## SOLUTIONS MANUAL



# Chapter 2. Tabular and Graphical Methods Solutions 

1. 

a.

| Rating | Frequency | Relative Frequency |
| :---: | :---: | :---: |
| 5 | 12 | $12 / 36=0.333$ |
| 4 | 9 | $9 / 36=0.250$ |
| 3 | 7 | $7 / 36=0.194$ |
| 2 | 5 | $5 / 36=0.139$ |
| 1 | 3 | $3 / 36=0.083$ |
| Total | 36 | $\approx 1.000$ |

b. More than a third of the patrons are very satisfied with the entrees. Overall more than half of the customers gave a top rating of either 4 or 5. Only 8.3\% gave the lowest rating.
2.
a.

| Rating | Frequency | Relative Frequency |
| :---: | :---: | :---: |
| Excellent | 5 | $5 / 24=0.208$ |
| Good | 12 | $12 / 24=0.500$ |
| Fair | 4 | $4 / 24=0.167$ |
| Poor | 3 | $3 / 24=0.125$ |
| Total | 24 | 1.000 |

b. The most common response is Good which comprises $50 \%$ of total responses. More than $70 \%$ of the patients reveal that they are in good or excellent health conditions.
3.
a.

| Expectation | Frequency | Relative Frequency |
| :---: | :---: | :---: |
| Better | 5 | $5 / 25=0.20$ |
| Same | 16 | $16 / 25=0.64$ |
| Worse | 4 | $4 / 25=0.16$ |


| Total | 25 | 1.00 |
| :---: | :---: | :---: |

Most of the chief executives (64\%) believed that the economy would be the same in the next 12 months.
b.


4.
a.

| Delays | Frequency | Relative Frequency |
| :---: | :---: | :---: |
| PM Delays | 1 | $1 / 18=0.056$ |
| All Day Delays | 6 | $6 / 18=0.333$ |
| AM Delays | 4 | $4 / 18=0.222$ |
| None | 7 | $7 / 18=0.389$ |


| Total | 18 | 1.000 |
| :---: | :---: | :---: |

The most common type of delays was 'None', comprising $38.9 \%$ of all types. The second most common type was 'All Day Delays', comprising 33.3\%.
b.


5.
a. $22(18+4)$ out of 50 rookies received a rating of 4 or better; $14(10+4)$ out of 50 rookies received a rating of 2 or worse.
b.

| Rating | Relative Frequency |
| :---: | :---: |
| 1 | $4 / 50=0.08$ |
| 2 | $10 / 50=0.20$ |
| 3 | $14 / 50=0.28$ |
| 4 | $18 / 50=0.36$ |
| 5 | $4 / 50=0.08$ |
| Total | 1.00 |

$8 \%$ of the rookies received a rating of 5 .
c.

6.
a.

| Response | Frequency |
| :---: | :---: |
| Good Jobs | $0.37 \times 5,324=1,970$ |
| Affordable homes | $0.15 \times 5,324=799$ |
| Top schools | $0.11 \times 5,324=586$ |
| Low crimes | $0.23 \times 5,324=1225$ |
| Things to do | $0.14 \times 5,324=745$ |
| Total | 5,324 |

1225 respondents considered 'Low crimes' as the most important criterion.
b.

7.
a.

| Top Vacation Choice | Relative Frequency |
| :---: | :---: |
| Cruises | $140 / 316=0.443$ |
| Beaches | $68 / 316=0.215$ |
| Amusement Parks | $68 / 316=0.215$ |
| Big Cities | $20 / 316=0.063$ |
| Lakes | $12 / 316=0.038$ |
| Summer Camp | $8 / 316=0.025$ |
| Total | $\approx 1.000$ |

$44.3 \%$ of the children cited 'Cruises' as the perfect summer trip.
b.

8.
a.

| Car-Rental Company | Relative Frequency <br> (Market Share) |
| :---: | :---: |
| Enterprise | $10.7 / 21.9=0.489$ |
| Hertz | $4.7 / 21.9=0.215$ |
| Avis Budget | $4 / 21.9=0.183$ |
| Dollar Thrifty | $1.5 / 21.9=0.068$ |
| Other | $1 / 21.9=0.046$ |
| Total | 1.000 |

b. Hertz accounted for $21.5 \%$ of sales.
C.

9.
a.


b. $\quad(0.4 * 829)=332$ respondents believe that a cure for cancer will be found.
10.
a. The number of responses for "Others" is the difference between the total number of responses and the sum of responses in the table. That is, $20,825-15,241=5,584$.
b. The proportion of respondents that felt that the Green Bay Packers would win Super Bowl XLV is $1,076 / 20,825=0.052$.
c.

| Team | Relative Frequency |
| :---: | :---: |
| Falcons | $4,040 / 20,825=0.194$ |
| Saints | $1,880 / 20,825=0.090$ |
| Texans | $1,791 / 20,825=0.086$ |


| Cowboys | $1,631 / 20,825=0.078$ |
| :---: | :---: |
| Vikings | $1,438 / 20,825=0.069$ |
| Colts | $1,149 / 20,825=0.055$ |
| Steelers | $1,141 / 20,825=0.055$ |
| Patriots | $1,095 / 20,825=0.053$ |
| Packers | $1,076 / 20,825=0.052$ |
| Others | $5,584 / 20,825=0.268$ |
| Total | 1.000 |


