## SOLUTIONS MANUAL



## Chapter 2 <br> Descriptive Statistics: Tabular and Graphical Presentations

## Learning Objectives

1. Learn how to construct and interpret summarization procedures for qualitative data such as: frequency and relative frequency distributions, bar graphs and pie charts.
2. Learn how to construct and interpret tabular summarization procedures for quantitative data such as: frequency and relative frequency distributions, cumulative frequency and cumulative relative frequency distributions.
3. Learn how to construct a dot plot, a histogram, and an ogive as graphical summaries of quantitative data.
4. Learn how the shape of a data distribution is revealed by a histogram. Learn how to recognize when a data distribution is negatively skewed, symmetric, and positively skewed.
5. Be able to use and interpret the exploratory data analysis technique of a stem-and-leaf display.
6. Learn how to construct and interpret cross tabulations and scatter diagrams of bivariate data.

## Solutions:

1. 

| Class | Frequency | Relative Frequency |
| :---: | :---: | :---: |
| A | 60 | $60 / 120=0.50$ |
| B | 24 | $24 / 120=0.20$ |
| C | $\underline{36}$ | $36 / 120=\underline{0.30}$ |
|  | 120 | 1.00 |

2. a. $1-(.22+.18+.40)=.20$
b. $.20(200)=40$
c/d.

| Class | Frequency | Percent Frequency |
| :---: | :--- | :---: |
| A | $.22(200)=44$ | 22 |
| B | $.18(200)=36$ | 18 |
| C | $.40(200)=80$ | 40 |
| D | $.20(200)=\frac{40}{200}$ | $\underline{20}$ |
| Total |  | 100 |

3. a. $360^{\circ} \times 58 / 120=174^{\circ}$
b. $360^{\circ} \times 42 / 120=126^{\circ}$
c.

d.

4. a. Categorical
b.

Percent

| TV Show | Frequency | Frequency |
| :--- | :---: | :---: |
| Law \& Order | 10 | $20 \%$ |
| CSI | 18 | $36 \%$ |
| Without a Trace | 9 | $18 \%$ |
| Desperate Housewives | 13 | $26 \%$ |
|  | Total: | 50 |



d. CSI had the largest viewing audience. Desperate Housewives was in second place.
5. a.

| Name | Frequency | Relative Frequency | Percent Frequency |
| :--- | :---: | :---: | :---: |
| Brown | 7 | .14 | $14 \%$ |
| Davis | 6 | .12 | $12 \%$ |
| Johnson | 10 | .20 | $20 \%$ |
| Jones | 7 | .14 | $14 \%$ |
| Smith | 12 | .24 | $24 \%$ |
| Williams | $\underline{8}$ | $\underline{16}$ | $16 \%$ |

b.

c. Brown $.14 \times 360=50.4^{\circ}$

Davis $\quad .12 \times 360=43.2^{\circ}$
Johnson $.20 \times 360=72.0^{\circ}$
Jones $\quad .14 \times 360=50.4^{\circ}$
Smith $\quad .24 \times 360=86.4^{\circ}$
Williams . $16 \times 360=57.6^{\circ}$

d. Most common: Smith, Johnson and Williams
6. a.

| Network | Frequency | Percent Frequency |
| :---: | :---: | :---: |
| ABC | 15 | $30 \%$ |
| CBS | 17 | $34 \%$ |
| FOX | 1 | $2 \%$ |
| NBC | $\underline{17}$ | $\underline{34 \%}$ |
| Total | 50 | $100 \%$ |


b. CBS and NBC are tied, each with 17 of the top rated television shows. ABC is a close third with 15 . The fact that the three networks are so close is surprising. FOX, the newest television network, does not have the history to compete with the other three networks in term of the top rated shows in television history.
7. a .

| Rating | Frequency | Percent Frequency |
| :--- | :---: | :---: |
| Excellent | 20 | 40 |
| Very Good | 23 | 46 |
| Good | 4 | 8 |
| Fair | 1 | 2 |
| Poor | $\underline{2}$ | $\underline{4}$ |
|  | 50 | 100 |



Management should be very pleased with the survey results. $40 \%+46 \%=86 \%$ of the ratings are very good to excellent. $94 \%$ of the ratings are good or better. This does not look to be a Delta flight where significant changes are needed to improve the overall customer satisfaction ratings.
b. While the overall ratings look fine, note that one customer ( $2 \%$ ) rated the overall experience with the flight as Fair and two customers (4\%) rated the overall experience with the flight as Poor. It might be insightful for the manager to review explanations from these customers as to how the flight failed to meet expectations. Perhaps, it was an experience with other passengers that Delta could do little to correct or perhaps it was an isolated incident that Delta could take steps to correct in the future.
8. a.

| Position | Frequency | Relative Frequency |
| :--- | :---: | :---: |
| Pitcher | 17 | 0.309 |
| Catcher | 4 | 0.073 |
| 1st Base | 5 | 0.091 |
| 2nd Base | 4 | 0.073 |
| 3rd Base | 2 | 0.036 |
| Shortstop | 5 | 0.091 |
| Left Field | 6 | 0.109 |
| Center Field | 5 | 0.091 |
| Right Field | $\underline{7}$ | $\underline{0.127}$ |
|  | 55 | 1.000 |

b. Pitchers (Almost 31\%)
c. 3rd Base (3-4\%)
d. Right Field (Almost 13\%)
e. Infielders ( 16 or $29.1 \%$ ) to Outfielders ( 18 or $32.7 \%$ )
9. a .

| Living Area | Live Now | Ideal Community |
| :--- | :---: | :---: |
| City | $32 \%$ | $24 \%$ |
| Suburb | $26 \%$ | $25 \%$ |
| Small Town | $26 \%$ | $30 \%$ |
| Rural Area | $16 \%$ | $21 \%$ |
| Total | $100 \%$ | $100 \%$ |

b. Where do you live now?


What do you consider the ideal community?

c. Most adults are now living in a city $(32 \%)$.
d. Most adults consider the ideal community a small town (30\%).
e. Percent changes by living area: City $-8 \%$, Suburb $-1 \%$, Small Town $+4 \%$, and Rural Area $+5 \%$.

