

SOLUTIONS MANUAL



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Fourth Edition



Econometric Analysis of Panel Data

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Chapter 2
The One-way Error Component Regression Model

- 2.2 (a) $Q = I_{NT} - P$ where $P = I_N \otimes J_T$ is idempotent and is therefore its own generalized inverse. The variance-covariance matrix of the disturbance $\tilde{v} = Qv$ in (2.6) is

$$E(\tilde{v}\tilde{v}') = E(Qvv'Q) = \sigma_v^2 Q$$

with generalized inverse Q/σ_v^2 . OLS on (2.6) yields

$$\hat{\beta} = (X'QQX)^{-1}X'QQy = (X'QX)^{-1}XQy$$

which is $\tilde{\beta}$ given in (2.7). Also, GLS on (2.6) using generalized inverse yields

$$\hat{\beta} = (X'QQQX)^{-1}X'QQQy = (X'QX)^{-1}X'Qy = \tilde{\beta}$$

(b) For the general linear model $y = X\beta + u$ with $E(uu') = \Omega$, a necessary and sufficient condition for OLS to be equivalent to GLS is given by $X'\Omega^{-1}P_X = 0$, where $P_X = I - P_X$ and $P_X = X(X'X)^{-1}X'$, see Baltagi (1989). For (2.6), this condition can be written as

$$(X'Q)(Q/\sigma_v^2)P_{QX} = 0$$

using the fact that Q is idempotent, the left hand side can be written as $(X'Q)\bar{P}_{QX}/\sigma_v^2$ which is clearly 0, since \bar{P}_{QX} is the orthogonal projection of QX .

- 2.5 $E(u'Pu) = E(\text{tr}(uu'P)) = \text{tr}(E(uu')P) = \text{tr}(\Omega P)$. From (2.18), $\Omega P = \sigma_1^2 P$ since $PQ = 0$. Hence, from (2.21), $E(\hat{\sigma}_1^2) = \frac{E(u'Pu)}{\text{tr}(P)} = \frac{\text{tr}(\sigma_1^2 P)}{\text{tr}(P)} = \sigma_1^2$.

Similarly, $E(u'Qu) = \text{tr}(\Omega Q) = \text{tr}(\sigma_v^2 Q)$ where the last equality follows from (2.18) and the fact that $\Omega Q = \sigma_v^2 Q$ since $PQ = 0$. Hence from (2.22), $E(\hat{\sigma}_v^2) = \frac{E(u'Qu)}{\text{tr}(Q)} = \frac{\text{tr}(\sigma_v^2 Q)}{\text{tr}(Q)} = \sigma_v^2$.

2.7 (b) GLS on (2.28) yields

$$\widehat{\delta}_{GLS} = \left[(Z'Q, Z'P) \begin{bmatrix} \sigma_v^2 Q & 0 \\ 0 & \sigma_1^2 P \end{bmatrix}^{-1} \begin{pmatrix} QZ \\ PZ \end{pmatrix} \right]^{-1} \\ \times (Z'Q, Z'P) \begin{bmatrix} \sigma_v^2 Q & 0 \\ 0 & \sigma_1^2 P \end{bmatrix}^{-1} \begin{pmatrix} Qy \\ Py \end{pmatrix}$$

Using generalized inverse

$$\begin{bmatrix} \sigma_v^2 Q & 0 \\ 0 & \sigma_1^2 P \end{bmatrix}^{-1} = \begin{bmatrix} Q/\sigma_v^2 & 0 \\ 0 & P/\sigma_1^2 \end{bmatrix}$$

one gets

$$\widehat{\delta}_{GLS} = [(Z'QZ)/\sigma_v^2 + (Z'PZ)/\sigma_1^2]^{-1} [(Z'QZ)/\sigma_v^2 + (Z'Py)/\sigma_1^2] \\ = (Z'\Omega^{-1}Z)^{-1} Z'\Omega^{-1}y$$

where Ω^{-1} is given by (2.19).

(a) OLS on (2.28) yields

$$\widehat{\delta}_{OLS} = \left[Z'Q, Z'P \begin{pmatrix} QZ \\ PZ \end{pmatrix} \right]^{-1} (Z'Q, Z'P) \begin{pmatrix} Qy \\ Py \end{pmatrix} \\ = (Z'QZ + Z'PZ)^{-1} (Z'Qy + Z'Py) \\ = (Z'(Q + P)Z)^{-1} Z'(Q + P)y = (Z'Z)^{-1} Z'y$$

since $Q + P = I_{NT}$.

2.10 (a) From (2.2) and (2.38), $E(u_{i,T+Su_{ji}}) = \sigma_\mu^2$, for $i = j$ and zero otherwise. The only correlation over time occurs because of the presence of the same individual across the panel. The v_{it} 's are not correlated for different time periods. In vector form

$$w = E(u_{i,T+Su}) = \sigma_\mu^2(0, \dots, 0, \dots, 1, \dots, 1, \dots, 0, \dots, 0)'$$

where there are T ones for the i -th individual. This can be rewritten as $w = \sigma_\mu^2(\ell_i \otimes \iota_T)$ where ℓ_i is the i -th column of I_N , i.e., ℓ_i is a vector that has 1 in the i -th position and zero elsewhere. ι_T is a vector of ones of dimension T .

(b) $(\ell_i' \otimes \iota_T')P = (\ell_i' \otimes \iota_T')(I_N \otimes \frac{\iota_T \iota_T'}{T}) = (\ell_i' \otimes \iota_T')$. Therefore, in (2.39)

$$w'\Omega^{-1} = \sigma_\mu^2(\ell_i' \otimes \iota_T') \left[\frac{1}{\sigma_1^2} P + \frac{1}{\sigma_v^2} Q \right] = \frac{\sigma_\mu^2}{\sigma_1^2} (\ell_i' \otimes \iota_T')$$

since $(\ell_i' \otimes \iota_T')Q = (\ell_i' \otimes \iota_T')(I_{NT} - P) = (\ell_i' \otimes \iota_T') - (\ell_i' \otimes \iota_T') = 0$.

- 2.11 The following program, using the Grunfeld (1958) data on investment on the Wiley web site, gives the SAS program and output for the estimation of a “One-way Error Component Regression”. The estimators are OLS, WITHIN, BETWEEN, WALHUS, AMEMIYA, SWAR, NERLOVE, AND IMLE. The results do not replicate exactly those in Table 2.1 because there is no correction for degrees of freedom in these programs. However, the output reported below using EViews should match the results in Table 2.1.

```

DATA GRUNFELD;
  INFILE 'A:\GRUNFELD.FIL';
  INPUT FIRM YEAR INVEST STOCK CAPITAL;

PROC IML;
  USE GRUNFELD;  READ ALL INTO TEMP;
  N=10;  T=20;  NT=N*T;
  One=Repeat(1,NT,1);

Y=Temp[,3];  X=Temp[,4:5];  Z=One||X;  K=NCOL(X);
/* I, J, P and Q Matrices */
I_t=J(T,1,1);  JT=(I_t*I_t');  Z_U=I(N)@I_t;
P=I(N)@JT/T;  Q=I(NT)-P;
JNT=Repeat(JT,N,N);  JNT_BAR=JNT/NT;

*----- OLS ESTIMATORS -----*;

  OLS_BETA=INV(Z'*Z)*Z'*Y;
  OLS_RES=Y-Z*OLS_BETA;
  VAR_REG=SSQ(OLS_RES)/(NT-NCOL(Z));
  VAR_COV=VAR_REG*INV(Z'*Z);
  STD_OLS=SQRT(VECDIAG(VAR_COV));
  T_OLS=OLS_BETA/STD_OLS;

  LOOK1=OLS_BETA||STD_OLS||T_OLS;
  CTITLE={'PARAMETER' 'STANDARD ERROR' 'T-STATISTICS'};
  RTITLE={'INTERCEPT' 'FIRMV' 'CAPITALV'};
  PRINT 'RESULTS OF OLS',,
  LOOK1(|COLNAME=CTITLE ROWNAME=RTITLE FORMAT=8.5|);

*----- BETWEEN ESTIMATOR -----*;

  BW_BETA=INV(Z'*P*Z)*Z'*P*Y;
  BW_RES=P*Y-P*Z*BW_BETA;
  VAR_BW=SSQ(BW_RES)/(N-NCOL(Z));  /* Equation 2.27 */
  V_C_BW=VAR_BW*INV(Z'*P*Z);
  STD_BW=SQRT(VECDIAG(V_C_BW));
  T_BW=BW_BETA/STD_BW;

  LOOK1=BW_BETA||STD_BW||T_BW;
  CTITLE={'PARAMETER' 'STANDARD ERROR' 'T-STATISTICS'};
  RTITLE={'INTERCEPT' 'FIRMV' 'CAPITALV'};
  PRINT 'RESULTS OF BETWEEN',,
  LOOK1(|COLNAME=CTITLE ROWNAME=RTITLE FORMAT=8.5|);

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*----- WITHIN ESTIMATORS -----*;

WT_BETA=INV(X'*Q*X)*X'*Q*Y;          /* Equation 2.7*/
WT_RES=Q*Y-Q*X*WT_BETA;
VAR_WT=SSQ(WT_RES)/(NT-N-NCOL(X));  /* Equation 2.24 */
V_C_WT=VAR_WT*INV(X'*Q*X);
STD_WT=SQRT(VECDIAG(V_C_WT));
T_WT=WT_BETA/STD_WT;

WH_V_1=(OLS_RES'*P*OLS_RES)/N;
      /* Equation 2.21 with U=OLS residuals */

***** Checking for negative VAR_MHU *****;

WH_V_MHU=(WH_V_1-WH_V_V)/T;
IF WH_V_MHU<0 THEN NEGA_WH=1; ELSE NEGA_WH=0;
WH_V_MHU=WH_V_MHU # (WH_V_MHU>0);
WH_V_1=(T*WH_V_MHU)+WH_V_V;
WH_V_T=WH_V_V+WH_V_MHU;
WH_RHO=WH_V_MHU/WH_V_T;

*****;

OMEGA_WH=(Q/WH_V_V)+(P/WH_V_1);     /* Equation 2.19 */
WH_BETA=INV(Z'*OMEGA_WH*Z)*Z'*OMEGA_WH*Y;
THETA_WH=1-(SQRT(WH_V_V)/SQRT(WH_V_1));
OMEGAWH=(Q/SQRT(WH_V_V)+(P/SQRT(WH_V_1));
WH_RES=(OMEGAWH*Y)-(OMEGAWH*Z*WH_BETA);
VAR_WH=SSQ(WH_RES)/(NT-NCOL(Z));
V_C_WH=INV(Z'*OMEGA_WH*Z);
STD_WH=SQRT(VECDIAG(V_C_WH));
T_WH=WH_BETA/STD_WH;

LOOK1=WH_BETA||STD_WH||T_WH;
CTITLE={'PARAMETER' 'STANDARD ERROR' 'T-STATISTICS'};
RTITLE={'INTERCEPT' 'FIRMV' 'CAPITALV'};
PRINT 'RESULTS OF WALLACE-HUSSAIN',,
LOOK1(|COLNAME=CTITLE ROWNAME=RTITLE FORMAT=8.5|);

FREE OMEGA_WH OMEGAWH WH_RES;

*----- AMEMIYA ESTIMATOR OF VARIANCE COMPONENTS -----*;

Y_BAR=Y[:]; X_BAR=X[:,];
ALPHA_WT=Y_BAR-X_BAR*WT_BETA;
LSDV_RES=Y-ALPHA_WT*ONE-X*WT_BETA;
AM_V_V=(LSDV_RES'*Q*LSDV_RES)/(NT-N);
      /* Equation 2.22 with U=LSDV residuals */
AM_V_1=(LSDV_RES'*P*LSDV_RES)/N;
      /*Equation 2.21 with U=LSDV residuals */