11.
a. Since $60 \%$ favored Obama and $30 \%$ favored Romney in terms of likeability, then $10 \%$ favored neither Obama nor Romney.
b. Of the 500 respondents, $300(=500 \times 0.60)$ favored Obama and 150 ( $=500 \times 0.30$ ) favored Romney. So Obama was favored by 150 more respondents.
12.
a. According to this survey, an athlete in football was most likely to sustain an injury
with lifelong consequences. An athlete in martial arts was least likely to sustain an injury with lifelong
consequences.
b. Approximately 79 respondents ( $=992 \times 0.08$ ) believed that professional hockey players were most likely to sustain an injury with lifelong consequences.
13. This graph does not correctly depict what has happened to Caterpillar's stock price over this period. The graph has been given a relatively high value of $\$ 500$ on the vertical axis. This compresses the data so that the increase of the stock price is not as apparent as it should be.
14. This graph does not correctly depict what has happened to sales over the most recent five-year period. The vertical axis has been stretched so that the increase in sales appears more pronounced than warranted.
15.
a.

| Class | Frequency |  |  |
| :---: | :---: | :---: | :---: |
| 3 up to 5 | 5 |  |  |
| 5 up to 7 | 5 |  |  |
| 7 up to 9 | 8 |  |  |
| 9 up to 11 | 4 |  |  |
| 11 up to 13 | 5 |  |  |
| 13 up to 15 | 3 |  |  |
| Total $=30$ |  |  |  |

b.

| Classes | Relative <br> Frequency | Cumulative Frequency | Cumulative <br> Relative Frequency |
| :---: | ---: | ---: | ---: |
| 3 up to 5 | $5 / 30=0.17$ | 5 | 0.17 |
| 5 up to 7 | $5 / 30=0.17$ | $5+5=10$ | $0.17+0.17=0.34$ |
| 7 up to 9 | $8 / 30=0.27$ | $5+5+8=18$ | $0.34+0.27=0.61$ |
| 9 up to 11 | $4 / 30=0.13$ | $5+5+8+4=22$ | $0.61+0.13=0.74$ |
| 11 up to 13 | $5 / 30=0.17$ | $5+5+8+4+5=27$ | $0.74+0.17=0.91$ |
| 13 up to 15 | $3 / 30=0.10$ | $5+5+8+4+5+3=30$ | 1.00 |
|  | Total $=1.00$ |  |  |

c. 8 observations are at least 7 but less than $9 ; 18$ observations are less than 9 .
d. $27 \%$ of the observations are at least 7 but less than $9 ; 61 \%$ are less than 9.
e.

f.

16.
a.

| Classes | Frequency |
| :---: | :---: |
| -10 up to 0 | 9 |
| 0 up to 10 | 31 |
| 10 up to 20 | 19 |
| 20 up to 30 | 8 |
| 30 up to 40 | 3 |
|  | Total $=70$ |

19 observations are at least 10 but less than 20.
b.

| Classes | Relative Frequency | Cumulative Relative Frequency |  |
| :---: | :---: | :---: | :---: |
| -10 up to 0 | $9 / 70=0.129$ |  | 0.129 |


| 0 up to 10 | $31 / 70=0.443$ | $0.129+0.443=0.572$ |
| :---: | :---: | ---: |
| 10 up to 20 | $19 / 70=0.271$ | $0.129+0.443+0.271=0.843$ |
| 20 up to 30 | $8 / 70=0.114$ | $0.129+0.443+0.271+0.114=0.957$ |
| 30 up to 40 | $3 / 70=0.043$ | $0.129+0.443+0.271+0.114+0.043=1.000$ |
|  | Total $\approx 1.000$ |  |

$27.1 \%$ of the observations are at least 10 but less than $20 ; 84.3 \%$ are less than 20.
c.


The distribution is not symmetric. It is positively skewed.
17.
a.

| Class | Relative Frequency |
| :---: | :---: |
| 10 up to 20 | $12 / 56=0.214$ |
| 20 up to 30 | $15 / 56=0.268$ |
| 30 up to 40 | $25 / 56=0.446$ |
| 40 up to 50 | $4 / 56=0.071$ |
|  | Total $\approx 1.000$ |


b.

| Class | Cumulative Frequency | Cumulative <br> Relative Frequency |
| :---: | ---: | :---: |
| 10 up to 20 | 12 | $12 / 56=0.214$ |
| 20 up to 30 | $12+15=27$ | $27 / 56=0.482$ |
| 30 up to 40 | $12+15+25=52$ | $52 / 56=0.928$ |
| 40 up to 50 | $12+15+25+4=56$ | $56 / 56=1.000$ |

c. $44.6 \%$ of the observations are at least 30 but less than $40 ; 92.8 \%$ are less than 40 .
18.
a.

| Class | Relative Frequency |
| :---: | :---: |
| 1,000 up to 1,100 | $2 / 16=0.1250$ |
| 1,100 up to 1,200 | $7 / 16=0.4375$ |
| 1,200 up to 1,300 | $3 / 16=0.1875$ |
| 1,300 up to 1,400 | $4 / 16=0.2500$ |
|  | Total $=1.0000$ |

$43.75 \%$ of the observations are at least 1,100 but less than 1,200 .
b.

| Class | Cumulative <br> Frequency | Cumulative <br> Relative Frequency |
| :---: | ---: | :---: |
| 1000 up to 1100 | 2 | $2 / 16=0.125$ |
| 1100 up to 1200 | $2+7=9$ | $9 / 16=0.562$ |


| 1200 up to 1300 | $2+7+3=12$ | $12 / 16=0.750$ |
| :--- | ---: | ---: |
| 1300 up to 1400 | $2+7+3+4=16$ | $16 / 16=1.000$ |

12 of the observations are less than 1300 .
c.

