

SOLUTIONS MANUAL



Engineering Fundamentals of the Internal Combustion Engine

Second Edition



Willard W. Pulkrabek

Solutions Manual

Engineering Fundamentals of the Internal Combustion Engine Second Edition

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CHAPTER 1

(1-1)

**SI engines use spark plugs.
CI engines use self-ignition.**

**SI engines intake an air-fuel mixture.
CI engines intake air only.**

**SI engines have combustion at about constant volume.
CI engines have some combustion at about constant pressure.**

**SI engines use gasoline fuel.
CI engines use diesel oil fuel.**

**SI engines use carburetors or fuel injectors in the intake system.
CI engines have fuel injectors in the combustion chamber.**

(1-2)

Two stroke cycle engines have no exhaust stroke. Excess exhaust must be pushed out of cylinder (scavenged) by the intake air-fuel mixture (or intake air in CI engines). This requires that the intake mixture be at a higher pressure than the exhaust residual.

(1-3)

Advantages of two stroke cycle:

**Smoother cycle with a power stroke from every cylinder on every revolution.
Do not need mechanical valves.
More power from same weight engine.**

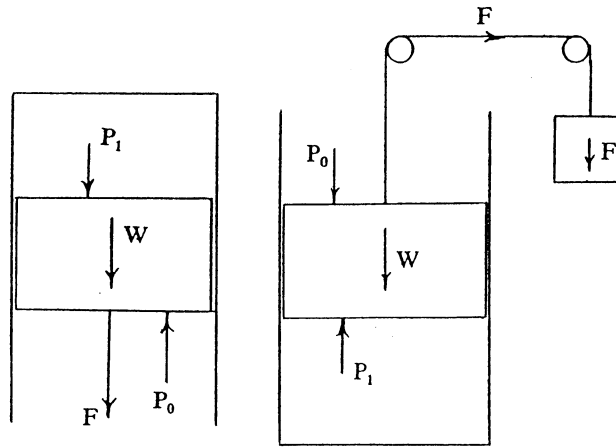
Advantages of four stroke cycle:

**Can operate without an intake pressure boost.
Cleaner operation with less exhaust pollution.
Can use crankcase for oil reservoir.**

(1-4)

- (a) They do not need mechanical valves. Valve mechanism for a very small engine would need to be high precision and costly. With no valves engines can be made cheaper and lighter which is very desirable for small engines.
- (b) Very large engines operate at a very low RPM. Because of this they need a power stroke from every cylinder during every revolution to have a smooth operating cycle.
- (c) Because of large valve overlap there is too much pollution in the exhaust of a two stroke cycle engine. They cannot pass automobile emission standards required by law.
- (d) More power can be obtained from the same weight engine.

(1-5)



(a) weight of piston

$$W = mg/g_c = [(2700 \text{ kg})(9.81 \text{ m/sec}^2)]/[(1 \text{ kg}\cdot\text{m}/\text{N}\cdot\text{sec}^2)(1000 \text{ N}/\text{kN})] = 26.487 \text{ kN}$$

forces down = forces up

$$P_1(\text{piston face area}) + \text{weight} + F = P_0(\text{piston face area})$$

$$(22 \text{ kPa})[(\pi/4)(1.2 \text{ m})^2] + (26.487 \text{ kN}) + F = (98 \text{ kPa})[(\pi/4)(1.2 \text{ m})^2]$$

$$F = 59.5 \text{ kN} = mg/g_c = m(9.81)/(1)(1000)$$

$$\underline{m = 6062 \text{ kg}}$$

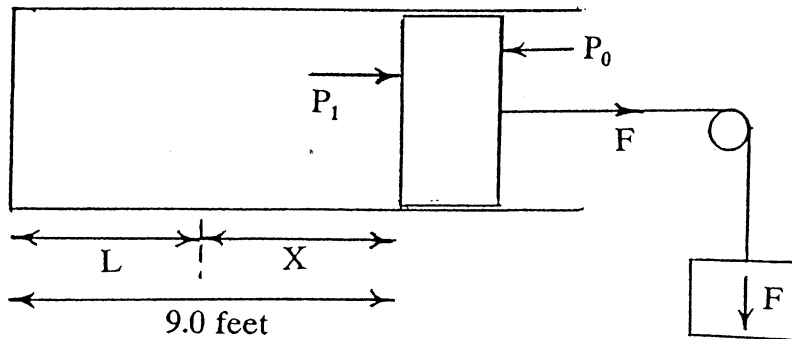
(b) $P_0(\text{piston face area}) + \text{weight} = F + P_1(\text{piston face area})$

$$(98 \text{ kPa})[(\pi/4)(1.2 \text{ m})^2] + (26.487 \text{ kN}) = F + (22 \text{ kPa})[(\pi/4)(1.2 \text{ m})^2]$$

$$F = 112.441 \text{ kN} = mg/g_c = m(9.81)/(1)(1000)$$

$$\underline{m = 11,462 \text{ kg}}$$

(1-6)



