## SOLUTIONS MANUAL



## Solutions to Chapter 2 Problems

A Note To Instructors: Because of volatile energy prices in today's world, the instructor is encouraged to vary energy prices in affected problems (e.g. the price of a gallon of gasoline) plus and minus 50 percent and ask students to determine whether this range of prices changes the recommendation in the problem. This should make for stimulating inclass discussion of the results.

## 2-1 Fixed Cost Elements:

- Executive salaries and the related cost of benefits
- Salaries and other expenses associated with operating a legal department
- Operation and maintenance (O\&M) expenses for physical facilities (buildings, parking lots, landscaping, etc.)
- Insurance, property taxes, and any license fees
- Other administrative expenses (personnel not directly related to production; copying, duplicating, and graphics support; light vehicle fleet; etc.)
- Interest cost on borrowed capital


## Variable Cost Elements:

- Direct labor
- Materials used in the product or service
- Electricity, lubricating and cutting oil, and so on for equipment used to produce a product or deliver a service
- Replacement parts and other maintenance expenses for jigs and fixtures
- Maintenance material and replacement parts for equipment used to produce a product or deliver a service
- The portion of the costs for a support activity (to production or service delivery) that varies with quantity of output (e.g., for central compressed air support: electricity, replacement parts, and other O\&M expenses)

|  | Fixed | Variable |
| :--- | :---: | :---: |
| Raw Materials |  | X |
| Direct Labor |  | X |
| Supplies | X | X |
| Utilities* | X | X |
| Property Taxes | X |  |
| Administrative Salaries | X | X |
| Payroll Taxes | X |  |
| Insurance-Building and Equipment | X |  |
| Clerical Salaries | X | X |
| Sales Commissions | X |  |
| Rent |  |  |
| Interest on Borrowed Money |  |  |
| *Classification is situation dependent |  |  |

2-3
(a) \# cows $=\frac{1,000,000 \text { miles } / \text { year }}{(365 \text { days } / \text { y ear })(15 \text { miles } / \text { day })}=182.6$ or 183 cows
annual cost $=(1,000,000$ miles $/$ year $)(\$ 5 / 60$ miles $)=\$ 83,333$ per year
(b) Annual cost of gasoline $=\frac{1,000,000 \text { miles } / \text { y ear }}{30 \text { miles } / \text { gall on }}(\$ 3 /$ gallon $)=\$ 100,000$ per year

It would cost $\$ 16,667$ more per year to fuel the fleet of cars with gasoline.

| Cost | Site A | Site B |
| :--- | :---: | :---: |
| Rent | $=\$ 5,000$ | $=\$ 100,000$ |
| Hauling | $(4)(200,000)(\$ 1.50)=$ | $(3)(200,000)(\$ 1.50)=\$ 900,000$ |
|  | $\$ 1,200,000$ |  |
| Total | $\$ 1,205,000$ | $\$ 1,000,000$ |

Note that the revenue of $\$ 8.00 / \mathrm{yd}^{3}$ is independent of the site selected. Thus, we can maximize profit by minimizing total cost. The solid waste site should be located in Site B.

2-5 Stan's asking price of $\$ 4,000$ is probably too high because the new transmission adds little value to the N.A.D.A. estimate of the car's worth. (Low mileage is a typical consideration that may inflate the N.A.D.A. estimate.) If Stan can get $\$ 3,000$ for his car, he should accept this offer. Then the $\$ 4,000-$ $\$ 3,000=\$ 1,000$ "loss" on his car is a sunk cost.

2-6 The $\$ 97$ you spent on a passport is a sunk cost because you cannot get your money back. If you decide to take a trip out of the U.S. at a later date, the passport's cost becomes part of the fixed cost of making the trip (just as the cost of new luggage would be).

2-7 If the value of the re-machining option ( $\$ 60,000$ ) is reasonably certain, this option should be chosen. Even if the re-machined parts can be sold for only $\$ 45,001$, this option is attractive. If management is highly risk adverse (they can tolerate little or no risk), the second-hand market is the way to proceed to guarantee $\$ 15,000$ on the transaction.

2-8 The certainty of making $\$ 200,000-\$ 120,000=\$ 80,000$ net income is not particularly good. If your friend keeps her present job, she is turning away from a risky $\$ 80,000$ gain. This "opportunity cost" of $\$ 80,000$ balanced in favor of a sure $\$ 60,000$ would indicate your friend is risk averse and does not want to work hard as an independent consultant to make an extra $\$ 20,000$ next year.

2-9 (a) If you purchase a new car, you are turning away from a risky $20 \%$ per year return. If you are a risk taker, your opportunity cost is $20 \%$, otherwise; it is $6 \%$ per year.
(b) When you invest in the high tech company's common stock, the next best return you've given up is $6 \%$ per year. This is your opportunity cost in situation (b).

2-10 (a) The life cycle cost concept encompasses a time horizon for a product, structure, system, or service from the initial needs assessment to final phaseout and disposal activities. Definition of requirements; conceptual design, advanced development, and prototype testing; detailed design and resource acquisition for production or construction; actual production or construction; and operation and customer use, and maintenance and support are other primary activities involved during the life cycle.
(b) The acquisition phase includes the definitions of requirements as well as the conceptual and detailed design activities. It is during these activities that the future costs to produce (or construct), operate, and maintain a product, structure, system, or service are predetermined. Since these future costs (during the operation phase) are $80-90$ percent of the life cycle costs, the greatest potential for lowering life cycle costs is during the acquisition phase (in the definition of requirements and design activities).
(a)

(b) Fixed costs that could change the BE point from 62 passengers to a lower number include: reduced aircraft insurance costs (by re-negotiating premiums with the existing insurance company or a new company), lower administrative expenses in the front office, increased health insurance costs for the employees (i.e. lowering the cost of the premiums to the airline company) by raising the deductibles on the group policy.
(c) Variable costs that could be reduced to lower the BE point include: no more meals on flights, less external air circulated throughout the cabin, fewer flight attendants. Note: One big cost is fuel, which is fixed for a given flight but variable with air speed. The captain can fly the aircraft at a lower speed to save fuel.
(a) $\mathrm{p}=150-0.02 \mathrm{D} ; \quad \mathrm{C}_{\mathrm{F}}=\$ 42,000 ; \quad \mathrm{c}_{\mathrm{V}}=\$ 53 /$ circuit board
$\mathrm{D}^{*}=\frac{\mathrm{a}-\mathrm{c}_{\mathrm{v}}}{2 \mathrm{~b}}=\frac{150-53}{2(0.02)}=\underline{2,425 \text { circuit boards } / \text { month }}$
(b) Profit (loss) $=$ Total Revenue - Total Cost

$$
\begin{aligned}
& =150 D-0.02 D^{2}-(42,000+53 D) \\
& =150(2,425)-0.02(2,425)^{2}-42,000-53(2,425) \\
& =\$ 75,612.50 / \text { month } \quad \quad \quad \text { (maximum profit) }
\end{aligned}
$$

(c) Breakeven occurs when profit $=0$.

$$
\begin{aligned}
\text { Profit } & =0=-0.02 D^{2}+97 D-42,000 \\
& =D^{2}-4,850 D+2,100,000
\end{aligned}
$$

$$
\mathrm{D}^{\prime}=\frac{4,850 \pm \sqrt{(4,850)^{2}-4(2,100,000)}}{2}
$$

$\mathrm{D}_{1}^{\prime}=480.6 \approx 481$ circuit boards / month
$D_{2}^{\prime}=4,369.4 \approx 4,369$ circuit boards / month
(d) The range of profitable demand is 481 to 4,369 circuit boards per month.