19.
a.

| Class | Frequency |
| :---: | ---: |
| 15 up to 25 | 30 |
| 25 up to 35 | $50-30=20$ |
| 35 up to 45 | $120-50=70$ |
| 45 up to 55 | $130-120=10$ |

70 observations are at least 35 but less than 45 .
b.

c. $120 / 130=0.923$, so $92.3 \%$ of the observations are less than 45 .
20.
a.

| Class | Frequency |
| :---: | :---: |
| -20 up to -10 | $0.04 \times 50=2$ |
| -10 up to 0 | $0.28 \times 50=14$ |
| 0 up to 10 | $0.26 \times 50=13$ |
| 10 up to 20 | $0.22 \times 50=11$ |
| 20 up to 30 | $0.20 \times 50=10$ |
|  | Total $=50$ |

14 observations are at least -10 but less than 0 .
b.

| Class | Cumulative <br> Frequency |
| :---: | ---: |
| -20 up to -10 | 2 |
| -10 up to 0 | $2+14=16$ |
| 0 up to 10 | $16+13=29$ |
| 10 up to 20 | $29+11=40$ |
| 20 up to 30 | $40+10=50$ |

40 observations are less than 20.
c.

21.
a.

| Class | Relative Frequency |
| :---: | ---: |
| 150 up to 200 | 0.10 |
| 200 up to 250 | $0.35-0.10=0.25$ |
| 250 up to 300 | $0.70-0.35=0.35$ |
| 300 up to 350 | $1-0.70=0.30$ |
|  | Total $=1.00$ |

$35 \%$ of the observations are at least 250 but less than 300 .
b.

22.
a.

| Assets (in billions) | Frequency |
| :---: | :---: |
| 40 up to 70 | 9 |
| 70 up to 100 | 8 |
| 100 up to 130 | 2 |
| 130 up to 160 | 0 |
| 160 up to 190 | 1 |
|  | Total $=20$ |

b.

| Assets (in billions) | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative Frequency |
| :---: | :---: | :---: | :---: |
| 40 up to 70 | $9 / 20=0.45$ | 9 | $9 / 20=0.45$ |
| 70 up to 100 | $8 / 20=0.40$ | $9+8=17$ | $17 / 20=0.85$ |
| 100 up to 130 | $2 / 20=0.10$ | $17+2=19$ | $19 / 20=0.95$ |
| 130 up to 160 | $0 / 20=0$ | $19+0=19$ | $19 / 20=0.95$ |
| 160 up to 190 | $1 / 20=0.05$ | $19+1=20$ | $20 / 20=1$ |

c. Two funds had assets of at least 100 but less than 130 (in \$ billions); 19 funds had assets less than $\$ 160$ billion.
d. $40 \%$ of the funds had assets of at least $\$ 70$ but less than $\$ 100$ (in billions); 95\% of the funds had assets less than $\$ 130$ billion.
e.


The distribution is positively skewed.
Note: The histogram could have also been made with relative frequencies. It would have had the same positive skewness.
23.
a.

| Texts | Frequency |
| :---: | :---: |
| 500 up to 600 | 4 |
| 600 up to 700 | 7 |
| 700 up to 800 | 5 |
| 800 up to 900 | 4 |
| 900 up to 1000 | 5 |
|  | Total $=25$ |

b.

| Texts | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative Frequency |
| :---: | :---: | :---: | :---: |
| 500 up to 600 | $4 / 25=0.16$ | 4 | $4 / 25=0.16$ |
| 600 up to 700 | $7 / 25=0.28$ | $4+7=11$ | $11 / 25=0.44$ |
| 700 up to 800 | $5 / 25=0.20$ | $11+5=16$ | $16 / 25=0.64$ |
| 800 up to 900 | $4 / 25=0.16$ | $16+4=20$ | $20 / 25=0.80$ |
| 900 up to 1000 | $5 / 25=0.20$ | $20+5=25$ | $25 / 25=1.00$ |
| Total | 1.00 |  |  |

c. 7 teens sent at least 600 but less than 700 texts; 16 sent less than 800 texts.
d. $16 \%$ of the teens sent at least 500 but less than 600 texts; $44 \%$ of them sent less than 700 texts.
e.