- (a) after combustion air in cylinder cools at constant volume
pressure in cylinder P_1 when piston is first unlocked

$$P_1 = P_0(T_0/T_{\text{comb}}) = (14.7 \text{ psia})(530/1000) = 7.8 \text{ psia}$$

balance of forces on piston

$$P_1(\text{piston face area}) + F = P_0(\text{piston face area})$$

$$[(7.8)(144) \text{ lbf/ft}^2][(\pi/4)(3.2 \text{ ft})^2] + F = [(14.7)(144) \text{ lbf/ft}^2][(\pi/4)(3.2 \text{ ft})^2]$$

$$F = 7991 \text{ lbf}$$

- (b) cylinder volume before cooling

$$V_1 = (\pi/4)B^2S = (\pi/4)(3.2 \text{ ft})^2(9 \text{ ft}) = 72.38 \text{ ft}^3$$

with no load piston will move at constant temperature

until cylinder pressure $P_2 = P_0 = 14.7 \text{ psia}$

$$V_2 = V_1(P_1/P_2) = (72.38 \text{ ft}^3)(7.8/14.7) = 38.41 \text{ ft}^3$$

after piston movement

$$V_2 = (\pi/4)(3.2 \text{ ft})^2L = 38.41 \text{ ft}^3 \quad L = 4.78 \text{ ft}$$

distance piston moves $X = \text{effective power stroke}$

$$X = 9 - 4.78 = 4.22 \text{ ft}$$

- (c) cylinder volume at end of power stroke

$$V_2 = 38.41 \text{ ft}^3 \quad \text{from above}$$

(1-7)

- (a) Shorter engine length allows for shorter engine compartment.**

Shorter crankshaft will have less bending stress.

- (b) Smaller diameter cylinders will have shorter flame travel distance.**

Smoother engine cycle with more power strokes per revolution.

- (c) Less mechanical friction in engine.**

Larger cylinder volume/surface area ratio giving less heat loss per cycle.

- (d) Lower engine height.**

Shorter engine length.

Shorter engine crankshaft.

- (e) Smoother engine cycle with more power strokes per revolution.**

Smaller diameter cylinders will have shorter flame travel distance.

(1-8)

- (a) as a radial engine rotates every other cylinder fires
giving 4.5 ignitions and power strokes per revolution**

$$(360^\circ/\text{rev})/(4.5 \text{ ignitions}/\text{rev}) = \underline{80^\circ/\text{ignition}}$$

- (b) 4.5 power strokes/rev**

- (c) $(4.5 \text{ power strokes}/\text{rev})(900/60 \text{ rev}/\text{sec}) = \underline{67.5 \text{ power strokes}/\text{sec}}$**

(1-9)

(a) standard automobile

$$m_f = (16,000 \text{ miles}) / (31 \text{ miles/gal}) = \underline{516.1 \text{ gal}}$$

hybrid automobile

$$m_f = (16,000 \text{ miles}) / (82 \text{ miles/gal}) = \underline{195.1 \text{ gal}}$$

(b) $(516.1) - (195.1) = (321.0 \text{ gal/year})(\$1.65) = \underline{\$529.65/\text{year}}$

(c) difference in cost

$$(\$32,000) - (\$18,000) = \$14,000$$

$$t = (\$14,000) / (\$529.65/\text{year}) = \underline{26.4 \text{ years} = 317 \text{ months}}$$

CHAPTER 2

(2-1)

(a) $[(171,000 \text{ miles})(60 \text{ min/hr})(1700 \text{ rev/min})]/(40 \text{ miles/hr}) = \underline{4.36 \times 10^8 \text{ rev}}$

(b) $(4.36 \times 10^8 \text{ rev})(4 \text{ firings/rev}) = \underline{1.744 \times 10^9 \text{ firings}}$

(c) there are same number of intake strokes as spark plug firings

$$(1.744 \times 10^9 \text{ intake strokes/engine})/(8 \text{ cyl/engine}) = \underline{2.18 \times 10^8 \text{ strokes/cyl}}$$

(2-2)

(a) Eq. (2-9)

$$V_d = N_c(\pi/4)B^2S = (4 \text{ cyl})(\pi/4)(10.9 \text{ cm})^2(12.6 \text{ cm}) = \underline{4703 \text{ cm}^3} = \underline{4.703 \text{ L}}$$

(b) Eq. (2-2)

$$\bar{U}_p = 2SN = (2 \text{ strokes/rev})(0.126 \text{ m/stroke})(2000/60 \text{ rev/sec}) = \underline{8.40 \text{ m/sec}}$$