2-13 (a) Total Revenue $=p \mathrm{D}=(180-5 \mathrm{D}) \mathrm{D}=180 \mathrm{D}-5 \mathrm{D}^{2}$
Total Cost $=(40 D) D=40 D^{2}$
Total Profit $=-5 D^{2}+180 D-40 D^{2}$

$$
\begin{aligned}
& \frac{d(\text { Profit })}{d \mathrm{D}}=-10 \mathrm{D}+180-80 \mathrm{D}=0 ; 90 \mathrm{D}=180 ; \mathrm{D}^{*}=2 \text { units/week } \\
& \frac{d^{2}(\text { Profit })}{d \mathrm{D}^{2}}=-90<0 \therefore \text { maximum profit }
\end{aligned}
$$

(b) Total Profit $=-5\left(2^{2}\right)+180(2)-40\left(2^{2}\right)$

$$
=-20+360-160=\$ 180 / \text { week }
$$

2-14 (a) $\mathrm{p}=600-0.05 \mathrm{D} ; \quad \mathrm{C}_{\mathrm{F}}=\$ 900,000 /$ month; $\quad \mathrm{c}_{\mathrm{v}}=\$ 131.50$ per unit
The unit demand, D , is one thousand board feet.

$$
\begin{equation*}
\mathrm{D}^{*}=\frac{\mathrm{a}-\mathrm{c}_{\mathrm{v}}}{2 \mathrm{~b}}=\frac{600-131.50}{2(0.05)}=\underline{4,685 \mathrm{units} / \mathrm{month}} \tag{Eqn.2-10}
\end{equation*}
$$

$$
\begin{aligned}
\text { Profit (loss) } & =600 \mathrm{D}-0.05 \mathrm{D}^{2}-(900,000+131.50 \mathrm{D}) \\
& =\left[600(4,685)-0.05(4,685)^{2}\right]-[\$ 900,000+\$ 131.50(4,685)] \\
& =\$ 197,461.25 / \text { month } \quad(\text { maximum profit })
\end{aligned}
$$

(b) $\quad \mathrm{D}^{\prime}=\frac{468.5 \pm \sqrt{(468.5)^{2}-4(0.05)(9,000,000)}}{2(0.05)}$
$\mathrm{D}_{1}^{\prime}=\frac{468.5-198.73}{0.1}=2,698$ units $/ \mathrm{month}$
$\mathrm{D}_{2}^{\prime}=\frac{468.5+198.73}{0.1}=6,672$ units $/$ month
Range of profitable demand is $\underline{2,698}$ units to 6,672 units per month.

2-15
(a) Profit $=\left[38+\frac{2700}{\mathrm{D}}-\frac{5000}{\mathrm{D}^{2}}\right] \mathrm{D}-1000-40 \mathrm{D}$

$$
=38 \mathrm{D}+2700-\frac{5000}{\mathrm{D}}-1000-40 \mathrm{D}
$$

Profit $=-2 \mathrm{D}-\frac{5000}{\mathrm{D}}+1700$
$\frac{d(\text { Profit })}{d \mathrm{D}}=-2+\frac{5000}{\mathrm{D}^{2}}=0$
or, $\quad \mathrm{D}^{2}=\frac{5000}{2}=2500 \quad$ and $\quad \mathrm{D}^{*}=\underline{50 \text { units per month }}$
(b) $\frac{d^{2} \text { (Profit) }}{d \mathrm{D}^{2}}=\frac{-10,000}{\mathrm{D}^{3}}<0$ for $\mathrm{D}>1$

Therefore, $\underline{D}^{*}=50$ is a point of maximum profit.

$$
\begin{aligned}
& =\left(15 \mathrm{X}-0.2 \mathrm{X}^{2}\right)-\left(12+0.3 \mathrm{X}+0.27 \mathrm{X}^{2}\right) \\
& =14.7 \mathrm{X}-0.47 \mathrm{X}^{2}-12 \\
& \frac{d \text { Profit }}{d \mathrm{X}}=0=14.7-0.94 \mathrm{X}
\end{aligned}
$$

$X=\underline{15.64 \text { megawatts }}$
Note: $\frac{d^{2} \text { Profit }}{d \mathrm{X}^{2}}=-0.94$ thus, $\mathrm{X}=15.64$ megawatts maximizes profit

2-17 Breakeven point in units of production:
$\mathrm{C}_{\mathrm{F}}=\$ 100,000 / \mathrm{yr} ; \mathrm{C}_{\mathrm{V}}=\$ 140,000 / \mathrm{yr}$ (70\% of capacity)
Sales $=\$ 280,000 / \mathrm{yr}$ ( $70 \%$ of capacity); $\mathrm{p}=\$ 40 /$ unit
Annual Sales (units) $=\$ 280,000 / \$ 40=7,000$ units $/ \mathrm{yr}(70 \%$ capacity $)$
$c_{v}=\$ 140,000 / 7,000=\$ 20 /$ unit
$\mathrm{D}^{\prime}=\frac{\mathrm{C}_{\mathrm{F}}}{\mathrm{p}-\mathrm{c}_{\mathrm{v}}}=\frac{\$ 100,000}{(\$ 40-\$ 20)}=5,000$ units $/ \mathrm{yr}$
or in terms of capacity, we have: 7,000 units $/ 0.7=x$ units $/ 1.0$

Thus, $x(100 \%$ capacity $)=7,000 / 0.7=10,000$ units $/ \mathrm{yr}$
$\mathrm{D}^{\prime}(\%$ of cap acity $)=\frac{\$ 5,000}{(10,000}=\underline{0.5 \text { or } 50 \% \text { of capacity }}$

2-18 $C_{F}=\$ 504,000$ per month; $c_{v}=\$ 166$ per unit; $p=\$ 328$ per unit

$$
D^{\prime}=\frac{C_{F}}{p-c_{v}}=\frac{\$ 504,000}{(\$ 328-\$ 166) / \text { unit }}=3,112 \text { pumpsper month }
$$

Reduced Costs: $\mathrm{C}_{\mathrm{F}}$ at $(-18 \%)=\$ 504,000(1-0.18)=\$ 413,280$
$c_{v}$ at $(-6 \%)=\$ 166(1-0.06)=\$ 156.04$
$\mathrm{D}^{\prime}=\frac{\$ 413,280}{(\$ 328-\$ 156.04) / \text { unit }}=\underline{2,404 \text { pumpsper month }}$
(Eqn. 2-13)
$\frac{3,112-2,404}{3,112}=0.2275$, or a $22.75 \%$ reduction in the breakeven point.

2-19 (a) $\mathrm{BE}=\$ 1,000,000 /(\$ 29.95-\$ 20.00)=100,503$ customers per month
(b) New BE point $=\$ 1,000,000 /(\$ 39.95-\$ 25.00)=66,890$ per month
(c) For 75,000 subscribers per month, profit equals

$$
75,000(\$ 39.95-\$ 25.00)-\$ 1,000,000=\$ 121,250 \text { per month }
$$

This improves on the monthly loss experienced in part (a).