```

```

LOOK1=WT_BETA||STD_WT||T_WT;
CTITLE={'PARAMETER' 'STANDARD ERROR' 'T-STATISTICS'};
RTITLE={'FIRMV' 'CAPITALV'};
PRINT 'RESULTS OF WITHIN',,
LOOK1(|COLNAME=CTITLE ROWNAME=RTITLE FORMAT=8.5|);

*----- WALLACE & HUSSAIN ESTIMATOR OF VARIANCE COMPONENTS -----*;

WH_V_V=(OLS_RES'*Q*OLS_RES)/(NT-N);
      /* Equation 2.22 with U=OLS residuals */

THETA_AM=1-(SQRT(AM_V_V)/SQRT(AM_V_1));
OMEGAAM=(Q/SQRT(AM_V_V)+(P/SQRT(AM_V_1)));
AM_RES=(OMEGAAM*Y)-(OMEGAAM*Z*AM_BETA);
VAR_AM=SSQ(AM_RES)/(NT-NCOL(Z));
V_C_AM=INV(Z'*OMEGA_AM*Z);
STD_AM=SQRT(VECDIAG(V_C_AM));
T_AM=AM_BETA/STD_AM;

LOOK1=AM_BETA||STD_AM||T_AM;
CTITLE={'PARAMETER' 'STANDARD ERROR' 'T-STATISTICS'};
RTITLE={'INTERCEPT' 'FIRMV' 'CAPITALV'};
PRINT 'RESULTS OF AMEMIYA',,
LOOK1(|COLNAME=CTITLE ROWNAME=RTITLE FORMAT=8.5|);

FREE OMEGA_AM OMEGAAM AM_RES;

*----- SWAMY & ARORA ESTIMATOR OF VARIANCE COMPONENTS -----*;

***** Checking for negative VAR_MHU *****;

AM_V_MHU=(AM_V_1-AM_V_V)/T;
IF AM_V_MHU<0 THEN NEGA_AM=1; ELSE NEGA_AM=0;
AM_V_MHU=AM_V_MHU # (AM_V_MHU>0);
AM_V_1=(T*AM_V_MHU)+AM_V_V;

AM_V_T=AM_V_V+AM_V_MHU;
AM_RHO=AM_V_MHU/AM_V_T;

*****;

OMEGA_AM=(Q/AM_V_V)+(P/AM_V_1);      /*Equation 2.19 */
AM_BETA=INV(Z'*OMEGA_AM*Z)*Z'*OMEGA_AM*Y;

SA_V_V=(Y'*Q*Y-Y'*Q*X*INV(X'*Q*X)*X'*Q*Y)/(NT-N-K);
      /* Equation 2.24 */
SA_V_1=(Y'*P*Y-Y'*P*Z*INV(Z'*P*Z)*Z'*P*Y)/(N-K-1);
      /* Equation 2.27 */

***** Checking for negative VAR_MHU *****;

SA_V_MHU=(SA_V_1-SA_V_V)/T;
IF SA_V_MHU<0 THEN NEGA_SA=1; ELSE NEGA_SA=0;
SA_V_MHU=SA_V_MHU # (SA_V_MHU>0);
SA_V_1=(T*SA_V_MHU)+SA_V_V;

```

```

SA_V_T=SA_V_V+SA_V_MHU;
SA_RHO=SA_V_MHU/SA_V_T;

*****;

OMEGA_SA=(Q/SA_V_V)+(P/SA_V_1); /* Equation 2.19 */
SA_BETA=INV(Z'*OMEGA_SA*Z)*Z'*OMEGA_SA*Y;
THETA_SA=1-(SQRT(SA_V_V)/SQRT(SA_V_1));
OMEGASA=(Q/SQRT(SA_V_V)+(P/SQRT(SA_V_1));
SA_RES=(OMEGASA*Y)-(OMEGASA*Z*SA_BETA);
VAR_SA=SSQ(SA_RES)/(NT-NCOL(Z));
V_C_SA=INV(Z'*OMEGA_SA*Z);
STD_SA=SQRT(VECDIAG(V_C_SA));
T_SA=SA_BETA/STD_SA;

LOOK1=SA_BETA||STD_SA||T_SA;
CTITLE={'PARAMETER' 'STANDARD ERROR' 'T-STATISTICS'};
RTITLE={'INTERCEPT' 'FIRMV' 'CAPITALV'};
PRINT 'RESULTS OF SWAMY-ARORA',,
LOOK1(|COLNAME=CTITLE ROWNAME=RTITLE FORMAT=8.5|);

FREE OMEGA_SA OMEGASA SA_RES;

*----- NERLOVE ESTIMATOR OF VARIANCE COMPONENTS AND BETA -----*;

MHU=P*LSDV_RES;
MEAN_MHU=MHU[:];
DEV_MHU=MHU-(ONE*MEAN_MHU);
VAR_MHU=SSQ(DEV_MHU)/(T*(N-1));
NL_V_V=SSQ(WT_RES)/NT;
NL_V_1=T*VAR_MHU+NL_V_V;
OMEGA_NL=(Q/NL_V_V)+(P/NL_V_1); /* Equation 2.19 */
NL_BETA=INV(Z'*OMEGA_NL*Z)*Z'*OMEGA_NL*Y;
THETA_NL=1-(SQRT(NL_V_V)/SQRT(NL_V_1));
OMEGANL=(Q/SQRT(NL_V_V)+(P/SQRT(NL_V_1));
NL_RES=(OMEGANL*Y)-(OMEGANL*Z*NL_BETA);
VAR_NL=SSQ(NL_RES)/(NT-NCOL(Z));
V_C_NL=INV(Z'*OMEGA_NL*Z);
STD_NL=SQRT(VECDIAG(V_C_NL));
T_NL=NL_BETA/STD_NL;

NL_V_T=NL_V_V+VAR_MHU;
NL_RHO=VAR_MHU/NL_V_T;

LOOK1=NL_BETA||STD_NL||T_NL;
CTITLE={'PARAMETER' 'STANDARD ERROR' 'T-STATISTICS'};
RTITLE={'INTERCEPT' 'FIRMV' 'CAPITALV'};
PRINT 'RESULTS OF NERLOVE',,
LOOK1(|COLNAME=CTITLE ROWNAME=RTITLE FORMAT=8.5|);

FREE OMEGA_NL OMEGANL NL_RES;

*----- MAXIMUM LIKELIHOOD ESTIMATION -----*;
/* START WITH WITHIN AND BETWEEN BETA SUGGESTED BY BREUSCH(1987) */;

CRITICAL=1;
BETA_W=WT_BETA;
BETA_B=BW_BETA[2:K+1,];
BETA_MLE=WT_BETA;

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*OMEGA_ML=(Q+PHISQ_ML*P)/VAR_V_ML;
*V_C_MLE=INV(X'*OMEGA_ML*X);
*STD_MLE=SQRT(VECDIAG(V_C_MLE));
VAR_1_ML=VAR_V_ML/PHISQ_ML;
OMEGA_ML=(Q/VAR_V_ML)+(P/VAR_1_ML);

ML_BETA=INV(Z'*OMEGA_ML*Z)*Z'*OMEGA_ML*Y;
OMEGAML=(Q/SQRT(VAR_V_ML)+(P/SQRT(VAR_1_ML)));
ML_RES=(OMEGAML*Y)-(OMEGAML*Z*ML_BETA);
VAR_ML=SSQ(ML_RES)/(NT-NCOL(Z));
V_C_ML=INV(Z'*OMEGA_ML*Z);
STD_ML=SQRT(VECDIAG(V_C_ML));
T_ML=ML_BETA/STD_ML;

LOOK1=ML_BETA||STD_ML||T_ML;
CTITLE=('PARAMETER' 'STANDARD ERROR' 'T-STATISTICS');
RTITLE=('INTERCEPT' 'FIRMV' 'CAPITALV');
PRINT 'RESULTS OF MAXIMUM LIKELIHOOD',,
LOOK1(|COLNAME=CTITLE ROWNAME=RTITLE FORMAT=8.5|);

FREE OMEGA_ML;

*----- PRINT AND OUTPUT INFORMATION -----*

BETA=OLS_BETA'[,2:K+1]//BW_BETA'[,2:K+1]//WT_BETA'//
WH_BETA'[,2:K+1]//AM_BETA'[,2:K+1]//
SA_BETA'[,2:K+1]//NL_BETA'[,2:K+1]//ML_BETA'[,2:K+1];

STD_ERR=STD_OLS'[,2:K+1]//STD_BW'[,2:K+1]//STD_WT'//
STD_WH'[,2:K+1]//STD_AM'[,2:K+1]//STD_SA'[,2:K+1]//
STD_NL'[,2:K+1]//STD_ML'[,2:K+1];

THETAS={0, ., 1}//THETA_WH//THETA_AM//THETA_SA//THETA_NL//THETA_ML;

NEGA_VAR={.,.,.}//NEGA_WH//NEGA_AM//NEGA_SA//{.,.};

OUTPUT=BETA||STD_ERR||THETAS||NAGA_VAR;

DO WHILE (CRITICAL>0.0001);
WT_RES=Y-X*BETA_W;
BW_RES=Y-X*BETA_B;
PHISQ_W=(WT_RES'*Q*WT_RES)/((T-1)*(WT_RES'*(P-JNT_BAR)*WT_RES));
/* Equation 2.35 */
PHISQ_B=(BW_RES'*Q*BW_RES)/((T-1)*(BW_RES'*(P-JNT_BAR)*BW_RES));
/* Equation 2.35 */
CRITICAL=PHISQ_W-PHISQ_B;
BETA_W=INV(X'*(Q+PHISQ_W*(P-JNT_BAR))*X)*X'*(Q+PHISQ_W*(P-JNT_BAR))*Y;
/* Equation 2.36 */
BETA_B=INV(X'*(Q+PHISQ_B*(P-JNT_BAR))*X)*X'*(Q+PHISQ_B*(P-JNT_BAR))*Y;
/* Equation 2.36 */
BETA_MLE=(BETA_W+BETA_B)/2;
END;
D_MLE=Y-X*BETA_MLE;
PHISQ_ML=(D_MLE'*Q*D_MLE)/((T-1)*D_MLE'*(P-JNT_BAR)*D_MLE);
/* Equation 2.35 */
THETA_ML=1-SQRT(PHISQ_ML);
VAR_V_ML=D_MLE'*(Q+PHISQ_ML*(P-JNT_BAR))*D_MLE/NT;

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```

C1={"BETA1" "BETA2" "STD_BETA1" "STD_BETA2" "THETA"};
C2={"BETA1" "BETA2" "BETA3" "STD_BETA1" "STD_BETA2"
    "STD_BETA3" "THETA"};

R={"OLS ESTIMATOR" "BETWEEN ESTIMATOR" "WITHIN ESTIMATOR"
  "WALLACE & HUSSAIN ESTIMATOR" "AMEMIYA ESTIMATOR"
  "SWAMY & ARORA ESTIMATOR" "NERLOVE ESTIMATOR" "IMLE"};

PRINT 'ONE-WAY ERROR COMPONENT MODEL WITH GRUNFELD DATA:
      BETA, VARIANCES OF BETA, AND THETA'
      ,,OUTPUT (|ROWNAME=R COLNAME=C1 FORMAT=8.5|);

PRINT 'NEGATIVE VAR_MHU', ,NEGA_VAR (|ROWNAME=R|);
WH_VAR=WH_V_V|WH_V_MHU|WH_V_1|WH_V_T|WH_RHO;
AM_VAR=AM_V_V|AM_V_MHU|AM_V_1|AM_V_T|AM_RHO;
SA_VAR=SA_V_V|SA_V_MHU|SA_V_1|SA_V_T|SA_RHO;
NL_VAR=NL_V_V|VAR_MHU|NL_V_1|NL_V_T|NL_RHO;

OUTPUT=WH_VAR//AM_VAR//SA_VAR//NL_VAR;

R={'WALLACE & HUSSAIN ESTIMATOR' 'AMEMIYA ESTIMATOR'
  'SWAMY & ARORA ESTIMATOR' 'NERLOVE ESTIMATOR'};

C1={"SIGMA-NU-SQ" "SIGMA-MU-SQ" "SIGMA-1-SQ" "SIGMA-SQ" "RHO"};

PRINT 'ONE-WAY VARIANCE COMPONENTS FOR GRUNFELD DATA'
      ,,OUTPUT (|ROWNAME=R COLNAME=C1 FORMAT=12.3|);
/*

