

SOLUTIONS MANUAL



Modern
Semiconductor Devices
for Integrated Circuits



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Chapter 2

Mobility

2.1 (a) The mean free time between collisions using Equation (2.2.4b) is

$$\mu_n = \frac{q\tau_{mn}}{m_n} \rightarrow \tau_{mn} = \frac{\mu_n m_n}{q} = 2.85 \times 10^{-13} \text{ sec}$$

where μ_n is given to be $500 \text{ cm}^2/\text{Vsec}$ ($= 0.05 \text{ m}^2/\text{Vsec}$), and m_n is assumed to be m_0 .

(b) We need to find the drift velocity first:

$$v_d = \mu_n \mathcal{E} = 50000 \text{ cm/sec}.$$

The distance traveled by drift between collisions is

$$d = v_d \tau_{mn} = 0.14 \text{ nm}.$$

2.2 From the thermal velocity example, we know that the approximate thermal velocity of an electron in silicon is

$$v_{th} = \sqrt{\frac{3kT}{m}} = 2.29 \times 10^7 \text{ cm/sec}.$$

Consequently, the drift velocity (v_d) is $(1/10)v_{th} = 2.29 \times 10^6 \text{ cm/sec}$, and the time it takes for an electron to traverse a region of $1 \mu\text{m}$ in width is

$$t = \frac{10^{-4} \text{ cm}}{2.29 \times 10^6 \text{ cm/sec}} = 4.37 \times 10^{-11} \text{ sec}.$$

Next, we need to find the mean free time between collisions using Equation (2.2.4b):

$$\mu_n = \frac{q\tau_{mn}}{m_n} \rightarrow \tau_{mn} = \frac{\mu_n m_n}{q} = 2.10 \times 10^{-13} \text{ sec}$$

where μ_n is $1400 \text{ cm}^2/\text{Vsec}$ ($=0.14 \text{ m}^2/\text{Vsec}$, for lightly doped silicon, given in Table 2-1), and m_n is $0.26m_0$ (given in Table 1-3). So, the average number of collision is

$$\frac{t}{\tau_{mn}} = 207.7 \text{ collision} \Rightarrow 207 \text{ collisions} .$$

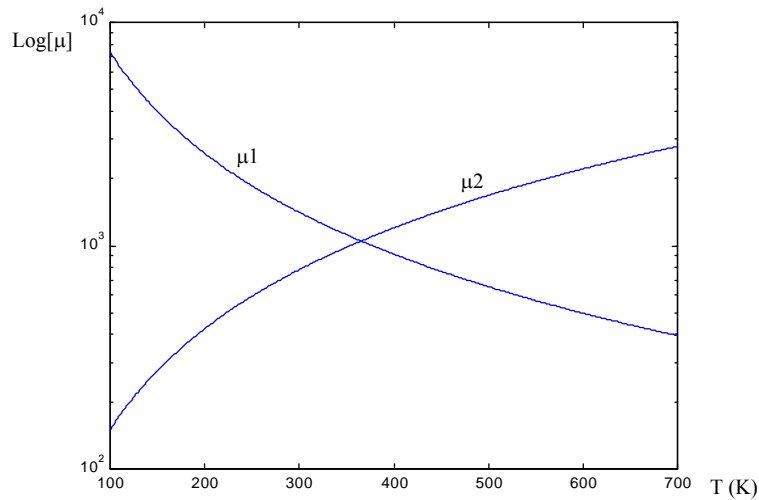
In order to find the voltage applied across the region, we need to calculate the electric field using Equation (2.2.3b):

$$v_d = -\mu_n \mathcal{E} \rightarrow \mathcal{E} = \frac{v_d}{\mu_n} = \frac{2.29 \times 10^6 \text{ cm/sec}}{1400 \text{ cm}^2 / \text{V sec}} = 1635.71 \text{ Vcm}^{-1} .$$