2-20
(a) $\quad \mathrm{D}^{\prime}=\frac{\mathrm{C}_{\mathrm{F}}}{\mathrm{p}-\mathrm{c}_{\mathrm{v}}}=\frac{\$ 2,000,000}{(\$ 90-\$ 40) / \text { unit }}=\underline{40,000 \text { units per year }}$

(b) Profit (Loss) $=$ Total Revenue - Total Cost

$$
\begin{aligned}
(90 \% \text { Capacity }) & =90,000(\$ 90)-[\$ 2,000,000+90,000(\$ 40)] \\
& =\$ \underline{2,500,000} \text { per year } \\
(100 \% \text { Capacity }) & =[90,000(\$ 90)+10,000(\$ 70)]-[\$ 2,000,000+100,000(\$ 40)] \\
& =\$ \underline{2,800,000} \text { per year }
\end{aligned}
$$

2-21 Annual savings are at least equal to $(\$ 60 / \mathrm{lb})(600 \mathrm{lb})=\$ 36,000$. So the company can spend no more than $\$ 36,000$ (conservative) and still be economical. Other factors include ease of maintenance / cleaning, passenger comfort and aesthetic appeal of the improvements. Yes, this proposal appears to have merit so it should be supported.

2-22 Jerry's logic is correct if the AC system does not degrade in the next ten years (very unlikely). Because the leak will probably get worse, two or more refrigerant re-charges per year may soon become necessary. Jerry's strategy could be to continue re-charging his AC system until two re-charges are required in a single year. Then he should consider repairing the evaporator (and possibly other faulty parts of his system).

2-23 Over 81,000 miles, the gasoline-only car will consume 2,700 gallons of fuel. The flex-fueled car will use 3,000 gallons of E85. So we have

$$
(3,000 \text { gallons })(\mathrm{X})+\$ 1,000=(2,700 \text { gallons })(\$ 2.89 / \mathrm{gal})
$$

and

$$
\mathrm{X}=\$ 2.268 \text { per gallon }
$$

This is $21.5 \%$ less expensive than gasoline. Can our farmers pull it off - maybe with government subsidies?

2-24 (a) Total Annual Cost $(T A C)=$ Fixed cost + Cost of Heat Loss $=450 \mathrm{X}+50+\frac{4.80}{\mathrm{X}^{1 / 2}}$

$$
\frac{d(\mathrm{TAC})}{d \mathrm{X}}=0=450-\frac{2.40}{\mathrm{X}^{3 / 2}}
$$

$$
\mathrm{X}^{3 / 2}=\frac{2.40}{450}=0.00533
$$

$X^{*}=\underline{0.0305 \text { meters }}$
(b) $\frac{d^{2}(\mathrm{TAC})}{d \mathrm{X}^{2}}=\frac{3.6}{\mathrm{X}^{5 / 2}}>0 \quad$ for $\mathrm{X}>0$.

Since the second derivative is positive, $\mathrm{X}^{*}=0.0305$ meters is a minimum cost thickness.
(c) The cost of the extra insulation (a directly varying cost) is being traded-off against the value of reduction in lost heat (an indirectly varying cost).

2-25 Let $X=$ number of weeks to delay harvesting
and $R=$ total revenue as a function of $X$
$\mathrm{R}=(1,000$ bushels $+1,000$ bushels $\cdot \mathrm{X})(\$ 3.00 /$ bushel $-\$ 0.50 /$ bushel $\cdot \mathrm{X})$
$R=\$ 3,000+\$ 2,500 X-\$ 500 X^{2}$
$\frac{\mathrm{dR}}{\mathrm{dX}}=2,500-1,000 \mathrm{X}=0$
So $\mathrm{X}^{*}=2.5$ weeks
$\frac{d^{2} R}{d X^{2}}=-1,000$ so, we have a stationary point, $X^{*}$, that is a maximum.
Maximum revenue $=\$ 3,000+\$ 2,500(2.5)-500(2.5)^{2}=\underline{\$ 6,125}$

$$
\begin{aligned}
& \mathrm{C}_{\mathrm{T}}=\mathrm{C}_{\mathrm{o}}+\mathrm{C}_{\mathrm{c}}=\mathrm{knv}^{2}+\frac{\$ 1,500 \mathrm{n}}{\mathrm{v}} \\
& \frac{d \mathrm{C}_{\mathrm{T}}}{d \mathrm{v}}=0=2 \mathrm{kv}-\frac{1,500}{\mathrm{v}^{2}}=\mathrm{kv}^{3}-750 \\
& \mathrm{v}=\sqrt[3]{\frac{750}{\mathrm{k}}}
\end{aligned}
$$

To find $k$, we know that

$$
\begin{aligned}
& \frac{\mathrm{C}_{\mathrm{o}}}{\mathrm{n}}=\$ 100 / \mathrm{mile} \text { at } \mathrm{v}=12 \mathrm{miles} / \mathrm{hr} \\
& \frac{\mathrm{C}_{0}}{\mathrm{n}}=\mathrm{kv}^{2}=\mathrm{k}(12)^{2}=100
\end{aligned}
$$

and

$$
\mathrm{k}=100 / 144=0.6944
$$

so, $\quad v=\sqrt[3]{\frac{750}{0.6944}}=10.25 \mathrm{miles} / \mathrm{hr}$.
The ship should be operated at an average velocity of 10.25 mph to minimize the total cost of operation and perishable cargo.

Note: The second derivative of the cost model with respect to velocity is:

$$
\frac{d^{2} \mathrm{C}_{\mathrm{T}}}{d \mathrm{v}^{2}}=1.388 \mathrm{n}+3,000 \frac{\mathrm{n}}{\mathrm{v}^{3}}
$$

The value of the second derivative will be greater than 0 for $n>0$ and $v>0$. Thus we have found a minimum cost velocity.

|  | R11 | R19 | R30 | R38 |
| :--- | ---: | ---: | ---: | ---: |
| A. Investment cost | $\$ 1,800$ | $\$ 2,700$ | $\$ 3,900$ | $\$ 4,800$ |
| B. Annual Heating Load $\left(10^{6} \mathrm{Btu} / \mathrm{yr}\right)$ | 74 | 69.8 | 67.2 | 66.2 |
| C. Cost of heat loss/yr | $\$ 1,609.50$ | $\$ 1,518.15$ | $\$ 1,461.60$ | $\$ 1,439.85$ |
| D. Cost of heat loss over 25 years | $\$ 40,238$ | $\$ 37,954$ | $\$ 36,540$ | $\$ 35,996$ |
| E. Total Life Cycle Cost = A + D | $\$ 42,038$ | $\$ 40,654$ | $\$ 40,440$ | $\$ 40,796$ |

R30 is the most economical insulation thickness.