```

SAS Output for Grunfield Data

RESULTS OF OLS

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	-42.7144	9.51168	-4.49073
	FIRMV	0.11556	0.00584	19.80259
	CAPITALV	0.23068	0.02548	9.05481

RESULTS OF BETWEEN

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	-8.52711	47.51531	-0.17946
	FIRMV	0.13465	0.02875	4.68408
	CAPITALV	0.03203	0.19094	0.16776

RESULTS OF WITHIN

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	FIRMV	0.11012	0.01186	9.28790
	CAPITALV	0.31007	0.01735	17.86656

RESULTS OF WALLACE-HUSSAIN

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	-57.5539	26.45011	-2.17594
	FIRMV	0.10971	0.01063	10.32157
	CAPITALV	0.30737	0.01803	17.04600

RESULTS OF AMEMIYA

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	-57.7711	27.75255	-2.08165
	FIRMV	0.10976	0.01034	10.61206
	CAPITALV	0.30795	0.01707	18.03867

RESULTS OF SWAMY-ARORA

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	-57.8344	28.88930	-2.00193
	FIRMV	0.10978	0.01049	10.46615
	CAPITALV	0.30811	0.01717	17.93989

RESULTS OF NERLOVE

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	-57.9074	29.24211	-1.98027
	FIRMV	0.10980	0.01027	10.68948
	CAPITALV	0.30829	0.01667	18.49906

RESULTS OF MAXIMUM LIKELIHOOD

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	-57.7632	27.64352	-2.08957
	FIRMV	0.10976	0.01033	10.62083
	CAPITALV	0.30793	0.01707	18.03485

**ONE-WAY ERROR COMPONENT MODEL WITH GRUNFELD DATA:
BETA, VARIANCES OF BETA, AND THETA**

OUTPUT	BETA1	BETA2	STD_BETA1	STD_BETA2	THETA
OLS ESTIMATOR	0.11556	0.23068	0.00584	0.02548	0.00000
BETWEEN ESTIMATOR	0.13465	0.03203	0.02875	0.19094	.
WITHIN ESTIMATOR	0.11012	0.31007	0.01186	0.01735	1.00000
WALLACE & HUSSAIN ESTIMATOR	0.10971	0.30737	0.01063	0.01803	0.83744
AMEMIYA ESTIMATOR	0.10976	0.30795	0.01034	0.01707	0.85569
SWAMY & ARORA ESTIMATOR	0.10978	0.30811	0.01049	0.01717	0.86122
NERLOVE ESTIMATOR	0.10980	0.30829	0.01027	0.01667	0.86774
IMLE	0.10976	0.30793	0.01033	0.01707	0.85501

NEGATIVE VAR_MHU

NEGA_VAR

```

OLS ESTIMATOR          .
BETWEEN ESTIMATOR      .
WITHIN ESTIMATOR       .
WALLACE & HUSSAIN ESTIMATOR  0
AMEMIYA ESTIMATOR      0
SWAMY & ARORA ESTIMATOR  0
NERLOVE ESTIMATOR     .
IMLE                   .

```

ONE-WAY VARIANCE COMPONENTS FOR GRUNFELD DATA

```

OUTPUT          SIGMA-NU-SQ  SIGMA-MU-SQ  SIGMA-1-SQ  SIGMA-SQ  RHO
WALLACE & HUSSAIN ESTIMATOR  3089.071    5690.182    116892.705    8779.252    0.648
AMEMIYA ESTIMATOR  2755.148    6477.298    132301.113    9232.446    0.702
SWAMY & ARORA ESTIMATOR  2784.458    7089.800    144580.460    9874.258    0.718
NERLOVE ESTIMATOR  2617.391    7350.062    149618.628    9967.453    0.737
*****

```

The following output was produced using EViews 5.0. This should replicate Table 2.1 and differs from the above SAS output in that degrees of freedom adjustments are made when estimating the variance components.

For Pooled OLS:

Dependent Variable: I
Method: Panel Least Squares

Sample: 1935 1954
Cross-sections included: 10
Total panel (balanced) observations: 200

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	-42.71437	9.511676	-4.490730	0.0000
F	0.115562	0.005836	19.80259	0.0000
K	0.230678	0.025476	9.054808	0.0000
R-squared	0.812408	Mean dependent var		145.9582
Adjusted R-squared	0.810504	S.D. dependent var		216.8753
S.E. of regression	94.40840	Akaike info criterion		11.94802
Sum squared resid	1755850.	Schwarz criterion		11.99750
Log likelihood	-1191.802	F-statistic		426.5757
Durbin-Watson stat	0.219599	Prob(F-statistic)		0.000000

For the one-way fixed effects estimator with firm effects:

Dependent Variable: I
Method: Panel Least Squares

Sample: 1935 1954
Cross-sections included: 10
Total panel (balanced) observations: 200

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	-58.74394	12.45369	-4.716990	0.0000
F	0.110124	0.011857	9.287901	0.0000
K	0.310065	0.017355	17.86656	0.0000

Effects Specification

Cross-section fixed (dummy variables)

R-squared	0.944073	Mean dependent var	145.9582
Adjusted R-squared	0.940800	S.D. dependent var	216.8753
S.E. of regression	52.76797	Akaike info criterion	10.82781
Sum squared resid	523478.1	Schwarz criterion	11.02571
Log likelihood	-1070.781	F-statistic	288.4996
Durbin-Watson stat	0.716733	Prob(F-statistic)	0.000000

For the Wallace and Hussain random effects estimator reported in Table 2.2, we get:

Dependent Variable: I
Method: Panel EGLS (Cross-section random effects)

