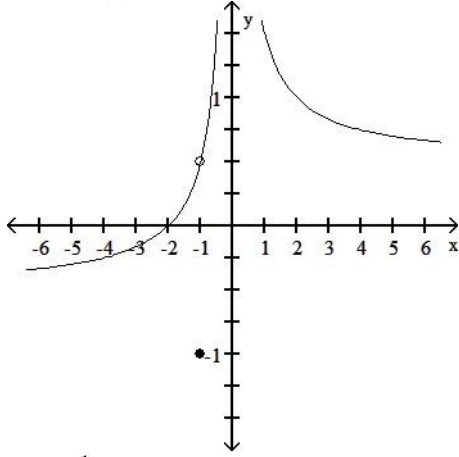
$x \rightarrow a$  from the right exists, and at least one of these limits is the same as  $f(a)$ .

D) Either the limit of  $f(x)$  as  $x \rightarrow a$  from the left exists or the limit of  $f(x)$  as  $x \rightarrow a$  from the right exists

Use the graph to evaluate the limit.

23)  $\lim_{x \rightarrow -1} f(x)$

23) \_\_\_\_\_



A)  $\frac{1}{2}$

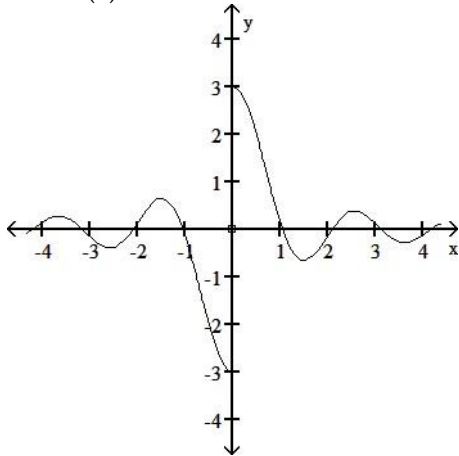
B)  $\infty$

C) -1

D)  $\frac{1}{2}$

24)  $\lim_{x \rightarrow 0} f(x)$

24) \_\_\_\_\_



A) -3

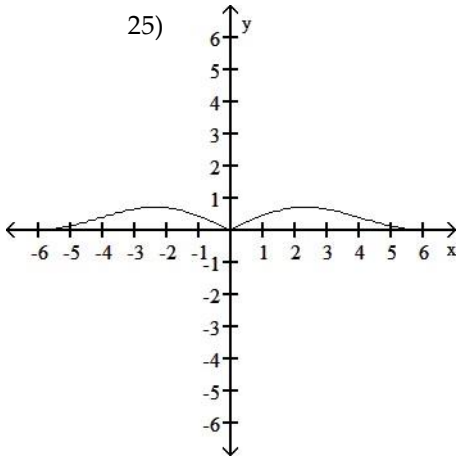
B) 0

C) 3

D) does not exist

25)  $\lim_{x \rightarrow 0} f(x)$

25)