The distribution is not symmetric; it is slightly positively skewed.
24.
a.

| Temperature | Frequency |
| :---: | :---: |
| 60 up to 70 | 2 |
| 70 up to 80 | 7 |
| 80 up to 90 | 14 |
| 90 up to 100 | 10 |
|  | Total $=33$ |

b.

| Temperature | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative Frequency |
| :---: | :---: | ---: | :---: |
| 60 up to 70 | $2 / 33=0.061$ | 2 | $2 / 33=0.061$ |
| 70 up to 80 | $7 / 33=0.212$ | $2+7=9$ | $9 / 33=0.273$ |
| 80 up to 90 | $14 / 33=0.424$ | $9+14=23$ | $23 / 33=0.697$ |
| 90 up to 100 | $10 / 33=0.303$ | $23+10=33$ | $33 / 33=1.000$ |
|  | Total $=1.000$ |  |  |

c. 9 cities had temperatures less than $80^{\circ}$.
d. $42.4 \%$ of the cities recorded temperatures of at least $80^{\circ}$ but less than $90^{\circ} ; 69.7 \%$ of the cities had temperatures less than $90^{\circ}$.
e.


The distribution is slightly negatively skewed.
25.
a.

| Vacancy Rate (\%) | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative Relative <br> Frequency |
| :---: | :---: | ---: | ---: |
| 0 up to 3 | $5 / 5=0.10$ | 5 | 0.10 |
| 3 up to 6 | $10 / 50=0.20$ | $5+10=15$ | $0.10+0.20=0.30$ |
| 6 up to 9 | $20 / 50=0.40$ | $15+20=35$ | $0.30+0.40=0.70$ |
| 9 up to 12 | $10 / 50=0.20$ | $35+10=45$ | $0.70+0.20=0.90$ |
| 12 up to 15 | $5 / 50=0.10$ | $45+5=50$ | $0.90+0.10=1.00$ |
|  | Total $=1.00$ |  |  |

b. 45 cities had a vacancy rate of less than $12 \% ; 40 \%$ of the cities had a vacancy rate of at least $6 \%$ but less than $9 \% ; 70 \%$ of the cities had a vacancy rate of less than $9 \%$.
c.


The distribution is symmetric.
26.
a.

| Age | Frequency | Cumulative <br> Frequency | Cumulative <br> Relative Frequency |
| :---: | :---: | :---: | ---: |
| 15 up to 20 | $0.10(2000)=200$ | 200 | 0.1 |
| 20 up to 25 | $0.25(2000)=500$ | $200+500=700$ | $0.10+0.25=0.35$ |
| 25 up to 30 | $0.28(2000)=560$ | $700+560=1,260$ | $0.35+0.28=0.63$ |
| 30 up to 35 | $0.24(2000)=480$ | $1,260+480=1,740$ | $0.63+0.24=0.87$ |
| 35 up to 40 | $0.11(2000)=220$ | $1,740+220=1,960$ | $0.87+0.11=0.98$ |


| 40 up to 45 | $0.02(2000)=40$ | $1,960+40=2,000$ | $0.98+0.02=1.00$ |
| :---: | :---: | :---: | :---: |
|  | Total $=2000$ |  |  |

b. $28 \%$ of the women were at least 25 but less than 30 years old; $87 \%$ were less than 35 years old.
c.


The distribution appears to be relatively symmetric with possibly a slight positive skew.
d.


If we draw a horizontal line that corresponds to the 0.5 value on the vertical axis, it will intersect the ogive at the age of approximately 28 years old.
27.
a.

| Age | Frequency | Relative Frequency | Cumulative <br> Relative Frequency |
| :---: | :---: | :---: | ---: |
| 18 up to 22 | 45 | $45 / 100=0.45$ | 0.45 |
| 22 up to 26 | $70-45=25$ | $25 / 100=0.25$ | $0.45+0.25=0.70$ |
| 26 up to 30 | $85-70=15$ | $15 / 100=0.15$ | $0.70+0.15=0.85$ |
| 30 up to 34 | $96-85=11$ | $11 / 100=0.11$ | $0.85+0.11=0.96$ |
|  |  |  | $0.96+0.04=$ |
| 34 up to 38 | $100-96=4$ | $4 / 100=0.04$ | 1.00 |
|  | Total $=100$ | Total $=1.00$ |  |

b. Fifteen guests were at least 26 but less than 30 years old; $25 \%$ of the guests were at least 22 but less than 26 years old; $96 \%$ of the guests were younger than 34 years old; $4 \%$ were 34 years or older.
c.


The histogram shows a positively skewed data set reflecting the relatively young age of the nightclub's guests.
28.
a. No. The distribution is not symmetric. It is positively skewed.
b. Forty-four percent of the states had median household income between $\$ 45,000$ and \$55,000.
c. Sixty-six percent of the states had median household income between $\$ 35,000$ and \$55,000.
29.
a. Draw a vertical line through Income of 50. It intercepts with the ogive at the point of about 0.4. Thus, about $40 \%$ of the states had median household income less than $\$ 50,000$.
b. Draw a vertical line through Income of 60 . It intercepts with the ogive at the point of about 0.80 . Thus, about $80 \%$ of the states had median household income less than $\$ 60,000$. It is equivalent that about $20 \%$ of the states had median household of more than $\$ 60,000$.
30.
a. No. The distribution is not symmetric. It is positively skewed.
b. The minimum monthly stock price is approximately $\$ 50$ and the maximum stock price is approximately $\$ 450$.
c. The $\$ 50-\$ 150$ class has the highest relative frequency, which is about 0.35 .
31.
a. No. The distribution is not symmetric. It is positively skewed.
b. Three $(0.10 \times 30)$ NBA players earned between $\$ 20,000,000$ and $\$ 24,000,000$.
c. About $26(0.43 \times 30+0.43 \times 30=25.8)$ NBA players earned between $\$ 12,000,000$ and $\$ 20,000,000$.
32.
a. Draw a vertical line through Salary of 18. It intercepts with the ogive at the point of about 0.70 . Thus, about $70 \%$ of the salaries were less than $\$ 18,000,000$.
b. Draw a vertical line through Salary of 14. It intercepts the ogive at the point of about 0.15 . Thus, about $15 \%$ of the salaries were less than $\$ 14,000,000$. It is equivalent that about $85 \%$ of the salaries were more than $\$ 14,000,000$.
33.
a.