Eq. (2-15)

$$A_p = (\pi/4)B^2N_c = (\pi/4)(0.109 \text{ m})^2(4 \text{ cyl}) = \underline{0.0373 \text{ m}^2}$$

Eq. (2-46)

$$W_b = (\text{bmep})A_p\bar{U}_p/2$$

$$88 \text{ kW} = (\text{bmep})(0.0373 \text{ m}^2)(8.40 \text{ m/sec})/2$$

$$\underline{\text{bmep} = 561 \text{ kPa}}$$

or using Eq. (2-88)

$$\text{bmep} = (1000)(88)(1)/(4.703)(2000/60) = \underline{561 \text{ kPa}}$$

(c) Eq. (2-40)

$$\tau = (\text{bmep})V_d/2\pi = (561 \text{ kPa})(0.004703 \text{ m}^3)/2\pi = \underline{0.420 \text{ kN-m}} = \underline{420 \text{ N-m}}$$

or using Eq. (2-76)

$$\tau = (159.2)(88)/(2000/60) = \underline{420 \text{ N-m}}$$

(d) for one cylinder

$$V_d = (4703 \text{ cm}^3)/4 = \underline{1176 \text{ cm}^3}$$

Eq. (2-12)

$$r_c = (V_d + V_c)/V_c = 18 = (1176 + V_c)/V_c$$

$$\underline{V_c = 69.2 \text{ cm}^3}$$

(2-3)

(a)

for one cylinder

$$V_d = (2.4 \text{ L})/4 = 0.6 \text{ L} = 600 \text{ cm}^3$$

Eq. (2-12)

$$r_c = (V_d + V_c)/V_c = 9.4 = (600 + V_c)/V_c$$

$$\underline{V_c = 71.43 \text{ cm}^3 = 0.07143 \text{ L} = 4.36 \text{ in.}^3}$$

(b)

Eq. (2-8)

$$V_d = 600 \text{ cm}^3 = (\pi/4)B^2S = (\pi/4)B^2(1.06 B)$$

$$\underline{B = 8.97 \text{ cm} = 3.53 \text{ in.}}$$

$$S = 1.06 B = (1.06)(8.97 \text{ cm}) = \underline{9.50 \text{ cm} = 3.74 \text{ in.}}$$

(c)

Eq. (2-2)

$$\begin{aligned} \bar{U}_p &= 2SN = (2 \text{ strokes/rev})(0.0950 \text{ m/stroke})(3200/60 \text{ rev/sec}) \\ &= \underline{10.13 \text{ m/sec} = 33.2 \text{ ft/sec}} \end{aligned}$$

(2-4)

Advantages of over square engine:

For the same cylinder displacement volume an over square engine will have a shorter stroke length. This will result in a lower average piston speed and lower friction losses.

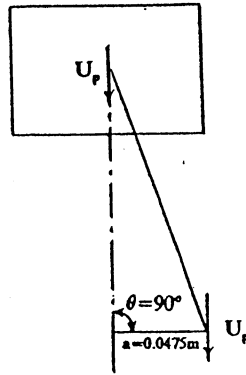
Cylinder lengths will be slightly shorter.

Advantages of under square engine:

An under square engine will have smaller diameter cylinders, resulting in a shorter flame travel distance.

Combustion chamber surface area will be smaller resulting in less heat loss per cycle.

(2-5)



(a) from Problem (2-3) $\bar{U}_p = 10.13 \text{ m/sec}$

- (b) approximate piston speed is as shown
crankshaft offset equals half of stroke length
 $a = S/2 = (0.095 \text{ m})/2 = 0.0475 \text{ m}$

$$U_p = \omega r = [(3200/60)(2\pi) \text{ radians/sec}](0.0475 \text{ m}) = 15.9 \text{ m/sec}$$

(2-6)

for one cylinder $V_d = (3.5 \text{ L})/5 = 0.7 \text{ L} = 0.0007 \text{ m}^3$

(a) Eq. (2-29)

$$\text{imep} = W/V_d = (1000 \text{ J})/[(0.0007 \text{ m}^3)(1000 \text{ J/kJ})] = 1429 \text{ kPa}$$

(b) Eq. (2-37c)

$$\text{bmep} = \eta_m \text{imep} = (0.62)(1429 \text{ kPa}) = 886 \text{ kPa}$$

(c) Eq. (2-37d)

$$\text{fmep} = \text{imep} - \text{bmep} = (1429 \text{ kPa}) - (886 \text{ kPa}) = 543 \text{ kPa}$$

(d) indicated power using Eq. (2-42)

$$\begin{aligned} \dot{W}_i &= WN/n \\ &= [(1 \text{ kJ/cyl-cycle})(2500/60 \text{ rev/sec})(5 \text{ cyl})]/(2 \text{ rev/cycle}) = 104.2 \text{ kW} \end{aligned}$$