2-28 Solve for $\mathrm{k}: \mathrm{C}_{0} / \mathrm{n}=\mathrm{kv} \quad \mathrm{v}$ in miles $/ \mathrm{hr}$
$\frac{1 \text { gallon }}{18 \text { miles }}=1 / 18$ miles $/ \mathrm{gal}=\mathrm{k} \cdot 70$ miles $/ \mathrm{hr} ; \mathrm{k}=1 / 1260 \mathrm{hr}-\mathrm{gal} / \mathrm{mi}^{2}$

$$
\mathrm{k}=0.000794 \mathrm{hr}-\mathrm{gal} / \mathrm{mi}^{2}
$$

$\mathrm{C}_{\mathrm{G}}=0.000794 \mathrm{hr}-\mathrm{gal} / \mathrm{mi}^{2} \cdot \mathrm{n} \cdot \mathrm{v} \cdot \$ 3.00 / \mathrm{gal}$
$\mathrm{C}_{\mathrm{FSS}}=\mathrm{n} \cdot \$ 5 / \mathrm{hr} \cdot 1 / \mathrm{v}$

## Find $C_{T}$

$$
\begin{aligned}
\mathrm{C}_{\mathrm{T}} & =\$ 0.002382 \mathrm{hr} / \mathrm{mi}^{2} \cdot \mathrm{v} \mathrm{mi} / \mathrm{hr}+\$ 5 / \mathrm{hr} \cdot \mathrm{v}^{-1} \mathrm{hr} / \mathrm{mil}(\$ / \mathrm{mile}) \\
\frac{d \mathrm{C}_{\mathrm{T}}}{d \mathrm{v}} & =0.002382-5 \mathrm{v}^{-2}=0 ; \quad 0.002382 \mathrm{v}^{2}=5 ; \quad \mathrm{v}^{2}=2099 ; \quad \mathrm{v}^{*}=45.8 \mathrm{mi} / \mathrm{hr}
\end{aligned}
$$

Check $\frac{d^{2} \mathrm{C}_{\mathrm{T}}}{d \mathrm{v}^{2}}=10 \mathrm{v}^{-3}$ which is positive for $\mathrm{v}>0$, so total cost is minimized.

2-29
(a) $\frac{d \mathrm{C}}{d \lambda}=-\frac{\mathrm{C}_{\mathrm{I}}}{\lambda^{2}}+\mathrm{C}_{\mathrm{R}} \mathrm{t}=0$
or, $\lambda^{2}=\mathrm{C}_{\mathrm{I}} / \mathrm{C}_{\mathrm{R}} \mathrm{t}$
and, $\lambda^{*}=\left(\mathrm{C}_{\mathrm{I}} / \mathrm{C}_{\mathrm{R}} \mathrm{t}\right)^{1 / 2}$; we are only interested in the positive root.
(b) $\frac{d^{2} \mathrm{C}}{d \lambda^{2}}=\frac{2 \mathrm{C}_{\mathrm{I}}}{\lambda^{3}}>0$ for $\lambda>0$

Therefore, $\lambda^{*}$ results in a minimum life-cycle cost value.
(c) Investment cost versus total repair cost


2-30 $\quad\left(\frac{100,000}{22 \mathrm{mpg}}-\frac{100,000}{28 \mathrm{mpg}}\right)(\$ 3.00 /$ gallon $)=\$ 2,922$
Total extra amount $=\$ 2,500+\$ 2,922=\$ 5,422$
Assume the time value of money can be ignored and that comfort and aesthetics are comparable for the two cars.

2-31 (a) With Dynolube you will average $(20 \mathrm{mpg})(1.01)=20.2$ miles per gallon (a $1 \%$ improvement). Over 50,000 miles of driving, you will save

$$
\frac{50,000 \mathrm{miles}}{20 \mathrm{mpg}}-\frac{50,000 \mathrm{miles}}{20.2 \mathrm{mpg}}=24.75 \text { gallons of gasoline. }
$$

This will save ( 24.75 gallons)(\$3.00 per gallon $)=\$ 74.25$.
(b) Yes, the Dynolube is an economically sound choice.

2-32 The cost of tires containing compressed air is $(\$ 200 / 50,000$ miles $)=\$ 0.004$ per mile. Similarly, the cost of tires filled with $100 \%$ nitrogen is $(\$ 220 / 62,500$ miles $)=\$ 0.00352$ per mile. On the face of it, this appears to be a good deal if the claims are all true (a big assumption). But recall that air is $78 \%$ nitrogen, so this whole thing may be a gimmick to take advantage of a gullible public. At 200,000 miles of driving, one original set of tires and three replacements would be needed for compressed-air tires. One original set and two replacements (close enough) would be required for the $100 \%$ nitrogen-filled tires. What other assumptions are being made?

2-33

| Cost Factor | Brass-Copper Alloy | Plastic Molding |
| :--- | ---: | ---: |
| Casting / pc | $(25 \mathrm{lb})(\$ 3.35 / \mathrm{lb})=\$ 83.75$ | $(20 \mathrm{lb})(\$ 7.40 / \mathrm{lb})=\$ 148.00$ |
| Machining $/ \mathrm{pc}$ | $\$ 6.00$ | 0.00 |
| Weight Penalty $/ \mathrm{pc}$ | $(25 \mathrm{lb}-20 \mathrm{lb})(\$ 6 / \mathrm{lb})=\$ 30.00$ | 0.00 |
| Total Cost $/ \mathrm{pc}$ | $\$ 119.75$ | $\$ 148.00$ |

The Brass-Copper alloy should be selected to save $\$ 148.00-\$ 119.75=\$ 28.25$ over the life cycle of each radiator.
(a) Machine A

Non-defective units/day $=(100$ units/hr) $(7 \mathrm{hrs} /$ day $)(1-0.25)(1-0.03)$

$$
\approx 509 \text { units/day }
$$

Note: 3 months $=(52$ weeks $/$ year $) / 4=13$ weeks
Non-defective units/3-months = (13 weeks)(5 days/week)(509 units/day)

$$
=33,085 \text { units (> 30,000 required) }
$$

## Machine B

Non-defective units/day $=(130$ units/hr $)(6 \mathrm{hrs} /$ day $)(1-0.25)(1-0.10)$

$$
\approx 526 \text { units/day }
$$

Non-defective units/3-months = (13 weeks)(5 days/week)(526 units/day)

$$
=34,190 \text { units }(>30,000 \text { required })
$$

Either machine will produce the required 30,000 non-defective units/3-months
(b) Strategy: Select the machine that minimizes costs per non-defective unit since revenue for 30,000 units over 3-months is not affected by the choice of the machine (Rule 2). Also assume capacity reductions affect material costs but not labor costs.

## Machine A

Total cost/day $=(100 \mathrm{units} / \mathrm{hr})(7 \mathrm{hrs} /$ day $)(1-0.25)(\$ 6 / \mathrm{unit})$

$$
+(\$ 15 / \mathrm{hr}+\$ 5 / \mathrm{hr})(7 \mathrm{hrs} / \text { day })
$$

$$
=\$ 3,290 / \text { day }
$$

Cost/non-defective unit $=(\$ 3,290 /$ day $) /(509$ non-defective units/day $)$

$$
=\$ 6.46 / \text { unit }
$$

## Machine B

Total cost/day $=(130$ units/hr)(6 hrs/day)(1-0.25)(\$6/unit)

$$
+(\$ 15 / \mathrm{hr}+\$ 5 / \mathrm{hr})(6 \mathrm{hrs} / \text { day })
$$

$$
=\$ 3,630 / \text { day }
$$

Cost/non-defective unit $=(\$ 3,630 /$ day $) /(526$ non-defective units/day $)$

$$
=\$ 6.90 / \text { unit }
$$

Select Machine A.