| SAT Scores | Frequency |
| :---: | :---: |
| $450-500$ | 6 |
| $501-550$ | 24 |
| $551-600$ | 15 |
| $601-650$ | 5 |



The distribution is positively skewed. Fifteen states had scores between 551 and 600.
b.

| SAT Scores | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative Frequency |
| :---: | :---: | :---: | :---: |
| $450-500$ | $6 / 50=0.12$ | 6 | $6 / 50=0.12$ |
| $501-550$ | $24 / 50=0.48$ | $6+24=30$ | $30 / 50=0.60$ |
| $551-600$ | $15 / 50=0.30$ | $30+15=45$ | $45 / 50=0.90$ |
| $601-650$ | $5 / 50=0.10$ | $45+5=50$ | $50 / 50=1.00$ |
|  | Total $=1.00$ |  |  |

c. 30 states had scores of 550 or less.
d. $30 \%$ of the states had scores between 551 and $600 ; 60 \%$ of the states had scores of 550 or less.
34.
a.

| House Value | Frequency |
| :---: | :---: |
| 0 up to 100,000 | 2 |
| 100,000 up to 200,000 | 26 |
| 200,000 up to 300,000 | 16 |
| 300,000 up to 400,000 | 4 |
| 400,000 up to 500,000 | 1 |
| 500,000 up to 600,000 | 1 |
|  | Total $=50$ |


b. No. The distribution is not symmetric. It is positively skewed.
c. The class " $\$ 100,000$ up to $\$ 200,000$ " has the highest frequency.
d. Eight percent $(4 / 50=0.08)$ of the states have median house values between $\$ 300,000$ and $\$ 400,000$.
e. Forty-four states $(2+16+26=44)$ have median house values less than $\$ 300,000$.
35.
a.

| Price/Gallon | Frequency |
| :---: | :---: |
| 3.5 up to 3.7 | 3 |
| 3.7 up to 3.9 | 27 |
| 3.9 up to 4.1 | 14 |
| 4.1 up to 4.3 | 4 |
| 4.3 up to 4.5 | 1 |
| 4.5 up to 4.7 | 1 |
|  | Total $=50$ |


b. No. The distribution is not symmetric. It is positively skewed.
c. The class " $\$ 3.7$ up to $\$ 3.9$ " has the highest frequency.
d.


Draw a vertical line through Price of 3.90. It intercepts the ogive at the point of about 30. Thus, about thirty states had average gas prices of $\$ 3.90$ or less, which is about $60 \%$ of the states. Consequently, about $40 \%$ of the states had average gas prices greater than $\$ 3.90$.
36.
a.

| DJIA Price Index | Frequency |
| :---: | :---: |
| 12,250 up to 12,500 | 10 |
| 12,500 up to 12,750 | 11 |
| 12,750 up to 13,000 | 26 |
| 13,000 up to 13,250 | 14 |
| 13,250 up to 13,500 | 1 |
|  | Total $=62$ |



The DJIA was less than 12,500 on 10 days during this quarter.
b.


The distribution is not symmetric. It is positively skewed.
C.


Draw a vertical line through Index of 13,000. It intercepts the ogive at the point of about 0.80 . Thus, approximately $80 \%$ of the days the DJIA was less than 13,000.
37.

| Stem | Leaf |
| :---: | :--- |
| 2. | 368 |
| 3. | 0223456 |
| 4. | 0222567 |
| 5. | 455 |

This distribution is symmetric. There are the same number of observations on each end of the data, and the same number of observations in the middle.
38.

| Stem | Leaf |
| :--- | :--- |
| -8 | 75532000 |
| -7 | 9753321 |
| -6 | 554 |
| -5 | 20 |

(Keep in mind that these values are negative.) The distribution is not symmetric; it is positively skewed. Most of the numbers are in the lower stems of -8 and -7 .
39.

| Stem | Leaf |
| :---: | :--- |
| 99 | 678 |
| 100 | 45 |
| 101 | 02223556 |
| 102 | 0122345 |

The temperatures ranged from a low of 99.6 to a high of 102.5. The distribution is not symmetric; it has negative skew. The majority of patients recorded a temperature higher than 101.
40.

| Stem | Leaf |
| :---: | :--- |
| 7 | 346788 |
| 8 | 0123444478 |
| 9 | 0001122233444445666889 |
| 10 | 67 |

Temperatures ranged from a low of 73 to a high of 107. The distribution is not symmetric; it has negative skew. Temperatures in 90s were the most frequent.
41.

| Stem | Leaf |
| :---: | :--- |
| 6 | 55677 |
| 7 | 00011223335589 |
| 8 | 000112 |

The officers concerns are warranted. The data shows that the majority of cars exceed the 65 miles-per-hour limit.
42.

