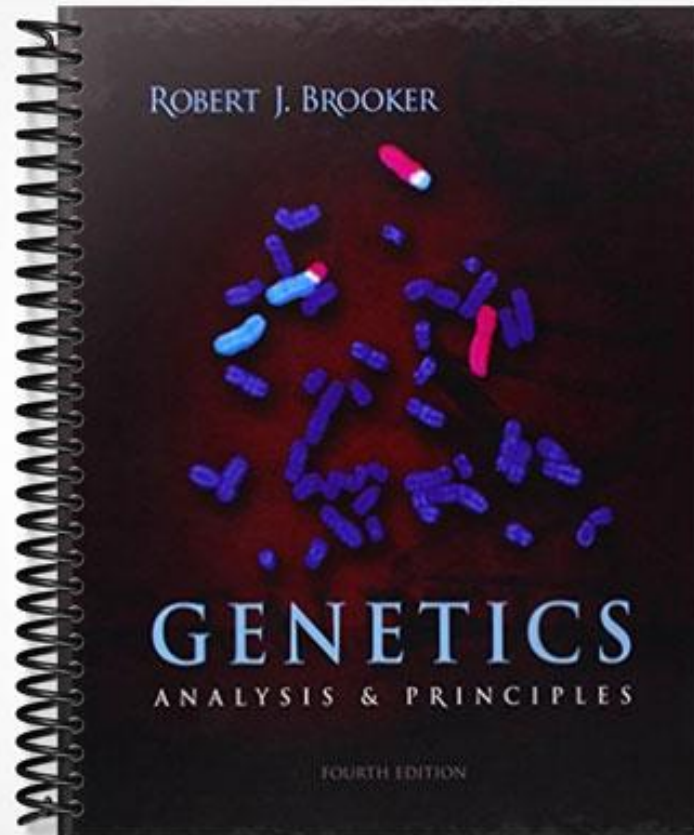


**SOLUTIONS MANUAL**



## Chapter 2: Mendelian Inheritance

### *Student Learning Objectives*

Upon completion of this chapter the student should be able to:

1. Recognize the importance of Mendel's work to the study of inheritance.
2. Construct Punnett square diagrams of one- and two- factor crosses to predict phenotypic and genotypic ratios of offspring.
3. Analyze pedigree diagrams for patterns of inheritance.
4. Apply the laws of probability (sum, product, and binomial expansion) to the study of patterns of inheritance.
5. Use the chi-square test to examine the validity of a hypothesis.

### *Key Terms*

Allele  
Anthers  
Binomial expansion equation  
Blending inheritance  
Characters  
Chi square test  
Crossed  
Degrees of freedom  
Dihybrid cross  
Dihybrid testcross  
Dominant  
Eggs  
Empirical approach  
Fertilization  
    Cross-fertilization  
    Self-fertilization  
Forked-line method  
Gamete  
Gene  
Genetic recombination  
Generations  
    F<sub>1</sub> generation  
    F<sub>2</sub> generation  
    Parental (P) generation  
Genotype  
Goodness of fit  
Heterozygous  
Homozygous  
Hybridization

Hybrids  
Hypothesis testing  
Law of Independent Assortment  
Law of Segregation  
Loss-of-function alleles  
Monohybrid cross  
Monohybrids  
Multinomial expansion equation  
Multiplication method  
Nonparentals  
Null hypothesis  
Ovaries  
Ovules  
P values  
Pangenesis  
Particulate theory of inheritance  
Pedigree analysis  
Phenotype  
Pollen grains  
Probability  
Product rule  
Punnett square  
Random sampling error  
Recessive  
Segregate  
Single-factor cross  
Sperm  
Stigma  
Strain  
Sum rule  
Trait  
True-breeding line  
Two-factor cross  
Variant

## ***Chapter Outline***

### *Introduction*

1. The concept of heredity predates the time of Mendel. The ancient Greek philosopher Hippocrates (around 400 B.C.E) proposed the concept of pangenesis.
  - a. “seeds” are produced by all parts of the body and are transmitted to the offspring
2. Greek theories persisted in some form for over 2,000 years.
  - a. homunculus – a tiny, fully formed human that lived within the sperm cells
  - b. ovists – egg was responsible for human characteristics of the offspring

- c. spermists – sperm was responsible for the human characteristics of the offspring
- 3. Work of Joseph Kölreuter (18<sup>th</sup> century) supported the blending theory of inheritance.
  - a. The idea that the factors that dictate heredity are blended together from one generation to the next.
  - b. By the mid-19<sup>th</sup> century it was believed that these blended traits could change over generations.