2-35 Strategy: Select the design which minimizes total cost for 125,000 units/year (Rule 2). Ignore the sunk costs because they do not affect the analysis of future costs.
(a) Design A

Total cost/125,000 units $=(16 \mathrm{hrs} / 1,000$ units $)(\$ 18.60 / \mathrm{hr})(125,000)$

$$
+(4.5 \mathrm{hrs} / 1,000 \text { units })(\$ 16.90 / \mathrm{hr})(125,000)
$$

$=\$ 46,706.25$, or $\$ 0.37365 /$ unit
Design B
Total cost/ 125,000 units $=(7 \mathrm{hrs} / 1,000$ units $)(\$ 18.60 / \mathrm{hr})(125,000)$
$+(12 \mathrm{hrs} / 1,000$ units $)(\$ 16.90 / \mathrm{hr})(125,000)$
$=\$ 41,625$, or $\$ 0.333 /$ unit

## Select Design B

(b) Savings of Design B over Design A are:

Annual savings (125,000 units) $=\$ 46,706.25-\$ 41,625=\$ 5081.25$
Or, savings/unit $=\$ 0.37365-\$ 0.333=\$ 0.04065 /$ unit.

2-36 Profit per day $=$ Revenue per day - Cost per day

$$
\begin{aligned}
= & (\text { Production rate })(\text { Production time })(\$ 30 / \text { part })[1-(\% \text { rejected }+\% \text { tested }) / 100] \\
& -(\text { Production rate })(\text { Production time })(\$ 4 / \text { part })-(\text { Production time })(\$ 40 / \mathrm{hr})
\end{aligned}
$$

Process 1: Profit per day $=(35$ parts/hr) $(4 \mathrm{hrs} /$ day $)(\$ 30 /$ part $)(1-0.2)-$
(35 parts/hr)(4 hrs/day)(\$4/part) - (4 hrs/day)(\$40/hr)

$$
=\$ 2640 / \mathrm{day}
$$

Process 2: Profit per day $=(15$ parts/hr) $(7 \mathrm{hrs} /$ day $)(\$ 30 /$ part $)(1-0.09)-$
(15 parts/hr)(7 hrs/day)(\$4/part) - (7 hrs/day)(\$40/hr) $=\$ 2155.60 / \mathrm{day}$

Process 1 should be chosen to maximize profit per day.

2-37 At 70 mph your car gets $0.8(30 \mathrm{mpg})=24 \mathrm{mpg}$ and at 80 mph it gets
$0.6(30 \mathrm{mpg})=18 \mathrm{mpg}$. The extra cost of fuel at 80 mph is:
$(400 \mathrm{miles} / 18 \mathrm{mpg}-400 \mathrm{miles} / 24 \mathrm{mpg})(\$ 3.00$ per gallon $)=\$ 16.67$
The reduced time to make the trip at 80 mph is about 45 minutes. Is this a good tradeoff in your opinion? What other factors are involved?

2-38 (a) Assume a fixed-size production run which is identical for both speeds. Revenue is therefore the same for both speeds. Also assume the decision will be made on economic grounds alone (quality considerations, for example, are not a factor).

| Speed A: | Cycle Time | $=15 \mathrm{hrs} .+1.5 \mathrm{hrs} .=16.5$ |
| :---: | :---: | :---: |
|  | Tool Cost | \$1,000/20 = \$50 per cycle |
|  | Sharpening Cost | = \$25 per cycle |
|  | Tool-Setter | \$18/hr (1.5 hr./cycle) = \$27 per cycle |
|  | Operator | $16.5 \mathrm{hrs} /$ cycle $(\$ 15 / \mathrm{hr})=\$ 247.50$ per cycle |
|  | Variable OH | $16.5 \mathrm{hrs} /$ cycle $(\$ 25 / \mathrm{hr})=\$ 412.50$ per cycle |

$$
\text { Total Cost per Cycle }=\$ 762
$$

$$
\text { Cost per Piece }=\frac{\$ 762 / \text { cycle }}{(15 \mathrm{hrs} / \text { cycle })(400 \mathrm{pc} / \mathrm{hr})}
$$

Cost per Piece $=\$ 0.127$


$$
\text { Cost per Piece }=\frac{\$ 562 / \text { cycle }}{(10 \mathrm{hrs} / \text { cy cle })(540 \mathrm{pc} / \mathrm{hr})}
$$

Cost per Piece $=\$ 0.104$ Therefore, select Speed B.
(b) Extra tooling and operating expenses are traded off for extra output (production).

2-39 Relevant costs: tool cost, grinding cost, tool setter, overhead Criterion: Minimum cost per piece
Assumption: All output can be used
Cycle $=$ Production time + Tool changing time
Speed A: $\quad$ Cycle $=15$ hours +1.5 hour $=16.5$ hours Number of cycles $=20$

$$
\begin{array}{lll}
\text { Tool cost } & =\$ 500 / 20 \text { cycles } & =\$ 25 / \text { cycle } \\
\text { Grinding } & =\$ 25 / \text { cycle } & =\$ 25 / \text { cycle } \\
\text { Tool Setter } & =(\$ 8 / \mathrm{hr})(1.5 \mathrm{hrs} / \text { cycle }) & =\$ 12 / \text { cycle } \\
\text { Overhead } & =(\$ 3.75 / \mathrm{hr})(16.5 \mathrm{hrs} / \text { cycle }) & =\$ 61.88 / \text { cycle } \\
& & \$ 123.88 / \text { cycle }
\end{array}
$$

$$
\text { Cost } / \text { piece }=\frac{\$ 123.88 / \text { cycle }}{(15 \mathrm{hrs} / \text { cy cle })(400 \mathrm{pc} / \mathrm{hr})}=\$ 0.0206 / \text { piece }
$$

Speed B: $\quad$ Cycle $=12$ hours +1.5 hour $=13.5$ hours Number of cycles $=20$

$$
\begin{array}{lll}
\text { Tool cost } & =\$ 500 / 20 \text { cycles } & =\$ 25 / \text { cycle } \\
\text { Grinding } & =\$ 25 / \text { cycle } & =\$ 25 / \text { cycle } \\
\text { Tool Setter } & =(\$ 8 / \mathrm{hr})(1.5 \mathrm{hrs} / \text { cycle }) & =\$ 12 / \text { cycle } \\
\text { Overhead } & =(\$ 3.75 / \mathrm{hr})(13.5 \mathrm{hrs} / \text { cycle }) & =\$ 50.63 / \text { cycle } \\
& & \$ 112.63 / \text { cycle }
\end{array}
$$

$$
\text { Cost } / \text { piece }=\frac{\$ 112.63 / \text { cycle }}{(12 \mathrm{hrs} / \text { cy cle })(480 \mathrm{pc} / \mathrm{hr})}=\$ 0.0196 / \text { piece }
$$

Speed C: Cycle $=10$ hours +1.5 hour $=11.5$ hours Number of cycles $=20$

$$
\begin{array}{lll}
\text { Tool cost } & =\$ 500 / 20 \text { cycles } & =\$ 25 / \text { cycle } \\
\text { Grinding } & =\$ 25 / \text { cycle } & =\$ 25 / \text { cycle } \\
\text { Tool Setter } & =(\$ 8 / \mathrm{hr})(1.5 \mathrm{hrs} / \text { cycle }) & =\$ 12 / \text { cycle } \\
\text { Overhead } & =(\$ 3.75 / \mathrm{hr})(11.5 \mathrm{hrs} / \text { cycle }) & =\$ 43.13 / \text { cycle } \\
& & \$ 105.13 / \text { cycle }
\end{array}
$$

$$
\text { Cost } / \text { piece }=\frac{\$ 105.13 / \text { cycle }}{(10 \mathrm{hrs} / \text { cy cle })(540 \mathrm{pc} / \mathrm{hr})}=\$ 0.0195 / \text { piece }
$$

Assuming all else equal (quality, etc.) choose speed C to minimize cost/piece.