Suburb living is steady, but the trend would be that living in the city would decline while living in small towns and rural areas would increase.
10. a.

| Rating | Frequency |
| :--- | :---: |
| Excellent | 20 |
| Good | 101 |
| Fair | 528 |
| Bad | 244 |
| Terrible | 122 |
| Total | 1015 |

b.

| Rating | Percent <br> Frequency |
| :--- | :---: |
| Excellent | 2 |
| Good | 10 |
| Fair | 52 |
| Bad | 24 |
| Terrible | 12 |
| Total | 100 |

c.

d. $24 \%+12 \%=36 \%$ of adults in the United Sates think the Federal Bank is doing a bad or a terrible job in handling the credit problems. Only $10 \%+2 \%=12 \%$ think the Federal Bank is doing a good or excellent job.
e. $40 \%+10 \%=50 \%$ of adults in Spain think the European Central Bank is doing a bad or terrible job in handling the credit problems. Only $4 \%$ of adults in Spain think the European Central Bank is doing a good or excellent job.

Both countries show pessimism and relatively low confidence in how the banks are handling the credit problems in the financial markets. But in comparing the two countries, adults in Spain show more concern and more pessimism about the bank's ability compared to adults in the United States.
11.

| Class | Frequency | Relative Frequency | Percent Frequency |
| :---: | :---: | :---: | :---: |
| $12-14$ | 2 | 0.050 | 5.0 |
| $15-17$ | 8 | 0.200 | 20.0 |
| $18-20$ | 11 | 0.275 | 27.5 |
| $21-23$ | 10 | 0.250 | 25.0 |
| $24-26$ | $\underline{9}$ | $\underline{0.225}$ | $\underline{22.5}$ |
|  | Total | 40 | 1.000 |

12. 

| Class | Cumulative Frequency | Cumulative Relative Frequency |
| :--- | :---: | :---: |
| less than or equal to 19 | 10 | .20 |
| less than or equal to 29 | 24 | .48 |
| less than or equal to 39 | 41 | .82 |
| less than or equal to 49 | 48 | .96 |
| less than or equal to 59 | 50 | 1.00 |

13. 



14. a.

b/c.

| Class | Frequency | Percent Frequency |
| :---: | :---: | :---: |
| $6.0-7.9$ | 4 | 20 |
| $8.0-9.9$ | 2 | 10 |
| $10.0-11.9$ | 8 | 40 |
| $12.0-13.9$ | 3 | 15 |
| $14.0-15.9$ | $\underline{3}$ | $\underline{15}$ |
|  | 20 | 100 |

15. $\mathrm{a} / \mathrm{b}$.

| Waiting Time | Frequency | Relative Frequency |
| :--- | :---: | :---: |
| $0-4$ | 4 | 0.20 |
| $5-9$ | 8 | 0.40 |
| $10-14$ | 5 | 0.25 |
| $15-19$ | 2 | 0.10 |
| $20-24$ | $\underline{1}$ | $\underline{0.05}$ |
| Totals | 20 | 1.00 |

c/d.

| Waiting Time | Cumulative Frequency | Cumulative Relative Frequency |
| :--- | :---: | :---: |
| Less than or equal to 4 | 4 | 0.20 |
| Less than or equal to 9 | 12 | 0.60 |
| Less than or equal to 14 | 17 | 0.85 |
| Less than or equal to 19 | 19 | 0.95 |
| Less than or equal to 24 | 20 | 1.00 |

e. $12 / 20=0.60$
16. a.

| Salary | Frequency |
| :---: | :---: |
| $150-159$ | 1 |
| $160-169$ | 3 |
| $170-179$ | 7 |
| $180-189$ | 5 |
| $190-199$ | 1 |
| $200-209$ | 2 |
| $210-219$ | $\underline{1}$ |
| Total | 20 |

b.

| Salary | Percent <br> Frequency |
| :---: | :---: |
| $150-159$ | 5 |
| $160-169$ | 15 |
| $170-179$ | 35 |
| $180-189$ | 25 |
| $190-199$ | 5 |
| $200-209$ | 10 |
| $210-219$ | $\underline{5}$ |
| Total | 100 |

c.

Salary
Less than or equal to 159
Less than or equal to 169
Less than or equal to 179
Less than or equal to 189
Less than or equal to 199
Less than or equal to 209
Less than or equal to 219
Total

## Cumulative Percent

Frequency
5
20
55
80
85
95
100
100
d.


Salary
e. There is skewness to the right.
f. $(3 / 20)(100)=15 \%$
17. a. The highest price stock is for IBM with a price of $\$ 109$ per share.

The lowest price stock is for Alcoa with a price of $\$ 11$ per share.
b. A class size of 10 results in 10 classes.

| Price per Share | Frequency |
| :---: | :---: |
| $\$ 10-19$ | 5 |
| $\$ 20-29$ | 10 |
| $\$ 30-39$ | 3 |
| $\$ 40-49$ | 2 |
| $\$ 50-59$ | 6 |
| $\$ 60-69$ | 2 |
| $\$ 70-79$ | 1 |
| $\$ 80-89$ | 0 |
| $\$ 90-99$ | 0 |
| $\$ 100-109$ | 1 |

c


The general shape of the distribution is skewed to the right. Half of the companies (15) have a price per share less than $\$ 30$. A mid-priced stock appears to be in the $\$ 30$ to $\$ 49$ range, while the most frequently priced stock is in the $\$ 20$ to $\$ 29$ range.

Five stocks are less than $\$ 20$ per share (Alcoa, Bank of America, General Electric, Intel and Pfizer). Four stocks are $\$ 60$ or more per share (3M, Chevron, ExxonMobil and IBM).
d. A variety of comparisons are possible depending upon when the study is done.
18. a. The lowest holiday spending is $\$ 180$; the highest $\$ 2050$.
b.

| Spending | Frequency | Percent |
| :---: | :---: | :---: |
| $0-249$ | 3 | 12 |
| $250-499$ | 6 | 24 |
| $500-749$ | 5 | 20 |
| $750-999$ | 5 | 20 |
| $1000-1249$ | 3 | 12 |
| $1250-1499$ | 1 | 4 |
| $1500-1759$ | 0 | 0 |
| $1750-1999$ | 1 | 4 |
| $2000-2249$ | 1 | $\underline{4}$ |
| Total | 25 | 100 |

c. The distribution shows a positive skewness.