Eq. (2-47)

$$\dot{W}_b = \eta_m \dot{W}_i = (0.62)(104.2 \text{ kW}) = 64.6 \text{ kW} = 86.6 \text{ hp}$$

or using Eq. (2-81)

$$\dot{W}_b = [(886)(3.5)(2500/60)]/[(1000)(2)] = 64.6 \text{ kW}$$

(e) Eq. (2-41)

$$\tau = (\text{bmep})V_d/4\pi = (886 \text{ kN/m}^2)(0.0035 \text{ m}^3)/4\pi = 247 \text{ N-m}$$

or using Eq. (2-76)

$$\tau = (159.2)(64.6)/(2500/60) = 247 \text{ N-m}$$

(2-7)

Eq. (2-8) for one cylinder

$$V_d = 0.0007 \text{ m}^3 = (\pi/4)B^2S = (\pi/4)B^3$$

$$B = S = 0.0962 \text{ m} = 9.62 \text{ cm}$$

(a)

Eq. (2-51)

$$SP = \dot{W}_b/A_p = \dot{W}_b/[(\pi/4)B^2N_c] = (64.6 \text{ kW})/[(\pi/4)(9.62 \text{ cm})^2(5 \text{ cyl})] = \underline{0.178 \text{ kW/cm}^2}$$

(b)

Eq. (2-52)

$$OPD = \dot{W}_b/V_d = (64.6 \text{ kW})/(3500 \text{ cm}^3) = \underline{0.0185 \text{ kW/cm}^3}$$

(c)

Eq. (2-53)

$$SV = V_d/\dot{W}_b = (3500 \text{ cm}^3)/(64.6 \text{ kW}) = \underline{54.1 \text{ cm}^3/\text{kW}}$$

(d)

Eq. (2-49)

$$\dot{W}_r = \dot{W}_i - \dot{W}_b = (104.2 \text{ kW}) - (64.6 \text{ kW}) = \underline{39.6 \text{ kW} = 53.1 \text{ hp}}$$

(2-8)

(a)

mass flow rate of fuel into engine

$$\dot{m}_r = 0.0060 \text{ kg/sec} \quad \text{from Example Problem 2-4}$$

mass flow of fuel not burned

$$(\dot{m}_{nb}) = \dot{m}_r(1 - \eta_c) = (0.0060 \text{ kg/sec})(1 - 0.97)(3600 \text{ sec/hr}) = \underline{0.648 \text{ kg/hr}}$$

(b)

Eq. (2-73)

$$(SE)_{\text{HC}} = \dot{m}_{\text{HC}}/\dot{W}_b = (648 \text{ gm/hr})/(77.3 \text{ kW}) = \underline{8.38 \text{ gm/kW-hr}}$$

(c)

mass flow of unburned fuel emissions

$$\dot{m}_{\text{HC}} = [(0.648 \text{ kg/hr})(1000 \text{ gm/kg})]/(3600 \text{ sec/hr}) = 0.18 \text{ gm/sec}$$

Eq. (2-74)

$$(EI)_{\text{HC}} = \dot{m}_{\text{HC}}/\dot{m}_r = (0.18 \text{ gm/sec})/(0.0060 \text{ kg/sec}) = \underline{30 \text{ gm/kg}}$$

(2-9)

(a)

Eq. (2-9)

$$V_d = N_c(\pi/4)B^2S = (8 \text{ cyl})(\pi/4)(5.375 \text{ in.})^2(8.0 \text{ in.}) = \underline{1452 \text{ in.}^3}$$

(b)

Eq. (2-15)

$$A_p = (\pi/4)B^2N_c = (\pi/4)(5.375 \text{ in.})^2(8 \text{ cyl}) = 181.5 \text{ in.}^2 = 1.260 \text{ ft}^2$$

Eq. (2-2)

$$\bar{U}_p = 2SN = (2 \text{ strokes/rev})(8/12 \text{ ft/stroke})(1000/60 \text{ rev/sec}) = 22.2 \text{ ft/sec}$$

Eq. (2-45)

$$\dot{W}_b = (\text{bmep})A_p\bar{U}_p/4 \\ (152 \text{ hp})(550 \text{ ft-lbf/sec/hp}) = (\text{bmep})(1.260 \text{ ft}^2)(22.2 \text{ ft/sec})/4$$

$$\text{bmep} = 11,955 \text{ lbf/ft}^2 = \underline{83.0 \text{ psia}}$$

or using Eq. (2-90)

$$\text{bmep} = [(396,000)(152)(2)]/[(1452)(1000)] = \underline{83.0 \text{ psia}}$$

(c)