Sample: 1935 1954
Cross-sections included: 10
Total panel (balanced) observations: 200
Wallace and Hussain estimator of component variances

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	-57.86253	29.90492	-1.934883	0.0544
F	0.109789	0.010725	10.23698	0.0000
K	0.308183	0.017498	17.61207	0.0000

Effects Specification

Cross-section random S.D. / Rho	87.35803	0.7254
Idiosyncratic random S.D. / Rho	53.74518	0.2746

Weighted Statistics

R-squared	0.769410	Mean dependent var	19.89203
Adjusted R-squared	0.767069	S.D. dependent var	109.2808
S.E. of regression	52.74214	Sum squared resid	548001.4
F-statistic	328.6646	Durbin-Watson stat	0.683829
Prob(F-statistic)	0.000000		

Unweighted Statistics

R-squared	0.803285	Mean dependent var	145.9582
Sum squared resid	1841243.	Durbin-Watson stat	0.203525

For the Amemiya random effects estimator (which EViews names the Wansbeek-Kapteyn estimator) reported in Table 2.3, we get:

Dependent Variable: I

Method: Panel EGLS (Cross-section random effects)

Sample: 1935 1954

Cross-sections included: 10

Total panel (balanced) observations: 200

Wansbeek and Kapteyn estimator of component variances

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	-57.82187	28.68562	-2.015710	0.0452
F	0.109778	0.010471	10.48387	0.0000
K	0.308081	0.017172	17.94062	0.0000

Effects Specification

Cross-section random S.D. / Rho	83.52354	0.7147
Idiosyncratic random S.D. / Rho	52.76797	0.2853

Weighted Statistics

R-squared	0.769544	Mean dependent var	20.41664
Adjusted R-squared	0.767205	S.D. dependent var	109.4431
S.E. of regression	52.80503	Sum squared resid	549309.2
F-statistic	328.9141	Durbin-Watson stat	0.682171
Prob(F-statistic)	0.000000		

Unweighted Statistics

R-squared	0.803313	Mean dependent var	145.9582
Sum squared resid	1840981.	Durbin-Watson stat	0.203545

For the Swamy and Arora random effects estimator reported in Table 2.4, we get:

Dependent Variable: I
Method: Panel EGLS (Cross-section random effects)

Sample: 1935 1954
Cross-sections included: 10
Total panel (balanced) observations: 200
Swamy and Arora estimator of component variances

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	-57.83441	28.88930	-2.001932	0.0467
F	0.109781	0.010489	10.46615	0.0000
K	0.308113	0.017175	17.93989	0.0000

Effects Specification

Cross-section random S.D. / Rho	84.20095	0.7180
Idiosyncratic random S.D. / Rho	52.76797	0.2820

Weighted Statistics

R-squared	0.769503	Mean dependent var	20.25556
Adjusted R-squared	0.767163	S.D. dependent var	109.3928
S.E. of regression	52.78556	Sum squared resid	548904.1
F-statistic	328.8369	Durbin-Watson stat	0.682684
Prob(F-statistic)	0.000000		

Unweighted Statistics

R-squared	0.803304	Mean dependent var	145.9582
Sum squared resid	1841062.	Durbin-Watson stat	0.203539

Now we reproduce some of these estimates for the Grunfeld data set using Stata

```
. infile fn yr I F C using a:/grunfeld.fil
'FN' cannot be read as a number for fn[1]
'YR' cannot be read as a number for yr[1]
'I' cannot be read as a number for I[1]
'F' cannot be read as a number for F[1]
'C' cannot be read as a number for C[1]
(201 observations read)
. list
```

	fn	yr	I	F	C
1.
2.	1	1935	317.6	3078.5	2.8
3.	1	1936	391.8	4661.7	52.6
4.	1	1937	410.6	5387.1	156.9
5.	1	1938	257.7	2792.2	209.2
6.	1	1939	330.8	4313.2	203.4
7.	1	1940	461.2	4643.9	207.2
8.	1	1941	512	4551.2	255.2
9.	1	1942	448	3244.1	303.7


```
. edit
- preserve
- drop in 1
- preserve
. sum
```

Variable	Obs	Mean	Std. Dev.	Min	Max
fn	200	5.5	2.879489	1	10
yr	200	1944.5	5.780751	1935	1954
I	200	145.9583	216.8753	.93	1486.7
F	200	1081.681	1314.47	58.12	6241.7
C	200	276.0172	301.1039	.8	2226.3

```
. reg I F C
```

Source	SS	df	MS	Number of obs =	200
Model	7604093.48	2	3802046.74	F(2, 197) =	426.58
Residual	1755850.43	197	8912.94636	Prob > F =	0.0000
Total	9359943.92	199	47034.8941	R-squared =	0.8124
				Adj R-squared =	0.8105
				Root MSE =	94.408

I	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
F	.1155622	.0058357	19.80	0.000	.1040537 .1270706
C	.2306785	.0254758	9.05	0.000	.1804382 .2809188
_cons	-42.71437	9.511676	-4.49	0.000	-61.47215 -23.95659

```
. lls fn
```

```
. xtreg I F C, re
```

```
Random-effects GLS regression                Number of obs   =    200
Group variable (i) : fn                     Number of groups =    10

R-sq:  within = 0.7668                      Obs per group:  min =    20
        between = 0.8196                      avg   =    20.0
        overall = 0.8061                      max   =    20
```

```
Random effects u_i ~ Gaussian                Wald chi2(2)    =    657.67
corr(u_i, X) = 0 (assumed)                  Prob > chi2     =    0.0000
```

I	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
F	.1097811	.0104927	10.46	0.000	.0892159 .1303464
C	.308113	.0171805	17.93	0.000	.2744399 .3417861
_cons	-57.83441	28.89893	-2.00	0.045	-114.4753 -1.193537
sigma_u	84.20095				
sigma_e	52.767964				
rho	.71800838	(fraction of variance due to u_i)			

```
. xtreg I F C, fe
```

```
Fixed-effects (within) regression           Number of obs   =    200
Group variable (i) : fn                     Number of groups =    10

R-sq:  within = 0.7668                      Obs per group:  min =    20
        between = 0.8194                      avg   =    20.0
        overall = 0.8060                      max   =    20
```

```

corr(u_i, Xb) = -0.1517
F(2,188) = 309.01
Prob > F = 0.0000

```

```

-----+-----
      I |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-----+-----
      F |   .1101238   .0118567     9.29   0.000   .0867345   .1335131
      C |   .3100653   .0173545    17.87   0.000   .2758308   .3442999
  _cons |  -58.74393  12.45369    -4.72   0.000  -83.31086  -34.177
-----+-----
sigma_u |  85.732501
sigma_e |  52.767964
rho     |   .72525012   (fraction of variance due to u_i)
-----+-----

```

```

F test that all u_i=0:      F(9, 188) = 49.18      Prob > F = 0.0000

```

```
. xtreg I F C, be
```

```

Between regression (regression on group means) Number of obs = 200
Group variable (i) : fn                          Number of groups = 10

```

```

R-sq:  within = 0.4778      Obs per group: min = 20
        between = 0.8578      avg = 20.0
        overall = 0.7551     max = 20

```

```

sd(u_i + avg(e_i.))= 85.02366
F(2,7) = 21.11
Prob > F = 0.0011

```

```

-----+-----
      I |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-----+-----
      F |   .1346461   .0287455     4.68   0.002   .0666739   .2026183
      C |   .0320315   .1909378     0.17   0.872  -0.4194647 .4835276
  _cons |  -8.527114  47.51531    -0.18   0.863  -120.883  103.8287
-----+-----

```

```
. xtreg I F C, i(fn) re
```

```

Random-effects GLS regression      Number of obs = 200
Group variable (i) : fn            Number of groups = 10

```

```

R-sq:  within = 0.7668      Obs per group: min = 20
        between = 0.8196      avg = 20.0
        overall = 0.8061     max = 20

```

```

Random effects u_i ~ Gaussian      Wald chi2(2) = 657.67
corr(u_i, X) = 0 (assumed)        Prob > chi2 = 0.0000

```

```

-----+-----
      I |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-----+-----
      F |   .1097811   .0104927    10.46   0.000   .0892159   .1303464
      C |   .308113    .0171805    17.93   0.000   .2744399   .3417861
  _cons |  -57.83441  28.89893    -2.00   0.045  -114.4753  -1.193537
-----+-----
sigma_u |  84.20095
sigma_e |  52.767964
rho     |   .71800838   (fraction of variance due to u_i)
-----+-----

```

```

. xtreg I F C, mle

Fitting constant-only model:
Iteration 0:   log likelihood = -1387.6302
Iteration 1:   log likelihood = -1291.9897
Iteration 2:   log likelihood = -1254.2888
Iteration 3:   log likelihood = -1243.6309
Iteration 4:   log likelihood = -1242.0548
Iteration 5:   log likelihood = -1241.9709
Iteration 6:   log likelihood = -1241.9696
Iteration 7:   log likelihood = -1241.9696

Fitting full model:
Iteration 0:   log likelihood = -1105.6101
Iteration 1:   log likelihood = -1098.8418
Iteration 2:   log likelihood = -1095.4188
Iteration 3:   log likelihood = -1095.2576
Iteration 4:   log likelihood = -1095.257

Random-effects ML regression              Number of obs   =       200
Group variable (i) : fn                  Number of groups =        10

Random effects u_i ~ Gaussian              Obs per group: min =        20
                                           avg =       20.0
                                           max =        20

Log likelihood = -1095.257                LR chi2(2)      =       293.43
                                           Prob > chi2     =        0.0000

-----+-----
      I |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-----+-----
      F |   .1097626   .0103389    10.62  0.000   .0894988   .1300265
      C |   .307942   .0171006    18.01  0.000   .2744254   .3414585
    _cons |  -57.7672   27.70004    -2.09  0.037  -112.0583  -3.476114
-----+-----
  /sigma_u |  80.29729   18.37811     4.37  0.000   44.27685   116.3177
  /sigma_e |  52.49255    2.69306    19.49  0.000   47.21424   57.77085
-----+-----
      rho |   .7005943   .0985226
-----+-----
Likelihood ratio test of sigma_u=0:  chibar2(01) = 193.09  Prob>=chibar2 = 0.0000
-----+-----

```

- 2.12 This program gives the SAS output for estimating “One-way Error Component Regression” for Gasoline. Estimators are OLS, WITHIN, BETWEEN, WALHUS, AMEMIYA, SWAR, NERLOVE, and IMLE. The results do not replicate exactly those in Table 2.5 because there is no correction for degrees of freedom in these programs. However, the output reported below using EViews should match the results in Table 2.5.