## Holiday Spending

d. The holiday spending ranges from $\$ 0$ to less than $\$ 2250$. The majority of the spending is between $\$ 250$ and $\$ 1000$ with 16 of the 25 customers, $64 \%$, in this range. The middle or average spending is around $\$ 750$ per customer. The distribution has a positive skewness with two consumers above $\$ 1750$. One consumer is above $\$ 2000$.
19. $\mathrm{a} / \mathrm{b} / \mathrm{c} / \mathrm{d}$.

| Revenue | Frequency | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative Relative <br> Frequency |
| :---: | :---: | :---: | :---: | :---: |
| $0-49$ | 6 | .12 | 6 | .12 |
| $50-99$ | 29 | .58 | 35 | .70 |
| $100-149$ | 11 | .22 | 46 | .92 |
| $150-199$ | 0 | .00 | 46 | .92 |
| $200-249$ | 1 | .02 | 47 | .94 |
| $250-299$ | 1 | .02 | 48 | .96 |
| $300-349$ | 0 | .00 | 48 | .96 |
| $350-399$ | 0 | .00 | 48 | .96 |
| $400-449$ | $\underline{2}$ | $\underline{04}$ | 50 | 1.00 |
| Total | 50 | 1.00 |  |  |

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e. The majority of the large corporations (40) have revenues in the $\$ 50$ billion to $\$ 149$ billion range. Only 4 corporations have revenues of over $\$ 200$ billion and only 2 corporations have revenues over $\$ 400$ billion. . 70 , or $70 \%$, of the corporations have revenues under $\$ 100$ billion. .30, or $30 \%$, of the corporations have revenues of $\$ 100$ billion or more.
f.


The histogram shows the distribution is skewed to the right with four corporations in the $\$ 200$ to $\$ 449$ billion range.
g. Exxon-Mobil is America's largest corporation with an annual revenue of $\$ 443$ billion. Walmart is the second largest corporation with an annual revenue of $\$ 406$ billion. All other corporations have annual revenues less than $\$ 300$ billion. Most (92\%) have annual revenues less than $\$ 150$ billion.
20. a.

| Off-Course Income <br> $(\$ 1000$ s $)$ | Frequency | Percent <br> Frequency |
| :---: | :---: | :---: |
| $0-4,999$ | 30 | 60 |
| $5,000-9,999$ | 9 | 18 |
| $10,000-14,999$ | 4 | 8 |
| $15,000-19,999$ | 0 | 0 |
| $20,000-24,999$ | 3 | 6 |
| $25,000-29,999$ | 2 | 4 |
| $30,000-34,999$ | 0 | 0 |
| $35000-39,999$ | 0 | 0 |
| $40,000-44,999$ | 1 | 2 |
| $45,000-49,999$ | 0 | 0 |
| Over 50,000 | 1 | 2 |
| Total | 50 | 100 |

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## b. Histogram of Off-Course Income



Note: The first class is labeled 5000 and provides the golfers who had an off-course income in the range 0 to 4999 or less than 5000 . These were the golfers with less than $\$ 5$ million in off-course income.
c. Off-course income is skewed to the right. Only Tiger Woods earns over $\$ 50$ million.
d. Considering the top 50 golfers, the majority ( $60 \%$ ) earn less than $\$ 5$ million in off-course income per year. $60 \%+18 \%=78 \%$ earn less than $\$ 10$ million. Five golfers ( $10 \%$ ) earn between $\$ 20$ million and $\$ 30$ million. Tiger Woods with $\$ 99.8$ million and Phil Mickelson with $\$ 40.2$ million in offcourse income are clearly the leaders in this income category.
21. $\mathrm{a} / \mathrm{b}$.

| Computer <br> Usage (Hours) | Frequency | Relative <br> Frequency |  |
| ---: | ---: | ---: | :---: |
| 0.0 | - | 2.9 | 5 |
| 3.0 | - | 5.9 | 28 |
| 6.0 | - | 8.9 | 8 |
| 9.0 | - | 11.9 | 6 |
| 12.0 | -14.9 | $\underline{3}$ | 0.10 |
|  |  | Total | 50 |

c.

d.

e. The majority of the computer users are in the 3 to 6 hour range. Usage is somewhat skewed toward the right with 3 users in the 12 to 14.9 hour range.
22.

| 5 | 7 | 8 |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 | 4 | 5 | 8 |  |  |  |  |
| 7 | 0 | 2 | 2 | 5 | 5 | 6 | 8 |
| 8 | 0 | 2 | 3 | 5 |  |  |  |

23. Leaf Unit $=.1$

| 6 | 3 |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| 7 | 5 | 5 | 7 |  |
| 8 | 1 | 3 | 4 | 8 |
| 9 | 3 | 6 |  |  |
| 10 | 0 | 4 | 5 |  |
| 11 | 3 |  |  |  |
|  |  |  |  |  |

24. $\quad$ Leaf Unit $=10$

| 11 | 6 |  |  |
| :--- | :--- | :--- | :--- |
| 12 | 0 | 2 |  |
| 13 | 0 | 6 | 7 |
| 14 | 2 | 2 | 7 |
| 15 | 5 |  |  |
| 16 | 0 | 2 | 8 |
| 17 | 0 | 2 | 3 |

25. 

| 9 | 8 | 9 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 2 | 4 | 6 | 6 |  |  |
| 11 | 4 | 5 | 7 | 8 | 8 | 9 |
| 12 | 2 | 4 | 5 | 7 |  |  |
| 13 | 1 | 2 |  |  |  |  |
| 14 | 4 |  |  |  |  |  |
| 15 | 1 |  |  |  |  |  |
|  |  |  |  |  |  |  |

26. Median Pay

| 6 | 6 | 7 | 7 |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 7 | 2 | 4 | 6 | 7 | 7 | 8 | 9 |
| 8 | 0 | 0 | 1 | 3 | 7 |  |  |
| 9 | 9 |  |  |  |  |  |  |
| 10 | 0 | 6 |  |  |  |  |  |
| 11 | 0 |  |  |  |  |  |  |
| 12 | 1 |  |  |  |  |  |  |

The median pay for these careers is generally in the $\$ 70$ and $\$ 80$ thousands. Only four careers have a median pay of $\$ 100$ thousand or more. The highest median pay is $\$ 121$ thousand for a finance director.
Top Pay

| 10 | 0 | 6 | 9 |  |
| :--- | :--- | :--- | :--- | :--- |
| 11 | 1 | 6 | 9 |  |
| 12 | 2 | 5 | 6 |  |
| 13 | 0 | 5 | 8 | 8 |
| 14 | 0 | 6 |  |  |
| 15 | 2 | 5 | 7 |  |
| 16 |  |  |  |  |
| 17 |  |  |  |  |
| 18 |  |  |  |  |
| 19 |  |  |  |  |
| 20 |  |  |  |  |
| 21 | 4 |  |  |  |
| 22 | 1 |  |  |  |

The most frequent top pay is in the $\$ 130$ thousand range. However, the top pay is rather evenly distributed between $\$ 100$ and $\$ 160$ thousand. Two unusually high top pay values occur at $\$ 214$ thousand for a finance director and \$221 thousand for an investment banker. Also, note that the top pay has more variability than the median pay.
27. a.

| 7 | 5 | 9 |  |
| ---: | :--- | :--- | :--- |
| 8 | 3 | 6 |  |
| 9 | 5 | 6 | 8 |
| 10 | 0 | 4 | 4 |
| 11 | 1 | 5 |  |
| 12 |  |  |  |
| 13 | 7 |  |  |
| 14 | 5 | 5 |  |

b. Observations such as the following can be made using the stem-and-leaf display.