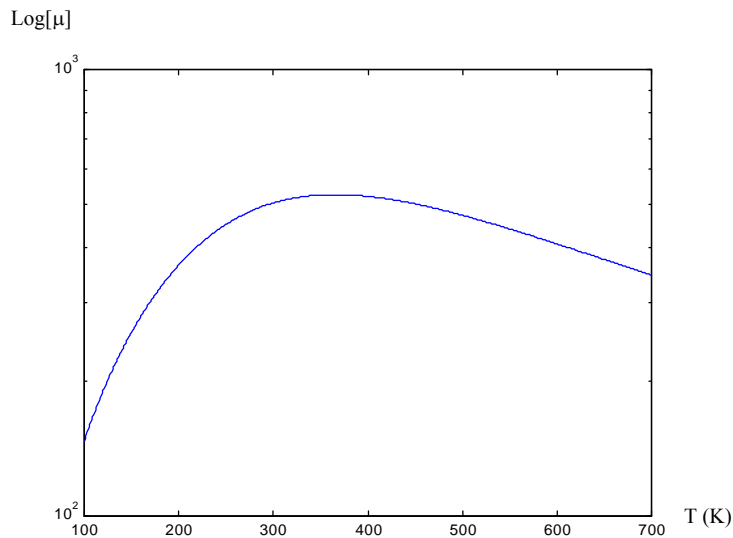
Then, the voltage across the region is

$$V = \mathcal{E} \times \text{width} = 1635.71 \text{ Vcm}^{-1} \times 10^{-4} \text{ cm} = 0.16 \text{ V} .$$

2.3 (a)



(b) If we combine μ₁ and μ₂,



The total mobility at 300 K is

$$\mu_{TOTAL}(300 K) = \left(\frac{1}{\mu_1(300 K)} + \frac{1}{\mu_2(300 K)} \right)^{-1} = 502.55 \text{ cm}^2 / V \text{ sec} .$$

(c) The applied electric field is

$$\mathcal{E} = \frac{V}{l} = \frac{1V}{1mm} = 10V / cm .$$

The current density is

$$J_{ndrift} = q\mu_n n \mathcal{E} = q\mu_n N_d \mathcal{E} = 80.41A / cm^2 .$$

Drift

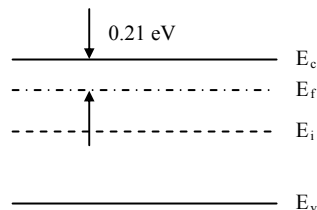
2.4 (a) From Figure 2-8 on page 45, we find the resistivity of the N-type sample doped with $1 \times 10^{16} \text{ cm}^{-3}$ of phosphorous is $0.5 \Omega\text{-cm}$.

(b) The acceptor density (boron) exceeds the donor density (P). Hence, the resulting conductivity is P-type, and the net dopant concentration is $N_{net} = |N_d - N_a| = p = 9 \times 10^{16} \text{ cm}^{-3}$ of holes. However, the mobilities of electrons and holes depend on the total dopant concentration, $N_T = 1.1 \times 10^{17} \text{ cm}^{-3}$. So, we have to use Equation (2.2.14) to calculate the resistivity. From Figure 2-5, $\mu_p(N_T = 1.1 \times 10^{17} \text{ cm}^{-3})$ is $250 \text{ cm}^2/V\text{sec}$. The resistivity is

$$\rho = \frac{1}{\sigma} = \frac{1}{qN_{net}\mu_p} = \frac{1}{q \times 9 \times 10^{16} \text{ cm}^{-3} \times (250 \text{ cm}^2 / V \text{ sec})} = 0.28 \Omega\text{cm} .$$

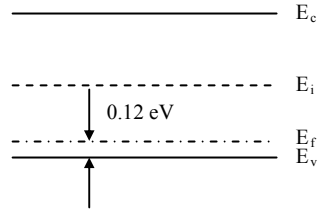
(c) For the sample in part (a),

$$E_c - E_f = kT \ln \left(\frac{N_c}{N_d} \right) = 0.026V \ln \left(\frac{2.8 \times 10^{19} \text{ cm}^{-3}}{10^{16} \text{ cm}^{-3}} \right) = 0.21 \text{ eV} .$$



For the sample in part (b),

$$E_f - E_v = kT \ln\left(\frac{N_v}{N_{net}}\right) = 0.026V \ln\left(\frac{1.04 \times 10^{19} \text{ cm}^{-3}}{9 \times 10^{16} \text{ cm}^{-3}}\right) = 0.12 \text{ eV}$$



2.5 (a) Sample 1: N-type □ Holes are minority carriers.

$$p = n_i^2/N_d = (10^{10} \text{ cm}^{-3})^2/10^{17} \text{ cm}^{-3} = 10^2 \text{ cm}^{-3}$$

Sample 2: P-type □ Electrons are minority carriers.

$$n = n_i^2/N_a = (10^{10} \text{ cm}^{-3})^2/10^{15} \text{ cm}^{-3} = 10^5 \text{ cm}^{-3}$$