### *2.1 Mendel's Laws of Inheritance*

1. Facts regarding Mendel's (1822-1884) life (Figure 2.1):
  - a. ordained Augustinian minister (1847) from the monastery of St. Thomas
  - b. interested in teaching, but failed entrance exams
  - c. enrolled at the University of Vienna and studied physics and mathematics
  - d. learned that natural laws can be stated as simple mathematical relationships
2. Mendel's experimental approach to heredity began in 1856 and lasted only 8 years.
  - a. worked in a small (115x23 foot) plot
  - b. kept detailed records that included quantitative data
  - c. 1866 paper, "Experiments on Plant Hybrids," was not well recognized by the scientific community
3. Mendel's work was independently rediscovered in 1900 by Hugh de Vries (Holland), Carl Correns (Germany), and Erich von Tschermak (Austria).

### Mendel Chose Pea Plants as His Experimental Organism

1. Prior to Mendel, plant breeders had crossed (mated) distinct individuals to produce hybrids.
  - a. process is called hybridization
2. Mendel believed that the patterns of traits in these hybridization experiments were rooted in physical laws that could be explained by mathematical principles.
3. Mendel used the garden pea (*Pisum sativum*) as his experimental system.
  - a. existed in several varieties with easily recognizable characteristics
  - b. pea plants can be easily mated (see #4)
4. Plant reproduction occurs by pollination (Figure 2.2).
  - a. Male gametes (sperm) are produced within pollen grains, which are formed within the anthers of the plant.
  - b. Female gametes are produced within the ovules, which are formed within the ovaries of the plant.
  - c. Pollen grains first land on the stigma. This is followed by the formation of a pollen tube, which delivers the sperm to the egg cell.
5. With plants, self-fertilization (sperm and egg from the same individual) is possible. The structure of a pea plant favors self-fertilization since the stamens are covered by a protective petal (the keel).
6. Cross-fertilization involves the use of two parents. The large flowers of the pea plant make it possible to remove stamens from the flower, preventing self-fertilization.
  - a. allowed selective breeding of pea plants to produce desired hybrids (Figure 2.3)

### Mendel Studied Seven Characteristics That Bred True

1. Mendel chose varieties of pea plants that had distinct morphological differences in their traits (characters).
2. These lines were true-breeding, or did not show any variation in the trait over time.
3. Mendel identified seven traits that existed in two variants (Figure 2.4)
  - a. flower color, flower position, seed color, seed shape, pod shape, pod color, height
4. Mendel conducted crosses between variants of a single trait.
  - a. called a monohybrid or single-factor cross

#### Mendel Followed the Outcome of a Single Character for Two Generations

1. Mendel conducted experiments to determine the mathematical relationship between hereditary traits.
  - a. this process is called the empirical approach
2. In a single-factor cross the parental generation (P generation) is a true-breeding line for the variant of the trait being studied (purple flower color, tall height, etc.)
  - a. The offspring of the parental generation are called the first filial (F<sub>1</sub>) generation.
  - b. The offspring of the F<sub>1</sub> generation are called the second filial (F<sub>2</sub>) generation.
3. Mendel's single-factor cross followed the following steps (Figure 2.5):
  - a. Two true-breeding lines were crosses that differed only for one trait.
  - b. The F<sub>1</sub> generation are allowed to self-fertilize, producing an F<sub>2</sub> generation.
4. The data (pg. 22) from these experiments yielded the following information regarding inheritance:
  - a. The F<sub>1</sub> generation did not exhibit blending. Rather, it showed that one of the traits was dominant over the other (recessive) trait.
  - b. The dominant trait was always displayed in the F<sub>1</sub> generation. In the F<sub>2</sub> generation the dominant trait was present in the majority (75%) of the plants, while the recessive trait was present in the minority (25%) of the plants.
  - c. The genetic information is passed on from one generation to the next as "unit factors," which are now called genes. This supported the particulate theory of inheritance which suggests that the units governing traits remain unchanged (unblended) from generation to generation.
  - d. The 3:1 ratio of dominant to recessive offspring in the F<sub>2</sub> generation suggested that each parent possesses two traits, which segregate during the formation of gametes.
  - e. Mendel was the first to apply quantitative analyses to the study of inheritance.