- The daily rate varies from $\$ 75$ to $\$ 145$
- Typical mid-priced daily rates are $\$ 95$ to $\$ 115$ with the average daily rate around $\$ 100$.
- A daily rate in excess of $\$ 115$ should be considered relatively high. High daily rates of $\$ 137$ and $\$ 145$ were found at three ski resorts.

28. a.

| 2 | 14 |
| :---: | :---: |
| 2 | 67 |
| 3 | 0111123 |
| 3 | 5677 |
| 4 | $\begin{array}{llllllllll}0 & 3 & 3 & 3 & 3\end{array}$ |
| 4 | 6679 |
| 5 | 00022 |
| 5 | 5679 |
| 6 | 14 |
| 6 | 6 |
| 7 | 2 |

b. Most frequent age group: 40-44 with 9 runners
c. 43 was the most frequent age with 5 runners
d. $4 / 40=10 \%$ of the runners were " 20 -something." With only $10 \%$ of the registrants " 20 -something," the article pointed out that surprisingly few registrants were in this age group. One suggested reason was that " 20 -somethings" don't have the time to train for a 13.1 mile race. For " 20 -somethings," college, starting careers, and starting families may take priority over training for long distance races.
29. a.

b.

|  | $\boldsymbol{y}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{x}$ | A | 1 | 2 | Total |
|  | B | 84.6 | 15.4 | 100.0 |
| C | 0.0 | 100.0 |  |  |
|  | 16.7 | 83.3 | 100.0 |  |

c.

| $y$ |  |  |
| :---: | :---: | :---: |
|  | 1 | 2 |
| A | 27.8 | 0.0 |
| B | 61.1 | 16.7 |
| C | 11.1 | 83.3 |
| Total | 100.0 | 100.0 |

d. Category A values for $x$ are always associated with category 1 values for $y$. Category B values for $x$ are usually associated with category 1 values for y . Category C values for $x$ are usually associated with category 2 values for $y$.
30. a.


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b. There is a negative relationship between $x$ and $y ; y$ decreases as $x$ increases.
31. a. Row Percentages:

|  | Household Income (\$1000s) |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| Education Level | Under 25 | $25.0-49.9$ | $50.0-74.9$ | $75.0-99.9$ | 100 or | Total |
| Not H.S. Graduate | 42.23 | 34.73 | 13.94 | 5.41 | 3.68 | 100.00 |
| H.S. Graduate | 22.25 | 31.00 | 22.75 | 11.93 | 12.07 | 100.00 |
| Some College | 13.99 | 26.20 | 23.31 | 16.20 | 20.30 | 100.00 |
| Bachelor's Degree | 6.42 | 15.19 | 20.66 | 18.72 | 39.02 | 100.00 |
| Beyond Bach. Deg. | 3.71 | 10.60 | 16.29 | 15.87 | 53.54 | 100.00 |
| Total | 17.77 | 25.08 | 20.64 | 13.90 | 22.62 | 100.00 |

There are six percent frequency distributions in this table with row percentages. The first five give the percent frequency distribution of income for each educational level. The total row provides an overall percent frequency distribution for household income.

The second row, labeled H.S. Graduate, is the percent frequency distribution for households headed by high school graduates. The fourth row, labeled Bachelor's Degree, is the percent frequency distribution for households headed by bachelor's degree recipients.
b. The percentage of households headed by high school graduates earning $\$ 75,000$ or more is $11.93 \%+$ $12.07=24.00 \%$. The percent of households headed by bachelor's degree recipients earning $\$ 75,000$ or more is $18.72 \%+39.02 \%=57.74 \%$.
c. The percent frequency histogram for high school graduates.


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The percent frequency distribution for college graduates with a bachelor's degree.


The histograms show that households headed by a college graduate with a bachelor's degree earn more than households headed by a high school graduate. Yes, there is a positive relationship between education level and income.
32. a. Column Percentages:

|  | Household Income (\$1000s) |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| Education Level | Under 25 | $25.0-49.9$ | $50.0-74.9$ | $75.0-99.9$ | 100 or More | Total |
| Not H.S. Graduate | 32.10 | 18.71 | 9.13 | 5.26 | 2.20 | 13.51 |
| H.S. Graduate | 37.52 | 37.05 | 33.04 | 25.73 | 16.00 | 29.97 |
| Some College | 21.42 | 28.44 | 30.74 | 31.71 | 24.43 | 27.21 |
| Bachelor's Degree | 6.75 | 11.33 | 18.72 | 25.19 | 32.26 | 18.70 |
| Beyond Bach. Deg. | 2.21 | 4.48 | 8.37 | 12.11 | 25.11 | 10.61 |
| Total | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 |

There are six percent frequency distributions in this table of column percentages. The first five columns give the percent frequency distributions for each income level. The percent frequency distribution in the "Total" column gives the overall percent frequency distributions for educational level. From that percent frequency distribution we see that $13.51 \%$ of the heads of households did not graduate from high school.
b. The column percentages show that $25.11 \%$ of households earning $\$ 100,000$ or more were headed by persons having schooling beyond a bachelor's degree. The row percentages show that $53.54 \%$ of the households headed by persons with schooling beyond a bachelor's degree earned $\$ 100,000$ or more. These percentages are different because they came from different percent frequency distributions and provide different kinds of information.
c. Compare the "under 25 " percent frequency distributions to the "Total" percent frequency distributions. We see that for this low income level the percentage with lower levels of education is higher than for the overall population and the percentage with higher levels of education is lower than for the overall population.

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Compare the "100 or more" percent frequency distribution to "Total" percent frequency distribution. We see that for this high income level the percentage with lower levels of education is lower than for the overall population and the percentage with higher levels of education is higher than for the overall population.