Eq. (2-41)

$$\tau = (\text{bmep})V_d/4\pi = (11,955 \text{ lbf/ft}^2)[1452/(12)^3]\text{ft}^3/(4\pi) = \underline{799 \text{ lbf-ft}}$$

or using Eq. (2-77)

$$\tau = (5252)(152)/1000 = \underline{799 \text{ lbf-ft}}$$

(d)

Eq. (2-47)

$$\dot{W}_i = \dot{W}_b/\eta_m = (152 \text{ hp})/0.60 = \underline{253 \text{ hp}}$$

(e)

Eq. (2-49)

$$\dot{W}_r = \dot{W}_i - \dot{W}_b = (253 \text{ hp}) - (152 \text{ hp}) = \underline{101 \text{ hp}}$$

(2-10)

(a)

Eq. (2-71)

$$\dot{m}_a = \rho_a V_d \eta_v N/n = (1.181)(0.001500)(0.92)(3000/60)/(2) = \underline{0.0407 \text{ kg/sec}}$$

(b)

rate of fuel into engine using Eq. (2-55)

$$\dot{m}_f = \dot{m}_a / (AF) = (0.0407 \text{ kg/sec})/21 = 0.00194 \text{ kg/sec} = 6.985 \text{ kg/hr}$$

Eq. (2-60)

$$\text{bsfc} = \dot{m}_f / W_b = (6.985 \text{ kg/hr})/(48 \text{ kW}) = 0.1455 \text{ kg/kW-hr} = \underline{145.5 \text{ gm/kW-hr}}$$

(c)

mass flow of exhaust equals air plus fuel

$$\dot{m}_{ex} = [(0.0407)(22/21) \text{ kg/sec}](3600 \text{ sec/hr}) = \underline{153.5 \text{ kg/hr}}$$

(d)

Eq. (2-52)

$$\text{OPD} = \dot{W}_b / V_d = (48 \text{ kW})/(1.5 \text{ L}) = \underline{32 \text{ kW/L}}$$

(2-11)

(a)

Eq. (2-8) for one cylinder

$$V_d = (5 \text{ L})/6 = 0.8333 \text{ L} = 833.3 \text{ cm}^3 = (\pi/4)B^2S = (\pi/4)(0.92)B^3$$

$$B = 10.49 \text{ cm} \quad S = 0.92 B = (0.92)(10.49 \text{ cm}) = \underline{9.65 \text{ cm}}$$

(b)

Eq. (2-2)

$$\bar{U}_p = 2SN = (2 \text{ strokes/rev})(0.0965 \text{ m/stroke})(2400/60 \text{ rev/sec}) = \underline{7.72 \text{ m/sec}}$$

(c)

Eq. (2-12)

$$r_c = (V_d + V_c)/V_c = 10.2 = (833.3 + V_c)/V_c$$

$$\underline{V_c = 90.6 \text{ cm}^3}$$

(d)

Eq. (2-71)

$$\dot{m}_a = \rho_a V_d \eta_v N/n = (1.181)(0.005)(0.91)(2400/60)/(2) = \underline{0.107 \text{ kg/sec}}$$

(2-12)

(a) $(500 \text{ miles}) / (18 \text{ gal}) = \underline{27.78 \text{ mpg}}$

(b) $(3.785 \text{ L/gal}) / [(27.78 \text{ miles/gal})(1.609 \text{ km/mile})]$
 $= 0.0847 \text{ L/km} = \underline{8.47 \text{ L/100 km}}$

(c) rate of fuel use during trip
 $\dot{m}_f = [(18 \text{ gal})(3.785 \text{ L/gal})(0.692 \text{ kg/L})] / [(12.5 \text{ hr})(3600 \text{ sec/hr})]$
 $= 0.001048 \text{ kg/sec}$

mass of CO
 $(0.001048 \text{ kg/sec}) [(28 \text{ gm/kg})] (3600 \text{ sec/hr}) (12.5 \text{ hr}) / (1000 \text{ gm/kg})$
 $= \underline{1.32 \text{ kg}}$

(2-13)

(a) displacement volume of one cylinder

$$V_d = (0.0056 \text{ m}^3) / (10 \text{ cylinders}) = 0.00056 \text{ m}^3/\text{cylinder}$$

eq (2-8)

$$V_d = (\pi/4) B^2 S = (0.00056 \text{ m}^3) = (\pi/4) B^2 (1.12 \text{ B})$$

$$B = 0.0860 \text{ m} \quad S = 1.12 B = (1.12)(0.0860 \text{ m}) = 0.0963 \text{ m}$$

eq (2-2)

$$\bar{U}_p = 2SN = (2 \text{ strokes/rev}) (0.0963 \text{ m/stroke}) (3600/60 \text{ rev/sec})$$
$$= \underline{11.56 \text{ m/sec}}$$