Spain

| Stem | Leaf |
| :---: | :--- |
| 2 | 11123344555678999 |
| 3 | 002 |

## Netherlands

| Stem | Leaf |
| :---: | :--- |
| 2 | 233455566677779 |
| 3 | 03559 |

Spain has a relatively younger team compared to Netherlands. Spain's ages range from 21 to 32 , while Netherlands' ages range from 22 to 39 . The majority of players in both teams are in their 20s. However, Netherlands has a couple of more players in their 30s than Spain.
43.


There is a negative linear relationship between $x$ and $y$. As $x$ increases, $y$ tends to decrease.
44.

## Chapter 02 - Tabular and Graphical Methods



There is no evident relationship between $x$ and $y$.
45.


There is a negative relationship between $x$ and $y$. As $x$ increases, $y$ tends to decrease.
46.


There is a positive relationship between number of hours spent studying and grades. As the number of hours spent studying increases, grades tend to increase.
47.


The results support the finding. As a mother's weight gain increases, the newborn's birth weight tends to increase well.
48.


There is a slightly negative relationship between the two assets. Therefore, it would be wise for the investor to include them in her portfolio.
49.


There is a positive relationship. The realtor can conclude that generally, with higher home prices, the number of days to sell the home will tend to be higher as well.
50.
a.

| Responses | Utah | Kentucky |
| :---: | :---: | :---: |
|  | Relative Frequency | Relative Frequency |
| Yes | $2 / 20=0.10$ | $9 / 20=0.45$ |
| No | $18 / 20=0.90$ | $11 / 20=0.55$ |


|  | Total $=1.00$ | Total $=1.00$ |
| :--- | :--- | :--- |

The sample responses show the difference regarding smoking behavior in the two states. Notice that 45\% of the households in Kentucky allow smoking at home whereas only $10 \%$ do so in Utah.
b.


The bar chart shows that smoking at home is much more common in Kentucky than in Utah.
51.
a.

| Rating | Frequency | Relative Frequency |
| :--- | :---: | :---: |
| Outstanding | 0 | $0 / 28=0$ |
| Good | 8 | $8 / 28=0.286$ |
| Ok | 7 | $7 / 28=0.250$ |
| Horrible | 13 | $13 / 28=0.464$ |
|  | Total $=28$ | Total $=1$ |

From the relative frequency distribution, we can conclude that the majority of the evaluations were either "OK" or "Horrible". Notice that none of the responses included "Outstanding". Therefore, it is necessary for the owner of the restaurant to improve the service and/or experience provided.
b.

## Recent Experience

\#Outstanding ${ }^{\text {E Good }} \mathrm{EOk}$ \# Horrible



The pie chart which depicts categorical data in percentage values demonstrates the poor evaluations received.


The bar chart is another way to depict categorical data effectively. We notice that the highest bar corresponds to the last category "Horrible", and that there are no responses given for "Outstanding."
52.
a.



The charts reveal parent preferences. Sixty-five percent of parents want their children to have a profession such as a doctor, lawyer, banker or president. Less preferable are other professions such humanitarian-aid worker or a movie star.
b. Since $9 \%$ of parents want their children to become an athlete, we find $550 \times 0.09 \approx 50$. Therefore, among 550 parents approximately 50 parents want their kids to become an athlete.
53.
a.

> Classes Frequency

| -20 up to -10 | 4 |
| :---: | :---: |
| -10 up to 0 | 7 |
| 0 up 10 | 9 |
| 10 up 20 | 3 |
| 20 up to 30 | 1 |
|  | Total $=24$ |

b.

| Classes (in \%) | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative Frequency |
| :---: | :---: | :---: | :---: |
| -20 up to -10 | $4 / 24=0.167$ | 4 | $4 / 24=0.167$ |
| -10 up to 0 | $4 / 24=0.292$ | $4+7=11$ | $11 / 24=0.458$ |
| 0 up 10 | $9 / 24=0.375$ | $11+9=20$ | $20 / 24=0.833$ |
| 10 up 20 | $3 / 24=0.125$ | $20+3=23$ | $23 / 24=0.958$ |
| 20 up to 30 | $1 / 24=0.042$ | $23+1=24$ | $24 / 24=1.000$ |
|  | Total $\approx 1.000$ |  |  |

c. Nine funds had returns of at least $0 \%$ but less than $10 \%$; there were 4 funds with returns of $10 \%$ or more.
d. $12.5 \%$ of the funds had a return of at least $10 \%$ but not greater than $20 \%$; $95.8 \%$ of the funds had returns less than $20 \%$.
54.
a.

| Region | Relative Frequency |
| :---: | :---: |
| Northeast | $6,166 / 37,276=0.165$ |
| Midwest | $7,237 / 37,276=0.194$ |
| South | $15,501 / 37,276=0.416$ |
| West | $8,372 / 37,276=0.225$ |
|  | Total $=1.000$ |

$19.4 \%$ of people living below the poverty level live in the Midwest region.
b.