From the comparisons it is clear that there is a positive relationship between household incomes and the education level of the head of the household.
33. a. The crosstabulation of condition of the greens by gender is below.

|  | Green Condition |  |  |
| :--- | :---: | :---: | :---: |
| Gender | Too Fast | Fine | Total |
| Male | 35 | 65 | 100 |
| Female | 40 | 60 | 100 |
| Total | 75 | 125 | 200 |

The female golfers have the highest percentage saying the greens are too fast: $40 / 100=40 \%$. Male golfers have $35 / 100=35 \%$ saying the greens are too fast.
b. Among low handicap golfers, $1 / 10=10 \%$ of the women think the greens are too fast and $10 / 50=$ $20 \%$ of the men think the greens are too fast. So, for the low handicappers, the men show a higher percentage who think the greens are too fast.
c. Among the higher handicap golfers, $39 / 51=43 \%$ of the woman think the greens are too fast and $25 / 50=50 \%$ of the men think the greens are too fast. So, for the higher handicap golfers, the men show a higher percentage who think the greens are too fast.
d. This is an example of Simpson's Paradox. At each handicap level a smaller percentage of the women think the greens are too fast. But, when the crosstabulations are aggregated, the result is reversed and we find a higher percentage of women who think the greens are too fast.

The hidden variable explaining the reversal is handicap level. Fewer people with low handicaps think the greens are too fast, and there are more men with low handicaps than women.
34. a.

|  | 5 Year Average Return |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Fund Type | $0-9.99$ | $10-19.99$ | $20-29.99$ | $30-39.99$ | $40-49.99$ | $50-59.99$ | Total |
| DE | 1 | 25 | 1 | 0 | 0 | 0 | 27 |
| FI | 9 | 1 | 0 | 0 | 0 | 0 | 10 |
| IE | 0 | 2 | 3 | 2 | 0 | 1 | 8 |
| Total | 10 | 28 | 4 | 2 | 0 | 1 | 45 |

b.

| 5 Year Average Return | Frequency |
| :---: | :---: |
| $0-9.99$ | 10 |
| $10-19.99$ | 28 |
| $20-29.99$ | 4 |
| $30-39.99$ | 2 |
| $40-49.99$ | 0 |
| $50-59.99$ | $\underline{1}$ |
| Total | 45 |

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c.

| Fund Type | Frequency |
| :---: | :---: |
| DE | 27 |
| FI | 10 |
| IE | $\underline{8}$ |
| Total | 45 |

d. The right margin shows the frequency distribution for the fund type variable and the bottom margin shows the frequency distribution for the 5 year average return variable.
e. Higher returns are associated with International Equity funds and lower returns are associated with Fixed Income funds.
35. a.

|  | Expense Ratio (\%) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Fund Type | $0-0.24$ | $0.25-0.49$ | $0.50-0.74$ | $0.75-0.99$ | $1.00-1.24$ | $1.25-1.49$ | Total |
| DE | 1 | 1 | 3 | 5 | 10 | 7 | 27 |
| FI | 2 | 4 | 3 | 0 | 0 | 1 | 10 |
| IE | 0 | 0 | 1 | 2 | 4 | 1 | 8 |
| Total | 3 | 5 | 7 | 7 | 14 | 9 | 45 |

b.

| Expense Ratio (\%) | Frequency | Percent |
| :---: | :---: | :---: |
| $0-0.24$ | 3 | 6.7 |
| $0.25-0.49$ | 5 | 11.1 |
| $0.50-0.74$ | 7 | 15.6 |
| $0.75-0.99$ | 7 | 15.6 |
| $1.00-1.24$ | 14 | 31.0 |
| $1.25-1.49$ | $\underline{9}$ | $\underline{20.0}$ |
| Total | 45 | 100 |

c. Higher expense ratios are associated with Domestic Equity funds and lower expense ratios are associated with Fixed Income fund
36. a. The scatter diagram is shown below:

b. There is some indication that higher 5-year returns are associated with higher net asset values.
37. a.

|  | Highway MPG |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Size | $15-19$ | $20-24$ | $25-29$ | $30-34$ | $35-39$ | Total |
| Compact | 26 | 76 | 9 | 0 | 0 | 111 |
| Midsize | 0 | 0 | 85 | 46 | 4 | 135 |
| Large | 0 | 0 | 65 | 0 | 0 | 65 |
| Total | 26 | 76 | 159 | 46 | 4 | 311 |

b. Higher fuel efficiencies are associated with midsize cars. In fact, for these data compact cars had the lowest fuel efficiencies.
c.

|  | City MPG |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Drive | $5-9$ | $10-14$ | $15-19$ | $20-24$ | $25-29$ | $30-35$ | Total |
| 4 | 0 | 10 | 51 | 8 | 0 | 0 | 69 |
| F | 0 | 2 | 80 | 74 | 9 | 2 | 167 |
| R | 1 | 23 | 50 | 1 | 0 | 0 | 75 |
| Total | 1 | 35 | 181 | 83 | 9 | 2 | 311 |

d. Higher fuel efficiencies are associated with front wheel drive cars. Rear wheel drive cars had somewhat lower fuel efficiencies than four wheel drive cars.
e.

|  | City MPG |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Fuel Type | $5-9$ | $10-14$ | $15-19$ | $20-24$ | $25-29$ | $30-35$ | Total |
| P | 1 | 33 | 105 | 18 | 0 | 0 | 157 |
| R | 0 | 2 | 76 | 65 | 9 | 2 | 154 |
| Total | 1 | 35 | 181 | 83 | 9 | 2 | 311 |

f. Higher fuel efficiencies are associated with cars that use regular fuel.
38. a.

|  | Highway MPG |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Displace | $15-19$ | $20-24$ | $25-29$ | $30-34$ | $35-39$ | Total |
| $1.0-2.9$ | 0 | 6 | 72 | 46 | 4 | 128 |
| $3.0-4.9$ | 3 | 56 | 86 | 0 | 0 | 145 |
| $5.0-6.9$ | 23 | 14 | 1 | 0 | 0 | 38 |
| Total | 26 | 76 | 159 | 46 | 4 | 311 |

b. Higher fuel efficiencies are associated with smaller displacement engines and lower fuel efficiencies are associated with larger displacement engines.
c. The scatter diagram is shown below:

d. The scatter diagram shows that lower fuel efficiencies are associated with larger displacement engines.
e. It is easier to see the relationship between the two variables using the scatter diagram.
39. a.

| Major | Frequency | Percent Frequency |
| :--- | :---: | :---: |
| Arts/Humanities | 7 | 10.9 |
| Business Administration | 13 | 20.3 |
| Engineering | 11 | 17.2 |
| Professional | 6 | 9.4 |
| Social Science | 5 | 7.8 |
| Other | $\underline{22}$ | $\underline{34.4}$ |
| Total | 64 | 100.0 |

b.