(b) eq (2-76)

$$\tau = [(159.2)(162)] / (3600/60) = \underline{429.8 \text{ N-m}}$$

(c) eq (2-87)

$$b_{mep} = [(6.28)(2)(429.8)] / (5.6) = \underline{964 \text{ kPa}}$$

(2-14)

(a) displacement volume of one cylinder

$$V_d = (4800 \text{ cm}^3)/(8) = 600 \text{ cm}^3/\text{cylinder}$$

Eq. (2-8)

$$V_d = (\pi/4)B^2S = 600 \text{ cm}^3 = (\pi/4)(1.06 \text{ S})^2S$$

$$S = 8.79 \text{ cm} = 0.0879 \text{ m}$$

(b) Eq. (2-2)

$$\begin{aligned} \bar{U}_p &= 2SN = (2 \text{ strokes/rev})(0.0879 \text{ m/stroke})(2000/60 \text{ rev/sec}) \\ &= 5.86 \text{ m/sec} \end{aligned}$$

(c) each spark plug fires once each cycle

$$\begin{aligned} &(2000/2 \text{ cycles/min})(60 \text{ min/hr})(24 \text{ hr/day})(5 \text{ days}) \\ &= 7.20 \times 10^6 \text{ cycles} \end{aligned}$$

(d) Eq. (2-71)

$$\begin{aligned} \dot{m}_a &= \eta_v \rho_a V_d N / n \\ &= (0.92)(1,181 \text{ kg/m}^3)(0.0048 \text{ m}^3/\text{cycle})(2000/60 \text{ rev/sec}) / (2 \text{ rev/cycle}) \\ &= 0.0870 \text{ kg/sec} \end{aligned}$$

(e) Eq. (2-55)

$$\dot{m}_f = \dot{m}_a / AF = (0.0870 \text{ kg/sec}) / (14.6) = 0.00595 \text{ kg/sec}$$

(2-15)

(a)

Eq. (2-8) with $B = S$

$$V_d = 6.28 \text{ cm}^3 = (\pi/4)B^2S = (\pi/4)B^3$$

$$B = 2.00 \text{ cm} = S$$

Eq. (2-2)

$$\bar{U}_p = 2SN = (2 \text{ strokes/rev})(0.0200 \text{ m/stroke})(8000/60 \text{ rev/sec}) = \underline{5.33 \text{ m/sec}}$$

(b)

Eq. (2-71)

$$\dot{m}_a = \rho_a V_d \eta_v N/n = (1.181)(0.00000628)(0.85)(8000/60)/(1) = \underline{0.00084 \text{ kg/sec}}$$

(c)

Eq. (2-56)

$$\dot{m}_r = (FA)\dot{m}_a = (0.067)(0.00084 \text{ kg/sec}) = \underline{5.63 \times 10^{-5} \text{ kg/sec}}$$

(d)

$$m_r = (5.63 \times 10^{-5} \text{ kg/sec})/[8000/60 \text{ rev/sec}](1 \text{ cycle/rev}] = \underline{4.22 \times 10^{-7} \text{ kg/cycle}}$$

(2-16)

(a)

brake power using Eq. (2-43)

$$\dot{W}_b = 2\pi N\tau = (2\pi \text{ radians/rev})(800/60 \text{ rev/sec})(76 \text{ N}\cdot\text{m})/(1000 \text{ W/kW}) = 6.365 \text{ kW}$$

or using Eq. (2-80)

$$\dot{W}_b = (800/60)(76)/159.2 = 6.365 \text{ kW}$$

mass flow rate of fuel

$$\dot{m}_f = (0.113/4 \text{ kg/min})(1000 \text{ gm/kg})(60 \text{ min/hr}) = 1695 \text{ gm/hr}$$

Eq. (2-60)

$$\text{bsfc} = \dot{m}_f/\dot{W}_b = (1695 \text{ gm/hr})/(6.365 \text{ kW}) = \underline{266.3 \text{ gm/kW}\cdot\text{hr}}$$

(b)

displacement volume using Eq. (2-9)

$$V_d = N_c(\pi/4)B^2S = (1 \text{ cyl})(\pi/4)(12.9 \text{ cm})^2(18.0 \text{ cm}) \\ = 2353 \text{ cm}^3 = 2.353 \text{ L} = 0.002353 \text{ m}^3$$

Eq. (2-41)

$$\text{bmep} = 4\pi\tau/V_d = (4\pi)(76 \text{ N}\cdot\text{m})/(0.002353 \text{ m}^3) = 405,700 \text{ N/m}^2 = \underline{405.7 \text{ kPa}}$$

or using Eq. (2-87)

$$\text{bmep} = (6.28)(2)(76)/(2.353) = \underline{405.7 \text{ kPa}}$$

or using Eq. (2-88)

$$\text{bmep} = (1000)(6.365)(2)/[(2.353)(800/60)] = \underline{405.7 \text{ kPa}}$$