SAS Output for Gasoline Data

RESULTS OF OLS			
LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS
INTERCEPT	2.39133	0.11693	20.45017
INCOME	0.88996	0.03581	24.85523
PRICE	-0.89180	0.03031	-29.4180
CAR	-0.76337	0.01861	-41.0232

RESULTS OF BETWEEN

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	2.54163	0.52678	4.82480
	INCOME	0.96758	0.15567	6.21571
	PRICE	-0.96355	0.13292	-7.24902
	CAR	-0.79530	0.08247	-9.64300

RESULTS OF WITHIN

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INCOME	0.66225	0.07339	9.02419
	PRICE	-0.32170	0.04410	-7.29496
	CAR	-0.64048	0.02968	-21.5804

RESULTS OF WALLACE-HUSSAIN

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	1.90580	0.19403	9.82195
	INCOME	0.54346	0.06353	8.55377
	PRICE	-0.47111	0.04550	-10.3546
	CAR	-0.60613	0.02840	-21.3425

RESULTS OF AMEMIYA

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	2.18445	0.21453	10.18228
	INCOME	0.60093	0.06542	9.18559
	PRICE	-0.36639	0.04138	-8.85497
	CAR	-0.62039	0.02718	-22.8227

RESULTS OF SWAMY-ARORA

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	1.99670	0.17824	11.20260
	INCOME	0.55499	0.05717	9.70689
	PRICE	-0.42039	0.03866	-10.8748
	CAR	-0.60684	0.02467	-24.5964

RESULTS OF NERLOVE

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	2.20177	0.21252	10.36040
	INCOME	0.60561	0.06432	9.41526
	PRICE	-0.36243	0.04049	-8.95152
	CAR	-0.62189	0.02666	-23.3289

RESULTS OF MAXIMUM LIKELIHOOD

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	2.10623	0.20096	10.48088
	INCOME	0.58044	0.06286	9.23388
	PRICE	-0.38582	0.04072	-9.47515
	CAR	-0.61401	0.02647	-23.2001

ONE-WAY ERROR COMPONENT MODEL WITH GASOLINE DATA:
BETA, VARIANCES OF BETA, AND THETA

OUTPUT	INCOME	PRICE	CAR	STD_INC	STD_PRICE	STD_CAR	THETA
OLS ESTIMATOR	0.88996	-0.89180	-0.76337	0.03581	0.03031	0.01861	0.00000
BETWEEN ESTIMATOR	0.96758	-0.96355	-0.79530	0.15567	0.13292	0.08247	.
WITHIN ESTIMATOR	0.66225	-0.32170	-0.64048	0.07339	0.04410	0.02968	1.00000
WALLACE & HUSSAIN ESTIMATOR	0.54346	-0.47111	-0.60613	0.06353	0.04550	0.02840	0.84802
AMEMIYA ESTIMATOR	0.60093	-0.36639	-0.62039	0.06542	0.04138	0.02718	0.93773
SWAMY & ARORA ESTIMATOR	0.55499	-0.42039	-0.60684	0.05717	0.03866	0.02467	0.89231
NERLOVE ESTIMATOR	0.60561	-0.36243	-0.62189	0.06432	0.04049	0.02666	0.94120
IMLE	0.58044	-0.38582	-0.61401	0.06286	0.04072	0.02647	0.92126

NEGATIVE VAR_MHU

NEGA_VAR	COL1
OLS ESTIMATOR	.
BETWEEN ESTIMATOR	.
WITHIN ESTIMATOR	.
WALLACE & HUSSAIN ESTIMATOR	0
AMEMIYA ESTIMATOR	0
SWAMY & ARORA ESTIMATOR	0
NERLOVE ESTIMATOR	.
IMLE	.

ONE-WAY VARIANCE COMPONENTS FOR GASOLINE DATA

OUTPUT	SIGMA-NU-SQ	SIGMA-MU-SQ	SIGMA-1-SQ	SIGMA-SQ	RHO
WALLACE & HUSSAIN ESTIMATOR	0.01351	0.03007	0.58487	0.04358	0.69003
AMEMIYA ESTIMATOR	0.00845	0.11420	2.17830	0.12265	0.93114
SWAMY & ARORA ESTIMATOR	0.00852	0.03824	0.73504	0.04676	0.81770
NERLOVE ESTIMATOR	0.00800	0.12139	2.31444	0.12939	0.93816

The following output was produced using EViews 5.0. This should replicate Table 2.5 and differs from the above SAS output in that degrees of freedom adjustments are made when estimating the variance components.

For Pooled OLS:

Dependent Variable: GAS
Method: Panel Least Squares

Sample: 1960 1978
Cross-sections included: 18
Total panel (balanced) observations: 342

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	2.391326	0.116934	20.45017	0.0000
INC	0.889962	0.035806	24.85523	0.0000
PMG	-0.891798	0.030315	-29.41796	0.0000
CAR	-0.763373	0.018608	-41.02325	0.0000
R-squared	0.854935	Mean dependent var	4.296242	
Adjusted R-squared	0.853648	S.D. dependent var	0.548907	
S.E. of regression	0.209990	Akaike info criterion	-0.271888	
Sum squared resid	14.90436	Schwarz criterion	-0.227037	
Log likelihood	50.49289	F-statistic	663.9993	
Durbin-Watson stat	0.137461	Prob(F-statistic)	0.000000	

For the **one-way fixed effects estimator** with country effects:

Dependent Variable: GAS
Method: Panel Least Squares

Sample: 1960 1978
Cross-sections included: 18
Total panel (balanced) observations: 342

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	2.402670	0.225309	10.66387	0.0000
INC	0.662250	0.073386	9.024191	0.0000
PMG	-0.321702	0.044099	-7.294964	0.0000
CAR	-0.640483	0.029679	-21.58045	0.0000

Effects Specification

Cross-section fixed (dummy variables)

R-squared	0.973366	Mean dependent var	4.296242
Adjusted R-squared	0.971706	S.D. dependent var	0.548907
S.E. of regression	0.092330	Akaike info criterion	-1.867450
Sum squared resid	2.736491	Schwarz criterion	-1.631979
Log likelihood	340.3340	F-statistic	586.5556
Durbin-Watson stat	0.326578	Prob(F-statistic)	0.000000

For the **Wallace and Hussain random effects estimator**, we get:

Dependent Variable: GAS
Method: Panel EGLS (Cross-section random effects)

Sample: 1960 1978
Cross-sections included: 18
Total panel (balanced) observations: 342
Wallace and Hussain estimator of component variances

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	1.938318	0.201817	9.604333	0.0000
INC	0.545202	0.065555	8.316682	0.0000
PMG	-0.447490	0.045763	-9.778438	0.0000
CAR	-0.605086	0.028838	-20.98191	0.0000
Effects Specification				
Cross-section random S.D. / Rho			0.196715	0.7508
Idiosyncratic random S.D. / Rho			0.113320	0.2492
Weighted Statistics				
R-squared	0.826568	Mean dependent var	0.562884	
Adjusted R-squared	0.825029	S.D. dependent var	0.233119	
S.E. of regression	0.097513	Sum squared resid	3.213953	
F-statistic	536.9632	Durbin-Watson stat	0.299781	
Prob(F-statistic)	0.000000			
Unweighted Statistics				
R-squared	0.750484	Mean dependent var	4.296242	
Sum squared resid	25.63603	Durbin-Watson stat	0.037583	

For the **Amemiya random effects estimator** (which EViews names the Wansbeek-Kapteyn estimator), we get:

Dependent Variable: GAS

Method: Panel EGLS (Cross-section random effects)

Sample: 1960 1978

Cross-sections included: 18

Total panel (balanced) observations: 342

Wansbeek and Kapteyn estimator of component variances

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	2.188322	0.216372	10.11372	0.0000
INC	0.601969	0.065876	9.137941	0.0000
PMG	-0.365500	0.041620	-8.781832	0.0000
CAR	-0.620725	0.027356	-22.69053	0.0000
Effects Specification				
Cross-section random S.D. / Rho			0.343826	0.9327
Idiosyncratic random S.D. / Rho			0.092330	0.0673

Weighted Statistics

R-squared	0.835065	Mean dependent var	0.264177
Adjusted R-squared	0.833602	S.D. dependent var	0.225791
S.E. of regression	0.092104	Sum squared resid	2.867329
F-statistic	570.4327	Durbin-Watson stat	0.315210
Prob(F-statistic)	0.000000		

Unweighted Statistics

R-squared	0.670228	Mean dependent var	4.296242
Sum squared resid	33.88179	Durbin-Watson stat	0.026675

For the Swamy and Arora random effects estimator, we get:

Dependent Variable: GAS

Method: Panel EGLS (Cross-section random effects)

Sample: 1960 1978

Cross-sections included: 18

Total panel (balanced) observations: 342

Swamy and Arora estimator of component variances

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	1.996698	0.178235	11.20260	0.0000
INC	0.554986	0.057174	9.706890	0.0000
PMG	-0.420389	0.038657	-10.87482	0.0000
CAR	-0.606840	0.024672	-24.59636	0.0000

Effects Specification

Cross-section random S.D. / Rho	0.195545	0.8177
Idiosyncratic random S.D. / Rho	0.092330	0.1823