c. $34.4 \%$ select another major. So $100 \%-34.4 \%=65.6 \%$ select one of the five most popular majors.
d. Business Administration is the most popular major selected by incoming freshmen, $20.3 \%$
40. a. Frequency distribution and percent frequency distribution of sales by division.

| Division | Frequency | Percent |
| :--- | :---: | :---: |
| Buick | 10 | 5 |
| Cadillac | 10 | 5 |
| Chevrolet | 122 | 61 |
| GMC | 24 | 12 |
| Hummer | 2 | 1 |
| Pontiac | 18 | 9 |
| Saab | 2 | 1 |
| Saturn | 12 | 6 |
| Total | 200 | 100 |

b.

c. Chevrolet is General Motors leading division with $61 \%$ of the vehicles sold. This is considered General Motors most important division.
d. Based on the percentages shown, the Hummer division at $1 \%$ and Saab division at $1 \%$ would be good candidates for General Motors to consider discontinuing. Chevrolet at $61 \%$ and GMC at $12 \%$ account for $73 \%$ of the total vehicles sold. General Motors would be almost certain to maintain these two divisions.

Pontiac remains a solid contributor with $9 \%$ of vehicles sold. At the time it was doubtful than General Motors would be able to maintain all three of the other divisions. Some elimination or merging of divisions was anticipated for Saturn 6\%, Buick 5\%, and Cadillac 5\%.
41. a.

| Yield $\%$ | Frequency | Percent Frequency |
| :---: | :---: | :---: |
| $0.0-0.9$ | 4 | 13.3 |
| $1.0-1.9$ | 2 | 6.7 |
| $2.0-2.9$ | 6 | 20.0 |
| $3.0-3.9$ | 10 | 33.3 |
| $4.0-4.9$ | 3 | 10.0 |
| $5.0-5.9$ | 2 | 6.7 |
| $6.0-6.9$ | 2 | 6.7 |
| $7.0-7.9$ | 0 | 0.0 |
| 8.0-8.9 | 0 | 0.0 |
| $9.0-9.9$ | $\underline{1}$ | 3.3 |
| Total | 30 | 100.0 |

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c. The distribution is skewed to the right.
d. Dividend yield ranges from $0 \%$ to over $9 \%$. The most frequent range is $3.0 \%$ to $3.9 \%$. Average dividend yields looks to be between $3 \%$ and $4 \%$. Over $50 \%$ of the companies (16) pay from $2.0 \%$ to $3.9 \%$. Five companies (AT\&T, DuPont, General Electric, Merck, and Verizon) pay $5.0 \%$ or more. Four companies (Bank of America, Cisco Systems, Hewlett-Packard, and J.P. Morgan Chase) pay less than $1 \%$.
e. General Electric had an unusually high dividend yield of $9.2 \%$. 500 shares at $\$ 14$ per share is an investment of $500(\$ 14)=\$ 7,000$. A $9.2 \%$ dividend yield provides $.092(7,000)=\$ 644$ of dividend income per year.
42. a.

| Class | Frequency |
| :---: | :---: |
| $800-999$ | 1 |
| $1000-1199$ | 3 |
| $1200-1399$ | 6 |
| $1400-1599$ | 10 |
| $1600-1799$ | 7 |
| $1800-1999$ | 2 |
| $2000-2199$ | 1 |
| Total | 30 |


b. The distribution if nearly symmetrical. It could be approximated by a bell-shaped curve.
c. 10 of 30 or $33 \%$ of the scores are between 1400 and 1599 . The average SAT score looks to be a little over 1500 . Scores below 800 or above 2200 are unusual.
43. a.

| State | Frequency |
| :--- | :---: |
| Arizona | 2 |
| California | 11 |
| Florida | 15 |
| Georgia | 2 |
| Louisiana | 8 |
| Michigan | 2 |
| Minnesota | 1 |
| Texas | 2 |
| Total | 43 |


b. A total of $15+11=26$, or $26 / 43(100)=60 \%$ of the Super Bowls were played in Florida or California. Only 3 Super Bowls, or $3 / 43(100)=7 \%$, have been played in the cold-weather states of Michigan and Minnesota.
c.

| 0 | 1333334444 |  |
| :--- | :--- | :--- |
| 0 | 57779 |  |
| 1 | 00012234 |  |
| 1 | 5677778999 |  |
| 2 | 123 |  |
| 2 | 577 |  |
| 3 | 2 |  |
| 3 | 56 |  |
| 4 |  |  |



Winning Points

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d. The most frequent winning points have been 0 to 4 points and 15 to 19 points. Both occurred in 10 Super Bowls. There were 10 close games with a margin of victory less than 5 points, 10/43(100) = $23 \%$ of the Super Bowls. There have also been 10 games, $23 \%$, with a margin of victory more than 20 points.
e. The closest games was the $25^{\text {th }}$ Super Bowl with a 1 point margin. It was played in Florida. The largest margin of victory occurred one year earlier in the $24^{\text {th }}$ Super Bowl. It had a 45 point margin and was played in Louisiana. More detailed information not available from the text information.

```
25}\mp@subsup{}{}{\mathrm{ th }}\mathrm{ Super Bowl: }1991\mathrm{ New York Giants 20 Buffalo Bills 19, Tampa Stadium, Tampa, FL
24 th Super Bowl: }1990\mathrm{ San Francisco 49ers 55 Denver Broncos 10, Superdome, New Orleans, LA
```

Note: The data set Super Bowl contains a list of the teams and the final scores of the 43 Super Bowls. This data set can be used in Chapter 2 and Chapter 3 to provide interesting data summaries about the points scored by the winning team and the points scored by the losing team in the Super Bowl. For example, using the median scores, the median Super Bowl score was 28 to 13 .
44. a.

| Population | Frequency | Percent Frequency |
| :---: | :---: | :---: |
| $0.0-2.4$ | 17 | 34 |
| $2.5-4.9$ | 12 | 24 |
| $5.0-7.4$ | 9 | 18 |
| $7.5-9.9$ | 4 | 8 |
| $10.0-12.4$ | 3 | 6 |
| $12.5-14.9$ | 1 | 2 |
| $15.0-17.4$ | 1 | 2 |
| $17.5-19.9$ | 1 | 2 |
| $20.0-22.4$ | 0 | 0 |
| $22.5-24.9$ | 1 | 2 |
| $25.0-27.4$ | 0 | 0 |
| $27.5-29.9$ | 0 | 0 |
| $30.0-32.4$ | 0 | 0 |
| $32.5-34.9$ | 0 | 0 |
| $35.0-37.4$ | $\underline{1}$ | 2 |
| Total | 50 | 100 |

b.