(c)

from above $\dot{W}_b = \underline{6.365 \text{ kW}}$

(d)

piston face area using Eq. (2-15)

$$A_p = (\pi/4)B^2 = (\pi/4)(12.9 \text{ cm})^2 = 130.7 \text{ cm}^2$$

Eq. (2-51)

$$\text{SP} = \dot{W}_b/A_p = (6.365 \text{ kW})/(130.7 \text{ cm}^2) = \underline{0.0487 \text{ kW/cm}^2}$$

(e)

Eq. (2-52) $\text{OPD} = \dot{W}_b/V_d = (6.365 \text{ kW})/(2.353 \text{ L}) = \underline{2.71 \text{ kW/L}}$

(f)

Eq. (2-53) $\text{SV} = V_d/\dot{W}_b = (2.353 \text{ L})/(6.365 \text{ kW}) = \underline{0.370 \text{ L/kW}}$

(2-17)

(a) $\dot{Q} = \dot{m}c_p\Delta T$
 $[(72 \text{ hp})(2545 \text{ BTU/hr/hp})(0.93)]/(60 \text{ min/hr})$
 $= (30 \text{ gal/min})(62.4 \text{ lbm/ft}^3)(0.1337 \text{ ft}^3/\text{gal})(1 \text{ BTU/lbm}\cdot\text{R})\Delta T$
 $\Delta T = 11^\circ \text{ F} \quad T_{\text{exit}} = 46^\circ + 11^\circ = \underline{57^\circ \text{ F}}$

(b) Eq. (2-43)

$$\dot{W}_b = 2\pi N\tau = (72 \text{ hp})(550 \text{ ft}\cdot\text{lbf/sec/hp})(60 \text{ sec/min}) = (2\pi \text{ radians/rev})(4050 \text{ rev/min})\tau$$
$$\tau = \underline{93.4 \text{ lbf}\cdot\text{ft}}$$

or using Eq. (2-77)

$$\tau = (5252)(72)/(4050) = \underline{93.4 \text{ lbf}\cdot\text{ft}}$$

(c) brake power $\dot{W}_b = (72 \text{ hp})(550 \text{ ft}\cdot\text{lbf/sec/hp})(60 \text{ sec/min}) = 2.376 \times 10^6 \text{ ft}\cdot\text{lbf/min}$

displacement $V_d = (302 \text{ in.}^3)/(12 \text{ in./ft})^3 = 0.1748 \text{ ft}^3$

Eq. (2-86)

$$\text{bmep} = n\dot{W}_b/V_dN = (2 \text{ rev/cycle})(2.376 \times 10^6 \text{ ft}\cdot\text{lbf/min})/(0.1748 \text{ ft}^3)(4050 \text{ rev/min})$$
$$= 6712.4 \text{ lbf/ft}^2 = \underline{46.6 \text{ psia}}$$

or using Eq. (2-90)

$$\text{bmep} = [(396,000)(72)(2)]/[(302)(4050)] = \underline{46.6 \text{ psia}}$$

(2-18)

(a) power out of generator

$$\dot{W}_g = (220 \text{ volts})(54.2 \text{ amps}) = 11,924 \text{ W} = 11.924 \text{ kW}$$

brake power from engine using Eq. (2-50)

$$\dot{W}_b = \dot{W}_g/\eta_{\text{gen}} = (11.924 \text{ kW})/0.87 = \underline{13.7 \text{ kW} = 18.4 \text{ hp}}$$

(b) Eq. (2-43)

$$\dot{W}_b = 2\pi N\tau = 13.7 \text{ kW} = (2\pi \text{ radians/rev})(1200/60 \text{ rev/sec})\tau$$
$$\tau = \underline{0.109 \text{ kN}\cdot\text{m} = 109 \text{ N}\cdot\text{m}}$$

or using Eq. (2-76)

$$\tau = (159.2)(13.7)/(1200/60) = \underline{109 \text{ N}\cdot\text{m}}$$

(c) Eq. (2-40)

$$\tau = (\text{bmep})V_d/2\pi = 109 \text{ N}\cdot\text{m} = (\text{bmep})(0.0031 \text{ m}^3/\text{rev})/(2\pi \text{ radians/rev})$$
$$\text{bmep} = 221,000 \text{ N/m}^2 = \underline{221 \text{ kPa}}$$

or using Eq. (2-87)

$$\text{bmep} = (6.28)(1)(109)/(3.1) = \underline{221 \text{ kPa}}$$

(2-19)

(a)

Eq. (2-55)

$$\dot{m}_a = \dot{m}_r(AF) = (0.198 \text{ kg/sec})(1.7) = 0.3366 \text{ kg/sec}$$