Sample 3: N-type □ Holes are minority carriers.

$$p = n_i^2/N_{net} = (10^{10} \text{ cm}^{-3})^2/(9.9 \times 10^{17} \text{ cm}^{-3}) \approx 10^2 \text{ cm}^{-3}$$

(b) Sample 1: $N_d = 10^{17} \text{ cm}^{-3}$

$$\mu_n(N_d = 10^{17} \text{ cm}^{-3}) = 750 \text{ cm}^2/\text{Vsec} \text{ (from Figure 2-4)}$$

$$\sigma = qN_d\mu_n = 12 \Omega^{-1}\text{cm}^{-1}$$

Sample 2: $N_a = 10^{15} \text{ cm}^{-3}$

$$\mu_p(N_a = 10^{15} \text{ cm}^{-3}) = 480 \text{ cm}^2/\text{Vsec} \text{ (from Figure 2-4)}$$

$$\sigma = qN_a\mu_p = 12 \Omega^{-1}\text{cm}^{-1}$$

Sample 3: $N_T = N_d + N_a = 1.01 \times 10^{17} \text{ cm}^{-3}$

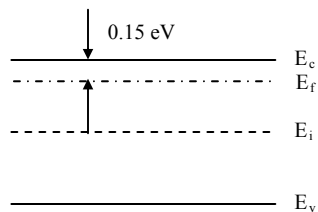
$$\mu_n(N_T = 1.01 \times 10^{17} \text{ cm}^{-3}) = 750 \text{ cm}^2/\text{Vsec} \text{ (from Figure 2-4)}$$

$$N_{net} = N_d - N_a = 0.99 \times 10^{17} \text{ cm}^{-3}$$

$$\sigma = qN_{net}\mu_n = 11.88 \Omega^{-1}\text{cm}^{-1}$$

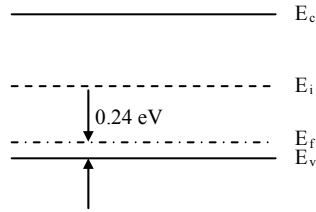
(c) For Sample 1,

$$E_c - E_f = kT \ln\left(\frac{N_c}{N_d}\right) = 0.026V \ln\left(\frac{2.8 \times 10^{19} \text{ cm}^{-3}}{10^{17} \text{ cm}^{-3}}\right) = 0.15 \text{ eV}$$



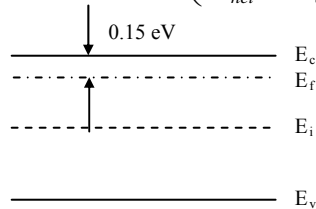
For Sample 2,

$$E_f - E_v = kT \ln\left(\frac{N_v}{N_a}\right) = 0.026V \ln\left(\frac{1.04 \times 10^{19} \text{ cm}^{-3}}{10^{15} \text{ cm}^{-3}}\right) = 0.24 \text{ eV} .$$



For Sample 3,

$$E_c - E_f = kT \ln\left(\frac{N_c}{N_{net} = N_d - N_a}\right) = 0.026V \ln\left(\frac{2.8 \times 10^{19} \text{ cm}^{-3}}{9.9 \times 10^{16} \text{ cm}^{-3}}\right) = 0.15 \text{ eV} .$$



2.6 (a) From Figure 2-5, $\mu_n(N_d = 10^{16} \text{ cm}^{-3}$ of As) is $1250 \text{ cm}^2/\text{Vs}$. Using Equation (2.2.14), we find

$$\rho = \frac{1}{\sigma} = \frac{1}{qn\mu_n} = 0.5 \Omega \text{ cm} .$$

(b) The mobility of electrons in the sample depends not on the net dopant concentration but on the total dopant concentration N_T :

$$N_T = N_d + N_a = 2 \times 10^{16} \text{ cm}^{-3} .$$

From Figure 2-5,

$$\mu_n(N_T) = 1140 \text{ cm}^2 / \text{Vs} \quad \text{and} \quad \mu_p(N_T) = 390 \text{ cm}^2 / \text{Vs} .$$

$N_{net} = N_d - N_a = 0$. Hence, we can assume that there are only intrinsic carriers in the sample. Using Equation (2.2.14),

$$\rho = \frac{1}{\sigma} = \frac{1}{qn_i\mu_n + qp_i\mu_p} = \frac{1}{qn_i(\mu_n + \mu_p)}$$

$$= \frac{1}{q \times 1 \times 10^{10} \text{ cm}^{-3} \times (1140 + 390) (\text{cm}^2 / \text{V sec})}$$

The resistivity is $4.08 \times 10^5 \Omega\text{-cm}$.