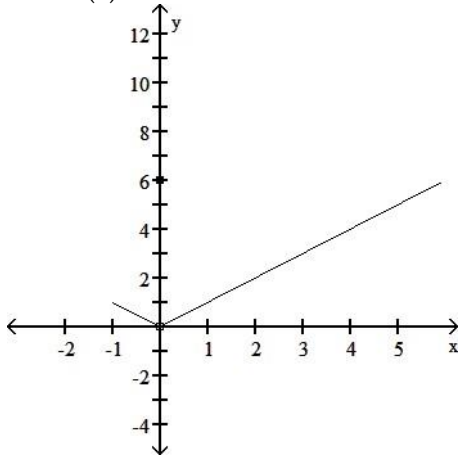


—  
—

- A) -1
- C) 1

- B) 0
- D) does not exist

26)  $\lim_{x \rightarrow 0} f(x)$

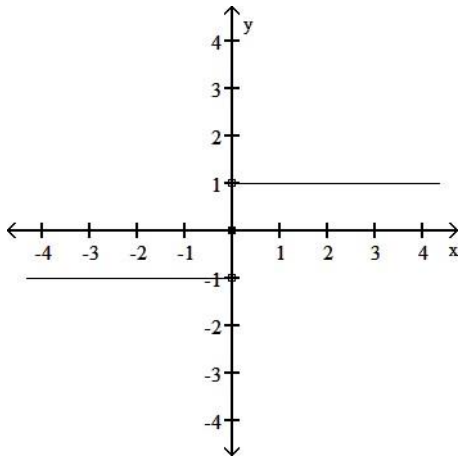


26) \_\_\_\_\_

- A) 0
- C) -1

- B) does not exist
- D) 6

27)  $\lim_{x \rightarrow 0} f(x)$

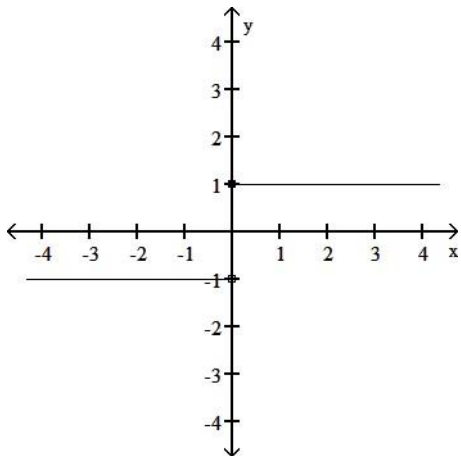


27) \_\_\_\_\_

- A)  $\infty$
- C) does not exist

- B) -1
- D) 1

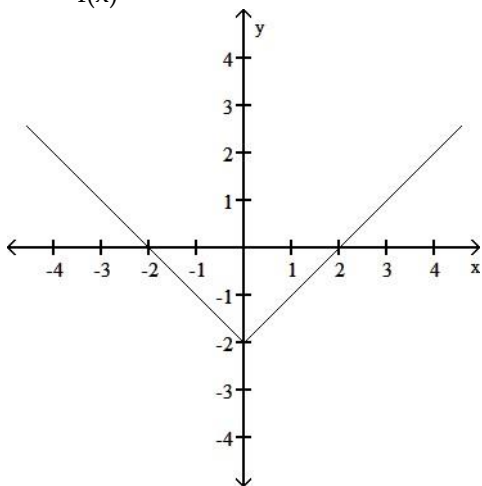
28)  $\lim_{x \rightarrow 0} f(x)$



- A) -1                      B) 1  
C) does not exist        D)  $\infty$

28) \_\_\_\_\_

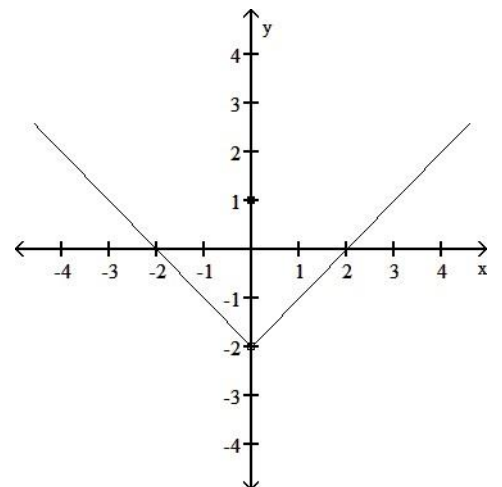
29)  $\lim_{x \rightarrow 0} f(x)$



- A) -2                      B) 0  
C) 2                        D) does not exist

29) \_\_\_\_\_

30)  $\lim_{x \rightarrow 0} f(x)$



30)  $\lim_{x \rightarrow 0} f(x)$



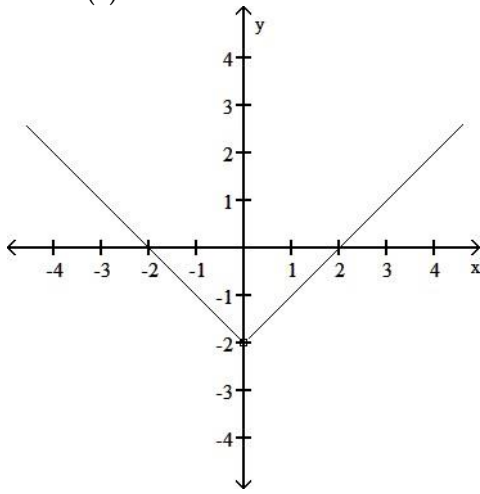
30)