These charts show that the highest percentage of people who live below the poverty level live in the South, and the lowest percentage live in the Northeast.
55.
a.

| Resolution | Relative Frequency |
| :---: | :---: |
| Saving more | $328 / 1026=0.32$ |
| Paying down debt | $257 / 1026=0.25$ |
| Making more income | $154 / 1026=0.15$ |
| Spending less | $133 / 1026=0.13$ |
| Investing more | $103 / 1026=0.10$ |
| Saving for large purchase | $41 / 1026=0.04$ |
| Don't know | $10 / 1026=0.01$ |
|  | Total $=1.00$ |

$25 \%$ of the respondents said paying down debt was their top financial resolution.
b.


The bar chart shows that "Saving more" is the top financial resolution, followed by "Paying down debt". Only a small portion of the respondents didn't know their financial resolution.
56.
a.

| Response | Frequency |
| :---: | :---: |
| A few days | $0.21(3057)=642$ |
| A few long weekends | $0.18(3057)=550$ |
| One week | $0.36(3057)=1101$ |
| Two weeks | $0.25(3057)=764$ |
|  | Total $=3057$ |

Approximately 1101 people are going to take a one week vacation.
b.

57.
a.


Notice that the most frequent responses were regards to paying off debts or putting it in the bank.
b. Since $11 \%$ of 1026 respondents said they would spend the refund, we find $0.11(1026) \approx 113$. Therefore, approximately 113 of the respondents would spend the tax refund.
58.
a. The pie chart is below.

# Percentage of People in Each Region 

\# Northeast ${ }^{\text {E }}$ Midwest - South ${ }^{\text {E West }}$



The chart shows the highest percentage of people live in the South and the lowest percentage live in the Northeast.
b.


The chart shows the highest percentage of people living in poverty are in the South and the lowest percentage of people living in poverty are living in the Northeast. The percentage of people living in poverty in the South is higher than the percentage of people that live in South, and the percentage of people living in poverty in the Northeast is less than the percentage of people that live in the Northeast.
59.
a.

| Attendance | Relative <br> Frequency | Cumulative <br> Frequency | CumulativeRelative <br> Frequency <br> 1000 up to 1250 $5 / 60=0.083$ |
| :---: | :---: | ---: | ---: |
| 5 | 0.083 |  |  |
| 1250 up to 1500 | $6 / 60=0.100$ | $5+6=11$ | $0.083+0.100=0.183$ |
| 1500 up to 1750 | $10 / 60=0.167$ | $11+10=21$ | $0.183+0.167=0.350$ |
| 1750 up to 2000 | $20 / 60=0.333$ | $21+20=41$ | $0.350+0.333=0.683$ |
| 2000 up to 2250 | $15 / 60=0.250$ | $41+15=56$ | $0.683+0.250=0.933$ |
| 2250 up to 2500 | $4 / 60=0.067$ | $56+4=60$ | $0.933+0.067=1.000$ |
|  | Total $=1.000$ |  |  |

b. The most likely attendance range is from 1,750 up to 2,000 with a $33 \%$ frequency; there were 41 times out of 60 that attendance was less than 2,000.
c. Attendance was at least 1,750 but less than $2,00033.3 \%$ of the time; Attendance was less than 1,750 people $35 \%$ of the time; therefore, attendance was 1,750 or more $65 \%$ of the time.
d.


The distribution is not symmetric; it is negatively skewed.
60.
a.

| Average MPG | Relative <br> frequency | Cumulative <br> Frequency | Cumulative Relative <br> Frequency |
| :---: | :---: | ---: | ---: |
| 15 up to 20 | $15 / 80=0.1875$ | 15 | 0.1875 |
| 20 up to 25 | $30 / 80=0.3750$ | $15+30=45$ | $45 / 80=0.5625$ |
| 25 up to 30 | $15 / 80=0.1875$ | $45+15=60$ | $60 / 80=0.7500$ |


| 30 up to 35 | $10 / 80=0.1250$ | $60+10=70$ | $70 / 80=0.8750$ |
| :--- | :---: | ---: | ---: |
| 35 up to 40 | $7 / 80=0.0875$ | $70+7=77$ | $77 / 80=0.9625$ |
| 40 up to 45 | $3 / 80=0.0375$ | $77+3=80$ | $80 / 80=1.0000$ |
|  | Total $=1.0000$ |  |  |

b. 60 cars got less than $30 \mathrm{mpg} ; 37.5 \%$ of the cars got at least 20 but less than 25 mpg ; $87.5 \%$ of the cars got less than 35 mpg ; Since $87.5 \%$ got less than $35 \mathrm{mpg}, 12.5 \%$ of the cars got 35 mpg or more.
c.


The distribution is not symmetric; it is positively skewed.
61.