2-40 Option A (Purchase):
$\mathrm{C}_{\mathrm{T}}=(10,000$ items $)(\$ 8.50 /$ item $)=\$ 85,000$
Option B (Manufacture):
$\begin{array}{ll}\text { Direct Materials } & =\$ 5.00 / \mathrm{item} \\ \text { Direct Labor } & =\$ 1.50 / \mathrm{item} \\ \text { Overhead } & =\frac{\$ 3.00 / \mathrm{item}}{\$ 9.50 / \mathrm{item}}\end{array}$
$\mathrm{C}_{\mathrm{T}}=(10,000$ items $)(\$ 9.50 / \mathrm{item})=\$ 95,000$

Choose Option A (Purchase Item).

2-41 Assume you cannot stand the anxiety associated with the chance of running out of gasoline if you elect to return the car with no gas in it. Therefore, suppose you leave three gallons in the tank as "insurance" that a tow-truck will not be needed should you run out of gas in an unfamiliar city. The cost (i.e., the security blanket) will be $(\$ 2.70+\$ 0.30=\$ 3.00) \times 3$ gallons $=\$ 9.00$. If you bring back the car with a full tank of gasoline, the extra cost will be $\$ 0.30 \mathrm{x}$ the capacity, in gallons, of the tank. Assuming a 15gallon tank, this option will cost you $\$ 4.50$. Hence, you will save $\$ 9.00-\$ 4.50=\$ 4.50$ by bringing back the car with a full tank of gasoline.

2-42 Assumptions: You can sell all the metal that is recovered

Select Method 1 ( $62 \%$ recovered) to maximize total profit from the mine.

2-43 Profit/oz. (Method A) = \$350/oz. - (\$220/t-water)/(0.9 oz./t-water)(0.85)

$$
=\$ 62.42 / \mathrm{oz}
$$

Profit/oz. $($ Method B) $=\$ 350 /$ oz. $-(\$ 160 / t-w a t e r) /(0.9$ oz./t-water)(0.65) $=\$ 76.50 / \mathrm{oz}$.

## Select Method B

(a) False; (d) False; (g) False; (j) False; (m) True; (p) False; (s) False
(b) False;
(e) True;
(h) True; (k) True; (n) True;
(q) True;
(c) True;
(f) True;
(i) True; (l) False; (o) True;
(r) True;

# 2-45 <br> (a) Loss $=\frac{(1,750,000 \mathrm{Btu})\left(\frac{\mathrm{lb} \mathrm{coal}}{12,000 \mathrm{Btu}}\right)}{0.30}=486 \mathrm{lbs}$ of coal 

(b) 486 pounds of coal produces $(486)(1.83)=889$ pounds of $\mathrm{CO}_{2}$ in a year.
(a) Let $\mathrm{X}=$ breakeven point in miles

Fuel cost $($ car dealer option $)=(\$ 2.00 / \mathrm{gal})(1 \mathrm{gal} / 20$ miles $)=\$ 0.10 / \mathrm{mile}$
Motor Pool Cost $=$ Car Dealer Cost
$(\$ 0.36 / \mathrm{mi}) \mathrm{X}=(6$ days $)(\$ 30 /$ day $)+(\$ 0.20 / \mathrm{mi}+\$ 0.10 / \mathrm{mi}) \mathrm{X}$
$\$ 0.36 \mathrm{X}=180+\$ 0.30 \mathrm{X} \quad$ and $\quad \mathrm{X}=\underline{3,000 \text { miles }}$
(b) 6 days $(100 \mathrm{miles} /$ day $)=600$ free miles

If the total driving distance is less than 600 miles, then the breakeven point equation is given by:
$(\$ 0.36 / \mathrm{mi}) \mathrm{X}=(6$ days $)(\$ 30 /$ day $)+(\$ 0.10 / \mathrm{mi}) \mathrm{X}$
$\mathrm{X}=692.3$ miles $>600$ miles
This is outside of the range [0,600], thus renting from State Tech Motor Pool is best for distances less than 600 miles.

If driving more than 600 miles, then the breakeven point can be determined using the following equation:
$(\$ 0.36 / \mathrm{mi}) \mathrm{X}=(6$ days $)(\$ 30 /$ day $)+(\$ 0.20 / \mathrm{mi})(\mathrm{X}-600 \mathrm{mi})+(\$ 0.10 / \mathrm{mi}) \mathrm{X}$
$X=\underline{1,000 \text { miles } \quad \text { The true breakeven point is } 1000 \text { miles. } . . . . ~}$
(c) The car dealer was correct in stating that there is a breakeven point at 750 miles. If driving less than 900 miles, the breakeven point is:

$$
\begin{aligned}
& (\$ 0.34 / \mathrm{mi}) \mathrm{X}=(6 \text { days })(\$ 30 / \text { day })+(\$ 0.10 / \mathrm{mi}) \mathrm{X} \\
& X=750 \text { miles }<900 \text { miles }
\end{aligned}
$$

However, if driving more than 900 miles, there is another breakeven point.

$$
\begin{aligned}
& (\$ 0.34 / \mathrm{mi}) \mathrm{X}=(6 \text { days })(\$ 30 / \mathrm{day})+(\$ 0.28 / \mathrm{mi})(\mathrm{X}-900 \mathrm{mi})+(\$ 0.10 / \mathrm{mi}) \mathrm{X} \\
& \mathrm{X}=1800 \text { miles }>900 \text { miles }
\end{aligned}
$$

The car dealer is correct, but only if the group travels in the range between 750 miles and 1,800 miles. Since the group is traveling more than 1,800 miles, it is better for them to rent from State Tech Motor Pool.

This problem is unique in that there are two breakeven points. The following graph shows the two points.


2-47 This problem is location specific. We'll assume the problem setting is in Tennessee. The eight years $(\$ 2,400 / \$ 300)$ to recover the initial investment in the stove is expensive (i.e. excessive) by traditional measures. But the annual cost savings could increase due to inflation. Taking pride in being "green" is one factor that may affect the homeowner's decision to purchase a corn-burning stove.