- A) 1
- C) -2

- B) does not exist
- D) 0

31)  $\lim_{x \rightarrow 0} f(x)$

31) \_\_\_\_\_

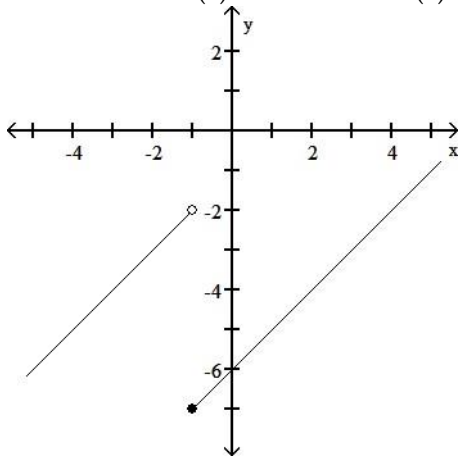


- A) 2
- C) -2

- B) does not exist
- D) -1

32) Find  $\lim_{x \rightarrow (-1)^-} f(x)$  and  $\lim_{x \rightarrow (-1)^+} f(x)$

32) \_\_\_\_\_



A) -7; -5

B) -2; -7

C) -7; -2

D) -5; -2

Use the table of values of f to estimate the limit.

33) Let  $f(x) = x^2 + 8x - 2$ , find  $\lim_{x \rightarrow 2} f(x)$ .

33) \_\_\_\_\_

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)						

A)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	16.692	17.592	17.689	17.710	17.808	18.789

; limit = 17.70

B)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	16.810	17.880	17.988	18.012	18.120	19.210

; limit = 18.0

C)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	5.043	5.364	5.396	5.404	5.436	5.763

; limit = 5.40

D)

x	1.9	1.99	1.999	2.001	2.01	2.1
f(x)	5.043	5.364	5.396	5.404	5.436	5.763

; limit =  $\infty$

34)

Let  $f(x) = \frac{x-4}{\sqrt{x}-2}$ , find  $\lim_{x \rightarrow 4} f(x)$ .

34) \_\_\_\_\_

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)						

A)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	1.19245	1.19925	1.19993	1.20007	1.20075	1.20745

; limit =  $\infty$

B)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	5.07736	5.09775	5.09978	5.10022	5.10225	5.12236

; limit = 5.10

C)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	1.19245	1.19925	1.19993	1.20007	1.20075	1.20745

; limit = 1.20

D)

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	3.97484	3.99750	3.99975	4.00025	4.00250	4.02485

; limit = 4.0

35)

Let  $f(x) = x^2 - 5$ , find  $\lim_{x \rightarrow 0} f(x)$ .

35) \_\_\_\_\_

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)						

A)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-4.9900	-4.9999	-5.0000	-5.0000	-4.9999	-4.9900

; limit = -5.0

B)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-2.9910	-2.9999	-3.0000	-3.0000	-2.9999	-2.9910

; limit = -3.0

C)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-1.4970	-1.4999	-1.5000	-1.5000	-1.4999	-1.4970

; limit =  $\infty$

D)

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)	-1.4970	-1.4999	-1.5000	-1.5000	-1.4999	-1.4970

; limit =  $\infty$

limit = -15.0

36)  $\frac{x-4}{x^2-5x+4}$ , find  $\lim_{x \rightarrow 4} f(x)$ . 36) \_\_\_\_\_

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)						

A) 

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	0.4448	0.4344	0.4334	0.4332	0.4322	0.4226

 ; limit = 0.4333

B) 

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	-0.3448	-0.3344	-0.3334	-0.3332	-0.3322	-0.3226

 ; limit = -0.3333

C) 

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	0.2448	0.2344	0.2334	0.2332	0.2322	0.2226

 ; limit = 0.2333

D) 

x	3.9	3.99	3.999	4.001	4.01	4.1
f(x)	0.3448	0.3344	0.3334	0.3332	0.3322	0.3226

 ; limit = 0.3333

37)  $\frac{x^2+2x-15}{x^2-2x-3}$ , find  $\lim_{x \rightarrow 3} f(x)$ . 37) \_\_\_\_\_

x	2.9	2.99	2.999	3.001	3.01	3.1
f(x)						

A) 

x	2.9	2.99	2.999	3.001	3.01	3.1
f(x)	-0.9048	-0.9900	-0.9990	-1.0010	-1.0101	-1.1053