#### Mendel's 3:1 Phenotypic Ratio Is Consistent with the Law of Segregation

1. Mendel was unaware of the concept of DNA or genes.
  - a. the term gene was first introduced by Wilhelm Johannsen
  - b. genes reside on chromosomes
  - c. the variants in the traits are due to versions of the gene called an allele
2. Mendel's law of segregation: *The two copies of a gene segregate from each other during transmission from parent to offspring.*
3. Alleles for a gene are typically represented using uppercase (for the dominant trait) and lowercase (for the recessive trait) letters (Figure 2.6).
4. The genotype is the genetic combination of an individual.

- a. homozygous indicates individuals with two identical alleles
- b. heterozygous indicates individuals with two different alleles
5. The observable characteristics of an organism are called the phenotype.

#### A Punnett Square Can Be Used to Predict the Outcome of Crosses

1. Allows you to predict the types of offspring the parents will produce and the proportion of the trait in the offspring.
2. Steps for preparing a Punnett Square
  - a. write down the genotypes of both parents
  - b. write down the possible gametes that each parent can make
  - c. create an empty Punnett square in which the number of columns equals the number of male gametes and the number of rows equals the number of female gametes
  - d. fill in the possible genotypes of the offspring by combining the alleles of the gametes in the empty boxes
  - e. determine the relative proportions of genotypes and phenotypes of the offspring

#### Mendel Also Analyzed Crosses Involving Two Different Characters

1. Mendel conducted crosses using two-factors to see if additional information regarding patterns of inheritance could be determined. These are now known as dihybrid crosses.
2. In a two-factor cross there are two possibilities of how the traits can be inherited (Figure 2.7)
  - a. They may be linked to one another and inherited as a single unit.
  - b. They may be unlinked and assort themselves independently during inheritance.
3. Mendel's experimental system followed the same pattern as the single-factor cross (Figure 2.8).
  - a. Two true-breeding lines were selected that were different with regards to two different traits (seed shape, seed color).
  - b. The F<sub>1</sub> plants were allowed to self-fertilize.
  - c. The phenotypic ratio of the F<sub>2</sub> generation was determined.
4. Mendel's experimental data (page 26) indicated the following:
  - a. The F<sub>2</sub> generation of seeds possessed a 9:3:3:1 phenotypic ratio, not the 1:2:1 ratio expected by a linked model.
  - b. Some seeds of the F<sub>2</sub> generation were nonparentals, thus further disproving that the traits were linked.
5. Mendel's law of independent assortment states that *two different genes will randomly assort their alleles during the formation of haploid reproductive cells.*
6. Independent assortment means that a single individual can produce a vast array of genetically different gametes (Figure 2.9).
7. An offspring receiving a different combination of alleles than are seen in the parental generation is known as genetic recombination.

#### A Punnett Square Can Also Be Used to Solve Independent Assortment Problems

1. For a two-factor cross, each parent can produce four types of gametes. Thus the Punnett square would have 16 cells (4 rows x 4 columns) (Figure 2.10).

2. Process is the same as the single-factor Punnett square.
3. Punnett squares are not practical for more than two traits. The forked-line method or multiplication method are more useful for larger crosses.
4. The dihybrid test cross involves using an individual who is homozygous recessive for both traits in the cross.

#### Modern Geneticists Are Often Interested in the Relationship Between the Molecular Expression of Genes and the Outcome of Traits

1. Genes encode proteins that perform the majority of cellular functions. Proteins influence an individual's expressed traits.
2. The study of loss-of-function alleles can assist geneticists in understanding the relationship between a gene and a phenotype.
  - a. The white flower color in Mendel's pea plants is an example of a loss-of-function allele (unknown to Mendel).