62.
a. There were 4 people out of 25 with a net worth greater than $\$ 20$ billion. Since $4 / 25=0.16,16 \%$ of the wealthiest people had net worth greater than $\$ 20$ billion.
b. Two people had a net worth less than $\$ 10$ billion, which is $2 / 25=0.08$, or $8 \%$. From the previous question, we know that $16 \%$ had a net worth greater than $\$ 20$ billion. Therefore, $16 \%+8 \%=24 \%$ did not have a net worth between $\$ 10$ and $\$ 20$ billion. Consequently, $76 \%$ had net worth between $\$ 10$ billion and $\$ 20$ billion.
c.

| Stem | Leaf |
| :---: | :--- |
| 3 | 66 |
| 4 | 47 |
| 5 | 3346 |
| 6 | 01556779 |
| 7 | 013337899 |

The distribution is not symmetric; it is negatively skewed. The majority of ages range from the 60 s to 70 s. Table 2.16 shows the majority of ages to be in the 50 s and 60 s. Further, this diagram shows ages ranging from 36 to 79, whereas Table 2.16 has ages ranging from 36 to 90.
63.

| Stem | Leaf |
| :---: | :--- |
| 0 | 8899 |
| 1 | 00112222334456688999 |


| 2 | 0099 |
| :--- | :--- |
| 3 | 07 |

The vast majority of the PEG ratios fall in the 1 range. The diagram represents somewhat positively skewed distribution; there are a few firms with relatively high PEG ratios.
64.
a.



These charts show that the majority ( $60 \%$ ) of houses were either Ranch or Colonial, but also $40 \%$ were either Contemporary or some other type.
b. To figure out how wide to make the classes, find the highest price and subtract the lowest price to get the range. That is $\$ 568,000-\$ 300,000=$ $\$ 268,000$. Then, since we want 7 classes, divide the range by 7 ;
$268,000 / 7=\$ 38,386$. However, for ease of interpretation, round to the
most sensible number: $\$ 50,000$. Therefore, our classes will have a width of $\$ 50,000$, with a lower bound of the first class of $\$ 300,000$.

| Classes | Frequency |
| :---: | :---: |
| 300,000 up to 350,000 | 4 |
| 350,000 up to 400,000 | 6 |
| 400,000 up to 450,000 | 4 |
| 450,000 up to 500,000 | 2 |
| 500,000 up to 550,000 | 3 |
| 550,000 up to 600,000 | 1 |
|  | Total $=20$ |

c.



The histogram shows that the most frequent house price is in the $\$ 350,000$ up to $\$ 400,000$ range. The ogive shows that the middle price (with a frequency of $10 / 20$ or $50 \%$ ) is about $\$ 400,000$.
65.


The scatter plot shows that the relation between Advertising and Sales is positive. The positive trend demonstrates that an increase in advertising will tend to increase sales.
66.


The scatterplot reveals no clear relationship between PPG and MPG.

## Case Study 2.1:

Frequency Distribution and Relative Frequency Distribution

| Sector | Frequency | Relative Frequency |
| :---: | :---: | :---: |
| Consumer | 3 | 0.233 |
| Energy | 2 | 0.067 |
| Finance | 5 | 0.167 |
| Health | 4 | 0.133 |
| Manufacturing | 5 | 0.167 |
| Technology | 7 | 0.233 |
| Total | 30 | 1.000 |

The pie chart is below.


The sectors with the largest representations are the technology, manufacturing and finance sectors. The sector with the lowest representation is the energy sector.

## Case Study 2.2

The net profit margin is a firm's net profit after taxes to revenue. It is measured in percentage, showing the percentage of net income per dollar in sales or other operating income.

| Net Profit Margin | Frequency | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative Frequency |
| :--- | :---: | :---: | :---: | ---: |
| $-10 \%$ up to $-5 \%$ | 1 | $1 / 32=0.031$ | 1 | $1 / 32=0.031$ |
| -5 up to 0 | 6 | $6 / 32=0.188$ | 7 | $7 / 32=0.219$ |
| 0 up to 5 | 10 | $10 / 32=0.313$ | 17 | $17 / 32=0.531$ |
| 5 up to 10 | 11 | $11 / 32=0.344$ | 28 | $28 / 32=0.875$ |
| 10 up to 15 | 2 | $2 / 32=0.063$ | 30 | $30 / 32=0.938$ |
| 15 up to 20 | 2 | $2 / 32=0.063$ | 32 | $32 / 32=1.000$ |
|  | Total $=32$ | Total $\approx 1$ |  |  |




The data tends to cluster between $0 \%$ and $10 \%$, as shown in the histogram. The net profit margins range from $-5.19 \%$ to $19.95 \%$. Approximately $53 \%$ of the firms have a net profit margin below $5 \%$.

## Case Study 2.3

| Life Expectancy | Frequency | Relative <br> Frequency | Cumulative <br> Frequency | Cumulative <br> Relative Frequency |
| :---: | :---: | :---: | :---: | ---: |
| 73.5 up to 75 | 1 | $1 / 50=0.02$ | 1 | $1 / 50=0.02$ |
| 75 up to 76.5 | 7 | $7 / 50=0.14$ | 8 | $8 / 50=0.16$ |
| 76.5 up to 78 | 9 | $9 / 50=0.18$ | 17 | $17 / 50=0.34$ |
| 78 up to 79.5 | 16 | $16 / 50=0.32$ | 33 | $33 / 50=0.66$ |
| 79.5 up to 81 | 16 | $16 / 50=0.32$ | 49 | $49 / 50=0.98$ |
| 81 up to 82.5 | 1 | $1 / 50=0.02$ | 50 | $50 / 50=1.00$ |



The data tends to cluster between 78 and 81, as shown in the histogram. The distribution is negatively skewed.