Weighted Statistics

R-squared	0.829310	Mean dependent var	0.462676
Adjusted R-squared	0.827795	S.D. dependent var	0.230099
S.E. of regression	0.095485	Sum squared resid	3.081707
F-statistic	547.3996	Durbin-Watson stat	0.304481
Prob(F-statistic)	0.000000		

Unweighted Statistics

R-squared	0.730918	Mean dependent var	4.296242
Sum squared resid	27.64625	Durbin-Watson stat	0.033940

Now we reproduce some of these estimates for the Gasoline data set using Stata

```

infile str8 co year c y p car using a:\gasoline.dat
'YR' cannot be read as a number for year[1]
'LN(Gas/Car)' cannot be read as a number for c[1]
'LN(Y/N)' cannot be read as a number for y[1]
'LN(Pmg/Pgdp)' cannot be read as a number for p[1]
'LN(Car/N)' cannot be read as a number for car[1]
(343 observations read)

. sum

      Variable |      Obs      Mean   Std. Dev.      Min      Max
-----+-----
           co |         0
        year |       342       1969   5.485251     1960     1978
            c |       342   4.296242   .5489071    3.380209    6.156644
            y |       342  -6.139425   .6345925   -8.072523   -5.221232
            p |       342  -5.231032   .6782225   -2.896497    1.125311
           car |       342  -9.041805   1.218896  -13.47518  -7.536176

. edit
- preserve
- drop in 1
- preserve

. sum

      Variable |      Obs      Mean   Std. Dev.      Min      Max
-----+-----
           co |         0
        year |       342       1969   5.485251     1960     1978
            c |       342   4.296242   .5489071    3.380209    6.156644
            y |       342  -6.139425   .6345925   -8.072523   -5.221232
            p |       342  -5.231032   .6782225   -2.896497    1.125311
           car |       342  -9.041805   1.218896  -13.47518  -7.536176

. gen coun=int(($_n-1)/19)+1

. edit
- preserve
. reg c y p car

      Source |      SS      df      MS                Number of obs =      342
-----+-----+-----+-----+-----+-----
      Model |  87.8386024      3  29.2795341          F( 3, 338) = 664.00
      Residual |  14.9043581    338   .044095734          Prob > F      = 0.0000
-----+-----+-----+-----+-----+-----
      Total |  102.742961    341   .301299005          R-squared      = 0.8549
                                          Adj R-squared  = 0.8536
                                          Root MSE      = .20999

-----+-----+-----+-----+-----+-----
           c |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-----+-----+-----+-----+-----+-----
           y |   .8899616   .0358058    24.86   0.000     .8195313   .9603919
           p |  -0.8917979   .0303147   -29.42   0.000    -0.9514272 -0.8321685
           car | -0.7633727   .0186083   -41.02   0.000    -0.7999754 -0.7267701
       _cons |   2.391326   .1169343    20.45   0.000     2.161315   2.621336
-----+-----+-----+-----+-----+-----

```

```
. iis coun

. xtreg c y p car, re theta

Random-effects GLS regression                Number of obs    =    342
Group variable (i) : coun                   Number of groups =    18

R-sq:  within = 0.8363                     Obs per group:  min =    19
                                     between = 0.7099                               avg =    19.0
                                     overall  = 0.7309                               max =    19

Random effects u_i ~ Gaussian              Wald chi2(3)     =   1642.20
corr(u_i, X) = 0 (assumed)                Prob > chi2      =    0.0000
theta = .89230675
```

c	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
y	.5549858	.0591282	9.39	0.000	.4390967	.6708749
p	-.4203893	.0399781	-10.52	0.000	-.498745	-.3420336
car	-.6068402	.025515	-23.78	0.000	-.6568487	-.5568316
_cons	1.996699	.184326	10.83	0.000	1.635427	2.357971
sigma_u	.19554468					
sigma_e	.09233034					
rho	.81769856	(fraction of variance due to u_i)				

```
. xtreg c y p car , fe

Fixed-effects (within) regression          Number of obs    =    342
Group variable (i) : coun                 Number of groups =    18

R-sq:  within = 0.8396                     Obs per group:  min =    19
                                     between = 0.5755                               avg =    19.0
                                     overall  = 0.6150                               max =    19

corr(u_i, Xb) = -0.2468                    F(3,321)        =    560.09
                                     Prob > F        =    0.0000
```

c	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
y	.6622498	.073386	9.02	0.000	.5178715	.8066282
p	-.3217025	.0440992	-7.29	0.000	-.4084626	-.2349425
car	-.6404829	.0296788	-21.58	0.000	-.6988725	-.5820933
_cons	2.40267	.2253094	10.66	0.000	1.959401	2.84594
sigma_u	.34841289					
sigma_e	.09233034					
rho	.93438173	(fraction of variance due to u_i)				

```
F test that all u_i=0:    F(17, 321) =    83.96          Prob > F = 0.0000
```

```
. xtreg c y p car, be

Between regression (regression on group means) Number of obs    =    342
Group variable (i) : coun                   Number of groups =    18
```

```
R-sq: within = 0.7337
      between = 0.8799
      overall = 0.8529
```

```
Obs per group: min = 19
                  avg = 19.0
                  max = 19
```

```
F(3,14) = 34.19
```

```
sd(u_i + avg(e_i.)) = .1966886
Prob > F = 0.0000
```

c	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
y	.9675763	.1556662	6.22	0.000	.6337055 1.301447
p	-.9635503	.1329214	-7.25	0.000	-1.248638 -.6784622
car	-.795299	.0824742	-9.64	0.000	-.9721887 -.6184094
_cons	2.54163	.5267845	4.82	0.000	1.411789 3.67147

```
. xtreg c y p car, mle
```

```
Fitting constant-only model:
```

```
Iteration 0: log likelihood = -298.79473
Iteration 1: log likelihood = -120.7272
Iteration 2: log likelihood = -48.602465
Iteration 3: log likelihood = -26.799172
Iteration 4: log likelihood = -22.837386
Iteration 5: log likelihood = -22.420508
Iteration 6: log likelihood = -22.396956
Iteration 7: log likelihood = -22.396801
```

```
Fitting full model:
```

```
Iteration 0: log likelihood = 216.74308
Iteration 1: log likelihood = 230.51837
Iteration 2: log likelihood = 273.0581
Iteration 3: log likelihood = 281.79287
Iteration 4: log likelihood = 282.47033
Iteration 5: log likelihood = 282.47697
Iteration 6: log likelihood = 282.47697
```

```
Random-effects ML regression
Group variable (i) : coun
Number of obs = 342
Number of groups = 18
```

```
Random effects u_i ~ Gaussian
Obs per group: min = 19
                  avg = 19.0
                  max = 19
```

```
Log likelihood = 282.47697
LR chi2(3) = 609.75
Prob > chi2 = 0.0000
```

c	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
y	.5881334	.0659581	8.92	0.000	.4588578 .717409
p	-.3780466	.0440663	-8.58	0.000	-.464415 -.2916782
car	-.6163722	.0272054	-22.66	0.000	-.6696938 -.5630506
_cons	2.136168	.2156039	9.91	0.000	1.713593 2.558744
/sigma_u	.2922939	.0545496	5.36	0.000	.1853786 .3992092
/sigma_e	.0922537	.0036482	25.29	0.000	.0851033 .099404
rho	.9094086	.0317608			.8303747 .9571561

```
Likelihood ratio test of sigma_u=0: chibar2(01) = 463.97 Prob>=chibar2 = 0.000
```

- 2.14 (a) This solution is based on Baltagi and Krämer (1994). From (2.3), one gets $\hat{\delta}_{OLS} = (Z'Z)^{-1}Z'y$ and $\hat{u}_{OLS} = y - Z\hat{\delta}_{OLS} = \bar{P}_Z u$ where $\bar{P}_Z = I_{NT} - P_Z$ with $P_Z = Z(Z'Z)^{-1}Z'$.

Also, $E(s^2) = E[\hat{u}'\hat{u}/(NT - K')] = E[u'P_Z u/(NT - K')] = \text{tr}(\Omega \bar{P}_Z)/(NT - K')$ which from (2.17) reduces to

$$E(s^2) = \sigma_v^2 + \sigma_\mu^2(NT - \text{tr}(I_N \otimes J_T)P_Z)/(NT - K')$$

since $\text{tr}(I_{NT}) = \text{tr}(I_N \otimes J_T) = NT$ and $\text{tr}(P_Z) = K'$. By adding and subtracting σ_μ^2 , one gets

$$E(s^2) = \sigma^2 + \sigma_\mu^2[K' - \text{tr}(I_N \otimes J_T)P_Z]/(NT - K')$$

where $\sigma^2 = E(u_{it}^2) = \sigma_\mu^2 + \sigma_v^2$ for all i and t .

(b) Nerlove (1971) derived the characteristic roots and vectors of Ω given in (2.17). These characteristic roots turn out to be σ_v^2 with multiplicity $N(T - 1)$ and $(T\sigma_\mu^2 + \sigma_v^2)$ with multiplicity N . Therefore, the smallest $(n - K')$ characteristic roots are made up of the $(n - N)\sigma_v^2$'s and $(N - K')$ of the $(T\sigma_\mu^2 + \sigma_v^2)$'s. This implies that the mean of the $(n - K')$ smallest characteristic roots of $\Omega = [(n - N)\sigma_v^2 + (N - K')(T\sigma_\mu^2 + \sigma_v^2)]/(n - K')$. Similarly, the largest $(n - K')$ characteristic roots are made up of the $N(T\sigma_\mu^2 + \sigma_v^2)$'s and $(n - N - K')$ of the σ_v^2 's. This implies that the mean of the $(n - K')$ largest characteristic roots of $\Omega = [N(T\sigma_\mu^2 + \sigma_v^2) + (n - N - K')\sigma_v^2]/(n - K')$. Using the Kiviet and Krämer (1992) inequalities, one gets

$$\begin{aligned} 0 &\leq \sigma_v^2 + (n - TK')\sigma_\mu^2/(n - K') \leq E(s^2) \\ &\leq \sigma_v^2 + n\sigma_\mu^2/(n - K') \leq n\sigma^2/(n - K') \end{aligned}$$

As $n \rightarrow \infty$, both bounds tend to σ^2 , and s^2 is asymptotically unbiased, irrespective of the particular evolution of X .