 ; limit = -1

B) 

x	2.9	2.99	2.999	3.001	3.01	3.1
f(x)	2.0256	2.0025	2.0003	1.9998	1.9975	1.9756

 ; limit = 2

C) 

x	2.9	2.99	2.999	3.001	3.01	3.1
f(x)	2.1256	2.1025	2.1003	2.0998	2.0975	2.0756

 ; limit = 2.1

D) 

x	2.9	2.99	2.999	3.001	3.01	3.1
f(x)	1.9256	1.9025	1.9003	1.8998	1.8975	1.8756

 ; limit = 1.9

38)  $\frac{\sin(5x)}{x}$ , find  $\lim_{x \rightarrow 0} f(x)$ . 38) \_\_\_\_\_

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(x)		4.99791693			4.99791693	

- A) limit = 5  
 C) limit does not exist
- B) limit = 0  
 D) limit = 4.5

39)  $\lim_{\theta \rightarrow 0} \frac{\cos(5\theta)}{\theta}$  \_\_\_\_\_  
 Let  $f(\theta) = \frac{\cos(5\theta)}{\theta}$ , find  $\lim_{\theta \rightarrow 0} f(\theta)$ .

x	-0.1	-0.01	-0.001	0.001	0.01	0.1
f(θ)	-8.7758256					8.7758256

- A) limit = 8.7758256  
 C) limit = 0
- B) limit = 5  
 D) limit does not exist

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

**Provide an appropriate response.**

40)  $\frac{x^2}{6} < \frac{x \sin(x)}{2 - 2 \cos(x)} < 1$  \_\_\_\_\_

It can be shown that the inequalities  $1 - \frac{x^2}{6} < \frac{x \sin(x)}{2 - 2 \cos(x)} < 1$  hold for all values of  $x$  close to zero. What, if anything, does this

tell you about  $\frac{x \sin(x)}{2 - 2 \cos(x)}$ ? Explain.

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

41) Write the formal notation for the principle "the limit of a quotient is the quotient of the limits" and include a statement of any restrictions on the principle. \_\_\_\_\_

A)  $\lim_{x \rightarrow a} \frac{g(x)}{f(x)} = \frac{g(a)}{f(a)}$

B) If  $\lim_{x \rightarrow a} g(x) = M$  and  $\lim_{x \rightarrow a} f(x) = L$ , then

$$\lim_{x \rightarrow a} \frac{g(x)}{f(x)} = \frac{\lim_{x \rightarrow a} g(x)}{\lim_{x \rightarrow a} f(x)} = \frac{M}{L}$$

C) If  $\lim_{x \rightarrow a} g(x) = M$  and  $\lim_{x \rightarrow a} f(x) = L$ , provided that  $f(a) \neq 0$ , then

$$\lim_{x \rightarrow a} \frac{g(x)}{f(x)} = \frac{\lim_{x \rightarrow a} g(x)}{\lim_{x \rightarrow a} f(x)} = \frac{M}{L}$$

D)  $\lim_{x \rightarrow a} \frac{g(x)}{f(x)} = \frac{g(a)}{f(a)}$ , provided that  $L \neq 0$ .

42) Provide a short sentence that summarizes the general limit principle given by the formal notation \_\_\_\_\_

$$\lim_{x \rightarrow a} [f(x) \pm g(x)] = \lim_{x \rightarrow a} f(x) \pm \lim_{x \rightarrow a} g(x) = L \pm M,$$

given that

$$\lim_{x \rightarrow a} f(x) = L \quad \text{and} \quad \lim_{x \rightarrow a} g(x) = M.$$



51)  $\lim_{x \rightarrow 6} f(x) = 2$  and  $\lim_{x \rightarrow 6} g(x) = 5$ . Find  $\lim_{x \rightarrow 6} [f(x) + g(x)]^2$ . 51) \_\_\_\_\_  
 Let A) 49 B) 7 C) -3 D) 29

52)  $\lim_{x \rightarrow 7} f(x) = 32$ . Find  $\lim_{x \rightarrow 7} \sqrt[5]{f(x)}$ . 52) \_\_\_\_\_  
 Let A) 7 B) 2 C) 32 D) 5

53)  $\lim_{x \rightarrow -7} f(x) = 2$  and  $\lim_{x \rightarrow -7} g(x) = 3$ . Find  $\lim_{x \rightarrow -7} \left[ \frac{8f(x) - 5g(x)}{4 + g(x)} \right]$ . 53) \_\_\_\_\_  
 Let A) -7 B) -1 C)  $\frac{31}{7}$  D)  $\frac{1}{7}$

**Find the limit.**

54)  $\lim_{x \rightarrow 2} (x^3 + 5x^2 - 7x + 1)$  54) \_\_\_\_\_  
 A) 29 B) 15  
 C) 0 D) does not exist