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c. High positive skewness.
d. 17 states $(34 \%)$ have a population less than 2.5 million. Over half of the states have population less than 5 million ( 29 states $-58 \%$ ). Only eight states have a population greater than 10 million (California, Florida, Illinois, Michigan, New York, Ohio, Pennsylvania and Texas). The largest state is California ( 35.9 million) and the smallest state is Wyoming (500 thousand).
45. a.

| 1 | 7 | 7 | 8 |
| :--- | :--- | :--- | :--- | :--- |
| 2 | 1 |  |  |
| 3 | 4 |  |  |
| 4 |  |  |  |
| 5 |  |  |  |
| 6 |  |  |  |
| 7 | 2 | 7 |  |
| 8 | 6 |  |  |
| 9 |  |  |  |
| 10 |  |  |  |
| 11 | 6 |  |  |
| 12 | 7 |  |  |

b. Smallest roughly $\$ 3$ billion or less; medium $\$ 7-\$ 8$ billion; largest $\$ 11-\$ 12$ billion.
c. CVS $(\$ 12,700)$ and Walgreens $(\$ 11,660)$
46. $\mathrm{a} \& \mathrm{~b}$.

c. The most frequent range for temperature was in the 60 s ( 9 of 20). Only one low temperature was above 54 . High temperatures were mostly 41 to 68 , while low temperatures were mostly 21 to 47.

Low was 11 ; High was 84 .
d.

| High Temp | Frequency | Low Temp | Frequency |
| :---: | :---: | :---: | :---: |
| $10-19$ | 0 | $10-19$ | 1 |
| $20-29$ | 0 | $20-29$ | 5 |
| $30-39$ | 1 | $30-39$ | 5 |
| $40-49$ | 4 | $40-49$ | 5 |
| $50-59$ | 3 | $50-59$ | 3 |
| $60-69$ | 9 | $60-69$ | 1 |
| $70-79$ | 2 | $70-79$ | 0 |
| $80-89$ | $\underline{1}$ | $80-89$ | $\underline{0}$ |
| Total | 20 | Total | 20 |

47. a.

b. There is a positive relationship between high temperature and low temperature for these cities. As one goes up so does the other.
48. a. | Level of Support | Percent Frequency |
| :--- | ---: |
| Strongly favor | $1617 / 5372=30.10$ |
| Favor more than oppose | $1871 / 5372=34.83$ |
| Oppose more than favor | $1135 / 5372=21.13$ |
|  | Strongly oppose |
| Total | $749 / 5372=\underline{13.94}$ |
|  |  |

The results show support for a higher tax. Note that $30.10 \%+34.83 \%=64.93 \%$ of the respondents said they strongly favor or favor more than oppose a higher tax on higher carbon emission cars.
b. Country

Percent Frequency
Great Britain $\quad 1087 / 5372=20.2$
Italy $\quad 1045 / 5372=19.5$
Spain $\quad 1109 / 5372=20.6$
Germany $\quad 1111 / 5372=20.7$
United States $\quad 1020 / 5372=\underline{19.0}$
Total 100.0

The poll had an approximately equal representation of the five countries with roughly $20 \%$ of the poll respondents coming from each country.

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$$

c. Converting the entries in the crosstabulation into column percentages provides the following results:

|  | Country |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Support | Great Britain | Italy | Spain | Germany | United States |
| Strongly favor | 31.00 | 31.96 | 45.99 | 19.98 | 20.98 |
| Favor more than oppose | 34.04 | 39.04 | 32.01 | 36.99 | 32.06 |
| Oppose more than favor | 23.00 | 17.99 | 13.98 | 24.03 | 26.96 |
| Strongly oppose | 11.96 | 11.01 | 8.03 | 18.99 | 20.00 |
| Total | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 |

Considering the percentage of respondents who favor the higher tax by either saying "strongly favor" or "favor more than oppose", we have the following favorable support for the higher tax in each country.

| Great Britain | $31.00+34.04=65.04 \%$ |
| :--- | :--- |
| Italy | $31.96+39.04=71.00 \%$ |
| Spain | $45.99+32.01=78.00 \%$ |
| Germany | $19.98+36.99=56.97 \%$ |
| United States | $20.98+32.06=53.04 \%$ |

More that $50 \%$ of the respondents favor the higher tax for the higher carbon emission cars in all five countries. But the support for the higher tax is greater in the European countries. Spain and Italy have the greatest support for the higher tax with $78 \%$ and $71 \%$ respectively. Germany is close in views to the United States with $56.97 \%$ expressing favor for the higher tax. United States shows the lowest level of support for the higher tax with $53.04 \%$. Note that United States ranks first in terms of the response "strongly oppose" the higher tax with $20 \%$ of the respondents providing this opinion.
49. a. The batting averages for the junior and senior years for each player are as follows:

Junior year:

$$
\begin{array}{lr}
\text { Allison Fealey } & 15 / 40=.375 \\
\text { Emily Janson } & 70 / 200=.350
\end{array}
$$

Senior year:

$$
\begin{array}{ll}
\text { Allison Fealey } & 75 / 250=.300 \\
\text { Emily Janson } & 35 / 120=.292
\end{array}
$$

Because Allison Fealey had the higher batting average in both her junior year and senior year, Allison Fealey should receive the scholarship offer.
b. The combined or aggregated two-year crosstabulation is as follows:

Combined 2-Year Batting

| Outcome | A. Fealey | E. Jansen |
| :--- | :---: | :---: |
| Hit | 90 | 105 |
| No Hit | 200 | 215 |
| Total At Bats |  | 290 |

Based on this crosstabulation, the batting average for each player is as follows:
Combined Junior/Senior Years

$$
\begin{array}{lr}
\text { Allison Fealey } & 90 / 290=.310 \\
\text { Emily Janson } & 105 / 320=.328
\end{array}
$$

Because Emily Janson has the higher batting average over the combined junior and senior years, Emily Janson should receive the scholarship offer.
c. The recommendations in parts (a) and (b) are not consistent. This is an example of Simpson's Paradox. It shows that in interpreting the results based upon separate or un-aggregated crosstabulations, the conclusion can be reversed when the crosstabulations are grouped or aggregated. When Simpson's Paradox is present, the decision maker will have to decide whether the un-aggregated or the aggregated form of the crosstabulation is the most helpful in identifying the desired conclusion. Note: The authors prefer the recommendation to offer the scholarship to Emily Janson because it is based upon the aggregated performance for both players over a larger number of at-bats. But this is a judgment or personal preference decision. Others may prefer the conclusion based on using the un-aggregated approach in part (a).
50. a.