#### Pedigree Analysis Can Be Used to Follow the Mendelian Inheritance of Traits in Humans

1. Mendel's approach works when large numbers of offspring can be produced and matings can be controlled. This is unethical in humans and impractical for many organisms.
2. A pedigree (family tree) is used to examine inheritance patterns in humans (Figure 2.11).
  - a. often used to study human disease
3. Example is the study of cystic fibrosis (CF) in humans
  - a. gene for CF encodes a protein called CFTR (cystic fibrosis transmembrane conductance regulator)
  - b. altered CFTR effects the ionic balance across the membrane
  - c. the mutated CFTR associated with CF is a recessive trait

### 2.2 Probability and Statistics

1. Mendel's work demonstrated that laws of inheritance can be used to predict the outcomes of genetic crosses.
2. Probability calculations are used to predict the outcomes of genetic crosses.

#### Probability Is the Likelihood That an Event Will Occur

1. Probability is the chance that a future event will occur
 
$$\text{Probability} = \frac{\text{number of times an event occurs}}{\text{total number of events}}$$
2. The accuracy of a probability calculation is determined by sample size.
3. The deviation between the observed outcome and the expected outcome is called the random sampling error.

#### The Sum Rule Can Be Used to Predict the Occurrence of Mutually Exclusive Events

1. A probability calculation involving the sum rule states that *the probability that one of two or more mutually exclusive independent events will occur is equal to the sum of the individual probabilities of the events.*

2. Based on an “or” event.
  - a. What is the probability that event A or B will occur?  

$$P = p(A) + p(B)$$

The Product Rule Can Be Used to Predict the Probability of Independent Events

1. A probability calculation involving the product rule states that *the probability that two or more independent events will occur is equal to the product of their individual probabilities.*
2. Based on an “and” event.
3. What is the probability that event A and B will occur?  

$$P = p(A) \times p(B)$$
4. The product rule can replace the use of the Punnett square for crosses involving two or more genes.

The Binomial Expansion Equation Can Be Used to Predict the Probability of an Unordered Combination of Events

1. Binomial expansion is used to give the probability that a certain proportion of offspring will be produced, regardless of order.
2. Equation (pg. 33)  

$$P = \frac{n!}{x!(n-x)!} p^x q^{n-x}$$

$P$  = probability that an unordered number of events will occur  
 $n$  = total number of events  
 $x$  = the total number of events in one category  
 $p$  = individual probability of  $x$   
 $q$  = individual probability of the other category  
 $!$  = factorial
3. The multinomial expansion equation is needed to solve unordered genetic problems that involve three or more phenotypic categories.

The Chi-Square Test Can Be Used to Test the Validity of a Genetic Hypothesis

1. Involved in hypothesis testing, such as determining if the data from a given genetic cross is consistent with a certain pattern of inheritance.
  - a. tests the goodness of fit between the observed data and that predicted by the hypothesis
  - b. This is sometimes called a null hypothesis because it assumes there is no real difference between the observed and expected values.
  - c. does not prove that a hypothesis is correct or incorrect
2. Formula (pg. 34)  

$$X^2 = \sum \frac{(O - E)^2}{E}$$

$O$  = observed data in each category  
 $E$  = expected data in each category  
 $\sum$  = sum of each category
3. Steps of a Chi square test.
  - a. Propose a hypothesis that allows us to calculate the expected values based on



- Mendel's laws.
- b. Calculate the expected values for each phenotype.
  - c. Apply the Chi square formula, using the data for the observed and expected values as calculated in step 2.
  - d. Interpret the results using a Chi square table.
4. P values (Table 2.1) allow us to determine the likelihood that the variation indicated by the Chi square calculation is due to random chance alone.
    - a. Hypotheses are usually rejected if the chi-square value results in a P value less than 0.05
  5. Degrees of freedom (df) is the measure of the number of categories in the experiment that are independent of one another.
    - a. represented as  $n-1$ , where  $n$  equals the number of categories

### ***List of Key Investigators***

Correns, Carl – scientist who rediscovered Mendel's principles of inheritance in 1900.

Hippocrates – Ancient Greek philosopher who believed in the concept of pangenesis.

Johannsen, Wilhelm – Dutch botanist who first introduced the term gene.

Kölreuter, Joseph – 18<sup>th</sup> century botanist who conducted a large number of crosses. He was a supporter of the blending theory of inheritance.

Mendel, Gregor – the father of transmission genetics. Established some of the early laws regarding heredity.

Punnett, Reginald – a geneticist who originally developed the Punnett square.

Tschermak, Erich von – scientist who rediscovered Mendel's principles of inheritance in 1900.

de Vries, Hugh – scientist who rediscovered Mendel's principles of inheritance in 1900.