- 2.15 This gives the SAS output for the estimation of "One-way Error Component Regression" for Public Capital data. Estimators are OLS, WITHIN, BETWEEN, WALHUS, AMEMIYA, SWAR, NERLOVE, and IMLE. The results do not replicate exactly those in Table 2.6 because there is no correction for degrees of freedom in these programs. However, the output reported below using EViews should match the results in Table 2.6.

SAS Output Public Capital Data

RESULTS OF OLS

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS
INTERCEPT	1.64330	0.05759	28.53587
PUBLIC_K	0.15501	0.01715	9.03632
PRIVATE_K	0.30919	0.01027	30.10033
LABOR	0.59393	0.01375	43.20324
UNEMP	-0.00673	0.00142	-4.75366

RESULTS OF BETWEEN

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	1.58944	0.23298	6.82225
	PUBLIC_K	0.17937	0.07197	2.49215
	PRIVATE_K	0.30195	0.04182	7.22007
	LABOR	0.57613	0.05637	10.21963
	UNEMP	-0.00389	0.00991	-0.39263

RESULTS OF WITHIN

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	PUBLIC_K	-0.02615	0.02900	-0.90166
	PRIVATE_K	0.29201	0.02512	11.62463
	LABOR	0.76816	0.03009	25.52725
	UNEMP	-0.00530	0.00099	-5.35815

RESULTS OF WALLACE-HUSSAIN

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	2.10882	0.13314	15.83867
	PUBLIC_K	0.00860	0.02369	0.36325
	PRIVATE_K	0.31283	0.01986	15.75035
	LABOR	0.72435	0.02510	28.86296
	UNEMP	-0.00628	0.00093	-6.75795

RESULTS OF AMEMIYA

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	2.15640	0.13661	15.78461
	PUBLIC_K	0.00125	0.02373	0.05268
	PRIVATE_K	0.30871	0.02019	15.29068
	LABOR	0.73378	0.02532	28.98434
	UNEMP	-0.00609	0.00091	-6.68722

RESULTS OF SWAMY-ARORA

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	2.13541	0.13299	16.05651
	PUBLIC_K	0.00444	0.02334	0.19021
	PRIVATE_K	0.31055	0.01974	15.73569
	LABOR	0.72967	0.02483	29.38330
	UNEMP	-0.00617	0.00090	-6.82720

RESULTS OF NERLOVE

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	2.16831	0.13473	16.09397
	PUBLIC_K	-0.00052	0.02328	-0.02253

PRIVATE_K	0.30766	0.01986	15.48794
LABOR	0.73608	0.02486	29.61146
UNEMP	-0.00604	0.00089	-6.80225

RESULTS OF MAXIMUM LIKELIHOOD

LOOK1	PARAMETER	STANDARD ERROR	T-STATISTICS	
	INTERCEPT	2.14292	0.13426	15.96155
	PUBLIC_K	0.00329	0.02347	0.14010
	PRIVATE_K	0.30989	0.01989	15.57784
	LABOR	0.73115	0.02500	29.24478
	UNEMP	-0.00614	0.00091	-6.77855

ONE-WAY ERROR COMPONENT MODEL WITH PUBLIC CAPITAL DATA (A. MUNNELL):
BETA, VARIANCES OF BETA, AND THETA

OUTPUT	PUBLIC_K	PRIV_K	LABOR	UNEMPLOY	STD-PUBK	STD-PRIVE	STD-LAB	STD-UNEMP	THETA
OLS ESTIMATOR	0.15501	0.30919	0.59393	-0.00673	0.01715	0.01027	0.01375	0.00142	0.00000
BETWEEN ESTIMATOR	0.17937	0.30195	0.57613	-0.00389	0.07197	0.04182	0.05637	0.00991	.
WITHIN ESTIMATOR	-0.02615	0.29201	0.76816	-0.00530	0.02900	0.02512	0.03009	0.00099	1.00000
WALLACE & HUSSAIN ESTIMATOR	0.00860	0.31283	0.72435	-0.00628	0.02369	0.01986	0.02510	0.00093	0.87809
AMEMIYA ESTIMATOR	0.00125	0.30871	0.73378	-0.00609	0.02373	0.02019	0.02532	0.00091	0.89707
SWAMY & ARORA ESTIMATOR	0.00444	0.31055	0.72967	-0.00617	0.02334	0.01974	0.02483	0.00090	0.88884
NERLOVE ESTIMATOR	-0.00052	0.30766	0.73608	-0.00604	0.02328	0.01986	0.02486	0.00089	0.90166
IMLE	0.00329	0.30989	0.73115	-0.00614	0.02347	0.01989	0.02500	0.00091	0.89180

NEGATIVE VAR_MHU

NEGA_VAR	COL1
OLS ESTIMATOR	.
BETWEEN ESTIMATOR	.
WITHIN ESTIMATOR	.
WALLACE & HUSSAIN ESTIMATOR	0
AMEMIYA ESTIMATOR	0
SWAMY & ARORA ESTIMATOR	0
NERLOVE ESTIMATOR	.
IMLE	.

ONE-WAY VARIANCE COMPONENTS FOR PUBLIC CAPITAL DATA

OUTPUT	SIGMA-NU-SQ	SIGMA-MU-SQ	SIGMA-1-SQ	SIGMA-SQ	RHO
WALLACE & HUSSAIN ESTIMATOR	0.00157	0.00614	0.10594	0.00771	0.79588
AMEMIYA ESTIMATOR	0.00145	0.00795	0.13655	0.00939	0.84599
SWAMY & ARORA ESTIMATOR	0.00145	0.00684	0.11770	0.00829	0.82460
NERLOVE ESTIMATOR	0.00136	0.00820	0.14082	0.00957	0.85764

The following output was produced using EViews 5.0. This should replicate Table 2.6 and differs from the above SAS output in that degrees of freedom adjustments are made when estimating the variance components.

For Pooled OLS:

Dependent Variable: LNY
Method: Panel Least Squares

Sample: 1970 1986
 Cross-sections included: 48
 Total panel (balanced) observations: 816

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	1.643302	0.057587	28.53588	0.0000
LNK1	0.155007	0.017154	9.036311	0.0000
LNK2	0.309190	0.010272	30.10036	0.0000
LNL	0.593935	0.013747	43.20329	0.0000
U	-0.006733	0.001416	-4.753682	0.0000
R-squared	0.992593	Mean dependent var		10.50885
Adjusted R-squared	0.992557	S.D. dependent var		1.021132
S.E. of regression	0.088096	Akaike info criterion		-2.014663
Sum squared resid	6.294143	Schwarz criterion		-1.985837
Log likelihood	826.9824	F-statistic		27171.71
Durbin-Watson stat	0.079269	Prob(F-statistic)		0.000000

For the one-way fixed effects estimator with state effects:

Dependent Variable: LNY
 Method: Panel Least Squares

Sample: 1970 1986
 Cross-sections included: 48
 Total panel (balanced) observations: 816

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	2.352878	0.174813	13.45938	0.0000
LNK1	-0.026146	0.029002	-0.901545	0.3676
LNK2	0.292008	0.025120	11.62467	0.0000
LNL	0.768156	0.030092	25.52708	0.0000
U	-0.005298	0.000989	-5.358296	0.0000

Effects Specification

Cross-section fixed (dummy variables)

R-squared	0.998692	Mean dependent var	10.50885
Adjusted R-squared	0.998605	S.D. dependent var	1.021132
S.E. of regression	0.038137	Akaike info criterion	-3.633657
Sum squared resid	1.111188	Schwarz criterion	-3.333866
Log likelihood	1534.532	F-statistic	11441.65
Durbin-Watson stat	0.413532	Prob(F-statistic)	0.000000

For the Wallace and Hussain random effects estimator, we get:

Dependent Variable: LNY

Method: Panel EGLS (Cross-section random effects)

Sample: 1970 1986

Cross-sections included: 48

Total panel (balanced) observations: 816

Wallace and Hussain estimator of component variances

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	2.128128	0.134569	15.81442	0.0000
LNK1	0.005565	0.023698	0.234824	0.8144
LNK2	0.311180	0.019998	15.56080	0.0000
LNL	0.728225	0.025192	28.90685	0.0000
U	-0.006202	0.000921	-6.731730	0.0000
Effects Specification				
Cross-section random S.D. / Rho			0.082369	0.8169
Idiosyncratic random S.D. / Rho			0.038992	0.1831
Weighted Statistics				
R-squared	0.959943	Mean dependent var	1.198662	
Adjusted R-squared	0.959745	S.D. dependent var	0.191062	
S.E. of regression	0.038334	Sum squared resid	1.191751	
F-statistic	4858.753	Durbin-Watson stat	0.393903	
Prob(F-statistic)	0.000000			
Unweighted Statistics				
R-squared	0.991686	Mean dependent var	10.50885	
Sum squared resid	7.065010	Durbin-Watson stat	0.066445	

For the Amemiya random effects estimator (which EViews names the Wansbeek-Kapteyn estimator), we get:

Dependent Variable: LNY

Method: Panel EGLS (Cross-section random effects)

Sample: 1970 1986

Cross-sections included: 48

Total panel (balanced) observations: 816

Wansbeek and Kapteyn estimator of component variances

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	2.153284	0.136382	15.78857	0.0000
LNK1	0.001719	0.023725	0.072440	0.9423
LNK2	0.308985	0.020167	15.32094	0.0000
LNL	0.733179	0.025302	28.97685	0.0000
U	-0.006100	0.000911	-6.692963	0.0000

Effects Specification

Cross-section random S.D./Rho	0.088336	0.8429
Idiosyncratic random S.D./Rho	0.038137	0.1571