|  | Fuel Type |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Year Constructed | Elec | Nat. Gas | Oil | Propane | Other | Total |
| 1973 or before | 40 | 183 | 12 | 5 | 7 | 247 |
| $1974-1979$ | 24 | 26 | 2 | 2 | 0 | 54 |
| $1980-1986$ | 37 | 38 | 1 | 0 | 6 | 82 |
| $1987-1991$ | 48 | 70 | 2 | 0 | 1 | 121 |
| Total | 149 | 317 | 17 | 7 | 14 | 504 |

b.

| Year Constructed | Frequency | Fuel Type | Frequency |
| :--- | :---: | :--- | :---: |
| 1973 or before | 247 | Electricity | 149 |
| $1974-1979$ | 54 | Nat. Gas | 317 |
| $1980-1986$ | 82 | Oil | 17 |
| $1987-1991$ | $\underline{121}$ | Propane | 7 |
|  | Total | 504 | Other |
|  |  |  | Total |
|  |  |  | $\underline{504}$ |

c. Crosstabulation of Column Percentages

|  |  | Fuel Type |  |  |  |
| :--- | ---: | :---: | ---: | :---: | :---: |
| Year Constructed | Elec | Nat. Gas | Oil | Propane | Other |
| 1973 or before | 26.9 | 57.7 | 70.5 | 71.4 | 50.0 |
| $1974-1979$ | 16.1 | 8.2 | 11.8 | 28.6 | 0.0 |
| $1980-1986$ | 24.8 | 12.0 | 5.9 | 0.0 | 42.9 |
| $1987-1991$ | 32.2 | 22.1 | 11.8 | 0.0 | 7.1 |
| Total | 100.0 | 100.0 | 100.0 | 100.0 | 100.0 |

d. Crosstabulation of row percentages.

|  |  | Fuel Type |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Year Constructed | Elec | Nat. Gas | Oil | Propane | Other | Total |
| 1973 or before | 16.2 | 74.1 | 4.9 | 2.0 | 2.8 | 100.0 |
| $1974-1979$ | 44.5 | 48.1 | 3.7 | 3.7 | 0.0 | 100.0 |
| $1980-1986$ | 45.1 | 46.4 | 1.2 | 0.0 | 7.3 | 100.0 |
| $1987-1991$ | 39.7 | 57.8 | 1.7 | 0.0 | 0.8 | 100.0 |

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e. Observations from the column percentages crosstabulation

For those buildings using electricity, the percentage has not changed greatly over the years. For the buildings using natural gas, the majority were constructed in 1973 or before; the second largest percentage was constructed in 1987-1991. Most of the buildings using oil were constructed in 1973 or before. All of the buildings using propane are older.

Observations from the row percentages crosstabulation
Most of the buildings in the CG\&E service area use electricity or natural gas. In the period 1973 or before most used natural gas. From 1974-1986, it is fairly evenly divided between electricity and natural gas. Since 1987 almost all new buildings are using electricity or natural gas with natural gas being the clear leader.
51. a. Crosstabulation for stockholder's equity and profit.

|  | Profits (\$000) |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $0-200$ | $200-400$ | $400-600$ | $600-800$ | $800-1000$ | $1000-1200$ | Total |  |
| $0-1200$ | 10 | 1 |  |  |  | 1 | 12 |  |  |
| $1200-2400$ | 4 | 10 |  |  | 2 | 1 | 16 |  |  |
| $2400-3600$ | 4 | 3 | 3 | 1 | 1 | 1 | 13 |  |  |
| $3600-4800$ |  | 2 | 3 | 1 | 1 | 2 | 3 |  |  |
| $4800-6000$ |  |  |  |  |  |  | 4 | 4 | 50 |

b. Crosstabulation of Row Percentages.

|  | Profits $(\$ 000)$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Stockholders' Equity (\$1000s) | $0-200$ | $200-400$ | $400-600$ | $600-800$ | $800-1000$ | $1000-1200$ | Total |
| $0-1200$ | 83.33 | 8.33 | 0.00 | 0.00 | 0.00 | 8.33 | 100 |
| $1200-2400$ | 25.00 | 62.50 | 0.00 | 0.00 | 12.50 | 0.00 | 100 |
| $2400-3600$ | 30.77 | 23.08 | 23.08 | 7.69 | 7.69 | 7.69 | 100 |
| $3600-4800$ |  | 0.00 | 0.00 | 0.00 | 33.33 | 66.67 | 100 |
| $4800-6000$ | 0.00 | 33.33 | 50.00 | 16.67 | 0.00 | 0.00 | 100 |

c. Stockholder's equity and profit seem to be related. As profit goes up, stockholder's equity goes up. The relationship, however, is not very strong.
52. a. Crosstabulation of market value and profit.

|  | Profit $(\$ 1000 \mathrm{~s})$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Market Value (\$1000s) | $0-300$ | $300-600$ | $600-900$ | $900-1200$ | Total |
| $0-8000$ | 23 | 4 |  |  | 27 |
| $8000-16000$ | 4 | 4 | 2 | 2 | 12 |
| $16000-24000$ |  | 2 | 1 | 1 | 4 |
| $24000-32000$ |  | 1 | 2 | 1 | 4 |
| $32000-40000$ |  | 2 | 1 |  | 3 |
| Total | 27 | 13 | 6 | 4 | 50 |

b. Crosstabulation of Row Percentages.

|  | $\operatorname{Profit}(\$ 1000 \mathrm{~s})$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Market Value $(\$ 1000 \mathrm{~s})$ | $0-300$ | $300-600$ | $600-900$ | $900-1200$ | Total |
| $0-8000$ | 85.19 | 14.81 | 0.00 | 0.00 | 100 |
| $8000-16000$ | 33.33 | 33.33 | 16.67 | 16.67 | 100 |
| $16000-24000$ | 0.00 | 50.00 | 25.00 | 25.00 | 100 |
| $24000-32000$ | 0.00 | 25.00 | 50.00 | 25.00 | 100 |
| $32000-40000$ | 0.00 | 66.67 | 33.33 | 0.00 | 100 |

c. There appears to be a positive relationship between Profit and Market Value. As profit goes up, Market Value goes up.
53. a. Scatter diagram of Profit vs. Stockholders' Equity.

b. Profit and Stockholders' Equity appear to be positively related.

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2-38
$$

54. a. Scatter diagram of Market Value and Stockholders' Equity.

b. There is a positive relationship between Market Value and Stockholders' Equity.