Eq. (2-71)

$$\eta_v = n\dot{m}_a / \rho_a V_d N = (2)(0.3366) / (1.181)(0.006)(6000/60) = 0.950 = \underline{95.0\%}$$

(b)

$$\dot{m}_a = \underline{0.3366 \text{ kg/sec}} \quad \text{from above}$$

(c)

Eq. (2-64) : heat in for engine per time

$$\dot{Q}_{in} = \dot{m}_r Q_{HV} \eta_c = (0.198 \text{ kg/sec})(10,920 \text{ kJ/kg})(0.99) = 2140.5 \text{ kJ/sec}$$

heat in for engine per cycle

$$Q_{in} = (2140.5 \text{ kJ/sec})(2 \text{ rev/cycle}) / (6000/60 \text{ rev/sec}) = 42.81 \text{ kJ/cycle}$$

heat in per cycle per cylinder

$$Q_{in} = (42.81 \text{ kJ/cycle}) / (8 \text{ cylinder}) = \underline{5.35 \text{ kJ/cyl-cycle}}$$

(d)

$$\dot{Q}_{unburned} = \dot{m}_r Q_{HV} (1 - \eta_c) = (0.198 \text{ kg/sec})(10,920 \text{ kJ/kg})(1 - 0.99) = \underline{21.6 \text{ kW}}$$

(2-20)

assuming four-stroke cycle

(a) Eq. (2-71)

$$\begin{aligned}\dot{m}_a &= \eta_v \rho_a V_d N / n \\ &= (0.51) (1.181 \text{ kg/m}^3) (0.0046 \text{ m}^3/\text{cycle}) (1750/60 \text{ rev/sec}) / (2 \text{ rev/cycle}) \\ &= \underline{0.0404 \text{ kg/sec}}\end{aligned}$$

(b) Eq. (2-55)

$$\dot{m}_f = \dot{m}_a / AF = (0.0404 \text{ kg/sec}) / (14.5) = \underline{0.00278 \text{ kg/sec}}$$

(c) Eq. (2-60)

$$\begin{aligned}\text{bsfc} = \dot{m}_f / \dot{W}_b &= [(0.00278 \text{ kg/sec}) (1000 \text{ gm/kg}) (3600 \text{ sec/hr})] / (32.4 \text{ kW}) \\ &= \underline{309 \text{ gm/kW-hr}}\end{aligned}$$

(d) with same indicated thermal efficiency and same combustion efficiency, fuel flow needed will be proportional to mechanical efficiency, fuel flow rate needed for V4:

$$\dot{m}_f = (0.00278 \text{ kg/sec}) [(75/87)] = 0.00240 \text{ kg/sec}$$

Eq. (2-55) gives air flow needed

$$\dot{m}_a = \dot{m}_f (AF) = (0.00240 \text{ kg/sec}) (18.2) = 0.0437 \text{ kg/sec}$$

use Eq. (2-71) to find needed engine speed

$$\begin{aligned}\dot{m}_a &= \eta_v \rho_a V_d N / n = (0.0437 \text{ kg/sec}) \\ &= (0.86) (1.181 \text{ kg/m}^3) (0.0023 \text{ m}^3/\text{cycle}) (N/60 \text{ rev/sec}) / (2 \text{ rev/cycle}) \\ N &= \underline{2245 \text{ RPM}}\end{aligned}$$

(e) Eq. (2-60)

$$\begin{aligned}\text{bsfc} = \dot{m}_f / \dot{W}_b &= [(0.00240 \text{ kg/sec}) (1000 \text{ gm/kg}) (3600 \text{ sec/hr})] / (32.4 \text{ kW}) \\ &= \underline{267 \text{ gm/kW-hr}}\end{aligned}$$

(2-21)

(a) $V_1 = (70 \text{ MPH}) / (2.237 \text{ MPH/m/sec}) = 31.29 \text{ m/sec}$

$$V_2 = (20) / (2.237) = 8.94 \text{ m/sec}$$

$$\begin{aligned}\Delta KE &= (m/2g_c) [V_1^2 - V_2^2] \\ &= (1900 \text{ kg}) / [(2) (1 \text{ kg-m/N-sec}^2)] [(31.29 \text{ m/sec})^2 - (8.94)^2] = 854,180 \text{ N-m} \\ &= 854.18 \text{ kJ}\end{aligned}$$

51% of this is recovered in battery

$$E = (854.18 \text{ kJ}) (0.51) = \underline{436 \text{ kJ}}$$

(b) 24% of chemical energy recovered

$$e = (26950 \text{ kJ/kg}) (0.24) = 6468 \text{ kJ/kg}$$

mass of fuel saved

$$m = (436 \text{ kJ}) / (6468 \text{ kJ/kg}) = \underline{0.067 \text{ kg}}$$