55)  $\lim_{x \rightarrow 2} (2x^5 - 3x^4 - 4x^3 + x^2 - 5)$  55) \_\_\_\_\_  
 A) 79 B) -49 C) 47 D) -17

56)  $\lim_{x \rightarrow -1} \frac{x}{3x + 2}$  56) \_\_\_\_\_  
 A) does not exist B)  $\frac{1}{5}$   
 C) 1 D) 0

57)  $\lim_{x \rightarrow 0} \frac{x^3 - 6x + 8}{x - 2}$  57) \_\_\_\_\_  
 A) Does not exist B) 0  
 C) -4 D) 4

58)  $\lim_{x \rightarrow 1} \frac{3x^2 + 7x - 2}{3x^2 - 4x - 2}$  58) \_\_\_\_\_  
 A)  $\frac{8}{3}$  B) Does not exist  
 C) 0 D)  $\frac{7}{4}$

59)  $\lim_{x \rightarrow -2} (x + 3)^2(x - 1)^3$  59) \_\_\_\_\_  
 A) -675 B) -27 C) -25 D) -1

60)  $\lim_{x \rightarrow 5} \sqrt{x^2 + 2x + 1}$  60) \_\_\_\_\_  
 A)  $\pm 6$  B) does not exist  
 C) 36 D) 6

61)  $\lim_{x \rightarrow -1} \sqrt{6x + 54}$  61) \_\_\_\_\_  
 A)  $4\sqrt{3}$       B) 48      C)  $-4\sqrt{3}$       D) -48

62)  $\lim_{h \rightarrow 0} \frac{2}{\sqrt{3h + 4} + 2}$  62) \_\_\_\_\_  
 A) 1/2      B) 2  
 C) Does not exist      D) 1

63)  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{x}$  63) \_\_\_\_\_  
 A) 1/4      B) 0  
 C) 1/2      D) Does not exist

**Determine the limit by sketching an appropriate graph.**

64)  $\lim_{x \rightarrow 6^-} f(x)$ , where  $f(x) = \begin{cases} -2x - 6 & \text{for } x < 6 \\ 4x - 5 & \text{for } x \geq 6 \end{cases}$  64) \_\_\_\_\_  
 A) -4      B) -5      C) 19      D) -18

65)  $\lim_{x \rightarrow 6^+} f(x)$ , where  $f(x) = \begin{cases} -4x - 3 & \text{for } x < 6 \\ 5x - 2 & \text{for } x \geq 6 \end{cases}$  65) \_\_\_\_\_  
 A) -2      B) -27      C) 28      D) -1

66)  $\lim_{x \rightarrow 4^+} f(x)$ , where  $f(x) = \begin{cases} x^2 + 4 & \text{for } x \neq 4 \\ 0 & \text{for } x = 4 \end{cases}$  66) \_\_\_\_\_  
 A) 20      B) 0      C) 12      D) 16

67)  $\lim_{x \rightarrow 5^-} f(x)$ , where  $f(x) = \begin{cases} \sqrt{16 - x^2} & 0 \leq x < 4 \\ 4 & 4 \leq x < 5 \\ 5 & x = 5 \end{cases}$  67) \_\_\_\_\_  
 A) Does not exist      B) 0  
 C) 4      D) 5

68)  $\lim_{x \rightarrow -7^+} f(x)$ , where  $f(x) = \begin{cases} x & -7 \leq x < 0, \text{ or } 0 < x \leq 3 \\ 1 & x = 0 \\ 0 & x < -7 \text{ or } x > 3 \end{cases}$  68) \_\_\_\_\_  
 A) 7      B) -0  
 C) -7      D) Does not exist

**Find the limit, if it exists.**

69)  $\lim_{x \rightarrow 0} \frac{x^3 + 12x^2 - 5x}{5x}$  69) \_\_\_\_\_  
 A) 5      B) Does not exist  
 C) -1      D) 0

70)  $\lim_{x \rightarrow 1} \frac{x^4 - 1}{x - 1}$  70) \_\_\_\_\_  
 A) 4      B) 2  
 C) Does not exist      D) 0