Reducing fixed costs has no impact on the optimum demand value, but does broaden the profitable range of demand. Reducing variable costs increase the optimum demand value as well as the range of profitable demand.

| Value Increase <br> $=$ | $\$$ | 0.10 | Speed $=$ | $\mathbf{5 , 0 0 0}$ | $\mathbf{6 , 0 0 0}$ |
| :--- | ---: | ---: | :--- | ---: | ---: |
| New Blade | $\$$ | 45.00 | Sharpen <br> Interval $=$ | 2.0 | 1.5 |
| Sharpening <br> Cost | $\$$ | 10.00 | bd-ft/hr $=$ | 1,000 | 1,200 |
| Change Over <br> (hrs.) |  | 0.25 |  |  |  |
| Blade Life <br> (cycles) |  | 8 | 8 | bd.-ft. <br> required $=$ | unlimited |


| Speed |  | $\mathbf{5 , 0 0 0}$ | $\mathbf{6 , 0 0 0}$ |
| :--- | ---: | ---: | ---: |
| Output/cycle | 2,000 | 1,800 |  |
| Number of |  | 3.56 | 4.57 |
| cycles |  |  |  |
| Resharpening <br> Cost $=$ | $\$ 35.56$ | $\$ 45.71$ |  |
| Blade Cost $=$ | $\$$ | 20.00 | $\$ 25.71$ |


| Speed | $\mathbf{5 , 0 0 0}$ | $\mathbf{6 , 0 0 0}$ |
| :--- | :---: | :---: |
| Value Added | $\$ 711.11$ | $\$ 822.86$ |
| Total Expense | $\$ 55.56$ | $\$ 71.43$ |
| Net Profit/day | $\$ 655.56$ | $\$ 751.43$ |

The new blade is not a good deal. The $10 \%$ reduction in the cost of the blade does not compensate for the $20 \%$ reduction in blade life.

| Value Increase | \$ | 0.10 |  | Speed = | 5,000 | 6,000 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| New Blade |  | \$ 50.00 |  | Sharpen |  |  |
|  |  |  |  | Interval = | 2.0 | 1.5 |
| Sharpening | \$ | 10.00 |  | bd-ft/hr = |  | 1,200 |
| Cost |  |  |  |  | 1,000 |  |
| Change Over (hrs.) |  | 0.25 |  |  |  |  |
| Blade Life (cycles) |  | 10 |  |  |  |  |
| Shift Length (hrs.) |  | 8 |  | bd. ft . required $=$ | 100,000 |  |
| Speed |  | 5,000 | 6,000 |  |  |  |
| Output/cycle |  | 2,000 | 1,800 |  |  |  |
| Number of cycles |  | 50.00 | 55.56 |  |  |  |
| Resharpening Cost = |  | \$ 500.00 | \$ 555.56 |  |  |  |
| Blade Cost = |  | \$ 250.00 | \$ 277.78 |  |  |  |
| Speed |  | 5,000 | 6,000 |  |  |  |
| Total Expense |  | \$ 750.00 | \$ 833.33 |  |  |  |
| Cost per bd-ft |  | \$ 0.0075 | \$ 0.0083 |  |  |  |

Operating the planer at $6,000 \mathrm{ft} / \mathrm{min}$ reduces the life of the blade, resulting in higher overall resharpening cost and blade cost, regardless of the job size. If these are the only factors considered, it will always be more economical to operate at $5,000 \mathrm{ft} / \mathrm{min}$ for a limited job size.

The benefit of operating at $6,000 \mathrm{ft} / \mathrm{min}$ is a reduction in the time required to complete the job. If the assumption that the operator is idle during any time savings is relaxed, we would see that it is more economical to operate at $6,000 \mathrm{ft} / \mathrm{min}$.

2-51 New annual heating load $=(230$ days $)\left(72{ }^{\circ} \mathrm{F}-46^{\circ} \mathrm{F}\right)=5,980$ degree days. Now, $136.7 \times 10^{6}$ Btu are lost with no insulation. The following U-factors were used in determining the new heating load for the various insulation thicknesses.

|  | U-factor | Heating Load |
| :--- | :--- | :--- |
| R11 | 0.2940 | $101.3 \times 10^{6} \mathrm{Btu}$ |
| R19 | 0.2773 | $95.5 \times 10^{6} \mathrm{Btu}$ |
| R30 | 0.2670 | $92 \times 10^{6} \mathrm{Btu}$ |
| R38 | 0.2630 | $90.6 \times 10^{6} \mathrm{Btu}$ |


|  | $\$ / \mathrm{kWhr}$ <br> Energy Cost | $\$ / 10^{6} \mathrm{Btu}$ <br> $\$ 25.20$ |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  | R 11 | R 19 | R 30 | R38 |

## Solutions to Case Study Exercises

2-52
In this problem we observe that "an ounce of prevention is worth a pound of cure." The ounce of prevention is the total annual cost of daylight use of headlights, and the pound of cure is postponement of an auto accident because of continuous use of headlights. Clearly, we desire to postpone an accident forever for a very small cost.

The key factors in the case study are the cost of an auto accident and the frequency of an auto accident. By avoiding an accident, a driver "saves" its cost. In postponing an accident for as long as possible, the "annual cost" of an accident is reduced, which is a good thing. So as the cost of an accident increases, for example, a driver can afford to spend more money each year to prevent it from happening through continuous use of headlights. Similarly, as the acceptable frequency of an accident is lowered, the total annual cost of prevention (daytime use of headlights) can also decrease, perhaps by purchasing less expensive headlights or driving less mileage each year.

Based on the assumptions given in the case study, the cost of fuel has a modest impact on the cost of continuous use of headlights. The same can be said for fuel efficiency. If a vehicle gets only 15 miles to the gallon of fuel, the total annual cost would increase by about $65 \%$. This would then reduce the acceptable value of an accident to "at least one accident being avoided during the next 16 years." To increase this value to a more acceptable level, we would need to reduce the cost of fuel, for instance. Many other scenarios can be developed.

2-53 Suppose my local car dealer tells me that it costs no more than $\$ 0.03$ per gallon of fuel to drive with my headlights on all the time. For the case study, this amounts to ( 500 gallons of fuel per year) x $\$ 0.03$ per gallon $=\$ 15$ per year. So the cost effectiveness of continuous use of headlights is roughly six times better than for the situation in the case study.

## Solutions to FE Practice Problems

2-54

$$
\begin{aligned}
& \mathrm{p}=400-\mathrm{D}^{2} \\
& \mathrm{TR}=\mathrm{p} \cdot \mathrm{D}=\left(400-\mathrm{D}^{2}\right) \mathrm{D}=400 \mathrm{D}-\mathrm{D}^{3} \\
& \mathrm{TC}=\$ 1125+\$ 100 \cdot \mathrm{D} \\
& \text { Total Profit } / \text { month }=\mathrm{TR}-\mathrm{TC}=400 \mathrm{D}-\mathrm{D}^{3}-\$ 1125-\$ 100 \mathrm{D} \\
& \\
& =-\mathrm{D}^{3}+300 \mathrm{D}-1125
\end{aligned} \quad \begin{array}{r}
\frac{d \mathrm{TP}}{d \mathrm{D}}=-3 \mathrm{D}^{2}+300=0 \rightarrow \mathrm{D}^{2}=100 \rightarrow \mathrm{D}^{*}=\underline{10 \text { units }}
\end{array} \quad \begin{array}{r}
\frac{d^{2} \mathrm{TP}}{\frac{d^{2}}{d \mathrm{D}^{2}}=-6 \mathrm{D} ; \text { at } \mathrm{D}=\mathrm{D}^{*}, \quad \frac{d^{2} \mathrm{TP}}{d \mathrm{D}^{2}}=-60}
\end{array}
$$

Negative, therefore maximizes profit.