- (c) Now, the total dopant concentration (N_T) is 0. Using the electron and hole mobilities for lightly doped semiconductors (from Table 2.1), we have

$$\mu_n = 1400 \text{ cm}^2 / \text{V sec} \quad \text{and} \quad \mu_p = 470 \text{ cm}^2 / \text{V sec}.$$

Using Equation (2.2.14),

$$\rho = \frac{1}{\sigma} = \frac{1}{qn_i\mu_n + qp_i\mu_p} = \frac{1}{qn_i(\mu_n + \mu_p)}$$

$$= \frac{1}{q \times 1 \times 10^{10} \text{ cm}^{-3} \times (1400 + 470) (\text{cm}^2 / \text{V sec})}$$

The resistivity is $3.34 \times 10^5 \Omega\text{-cm}$. The resistivity of the doped sample in part (b) is higher due to ionized impurity scattering.

2.7 It is given that the sample is *n*-type, and the applied electric field \mathcal{E} is 1000 V/cm . The hole velocity v_{dp} is $2 \times 10^5 \text{ cm/s}$.

- (a) From the velocity and the applied electric field, we can calculate the mobility of holes:

$$v_{dp} = \mu_p \mathcal{E}, \quad \mu_p = v_{dp} / \mathcal{E} = 2 \times 10^5 / 1000 = 200 \text{ cm}^2 / \text{V} \cdot \text{s}.$$

From Figure 2-5, we find N_d is equal to $4.5 \times 10^{17} / \text{cm}^3$. Hence,

$$n = N_d = 4.5 \times 10^{17} / \text{cm}^3, \quad \text{and} \quad p = n_i^2 / n = n_i^2 / N_d = 10^{20} / 4.5 \times 10^{17} = 222 / \text{cm}^3.$$

Clearly, the minority carriers are the holes.

- (b) The Fermi level with respect to E_c is

$$E_f = E_c - kT \ln(N_d / N_c) = E_c - 0.107 \text{ eV}.$$

- (c) $R = \rho L / A$. Using Equation (2.2.14), we first calculate the resistivity of the sample:

$$\sigma = q(\mu_n n + \mu_p p) \approx q\mu_n n = 1.6 \times 10^{-19} \times 400 \times 4.5 \times 10^{17} = 28.8 / \Omega\text{-cm}, \quad \text{and}$$

$$\rho = \sigma^{-1} = 0.035 \Omega\text{-cm}.$$

Therefore, $R = (0.035) \times 20\mu\text{m} / (10\mu\text{m} \times 1.5\mu\text{m}) = 467 \Omega$.

Diffusion

2.8 (a) Using Equation (2.3.2),

$$J = qn v = qD(dn/dx).$$

Therefore,

$$v = D(1/n)(dn/dx) = -D/\lambda. \quad (\text{constant})$$

(b) $J = q\mu_n n \mathcal{E} = qn v$ and $v = \mu_n \mathcal{E}$.

Therefore, $\mathcal{E} = -D/\mu_n \lambda = -(kT/q)/\lambda$.

(c) $\mathcal{E} = -1000\text{V/cm} = -0.026/\lambda$. Solving for λ yields $0.25\mu\text{m}$.

2.9 (a)
$$\mathcal{E} = -\frac{dV}{dx} = \frac{1}{q} \frac{dE_v}{dx} = \frac{1}{q} \frac{\Delta}{L} = \frac{\Delta}{qL}.$$

(b) E_c is parallel to E_v . Hence, we can calculate the electron concentration in terms of E_c .

$$n(x) = n_0 e^{-(E_c(x) - E_c(0))/kT} \quad \text{where} \quad E_c(x) - E_c(0) = (\Delta/L)x.$$

Therefore, $n(x) = n_0 e^{-x\Delta/LkT}$.

(c)
$$J_n q n \mu_n \mathcal{E} + q D_n \frac{dn}{dx} = 0$$

$$q n_i e^{-\Delta x/LkT} \mu_n \frac{\Delta}{qL} + q D_n n_i e^{-\Delta x/LkT} \left(-\frac{\Delta}{LkT} \right) = 0$$

Therefore,

$$\frac{\mu_n}{q} = \frac{D_n}{kT} \Rightarrow D_n = \frac{kT}{q} \mu_n.$$