- 71)  $\lim_{x \rightarrow 10} \frac{x^2 - 100}{x - 10}$  71) \_\_\_\_\_  
 A) 1 B) 20  
 C) 10 D) Does not exist
- 72)  $\lim_{x \rightarrow -9} \frac{x^2 + 17x + 72}{x + 9}$  72) \_\_\_\_\_  
 A) Does not exist B) 306  
 C) 17 D) -1
- 73)  $\lim_{x \rightarrow 5} \frac{x^2 + 3x - 40}{x - 5}$  73) \_\_\_\_\_  
 A) 3 B) Does not exist  
 C) 0 D) 13
- 74)  $\lim_{x \rightarrow 2} \frac{x^2 + 2x - 8}{x^2 - 4}$  74) \_\_\_\_\_  
 A)  $\frac{1}{2}$  B) Does not exist  
 C)  $\frac{3}{2}$  D) 0
- 75)  $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x^2 - 7x + 12}$  75) \_\_\_\_\_  
 A) Does not exist B) -3  
 C) -6 D) 0
- 76)  $\lim_{x \rightarrow 2} \frac{x^2 - 5x + 6}{x^2 + 3x - 10}$  76) \_\_\_\_\_  
 A)  $\frac{1}{7}$  B)  $\frac{5}{7}$   
 C) Does not exist D)  $\frac{1}{7}$
- 77)  $\lim_{h \rightarrow 0} \frac{(x+h)^3 - x^3}{h}$  77) \_\_\_\_\_  
 A) Does not exist B)  $3x^2$   
 C) 0 D)  $3x^2 + 3xh + h^2$
- 78)  $\lim_{x \rightarrow 9} \frac{|9-x|}{9-x}$  78) \_\_\_\_\_  
 A) 0 B) 1  
 C) Does not exist D) -1

Provide an appropriate response.

79)

It can be shown that the inequalities  $-x \leq x \cos\left(\frac{1}{x}\right) \leq x$  hold for all values of  $x \geq 0$ .

Find  $\lim_{x \rightarrow 0} \cos\left(\frac{1}{x}\right)$



if it  
exists.

79)

- A) 0.0007
- C) 1

- B) does not exist
- D) 0

—  
—

80)

The inequality  $1 - \frac{x^2}{2} < \frac{\sin x}{x} < 1$  holds when  $x$  is measured in radians and  $|x| < 1$ .

Find  $\lim_{x \rightarrow 0} \frac{\sin x}{x}$  if it exists.

- A) 0
- C) does not exist

- B) 0.0007
- D) 1

80) \_\_\_\_\_

81)

If  $x^3 \leq f(x) \leq x$  for  $x$  in  $[-1,1]$ , find  $\lim_{x \rightarrow 0} f(x)$  if it exists.

- A) -1
- C) 1

- B) does not exist
- D) 0

81) \_\_\_\_\_

- 1) A
- 2) D
- 3) A
- 4) B
- 5) C
- 6) B
- 7) C
- 8) D
- 9) B
- 10) C
- 11) B
- 12) B
- 13) B
- 14) B
- 15) D
- 16) B
- 17) B
- 18) C
- 19) D
- 20) D
- 21) A
- 22) A
- 23) A
- 24) D
- 25) B
- 26) A
- 27) C
- 28) C
- 29) A
- 30) C
- 31) C
- 32) B
- 33) B
- 34) D
- 35) A
- 36) D
- 37) B
- 38) A
- 39) D
- 40)

Answers may vary. One possibility:  $\lim_{x \rightarrow 0} 1 - \frac{x^2}{6} = \lim_{x \rightarrow 0} 1 = 1$ . According to the squeeze

theorem, the function  $\frac{x \sin(x)}{2 - 2 \cos(x)}$ , which is squeezed between  $1 - \frac{x^2}{6}$  and 1, must also

approach 1 as  $x$  approaches 0. Thus,  $\lim_{x \rightarrow 0} \frac{x \sin(x)}{2 - 2 \cos(x)} = 1$ .

- 41) C
- 42) A
- 43) C
- 44) C
- 45) C

- 46) D
- 47) D
- 48) B
- 49) B
- 50) A
- 51) A
- 52) B
- 53) D
- 54) B
- 55) D
- 56) C
- 57) C
- 58) A
- 59) B
- 60) D
- 61) A
- 62) A
- 63) C
- 64) D
- 65) C
- 66) A
- 67) C
- 68) C
- 69) C
- 70) A
- 71) B
- 72) D
- 73) D
- 74) C
- 75) C
- 76) A
- 77) B
- 78) C
- 79) D
- 80) D
- 81) D