## Select (a)

$-D^{3}+300 D-1125=0$ for breakeven

$$
\text { At } \underline{D=15 \text { units; } ; \quad-15^{3}+300(15)-1125=0}
$$

## Select (b)

$C_{F}=\$ 100,000+\$ 20,000=\$ 120,000$ per year
$\mathrm{C}_{\mathrm{V}}=\$ 15+\$ 10=\$ 25$ per unit
$\mathrm{p}=\$ 40$ per unit

$$
\mathrm{D}^{\prime}=\frac{\mathrm{C}_{\mathrm{F}}}{\mathrm{p}-\mathrm{c}_{\mathrm{v}}}=\frac{\$ 120,000}{(\$ 40-\$ 25)}=8,000 \text { units } / \mathrm{yr}
$$

## Select (c)

2-57 Profit $=\mathrm{pD}-\left(\mathrm{C}_{\mathrm{F}}+\mathrm{C}_{\mathrm{V}} \mathrm{D}\right)$
At $\mathrm{D}=10,000$ units/yr,
Profit/yr $=(40)(10,000)-[120,000+(25)(10,000)]=\$ 30,000$
Select (e)

2-58 Profit $=\mathrm{pD}-\left(\mathrm{C}_{\mathrm{F}}+\mathrm{C}_{\mathrm{V}} \mathrm{D}\right)$
$60,000=35 \mathrm{D}-(120,000+25 \mathrm{D})$
$180,000=10 \mathrm{D} ; \mathrm{D}=\underline{18,000}$ units/yr

Select (d)

2-59

| Castings <br> produced/hr. | 100 | 200 | 300 | 400 | 500 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Total revenue/hr. $\$ 2,000$ <br> Total cost/hr. $\$ 3,400$ <br> 1,000 2,600 | 3,800 | $\$ 6,000$ | $\$ 7,250$ |  |  |
| Profit/hr. | $\$ 1,000$ | $\$ 800$ | $\$ 1,600$ | $\$ 2,100$ | 4,700 |

Therefore, produce $\underline{500}$ castings per hour. Select (e)

## Select (d)

## Solutions to Problems in Appendix

## 2-A-1 (a) Details of transactions

(a) Smith invested $\$ 35,000$ cash to start the business.
(b) Purchased $\$ 350$ of office supplies on account.
(c) Paid $\$ 30,000$ to acquire land as a future building site.
(d) Earned service revenue and received cash of \$1,900.
(e) Paid $\$ 100$ on account.
(f) Paid for a personal vacation, which is not a transaction of the business.
(g) Paid cash expenses for rent, $\$ 400$, and utilities, $\$ 100$.
(h) Sold office supplies for cost of $\$ 150$.
(i) Withdrew $\$ 1,200$ cash for personal use.

Analysis of Transactions:

|  | ASSETS |  |  |  |  |  | LIABILITIES |  | OWNER'S EQUITY | Type of Owner's Equity Transaction |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) | $\begin{aligned} & \text { Cash } \\ & +35,000 \end{aligned}$ | + | Office <br> Supplies | + | Land |  | Payable | + | $\begin{aligned} & \text { Capital } \\ & +35,000 \end{aligned}$ | Owner investment |
| (b) |  |  | + 350 |  |  |  | + 350 |  |  |  |
| (c) | -30,000 |  |  |  | +30,000 |  |  |  |  |  |
| (d) | + 1,900 |  |  |  |  |  |  |  | +1,900 | Service revenue |
| (e) | - 100 |  |  |  |  | = | - 100 |  |  |  |
| (f) | Not a |  |  |  |  |  |  |  |  |  |
| (g) | - 400 |  |  |  |  |  |  |  | -400 | Rent expense |
|  | - 100 |  |  |  |  |  |  |  | -100 | Utilities expense |
| (h) | + 150 |  | - 150 |  |  |  |  |  |  |  |
| (i) | - 1,200 |  |  |  |  |  |  |  | -1,200 | Owner withdrawal |
| Bal. | 5,250 |  | 200 |  | 30,000 |  | 250 |  | 35,200 |  |
|  |  |  | 35,450 |  |  |  |  | 450 |  |  |

(b) Financial Statements of Campus Apartments Locators

Income Statement
Month Ended July 31, 2007
Revenue:

Expenses:

Utilities expense ............................................................. 100
Total expenses .
500
Net income
\$1,400

## Statement of Owner's Equity

Month Ended July 31, 2007
Jill Smith, capital, July 1, $2007 \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$


36,400

Less: Withdrawals by owner
$(1,200)$
Jill Smith, capital, July 31, 2007
\$35,200

Balance Sheet
July 31,2007

| Assets | Liabilities |  |  |
| :---: | :---: | :---: | :---: |
| Cash | \$5,250 | Accounts payable | \$ 250 |
| Office supplies | 200 |  |  |
| Land | 30,000 | Owner's Equity |  |
|  |  | Jill Smith, capital .......... | 35,200 |
|  |  | Total liabilities and |  |
| Total assets ........... | 35,450 | owner's equity . | \$35,450 |



Req. 2

| Peavy Design |  |  |
| :--- | ---: | ---: |
| Mncome Statement |  |  |
| Revench Ended May 31, 20X5 |  |  |
| Service revenue $(\$ 1,100+\$ 5,000)$ |  | $\$ 6,100$ |
| Expenses: | $\$ 1,200$ |  |
| Rent expense | 660 |  |
| Advertising expense |  | $\underline{1,860}$ |
| Total expenses |  | $\underline{\$ 4,240}$ |
| Net income |  |  |

Req. 3

| Peavy Design |  |
| :---: | :---: |
| Statement of Owner's Equity |  |
| Month Ended May 31, $20 \times 5$ |  |
| Daniel Peavy, capital, April 30, 20X5 | \$23,660 |
| Add: Investments by owner (\$12,000 + \$1,700) | 13,700 |
| Net income for the month | 4,240 |
|  | 41,600 |
| Less: Withdrawals by owner | $(4,000)$ |
| Daniel Peavy, capital, May 31, $20 \times 5$ | \$37,600 |

Req. 4

| Peavy Design |  |  |  |
| :---: | :---: | :---: | :---: |
| Balance Sheet |  |  |  |
| May 31, 20X5 |  |  |  |
| ASSETS |  | LIABILITIES |  |
| Cash | \$ 6,090 | Accounts payable | \$ 720 |
| Accounts receivable | 7,490 |  |  |
| Supplies | 640 | OWNER'S EQUITY |  |
| Land | 24,100 | Daniel Peavy, capital | 37,600 |
|  |  | Total liabilities and |  |
| Total assets | \$38,320 | owner's equity | \$38,320 |

## 2-A-3 <br> 1. Overhead

Compensation for non-chargeable time, $0.15 \times \$ 3,600,000$
\$ 540,000
Other costs
(a) Total overhead
\$1,989,000
(b) Direct labor, $0.85 \times \$ 3,600,000$

Overhead application rate, (a) $\div$ (b)
65\%
2. Hourly rate:
$\$ 60,000 \div(48 \times 40)=\$ 60,000 \div 1,920$
\$31.25

Many students will forget that "his work there" includes an overhead application:

Direct labor, $10 \times \$ 31.25$
Applied overhead, $\$ 312.50 \times 0.65$
Total costs applied
We point out that direct-labor time on a job is usually compiled for all classes of engineers and then applied at their different compensation rates. Overhead is usually not applied on the piecemeal basis demonstrated here. Instead, it is applied in one step after all the labor costs of the job have been accumulated.