Weighted Statistics

R-squared	0.957828	Mean dependent var	1.094387
Adjusted R-squared	0.957620	S.D. dependent var	0.185195
S.E. of regression	0.038125	Sum squared resid	1.178804
F-statistic	4604.932	Durbin-Watson stat	0.397124
Prob(F-statistic)	0.000000		

Unweighted Statistics

R-squared	0.991617	Mean dependent var	10.50885
Sum squared resid	7.123861	Durbin-Watson stat	0.065713

For the Swamy and Arora random effects estimator, we get:

Dependent Variable: LNY

Method: Panel EGLS (Cross-section random effects)

Sample: 1970 1986

Cross-sections included: 48

Total panel (balanced) observations: 816

Swamy and Arora estimator of component variances

Variable	Coefficient	Std. Error	t-Statistic	Prob.
C	2.135397	0.132994	16.05640	0.0000
LNK1	0.004441	0.023335	0.190316	0.8491
LNK2	0.310549	0.019735	15.73573	0.0000
LNL	0.729668	0.024833	29.38316	0.0000
U	-0.006173	0.000904	-6.827327	0.0000

Effects Specification

Cross-section random S.D./Rho	0.082690	0.8246
Idiosyncratic random S.D./Rho	0.038137	0.1754

Weighted Statistics

R-squared	0.959332	Mean dependent var	1.168214
Adjusted R-squared	0.959132	S.D. dependent var	0.189313
S.E. of regression	0.038271	Sum squared resid	1.187862
F-statistic	4782.777	Durbin-Watson stat	0.394873
Prob(F-statistic)	0.000000		

Unweighted Statistics

R-squared	0.991667	Mean dependent var	10.50885
Sum squared resid	7.081797	Durbin-Watson stat	0.066234

Now we reproduce some of these estimates for the Public Capital Productivity data set using Stata

```
. infile str12 st str2 abb yr pubk hwy wat util privk gsp emp u using a:\produc.prn
```

```
'YR' cannot be read as a number for yr[1]
```

```
'P-CAP' cannot be read as a number for pubk[1]
```

```
'HWY' cannot be read as a number for hwy[1]
```

```
'WATER' cannot be read as a number for wat[1]
```

```
'UTIL' cannot be read as a number for util[1]
```

```
'PC' cannot be read as a number for privk[1]
```

```
'GSP' cannot be read as a number for gsp[1]
```

```
'EMP' cannot be read as a number for emp[1]
```

```
'UNEMP' cannot be read as a number for u[1]
```

```
'.' cannot be read as a number for yr[818]
```

```
(eof not at end of obs)
```

```
(818 observations read)
```

```
. edit
```

```
- preserve
```

```
- drop in 1
```

```
- drop in 817
```

```
- preserve
```

```
. sum
```

Variable	Obs	Mean	Std. Dev.	Min	Max
st	0				
abb	0				
yr	816	1978	4.901984	1970	1986
pubk	816	25036.66	27780.4	2627.12	140217.3
hwy	816	10218.42	9253.597	1827.14	47699.42
wat	816	3618.784	4311.742	228.46	24592.33
util	816	11199.45	14768.87	538.49	80728.14
privk	816	58188.29	59770.78	4052.71	375341.6
gsp	816	61014.32	69973.9	4354	464550
emp	816	1747.101	1855.988	108.3	11258
u	816	6.602206	2.233217	2.8	18


```

. gen lny=log(gsp)

. gen lnk1=log(pubk)

. gen lnk2=log(privk)

. gen ln1=log(emp)

. reg lny lnk1 lnk2 ln1 u

```

Source	SS	df	MS	Number of obs = 816		
Model	843.514726	4	210.878682	F(4, 811) =27171.66		
Residual	6.29415387	811	.007760979	Prob > F = 0.0000		
				R-squared = 0.9926		
				Adj R-squared = 0.9926		
				Root MSE = .0881		

```

-----+-----
      lny |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-----+-----
      lnk1 |   .155007   .0171538     9.04   0.000   .121336   .1886781
      lnk2 |   .3091902  .010272     30.10   0.000   .2890273   .329353
       ln1 |   .5939349  .0137475    43.20   0.000   .5669501   .6209197
         u |  -.006733   .0014164    -4.75   0.000  -.0095132  -.0039528
      _cons |   1.643302  .0575873    28.54   0.000   1.530265   1.75634
-----+-----

```

```

. gen stid=int( [_n-1]/17)+1

. edit
- preserve

. iis stid

. xtreg lny lnk1 lnk2 ln1 u, re theta

```

Random-effects GLS regression		Number of obs = 816	
Group variable (i) : stid		Number of groups = 48	
R-sq: within = 0.9412		Obs per group: min = 17	
between = 0.9928		avg = 17.0	
overall = 0.9917		max = 17	
Random effects u_i ~ Gaussian		Wald chi2(4) = 19131.09	
corr(u_i, X) = 0 (assumed)		Prob > chi2 = 0.0000	
theta = .8888353			

```

-----+-----
      lny |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-----+-----
      lnk1 |   .0044388   .0234173     0.19   0.850  -.0414583   .0503359
      lnk2 |   .3105483   .0198047    15.68   0.000   .2717317   .3493649
       ln1 |   .7296705   .0249202    29.28   0.000   .6808278   .7785132
         u |  -.0061725   .0009073    -6.80   0.000  -.0079507  -.0043942
      _cons |   2.135411   .1334615    16.00   0.000   1.873831   2.39699
-----+-----
      sigma_u |   .0826905
      sigma_e |   .03813705
         rho |   .82460109   (fraction of variance due to u_i)
-----+-----

```

```
. xtreg lny lnk1 lnk2 ln1 u, fe
```

```
Fixed-effects (within) regression      Number of obs   =      816
Group variable (i) : stid              Number of groups =       48

R-sq:  within = 0.9413                  Obs per group:  min =      17
        between = 0.9921                  avg =          17.0
        overall = 0.9910                  max =          17

corr(u_i, Xb) = 0.0608                  F(4,764)        =    3064.81
                                          Prob > F        =      0.0000
```

```
-----+-----
      lny |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-----+-----
      lnk1 |  -.0261493   .0290016    -0.90   0.368   - .0830815   .0307829
      lnk2 |   .2920067   .0251197   11.62   0.000   .2426949   .3413185
       ln1 |   .7681595   .0300917   25.53   0.000   .7090872   .8272318
         u |  -.0052977   .0009887    -5.36   0.000  - .0072387  -.0033568
      _cons |   2.352898   .1748131   13.46   0.000   2.009727   2.696069
-----+-----
      sigma_u |   .09057293
-----+-----
      sigma_e |   .03813705
       rho    |   .8494045   (fraction of variance due to u_i)
-----+-----
```

```
F test that all u_i=0:      F(47, 764) =    75.82      Prob > F = 0.0000
```

```
. xtreg lny lnk1 lnk2 ln1 u, be
```

```
Between regression (regression on group means) Number of obs   =      816
Group variable (i) : stid              Number of groups =       48

R-sq:  within = 0.9330                  Obs per group:  min =      17
        between = 0.9939                  avg =          17.0
        overall = 0.9925                  max =          17

sd(u_i + avg(e_i.))= .0832062          F(4,43)        =    1754.11
                                          Prob > F        =      0.0000
```

```
-----+-----
      lny |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-----+-----
      lnk1 |   .1793651   .0719719     2.49   0.017   .0342199   .3245104
      lnk2 |   .3019542   .0418215     7.22   0.000   .2176132   .3862953
       ln1 |   .5761274   .0563746    10.22   0.000   .4624372   .6898176
         u |  -.0038903   .0099084    -0.39   0.697  - .0238724   .0160918
      _cons |   1.589444   .2329796     6.82   0.000   1.119596   2.059292
-----+-----
```

```
. xtreg lny lnk1 lnk2 ln1 u, mle
```

```
Fitting constant-only model:
```

```
Iteration 0: log likelihood = -7979.4497
Iteration 1: log likelihood = -4019.3964
Iteration 2: log likelihood = -1886.2544
Iteration 3: log likelihood = -774.44513
Iteration 4: log likelihood = -226.38653
Iteration 5: log likelihood = 21.808149
Iteration 6: log likelihood = 124.88827
Iteration 7: log likelihood = 168.03251
Iteration 8: log likelihood = 186.72907
Iteration 9: log likelihood = 193.60615
Iteration 10: log likelihood = 195.27915
Iteration 11: log likelihood = 195.44879
Iteration 12: log likelihood = 195.45155
Iteration 13: log likelihood = 195.45155
```

```
Fitting full model:
```

```
Iteration 0: log likelihood = 1374.1026
Iteration 1: log likelihood = 1398.8952
Iteration 2: log likelihood = 1401.8628
Iteration 3: log likelihood = 1401.9041
Iteration 4: log likelihood = 1401.9041
```

```
Random-effects ML regression
Group variable (i) : stid
```

```
Number of obs = 81
Number of groups = 4
```

```
Random effects u_i ~ Gaussian
```

```
Obs per group: min = 17
                avg = 17.0
                max = 17
```

```
Log likelihood = 1401.9041
```

```
LR chi2(4) = 2412.91
Prob > chi2 = 0.0000
```

```
-----+-----
```

lny	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
lnk1	.0031446	.0239185	0.13	0.895	-.0437348	.050024
lnk2	.309811	.020081	15.43	0.000	.270453	.349169
ln1	.7313372	.0256936	28.46	0.000	.6809787	.7816957
u	-.0061382	.0009143	-6.71	0.000	-.0079302	-.0043462
_cons	2.143865	.1376582	15.57	0.000	1.87406	2.413671
/sigma_u	.085162	.0090452	9.42	0.000	.0674337	.1028903
/sigma_e	.0380836	.0009735	39.12	0.000	.0361756	.0399916
rho	.8333481	.0304597			.7668537	.8861754

```
-----+-----
```

```
Likelihood ratio test of sigma_u=0: chibar2(01) = 1149.84 Prob>=chibar2 = 0.000
```